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INTRODUCING KOKKOS TO TPETRA FINITE ELEMENT ASSEMBLY

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2:30 PM Wednesday November 1st, 2023,

Trilinos User Group Meeting



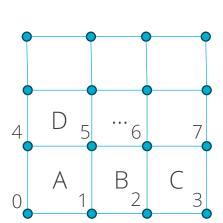


TPETRA'S FINITE ELEMENT ASSEMBLY EXAMPLE

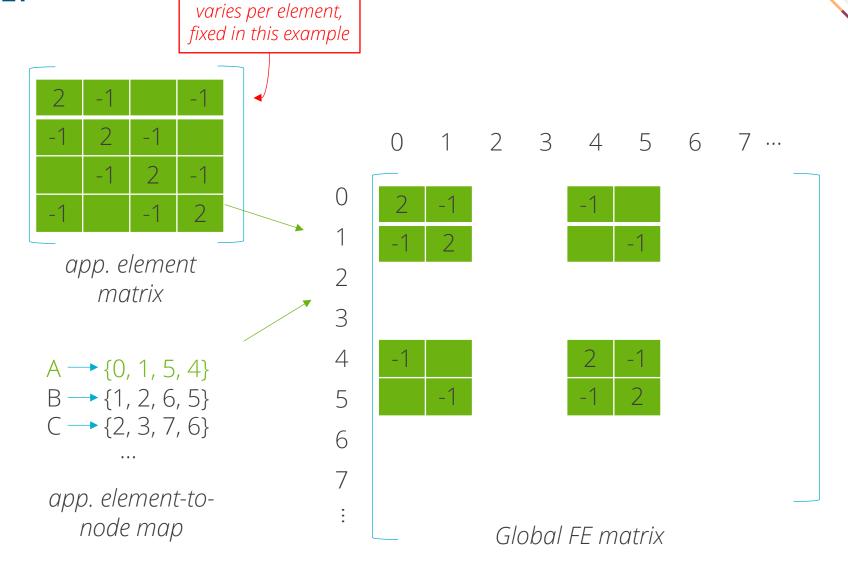
- Previously: [Link to TUG Kokkos Training Material]
 - Single code for all CPUs, GPUs, and whatever else Kokkos supports
- Trilinos/packages/tpetra/core/example/Finite-Element-Assembly
- Application provides (our example mocks these)
 - Map of elements to nodes in global indices
 - Methods for computing element matrices
- Type-1 assembly
 - Local elements contribute to off-rank FE matrix rows for off-rank nodes
- No worksetting



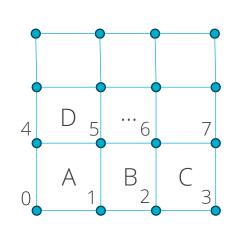
FE ASSEMBLY IN BRIEF



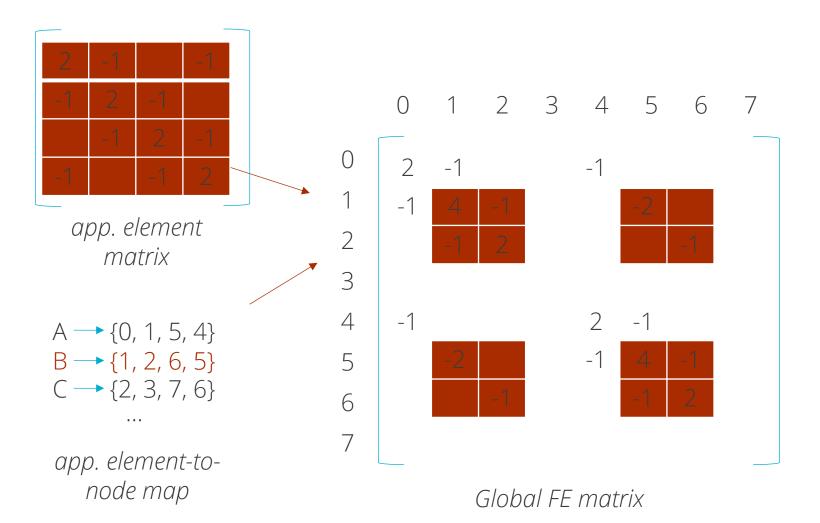
app. discretization



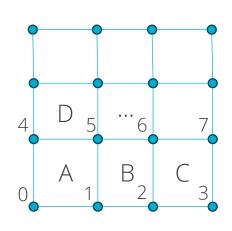
ELEMENT B'S CONTRIBUTION



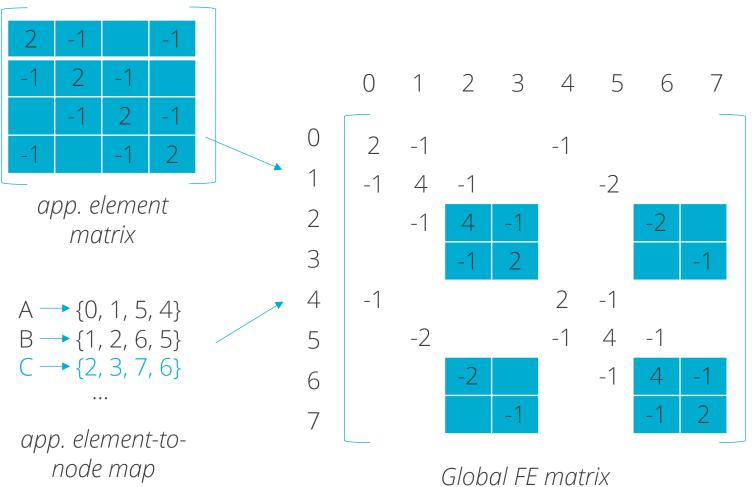
app. discretization



ELEMENT C'S CONTRIBUTION



app. discretization





FIVE CHANGES TO WATCH OUT FOR

Bare for-loops



- Kokkos::parallel_for
 - Allow device execution
 - Supports CPU execution too

Host allocations



Kokkos::View

Functions



KOKKOS_FUNCTION annotation

- Tpetra::[...]::getHostView()
 - Convenient use of global indices



- Tpetra::[]::getDeviceView()
 - Have to use local indices "on device"

Normal addition



Atomic addition



HOST LOOP -> KOKKOS::PARALLEL_FOR

```
Kokkos::View<local_ordinal_type[4][4], hostType>
Teuchos::Array<Scalar> element_rhs(4);
Teuchos::Array<global_ordinal_type>
Teuchos::Array<Scalar> column_scalar_values(4);
Tnetra::heginAssembly(*fe matrix *rhs):
for (int element gidx = 0;
     element_gidx < numOwnedElements;</pre>
     ++element gidx) {
  ReferenceQuad4(element_matrix);
  ReferenceQuad4RHS(element_rhs);
  for (size t element node idx=0;
         element node idx < nodesPerElem;</pre>
      owned_element_to_node_gids(
        element_gidx, element_node_idx);
  for (size_t element_node_idx = 0;
       element node idx < 4;
```

Tpetra: a single active thread, loops over each local element

Kokkos: operate on local elements in parallel

Also works on host, single-threaded (Kokkos::Serial)

or multi-threaded

(::OpenMP, ::Threads)

```
Tpetra::Access::OverwriteAll);
auto localMatrix = fe_matrix->getLocalMatrixDevice();
auto all element rhs unmanaged =
 makeUnmanaged(all element rhs);
auto all_element_matrix_unmanaged =
auto all lcids unmanaged = makeUnmanaged(all lcids);
Kokkos::parallel for
  Kokkos::RangePolicy<execution_space, int>(
    0, numOwnedElements),
  KOKKOS LAMBDA (const size t element idx) {
 const pair_type location_pair(
   nodesPerElem*element_idx,
   nodesPerElem*(element idx+1));
 auto element matrix = Kokkos::subview(
   all_element_matrix_unmanaged, location_pair,
   Kokkos::ALL):
 auto element_lcids = Kokkos::subview(
   all lcids unmanaged, location pair);
   all_element_rhs_unmanaged, location_pair);
 ReferenceOuad4(element matrix);
 ReferenceQuad4RHS(element rhs);
```

Tpetra + Kokkos



HOST ALLOCATIONS -> KOKKOS VIEW

```
Kokkos::View<local_ordinal_type[4][4], hostType>
Teuchos::Array<Scalar> element_rhs(4);
Teuchos::Array<global ordinal type>
 Feuchos::Array<Scalar> column_scalar_values(4);
Tpetra::beginAssembly(*fe_matrix,*rhs);
     element_gidx < numOwnedElements;</pre>
     ++element_gidx) {
  ReferenceQuad4(element_matrix);
  ReferenceQuad4RHS(element rhs);
         element_node_idx < nodesPerElem;</pre>
    column global ids[element node idx] =
      owned element to node gids(
       element node idx < 4;
       ++element_node_idx) {
```

Tpetra: allocate some scratch space on the stack. Reused for each iteration of element loop

Kokkos: allocate enough device memory for all active threads

Kokkos: each thread gets its own piece of the preallocated scratch space

```
scalar_2d_array_type all_element_matrix(
   "all_element_matrix",nodesPerElem*numOwned:lements);
scalar_1d_array_type all_element_rhs(
   "all_element_rhs",nodesPerElem*numOwnedElements);
   "all_element_single_view_type all_loids(
   "all_lids",nodesPerElem*numOwnedElements);

Tpetra::beginAssembly(*fe_matrix,*rhs);
auto owned_element_to_node_gids =
   mesh.getOwnedElementToNode().getDeviceView(
```

```
KOKKOS_LAMBDA (const size_t element_idx) {
const pair_type location_pair(
    nodesPerElem*element_idx,
    nodesPerElem*(element_idx+1));

auto element_matrix = Kokkos::subview(
    all_element_matrix_unmanaged, location_pair,
    Kokkos::ALL);
auto element_lcids = Kokkos::subview(
    all_lcids_unmanaged, location_pair);
auto element_rhs = Kokkos::subview(
    all_element_rhs_unmanaged, location_pair);

ReferenceQuad4(element_matrix);
ReferenceQuad4RHS(element_rhs);

for (int element_node_idx = 0;
```

Tpetra + Kokkos



HOST FUNCTIONS -> KOKKOS_FUNCTION

```
Kokkos::View<local_ordinal_type[4][4], hostType>
Teuchos::Array<Scalar> element_rhs(4);
Teuchos::Array<global_ordinal_type>
Teuchos::Array<Scalar> column scalar values(!);
Tpetra::beginAssembly(*fe_matrix,*rhs);
     ++element gidx) {
  ReferenceQuad4(element_matrix)
  ReferenceQuad4RHS(element_rhs):
         element node idx < nodesPerElem;</pre>
         ++element node idx) {
    column_global_ids[element_node_idx] =
      owned_element_to_node_gids(
  for (size_t element_node_idx = 0;
```

Tpetra: fill scratch space with matrix for this element

Kokkos: each thread fills scratch space in parallel

These functions must be allowed to execute on the device

```
KOKKOS_FUNCTION
void Reference4Quad(...) {
   ...
};
```

```
nodesPerElem*element_idx,
  nodesPerElem*(element idx+1));
auto element matrix = Kokkos::subview(
  all_element_matrix_unmanaged, location_pair,
auto element lcids = Kokkos::subview(
  all_lcids_unmanaged, location_pair);
auto element_rhs = Kokkos::subview(
  all_element_rhs_unmanaged, location_pair);
ReferenceQuad4(element_matrix);
ReferenceQuad4RHS(element rhs);
     element node idx < nodesPerElem;</pre>
      owned_element_to_node_gids(
     element_node_idx < nodesPerElem;</pre>
     ++element node idx) {
```

Tpetra Tpetra + Kokkos



GLOBAL INDICES -> LOCAL INDICES

```
element_gidx < numOwnedElements;</pre>
   ++element gidx) {
ReferenceQuad4(element matrix);
ReferenceQuad4RHS(element_rhs);
       element node idx < nodesPerElem;</pre>
  column_global_ids[element_node_idx] =
    owned_element_to_node_gids(
  global_ordinal_type global_row_id =
    owned_element_to_node_gids(
    column scalar values[col idx] =
      element matrix(element node idx, col idx);
  fe matrix->sumIntoGlobalValues(
    global_row_id, column_global_ids,
    column scalar values):
```

Tpetra: interact with FE matrix and RHS through global indices. Simpler interface, made possible by dynamic memory allocation

Kokkos: need a device Kokkos::View of the local FE matrix and RHS to operate on.

Kokkos: local FE matrix and RHS only understands local indices.
Use Tpetra::Maps to translate between local and global

```
Tpetra::Access::ReadOnly);
rhs->getLocalViewDevice(
nuto localMatrix = fe_matrix->getLocalMatrixDevice();
<mark>uto all_element_rns_unmanaged =</mark>
 makeUnmanaged(all element rhs):
 ReferenceOuad4(element matrix):
 ReferenceQuad4RHS(element rhs);
      element node idx < nodesPerElem;</pre>
   element lcids(element node idx) =
       owned_element_to_node_gids(
      element_node_idx < nodesPerElem;</pre>
     localMap.getLocalElement(owned_element_to_node_gits()
   for (int col_idx = 0; col_idx < nodesPerElem;</pre>
        ++col idx) {
     localMatrix.sumIntoValues(local row id,
```

Tpetra + Kokkos



ATOMIC ADDITION

```
element node idx < nodesPerElem;</pre>
column global ids[element node idx] =
 owned_element_to_node_gids(
   element_gidx, element_node_idx);
   ++element_node_idx) {
global_ordinal_type global_row_id =
 owned_element_to_node_gids(
   element matrix(element node idx, col idx);
fe matrix->sumIntoGlobalValues(
 global_row_id, column_global_ids,
rhs->sumIntoGlobalValue(
 global_row_id, 0,
 element_rhs[element_node_idx]);
```

Tpetra: contribute element values to FE matrix and RHS

Kokkos: atomic adds, since each thread (element) may contribute to the same node at the same time

```
element_node_idx < nodesPerElem;</pre>
   ++element_node_idx) {
    owned_element_to_node_gids(
   element node idx < nodesPerElem;</pre>
const local_ordinal_type local_row_id =
  localMap.getLocalElement(owned_element_to_node_gids(
for (int col_idx = 0; col_idx < nodesPerElem;</pre>
  localMatrix.sumIntoValues(local_row_id,
                             &(element_matrix(
Kokkos::atomic add(
  &(localRHS(local_row_id, 0)),
```

Tpetra + Kokkos



CONCLUSION

- Create parallel execution using Kokkos::parallel_for
 - also supports host CPU execution
- Kokkos::View for data accessed in parallel regions
 - convert std::vector, Teuchos::Array, malloc, new, ...
- Functions called in that region must be KOKKOS_FUNCTION
 - e.g. producing the element matrix
 - ...and any data it requires must be in a Kokkos::View (material properties, node coordinates, etc.)
- Use Tpetra::[]::get*Device() to get Kokkos::View of Tpetra data
 - As a consequence, have to operate with local rather than global indices
- Parallel regions may require atomics for their contributions