

## Exercise 2: Fundamentals of statistics

- Frequency functions, probability density and distribution function -

| Group: | Surname, First name: | Matriculation number: | Signature*: |
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\* With my signature I declare that I was involved in the elaboration of this homework.

Submission until: **10.11.2023**

### Objective

This exercise is based on the knowledge about absolute, relative and cumulative frequency function as well as the determination of variance and standard deviation of a series of measurements. In addition, it will focus on the determination of distribution and probability density functions as well as expectation, mean value and standard deviation.

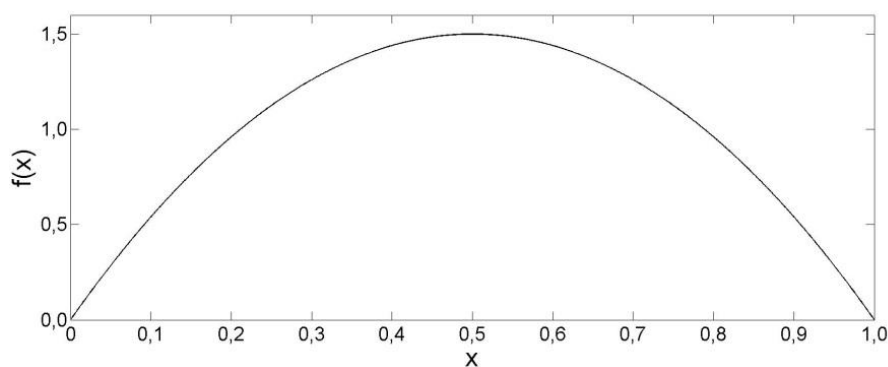


Figure 1: Probability density function

**Task 1:**

Figure 1 is showing a probability density function

$$f(x) = 6x - 6x^2 \quad x \in [0, 1]$$

for a random variable  $X$ . Use this function to calculate the following parameters.

- What is the distribution function  $F(X)$  for a random variable  $X$ ?
- Calculate the expectation  $E(x)$ .
- Calculate the standard deviation for a random variable  $X$ .
- What is the probability for a realisation  $x$  of a random variable  $X$   
 $P(x > 1.1)$   
 that is bigger than 1.1?
- What is the probability for a realisation  $x$  of a random variable  $X$   
 $P(x = 0.35)$   
 that is equal 0.35?
- What is the probability for a realisation  $x$  of a random variable  $X$   
 $P(0 \leq x \leq 0.5)$   
 that falls into the interval  $[0, 0.5]$ ?

**Task 2 (Homework):**

In Figure 2, a probability density function for a random variable  $X$  is described by a triangle. Use the graph to calculate the following parameters.

- Determine the coefficient  $C$ .
- Describe the graphical representation of the probability density function in an analytical form.
- What is the distribution function  $F(X)$  for a random variable  $X$ ?
- Calculate the expectation  $E(x)$ .
- Calculate the standard deviation for a random variable  $X$ .
- What is the probability for a realisation  $x$  of a random variable  $X$   
 $P(x < 0)$   
 that is smaller than 0?
- What is the probability for a realisation  $x$  of a random variable  $X$   
 $P(x = 3)$   
 that is equal 3?
- What is the probability for a realisation  $x$  of a random variable  $X$   
 $P(4 \leq x \leq 5)$   
 that falls into the interval  $[4, 5]$ ?

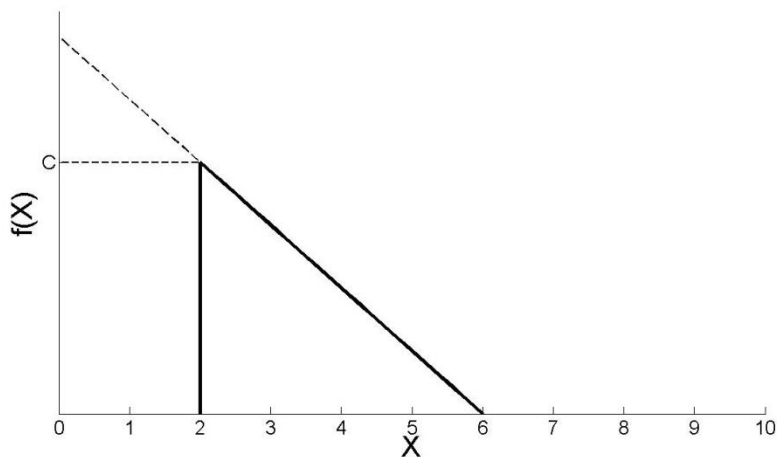


Figure 2: Probability density function

### Task 3 (Homework):

During a survey the students measured one side of a triangle. So, the expectation is unknown. The measurements are stored in the file *"distances.txt"*.

- Load the measurements from *"distances.txt"*.
- Plot the following graphs for the given distances
  - absolute frequency function/polygon,
  - relative frequency function/polygon,
  - cumulative frequency function/polygon.
- Calculate the mean value, variance and standard deviation of a single observation as well as for the arithmetic mean.
- Question: How often do you have to measure this distance with the previously determined standard deviation in order to obtain a precision for the arithmetic mean of  $s_{\bar{t}} \leq 0.1 \text{ mm}$ ?