TTIC 31230, Fundamentals of Deep Learning

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The Educational Framework (EDF)

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The educational frameword (EDF) is 150 lines of Python-NumPy that implement a deep learning framework.

In EDF we write

$$y = F(x)$$

$$z = G(y, x)$$

$$u = H(z)$$

$$\mathcal{L} = u$$

This is Python code where variables are bound to objects.

The EDF Framework

$$y = F(x)$$

$$z = G(y, x)$$

$$u = H(z)$$

$$\mathcal{L} = u$$

This is Python code.

x is an object in the class Input.

y is an object in the class F (subclass of CompNode).

z is an object in the class G (subclass of CompNode).

u and \mathcal{L} are the same object in the class H (suclass of CompNode).

The Core of EDF

```
def Forward():
   for c in CompNodes: c.forward()
def Backward(loss):
   for c in CompNodes + Parameters: c.grad = 0
   loss.grad = 1.
   for c in CompNodes[::-1]: c.backward()
def SGD():
   for p in Parameters:
       p.value -= eta*p.grad
```

```
y = F(x)
class F(CompNode):
     def __init__(self, x):
         CompNodes.append(self)
         self.x = x
     def forward(self):
         self.value = ... compute the value ...
     def backward(self):
```

self.x.addgrad(... compute the gradient ...)

Nodes of the Computation Graph

There are three kinds of nodes in a computation graph—inputs, parameters and computation nodes.

```
class Input:
    def __init__(self):
        pass
    def addgrad(self, delta):
        pass

class CompNode: #initialization is handled by the subclass
    def addgrad(self, delta):
        self.grad += delta
```

class Parameter:

```
def __init__(self,value):
    Parameters.append(self)
    self.value = value

def addgrad(self, delta):
    #sums over the minibatch
    self.grad += np.sum(delta, axis = 0)/nBatch
```

MLP in EDF

The following Python code constructs the computation graph of a multi-layer perceptron (NLP) with one hidden layer.

```
L1 = Sigmoid(Affine(Phi1,x))
Q = Softmax(Sigmoid(Affine(Phi2,L1))
ell = LogLoss(Q,y)
```

Here **x** and **y** are input computation nodes whose value have been set. Here **Phi1** and **Phi2** are "parameter packages" (a matrix and a bias vector in this case). We have computation node classes **Affine**, **Relu**, **Sigmoid**, **LogLoss** each of which has a forward and a backward method.

The Sigmoid Class

$$y[b,i] = \sigma(x[b,i])$$

$$y = \frac{1}{1+e^{-x}}$$

$$\frac{dy}{dx} = \frac{e^{-x}}{(1+e^{-x})^2}$$

$$= y(1-y)$$

 $x.\operatorname{grad}[b,i] += y.\operatorname{grad}[b,i]y.\operatorname{value}[b,i](1-y.\operatorname{value}[b,i])$

The Sigmoid Class

```
class Sigmoid:
    def __init__(self,x):
        CompNodes.append(self)
        self.x = x

    def forward(self):
        self.value = 1. / (1. + np.exp(-self.x.value))

    def backward(self):
        self.x.addgrad(self.grad*self.value*(1.-self.value))
```

The Affine Class

$$\begin{split} \tilde{y}[b,j] &= \sum_{i} W[i,j] \; x[b,i] = xW \\ y[b,j] &= \tilde{y}[b,j] - B[j] = \tilde{y} - B \; \text{(broadcasting)} \\ \tilde{y}.\text{grad}[b,j] &+= y.\text{grad}[b,j] \\ B.\text{grad}[j] &-= \frac{1}{B} \sum_{b} y.\text{grad}[b,j] \\ x.\text{grad}[b,i] &+= \sum_{j} \tilde{y}.\text{grad}[b,j]W[i,j] = yW^{\top} \\ W.\text{grad}[i,j] &+= \frac{1}{B} \sum_{b} \tilde{y}.\text{grad}[b,j]x[b,i] = ??? \end{split}$$

```
class Affine(CompNode):
    def __init__(self,Phi,x):
        CompNodes.append(self)
        self.x = x
        self.Phi = Phi
    def forward(self):
        self.value = (np.matmul(self.x.value,
                                self.Phi.w.value)
                      - self.Phi.b.value)
```

Procedures in EDF

```
def MLP(Phi,x)

if len(Phi) = 0
    return x

return Sigmoid(Affine(Phi[0],MLP(Phi[1:],x)))
```

\mathbf{END}