

Deep generative models for spatial transcriptomics

Clayton W. Seitz

January 27, 2022

Outline

Deep generative models

Generative modeling in transcriptomics

Future directions

References

The logic of generative modeling

Say we have a set of variables $x = (x_1, x_2, \dots, x_n)$ which might have some statistical dependence

The variable x might be an amino acid sequence, gene expression data, microscopy image, etc.

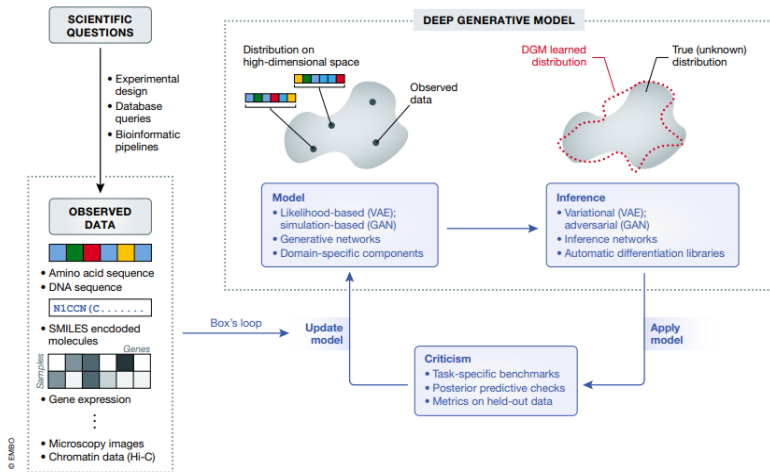
- ▶ Often we are handed a batch of empirical samples $\{x_i\}_{i=1}^N$
- ▶ We want to know the generating distribution $p(x)$

In supervised **generative learning**, we try to explicitly learn the joint distribution $p(x) = \prod_{i=1}^{N-1} p(x_i | x_{i+1:N}) p(x_N)$, which is generally more difficult than discriminative learning.

Perks of generative modeling

- ▶ Fitting complete multivariate distributions $p(\mathbf{x})$ goes beyond correlation-based or clustering approaches
- ▶ Correlations cannot discover partial correlation in the context of other neighbors
- ▶ Fitting $p(\mathbf{x})$ permits sampling based inference

Applying deep generative models to biological data



Why generative modeling is difficult

When describing a distribution over multiple variables, we may not know the proper normalization Z . That is,

$$p(x) = \frac{1}{Z} \tilde{p}(x)$$

This **very important** situation arises in several contexts:

1. In **Bayesian inference** where $p(x_1|x_2) = p(x_2|x_1)p(x_1)/p(x_2)$ is intractable due to $Z = p(x_2) = \int p(x_2|x_1)p(x_1)dx_1$. This integral can be very difficult or impossible to compute.
2. In models from statistical physics, e.g. the Ising model, we only know $\tilde{p}(x) = e^{-H(x)}$ where $H(x)$ is the Hamiltonian

Variational autoencoders (VAEs)

A variational solution to generative modeling

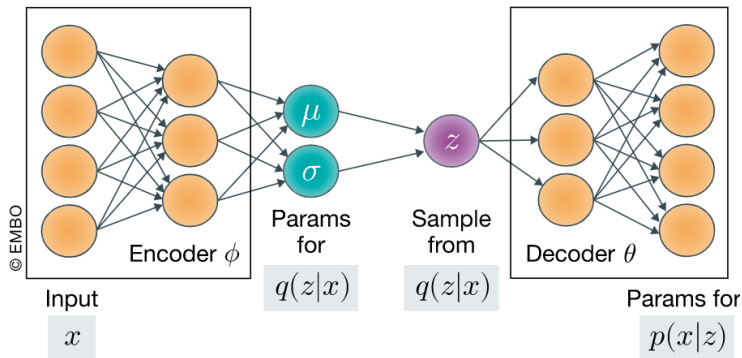


Figure 1: Variational autoencoder architecture Taken from Lopez 2020 in EMBO

Bayesian inference

The variable x has a latent representation or code z . We often say that z is the *causal source* of x . Ultimately, we would like to know the distribution $P_{\phi}(x)$

$$P_{\phi}(x) = \frac{P_{\phi}(x|z)P_{\phi}(z)}{Q_{\psi}(z|x)}$$

in order to find the model parameters that maximize the likelihood of the observed data:

$$\Phi^* = \underset{\Phi}{\operatorname{argmin}} -\log P_{\Phi}(x)$$

but we generally do not know $P_{\psi}(z|x)$ due to the intractable integral $Z = \int P_{\phi}(x|z)P_{\phi}(z)dz$ (see slide 5)

Computing the evidence

We can rewrite the evidence as

$$\begin{aligned}P_{\phi}(x) &= \int P_{\phi}(z)P_{\phi}(x|z)dz \\&= \int P_{\phi}(z)P_{\phi}(x|z)\frac{P_{\phi}(z|x)}{P_{\phi}(z|x)}dz \\&= \mathbb{E}_{z \sim P_{\phi}(z|x)} \frac{P_{\phi}(z)P_{\phi}(x|z)}{P_{\phi}(z|x)}\end{aligned}$$

where $P_{\phi}(z|x)$ is our model "encoder"

The evidence lower bound (ELBO)

$$\begin{aligned}\log P_\phi(x) &= \log \int_z P(x, z) dx \\&= \log \int_z P(x, z) \frac{Q(z|x)}{Q(z|x)} dz \\&= \log \mathbb{E}_{z \sim P_\phi(z|x)} \frac{P(x|z)P(z)}{Q(z|x)} \\&\geq \mathbb{E}_{z \sim P_\phi(z|x)} \log \frac{Q(x|z)}{P(z)} + \log P(x|z) \\-\log P_\phi(x) &\leq \mathbb{E}_{z \sim P_\phi(z|x)} \log \frac{Q(x|z)}{P(z)} - \log P(x|z)\end{aligned}$$

Applying the VAE to transcriptomics

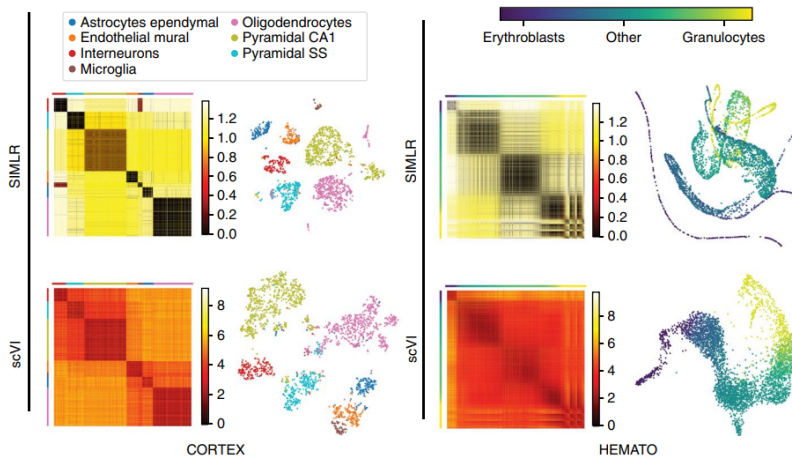
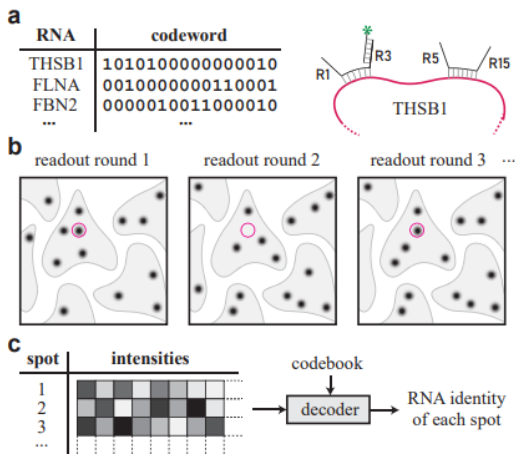


Figure 2: Distance matrices and 2D embedding of the latent space for CORTEX dataset ($n = 3005$ cells) and HEMATO ($n = 4016$ hematopoietic progenitor cells)

Previous studies lack interpretability and spatial information

- ▶ VAEs (and deep networks in general) are very flexible or “expressive”
- ▶ The latent distribution (which is typically multivariate normal) can be difficult to interpret
- ▶ But can still perform clustering, visualization, etc.
- ▶ Field is moving towards using spatial features as well

Multiplexed RNA imaging with MHD4 code



Open-source datasets from the Zhuang lab at Harvard

Multiplexed RNA imaging with MHD4 code

- ▶ Human genome codes nearly 30k non-redundant types of RNA molecules
- ▶ Some of those end up translated into protein
- ▶ Original study used 16-bit codes with minimum Hamming distance 4
- ▶ Code distance is chosen due to false positive and false negative rates

Using $L = 16$ bit codewords with distance 4, gives 140 unique RNAs. Other methods SlideSeq, 10x Visium can achieve whole-genome spatial transcriptomics

References I