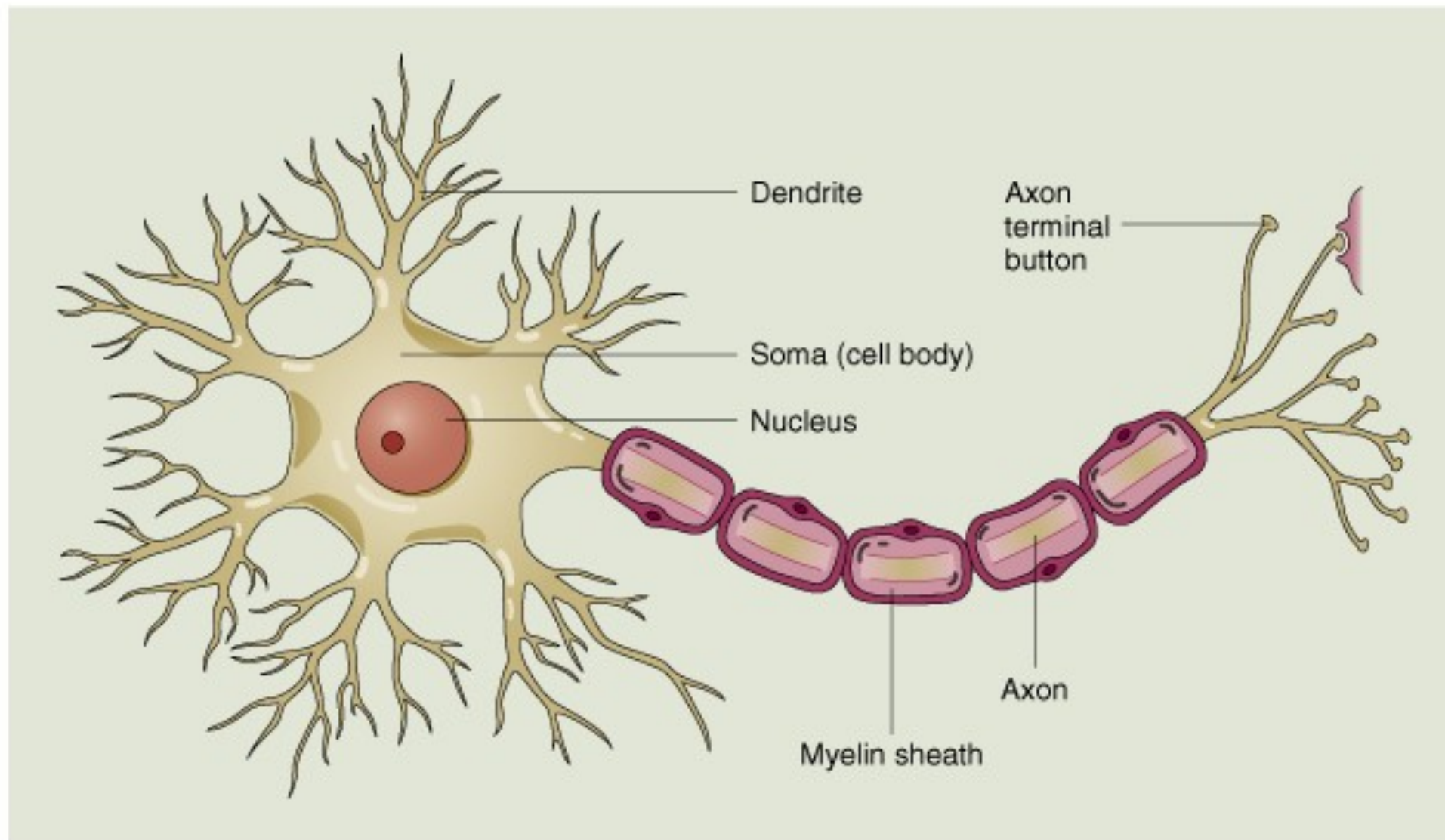
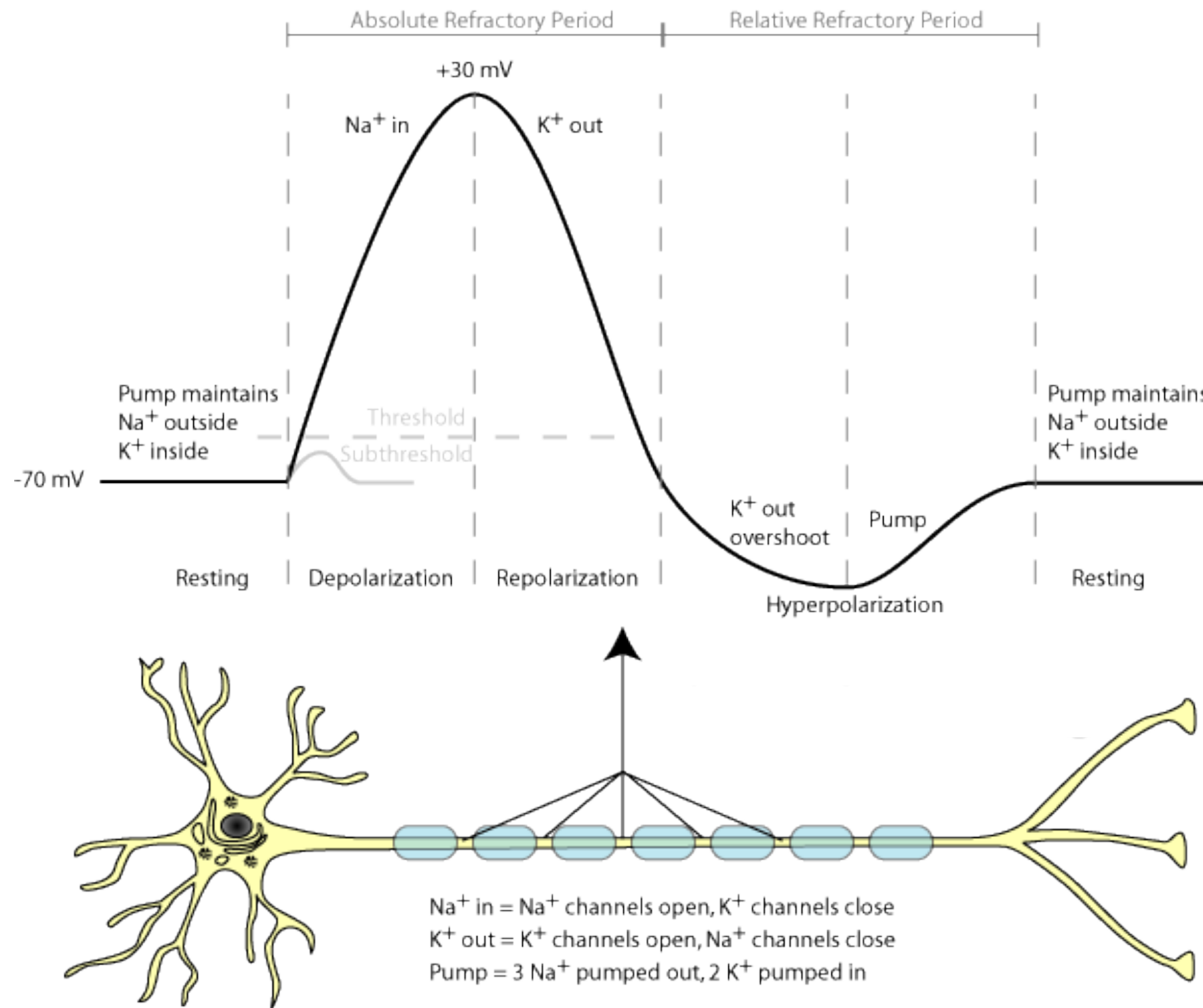


Anatomy of a neuron:

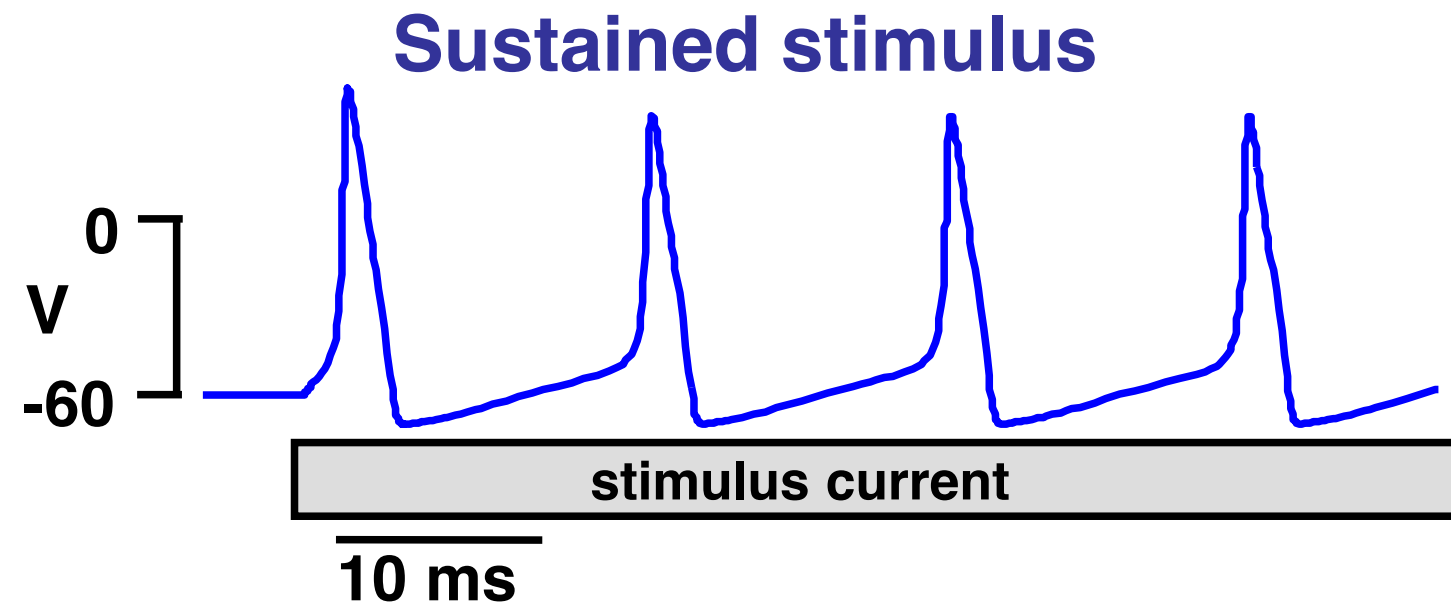
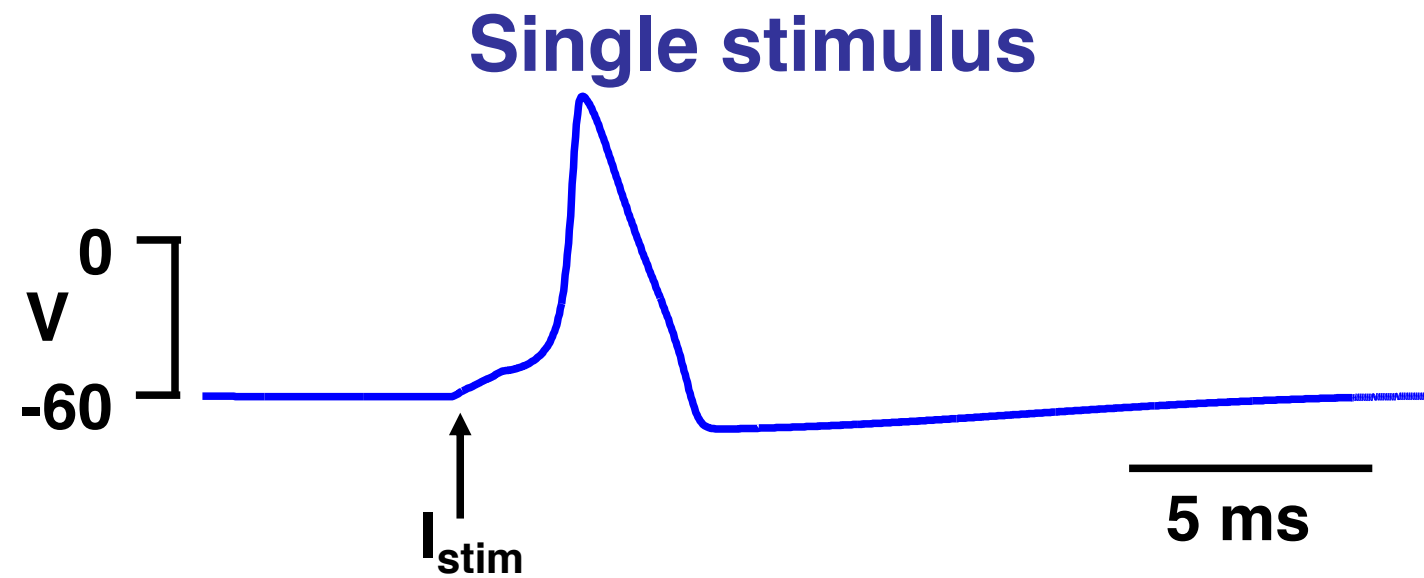


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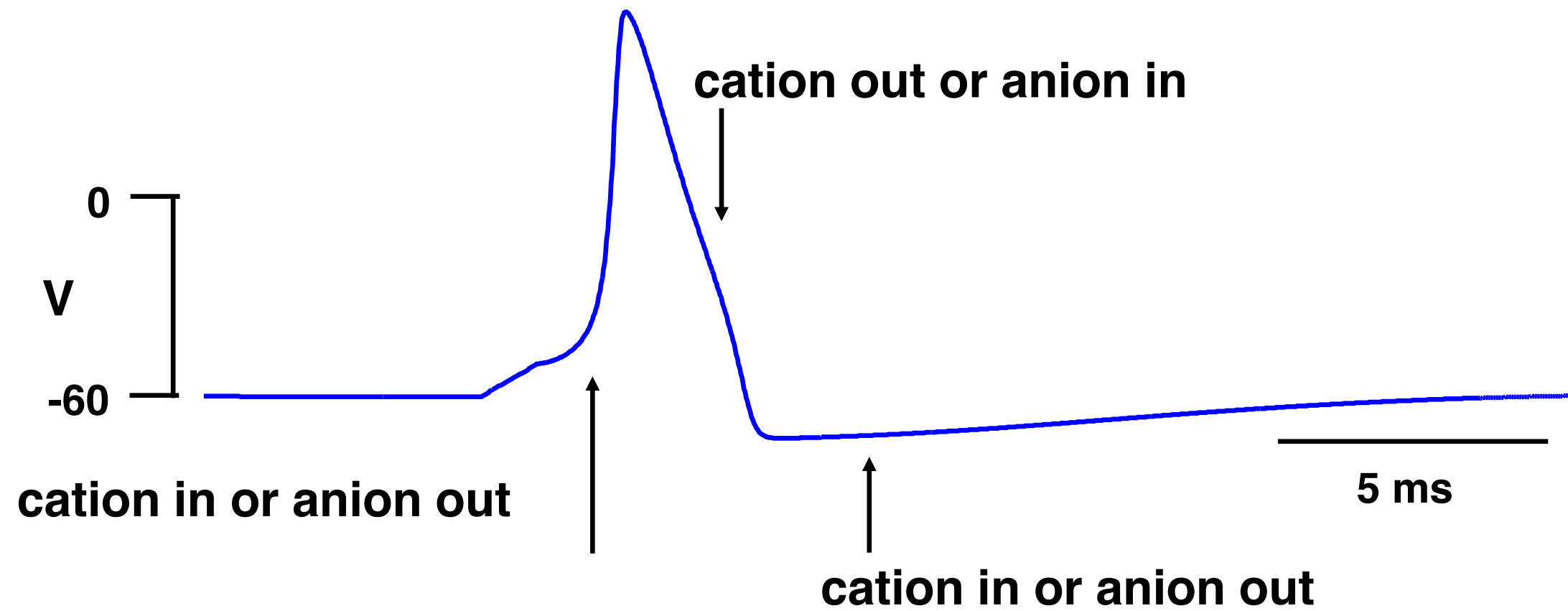
Anatomy of a spike:



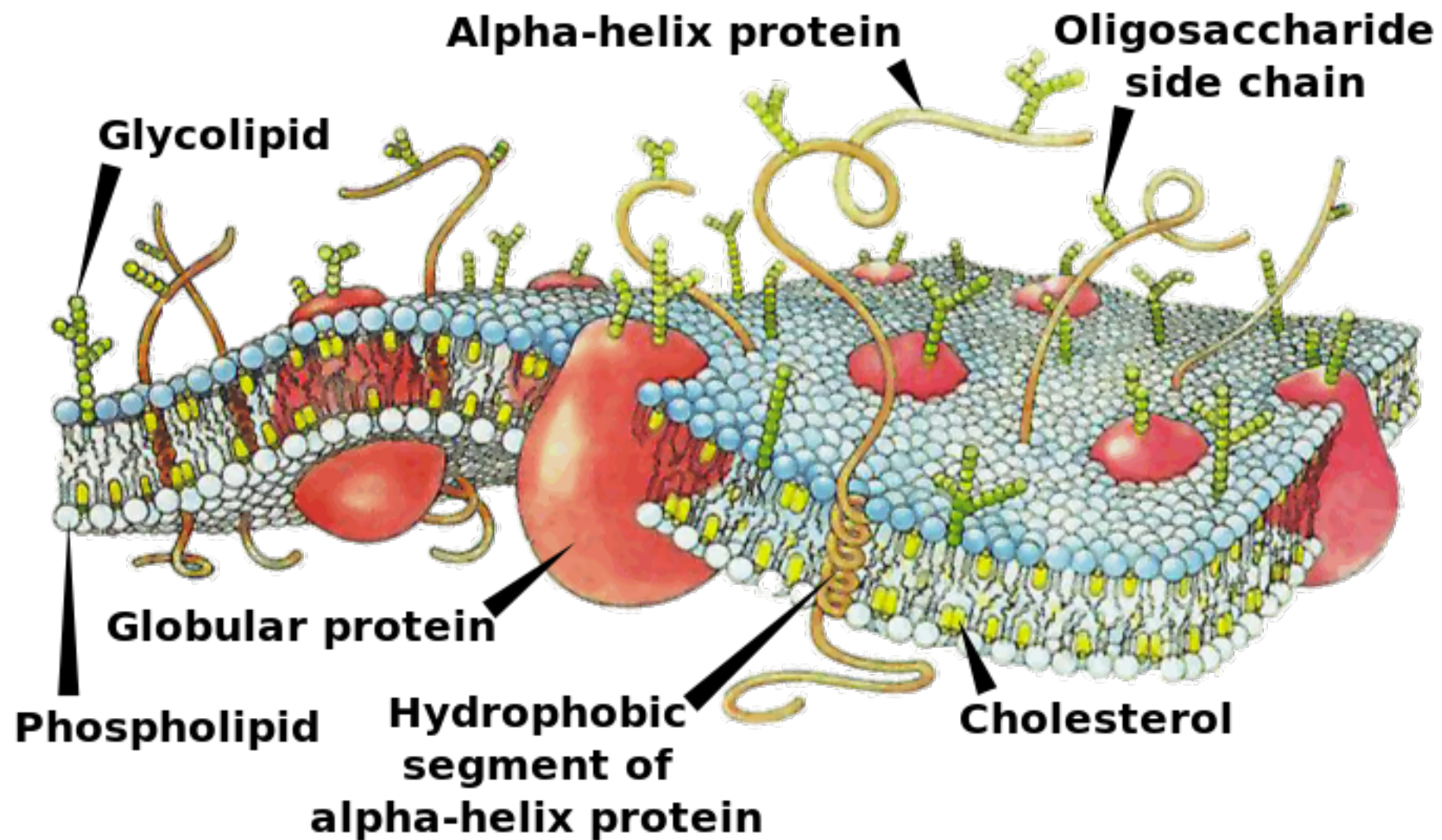
Properties of spiking:



We seek a quantitative description of this behavior:



Some basics:



chalkboard interlude

The Hodgkin-Huxley model:

Sir Alan Hodgkin



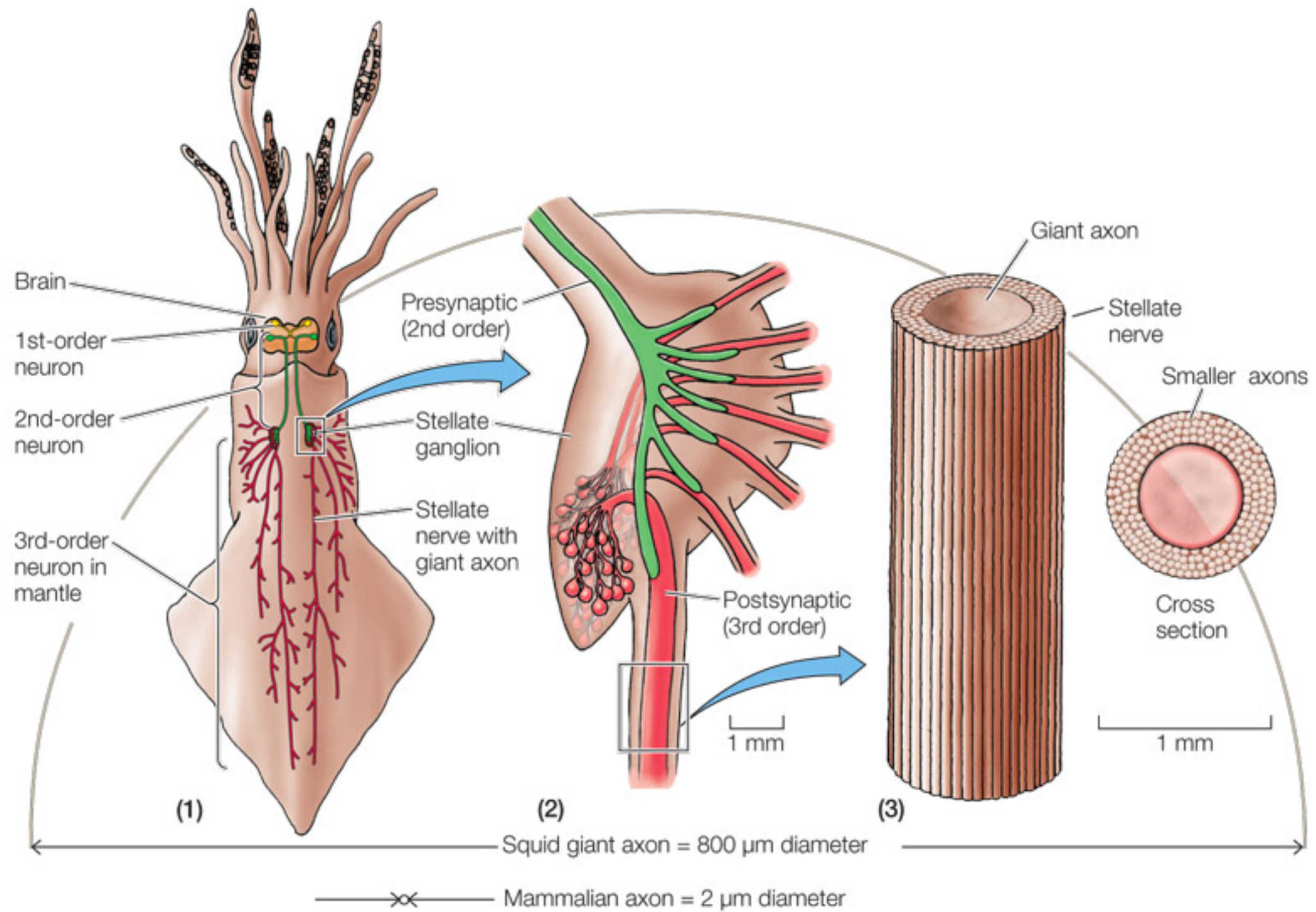
1914-1998
Nobel Prize 1963

Sir Andrew Huxley

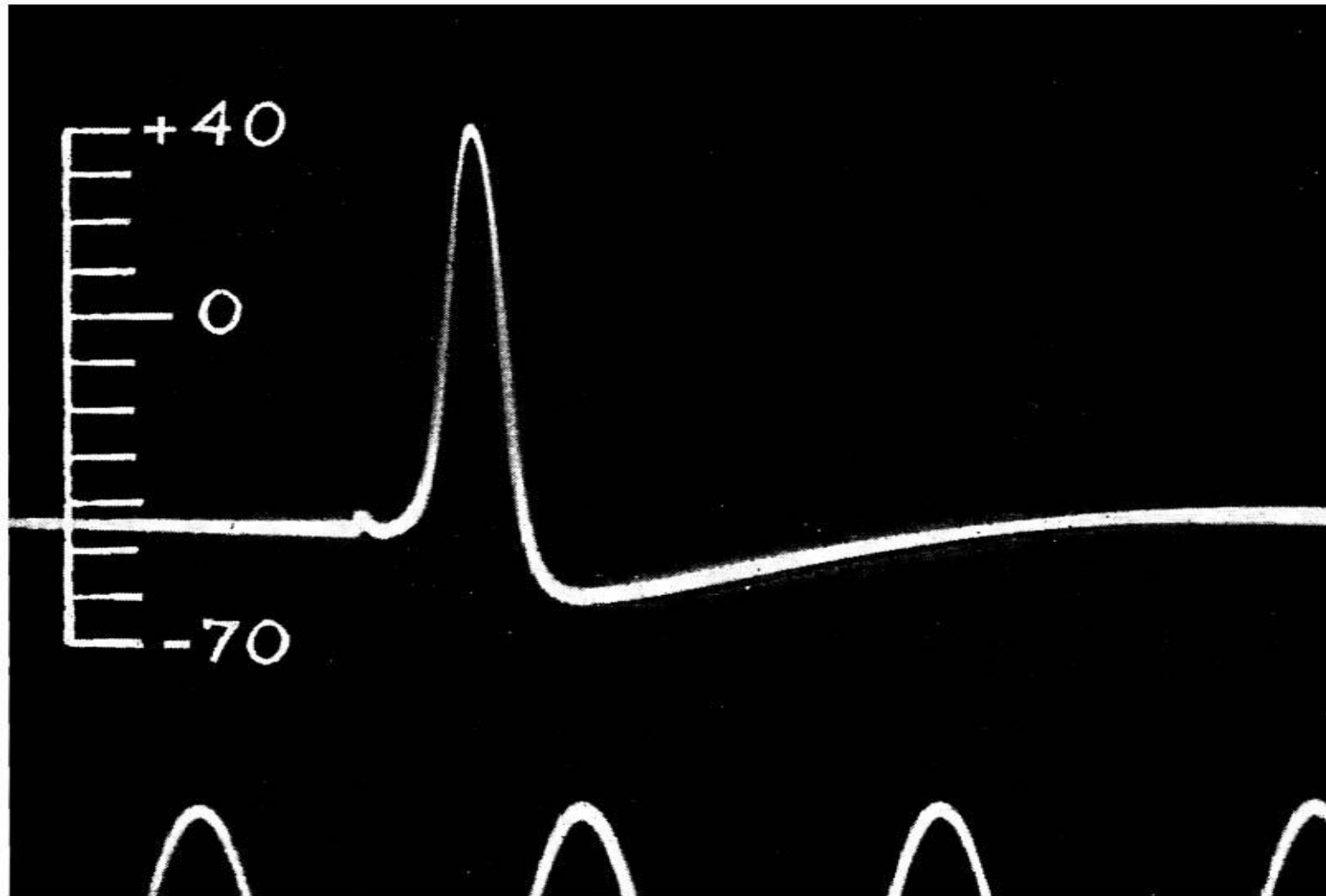


1917-2012
Nobel Prize 1963

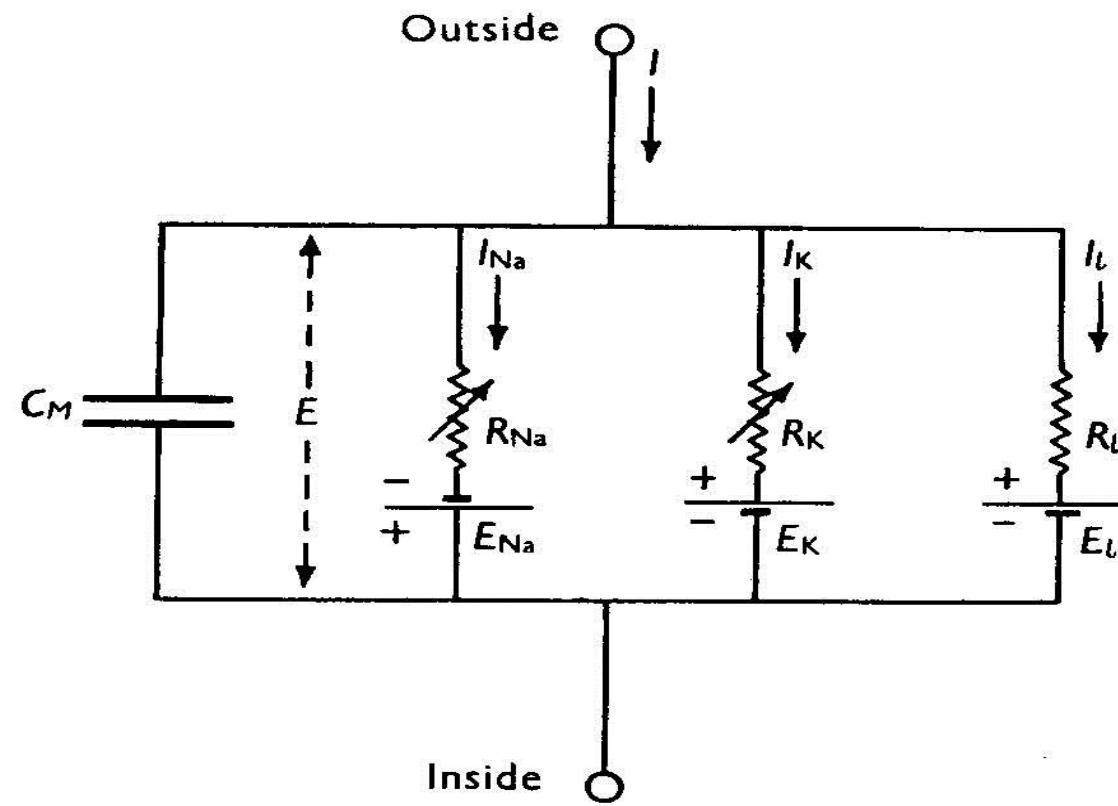
Squid giant axon:



The 1939 letter to Nature:



The final model:



Hodgkin & Huxley (1952), *J. Physiol.* 117:400.

$$C_m \frac{dV}{dt} = -g_L (V - V_L) - \bar{g}_{Na} m^3 h (V - V_{Na}) - \bar{g}_K n^4 (V - V_K)$$

$$\frac{dm}{dt} = \alpha_m(V)(1-m) - \beta_m(V)m$$

$$\alpha_m = 0.1(V_m + 35.0) / (1 - e^{-(V_m + 35.0)/10.0})$$

$$\beta_m = 4.0 e^{-(V_m + 60.0)/18.0}$$

$$\frac{dh}{dt} = \alpha_h(V)(1-h) - \beta_h(V)h$$

$$\alpha_h = 0.07 e^{-(V_m + 60.0)/20.0}$$

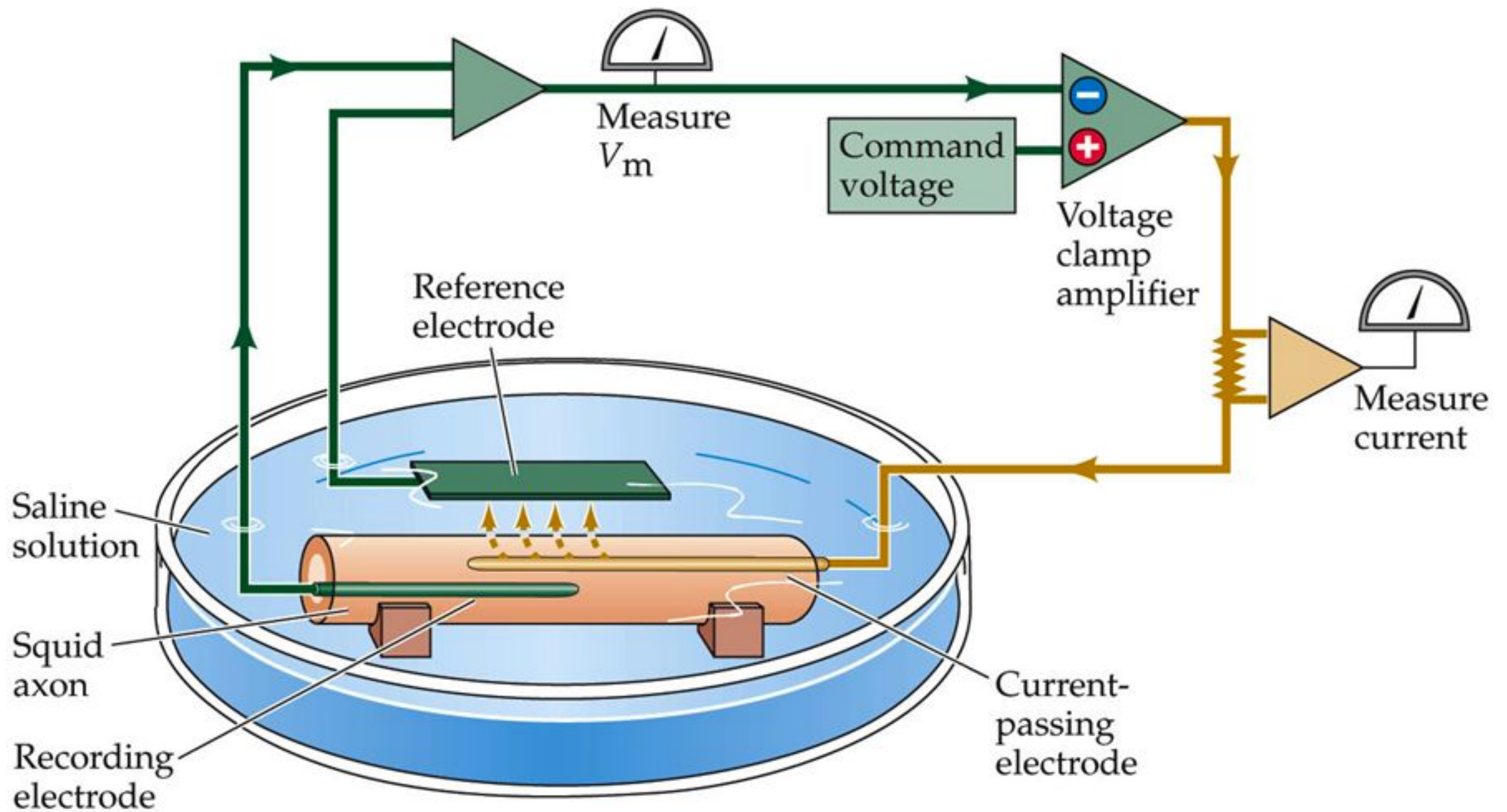
$$\beta_h = 1. / (1 + e^{-(V_m + 30.0)/10.0})$$

$$\frac{dn}{dt} = \alpha_n(V)(1-n) - \beta_n(V)n$$

$$\alpha_n = 0.01(V_m + 50.0) / (1 - e^{-(V_m + 50.0)/10.0})$$

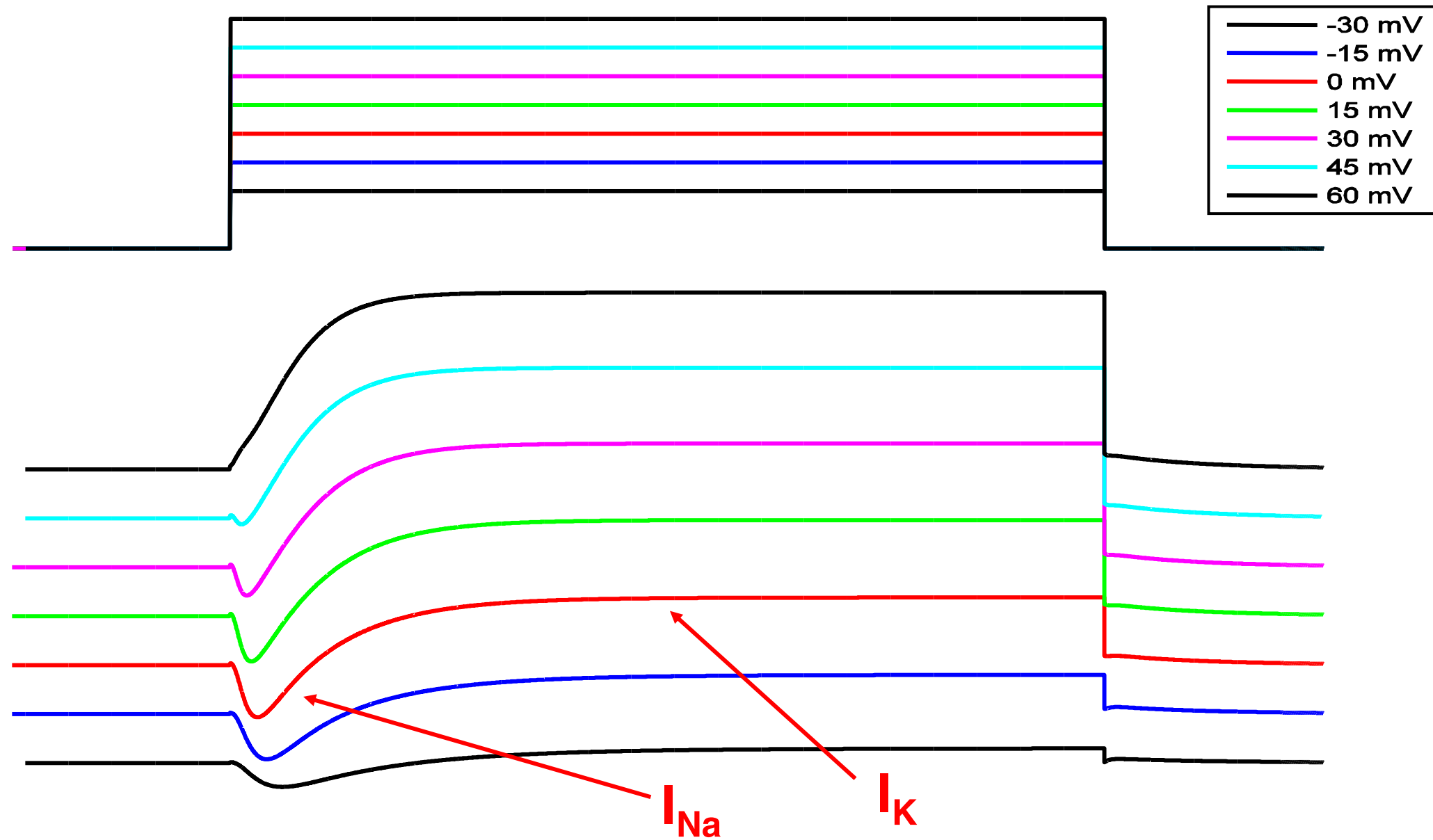
$$\beta_n = 0.125 e^{-(V_m + 60.0)/80.0}$$

Box 3A The Voltage Clamp Technique



chalkboard interlude

Make recordings, separate currents:



...and get conductances:



chalkboard interlude

Structure of the potassium ion channel (tetramer)

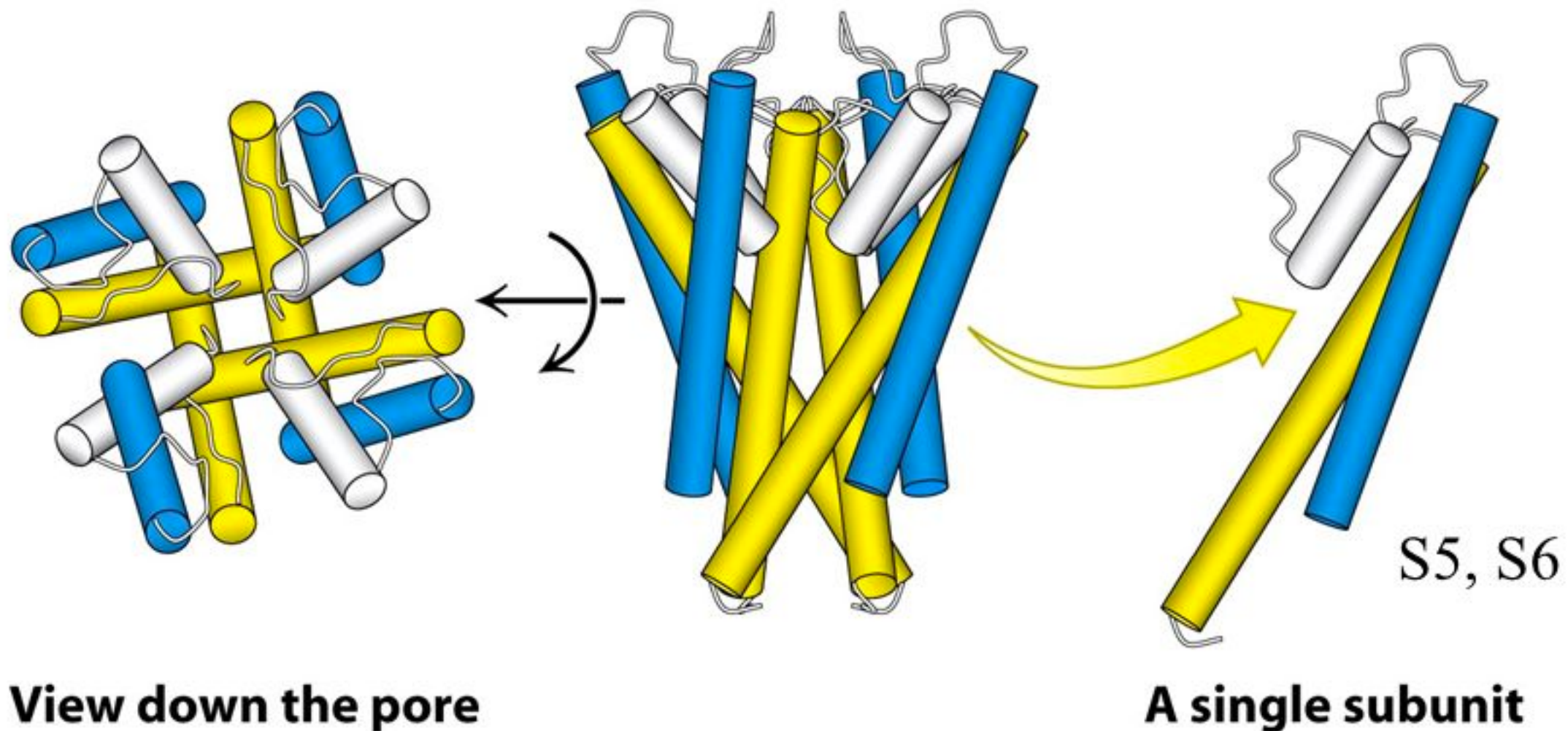
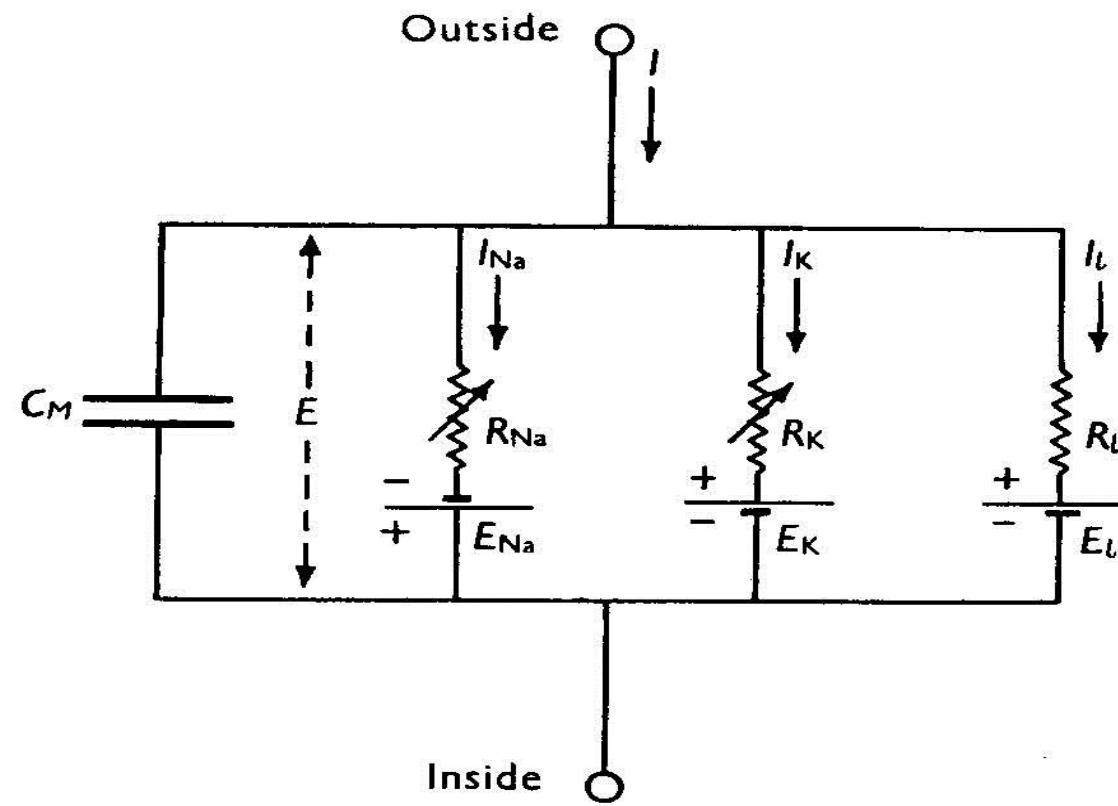


Figure 13-17
Biochemistry, Sixth Edition
© 2007 W. H. Freeman and Company

The final model:



Hodgkin & Huxley (1952), *J. Physiol.* 117:400.

$$C_m \frac{dV}{dt} = -g_L (V - V_L) - \bar{g}_{Na} m^3 h (V - V_{Na}) - \bar{g}_K n^4 (V - V_K)$$

$$\frac{dm}{dt} = \alpha_m(V)(1 - m) - \beta_m(V)m$$

$$\alpha_m = 0.1(V_m + 35.0) / (1 - e^{-(V_m + 35.0)/10.0})$$

$$\beta_m = 4.0 e^{-(V_m + 60.0)/18.0}$$

$$\frac{dh}{dt} = \alpha_h(V)(1 - h) - \beta_h(V)h$$

$$\alpha_h = 0.07 e^{-(V_m + 60.0)/20.0}$$

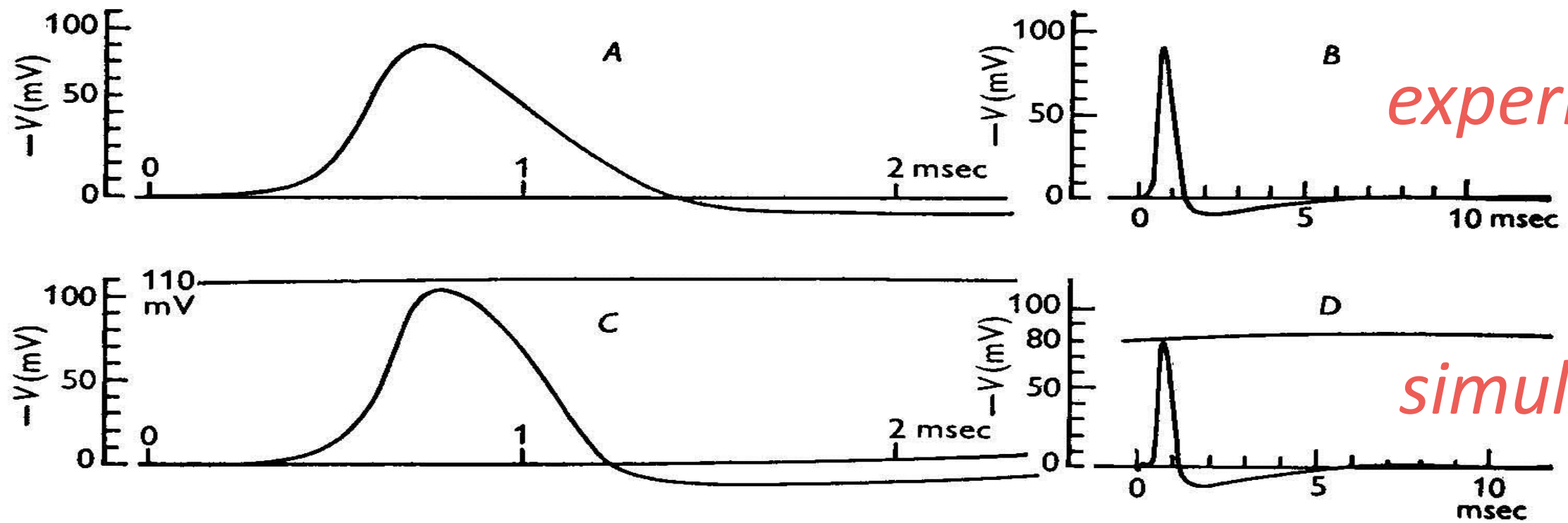
$$\beta_h = 1. / (1 + e^{-(V_m + 30.0)/10.0})$$

$$\frac{dn}{dt} = \alpha_n(V)(1 - n) - \beta_n(V)n$$

$$\alpha_n = 0.01(V_m + 50.0) / (1 - e^{-(V_m + 50.0)/10.0})$$

$$\beta_n = 0.125 e^{-(V_m + 60.0)/80.0}$$

...works well:



The Fitzhugh-Nagumo model:

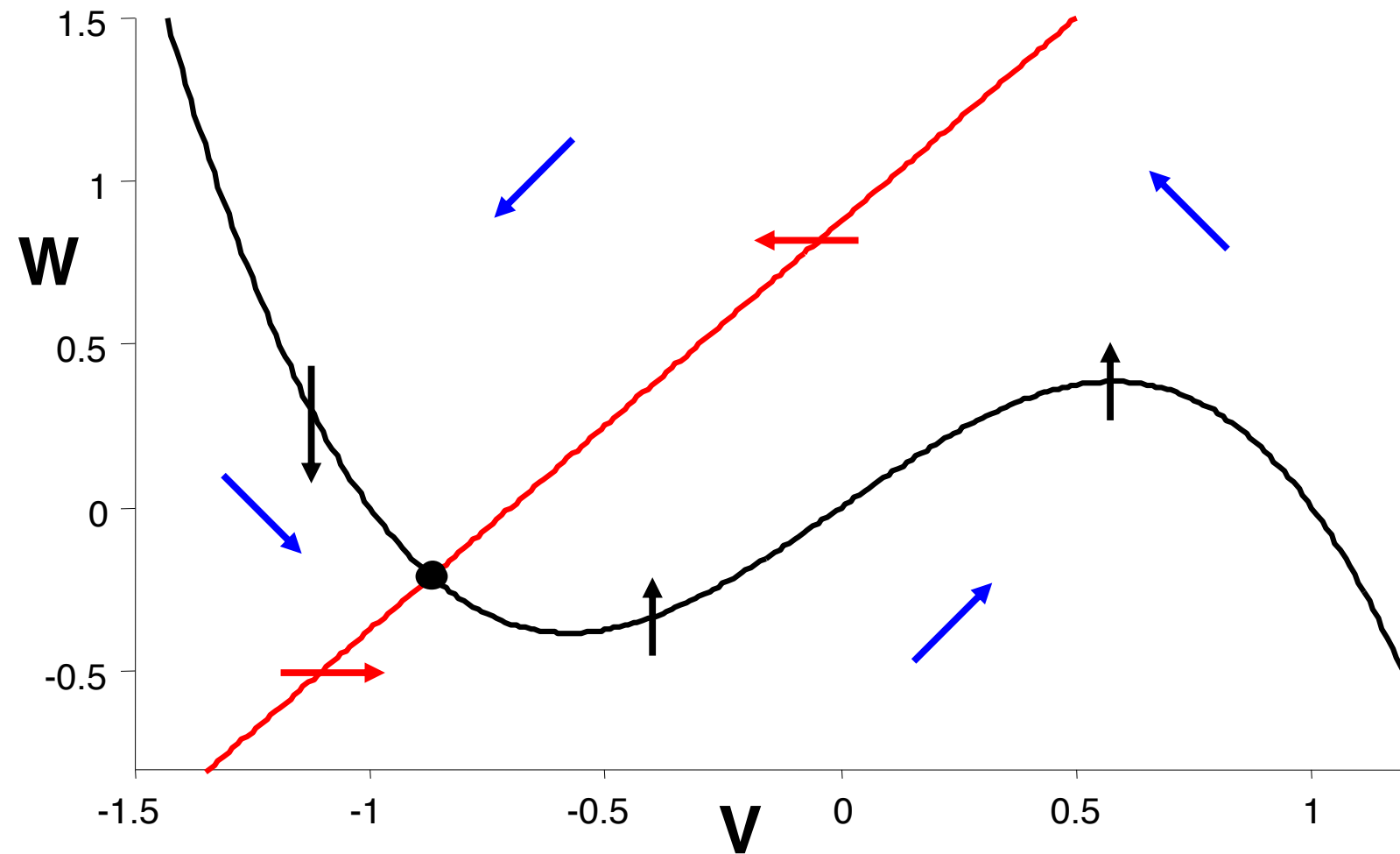


$$dV/dt = V - V^3 - W - I$$

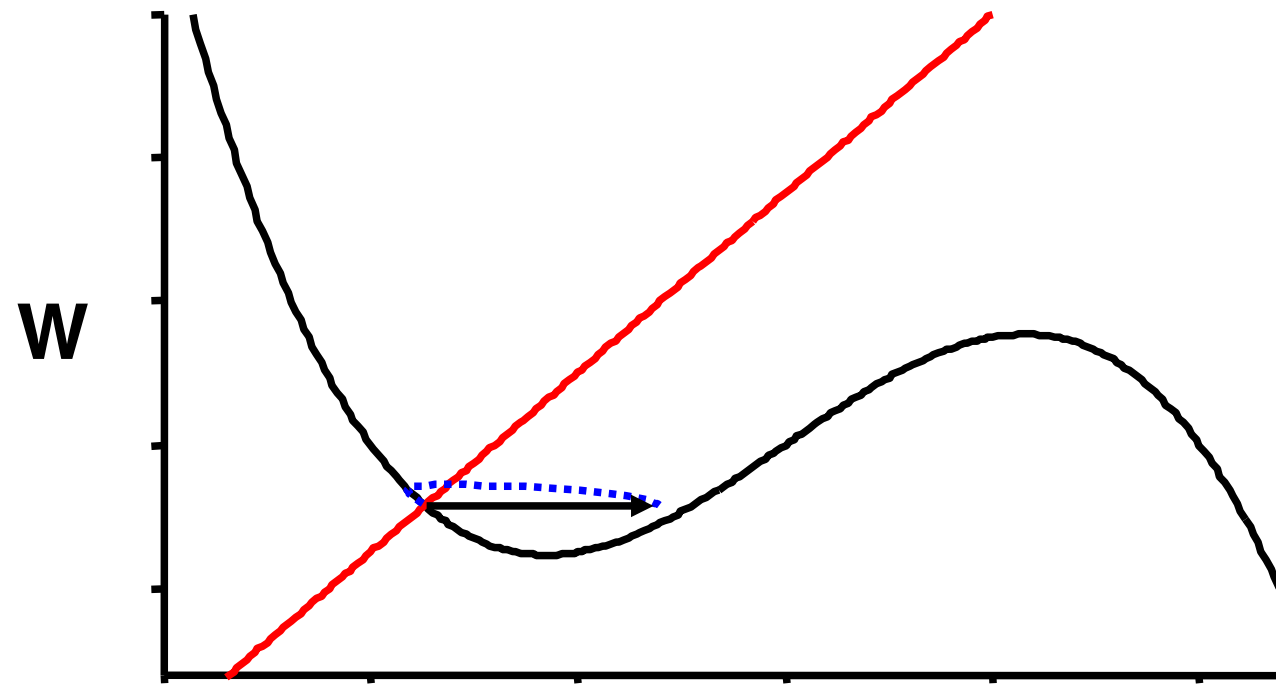
$$dW/dt = 0.08*(V + 0.7 - 0.8W)$$



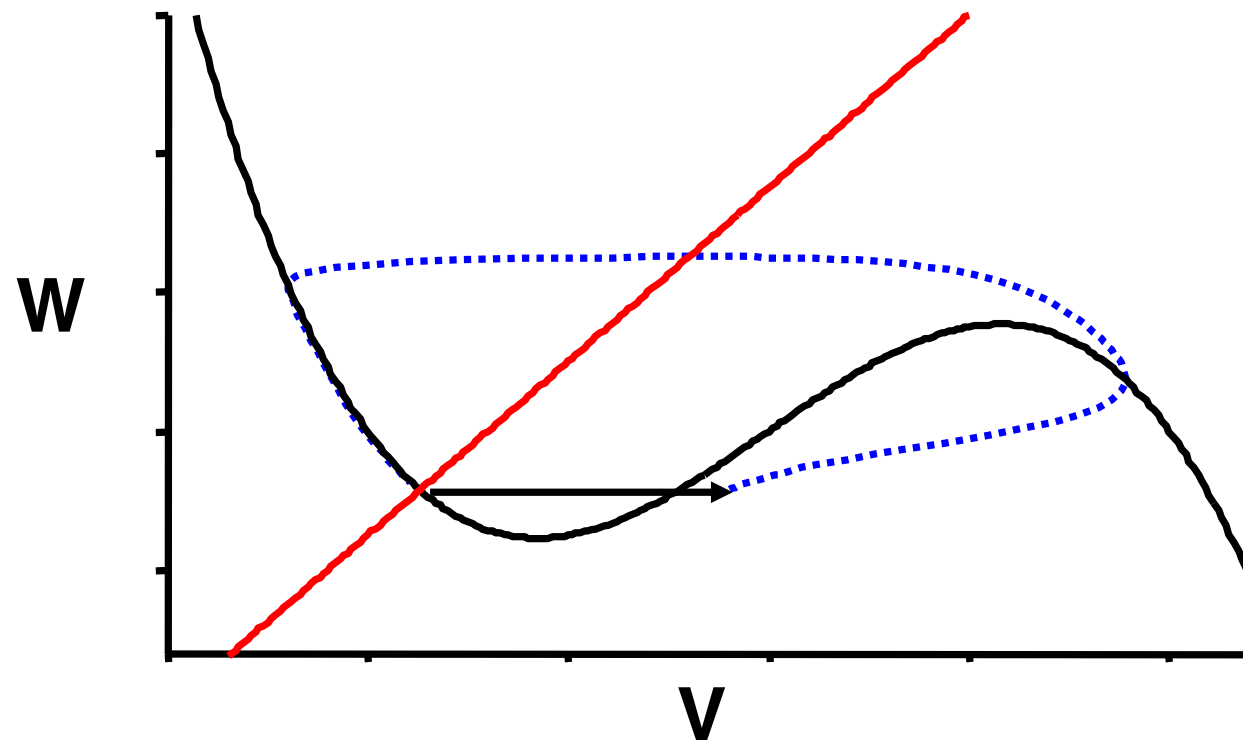
The Fitzhugh-Nagumo model is a useful simplification:



The Fitzhugh-Nagumo model is a useful simplification:



return to baseline



spike!

Even explains sustained firing!

