# TTIC 31230, Fundamentals of Deep Learning

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Deep Learning Frameworks

### Deep Learning Frameworks

A framework provides a high level language for writing models  $P_{\Phi}(y|x)$ .

A framework compiles a model into an optimization algorithm.

$$\Phi^* \approx \underset{\Phi}{\operatorname{argmin}} E_{(x,y) \sim \operatorname{Train}} - \ln P_{\Phi}(y|x)$$

A framework also typically provides support for managing large training sets and pre-trained model parameter values (also called "models").

#### Some Frameworks

- PyTorch
- Tensorflow
- Keras
- Microsoft Cogntive Toolkit
- Chainer

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• EDF (Educational Framework in Python/NumPy for earlier versions of this class).

### An Example

We consider the problem of taking an input x (such as an image of a hand written digit) and classifying it into some small number of classes (such as the digits 0 through 9) using a multi layer perceptron (MLP).

#### Multiclass Classification

Assume a population distribution on pairs (x, y) for  $x \in \mathbb{R}^d$  and  $y \in \{y_1, \dots, y_k\}$ .

For MNIST x is a  $28 \times 28$  image which we take to be a 784 dimensional vector giving  $x \in \mathbb{R}^{784}$ .

For MNIST k = 10.

Let Train be a sample  $(x_0, y_0), \ldots, (x_{N-1}, y_{N-1})$  drawn IID from the population.

## A Multi Layer Perceptron (MLP)

$$h = \sigma \left( W^0 x - b^0 \right)$$

$$s = \sigma \left( W^1 h - b^1 \right)$$

$$P_{\Phi}[\hat{y}] = \text{softmax } s[\hat{y}]$$

 $W^1$  and  $W^2$  are matrices.  $b_1$  and  $b_2$  are vectors.

 $\sigma$  is a scalar-to-scalar activation function applied to each component of a vector.

#### **Activation Functions**

An activation function  $\sigma : \mathbb{R} \to \mathbb{R}$  (scalar-to-scalar) is applied to each component of a vector.

$$\sigma(u) = \frac{1}{1+e^{-u}}$$
,  $\sigma(m) = P(y|m)$  for margin  $m$ .

other common activation functions are

$$ReLU(u) = max(0, u), tanh(u) = 2\sigma(u) - 1$$

#### The Framework Source Code

The source code is a sequence of assignment statements taking as input a training point, typically  $\langle x, y \rangle$ , and outputs a loss value  $\mathcal{L}$ , typically  $-\ln P_{\Phi}(y|x)$ .

$$\mathbf{h} = \sigma \left( W^0 \mathbf{x} - b^0 \right)$$

$$\mathbf{s} = \sigma \left( W^1 \mathbf{h} - b^1 \right)$$

$$P[\hat{y}] = \operatorname{softmax}_{\hat{y}} s[\hat{y}]$$

$$\mathcal{L} = -\ln P[y]$$

#### Source Code

$$h = \sigma \left( W^{0}x - b^{0} \right)$$

$$s = \sigma \left( W^{1}h - b^{1} \right)$$

$$P[\hat{y}] = \operatorname{softmax}_{\hat{y}} s[\hat{y}]$$

$$\mathcal{L} = -\ln P[y]$$

The source code is sometimes called a **computational graph**. I prefer to call it the source code.

#### Source Code

$$egin{aligned} m{h} &= \sigma \left( W^0 m{x} - b^0 
ight) \ m{s} &= \sigma \left( W^1 m{h} - b^1 
ight) \ P_{\Phi}[\hat{y}] &= \operatorname{softmax}_{\hat{y}} \, m{s}[\hat{y}] \ \mathcal{L} &= -\ln P[y] \end{aligned}$$

The framework automatically computes  $\nabla_{\Phi} \mathcal{L}_{\Phi}(\langle x, y \rangle)$  where  $\Phi = (W^0, b^0, W^1, b^1)$ .

## Frameworks Automate Stochastic Gradient Descent (SGD)

$$\Phi^* = \underset{\Phi}{\operatorname{argmin}} E_{z \sim \operatorname{Train}} \mathcal{L}_{\Phi}(z)$$

- 1. Randomly Initialize  $\Phi$  (initialization is important and must be done with care).
- 2. Repeat until "converged":
  - draw  $z \sim$  Train at random.
  - $\bullet \Phi = \eta \nabla_{\Phi} \mathcal{L}_{\Phi}(z)$

## **Epochs**

In practice we cycle through the training data visiting each training pair once.

One pass through the training data is called an **Epoch**.

### Summary

A framework provides a high level language for defining  $\mathcal{L}_{\Phi}(z)$ .

The framework compiles the source code for  $\mathcal{L}_{\Phi}(z)$  into an optimization algorithm.

$$\Phi^* = \underset{\Phi}{\operatorname{argmin}} E_{z \sim \operatorname{Train}} \mathcal{L}_{\Phi}(z)$$

## $\mathbf{END}$