

$$y_t = [x_{1t}, x_{2t}, \dots, x_{nt}] \cdot \begin{bmatrix} \beta_{1t} \\ \beta_{2t} \\ \vdots \\ \beta_{nt} \end{bmatrix} + e_t$$

A digression to show an example.

$$5 = \begin{bmatrix} 1, 7, -3 \end{bmatrix} \begin{bmatrix} a \\ b \\ c \end{bmatrix}$$

$$\begin{bmatrix} \beta_{1t} \\ \beta_{2t} \\ \vdots \\ \beta_{nt} \end{bmatrix} = \begin{bmatrix} \mu_1 \\ \mu_2 \\ \vdots \\ \mu_n \end{bmatrix} + \begin{bmatrix} f_{11} & f_{12} & \dots & f_{1n} \\ f_{21} & f_{22} & \dots & f_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ f_{n1} & f_{n2} & \dots & f_{nn} \end{bmatrix} \begin{bmatrix} \beta_{1(t-1)} \\ \beta_{2(t-1)} \\ \vdots \\ \beta_{n(t-1)} \end{bmatrix} + \begin{bmatrix} v_{1t} \\ v_{2t} \\ \vdots \\ v_{nt} \end{bmatrix}$$

$$\begin{bmatrix} v_1 \\ v_2 \\ \vdots \\ v_n \end{bmatrix} \sim N \left(\begin{bmatrix} 0 \\ 0 \\ \vdots \\ 0 \end{bmatrix}, \begin{bmatrix} \text{cov}(v_1, v_1) & \text{cov}(v_1, v_2) & \dots & \text{cov}(v_1, v_n) \\ \text{cov}(v_2, v_1) & \text{cov}(v_2, v_2) & \dots & \text{cov}(v_2, v_n) \\ \vdots & \vdots & \ddots & \vdots \\ \text{cov}(v_n, v_1) & \text{cov}(v_n, v_2) & \dots & \text{cov}(v_n, v_n) \end{bmatrix} \right)$$

et $\sim N(0, R)$

$$m = E(x)$$

$$E((x-m)(x-m)) = E((x-m)^2)$$

$$b_t = \mu + F B_{\{t-1\}} + v_t$$

$$E(b_t) = \mu + F E(b_{\{t-1\}}) + E(v_t)$$

$$E(b_t | t-1) = b_t | t-1$$

$$E(b_t | t-1) = \mu + F E(b_{\{t-1\}} | t-1)$$

$$b_t | t-1 = \mu + F b_{\{t-1\}} | t-1$$