
1.2 Questions

1. Write a function `remove_duplicates` that takes as input a sorted linked list of integers, `lnk`, and mutates `lnk` so that all duplicates are removed.

```
def remove_duplicates(lnk):  
    """  
    >>> lnk = Link(1, Link(1, Link(1, Link(1, Link(5)))))  
    >>> unique = remove_duplicates(lnk)  
    >>> len(unique)  
    2  
    >>> len(lnk)  
    2  
    """
```

2. Define `reverse`, which takes in a linked list and reverses the order of the links. The function may *not* return a new list; it must mutate the original list. Return a pointer to the head of the reversed list.

```
def reverse(lnk):  
    """  
    >>> a = Link(1, Link(2, Link(3)))  
    >>> r = reverse(a)  
    >>> r.first  
    3  
    >>> r.rest.first  
    2  
    """
```

3. Write `multiply_lnks`, which takes in a Python list of `Link` objects and multiplies them element-wise. It should return a new linked list. If not all of the `Link` objects are of equal length, return a linked list whose length is that of the shortest linked list given. You may assume the `Link` objects are shallow linked lists, and that `lst_of_lnks` contains at least one linked list.

```
def multiply_lnks(lst_of_lnks):  
    """  
    >>> a = Link(2, Link(3, Link(5)))  
    >>> b = Link(6, Link(4, Link(2)))  
    >>> c = Link(4, Link(1, Link(0, Link(2))))  
    >>> p = multiply_lnks([a, b, c])  
    >>> p.first  
    48  
    >>> p.rest.first  
    12  
    >>> p.rest.rest.rest  
    ()  
    """
```

2 Midterm Review

1. Define a function `foo` that takes in a list `lst` and returns a new list that keeps only the even-indexed elements of `lst` and multiplies each of those elements by the corresponding index.

```
def foo(lst):
```

```
    """
```

```
    >>> x = [1, 2, 3, 4, 5, 6]
```

```
    >>> foo(x)
```

```
    [0, 6, 20]
```

```
    """
```

```
    return [_____]
```

2. Implement the functions `max_product`, which takes in a list and returns the maximum product that can be formed using nonconsecutive elements of the list. The input list will contain only numbers greater than or equal to 1.

```
def max_product(lst):
```

```
    """Return the maximum product that can be formed using lst
    without using any consecutive numbers
```

```
    >>> max_product([10,3,1,9,2]) # 10 * 9
```

```
    90
```

```
    >>> max_product([5,10,5,10,5]) # 5 * 5 * 5
```

```
    125
```

```
    >>> max_product([])
```

```
    1
```

```
    """
```

3. An **expression tree** is a tree that contains a function for each non-leaf root, which can be either '+' or '*'. All leaves are numbers. Implement `eval_tree`, which evaluates an expression tree to its value. You may want to use the functions `sum` and `prod`, which take a list of numbers and compute the sum and product respectively.

```
def eval_tree(tree):  
    """Evaluates an expression tree with functions as root  
>>> eval_tree(tree(1))  
1  
>>> expr = tree('*', [tree(2), tree(3)])  
>>> eval_tree(expr)  
6  
>>> eval_tree(tree('+', [expr, tree(4), tree(5)]))  
15  
"""
```

4. The **quicksort** sorting algorithm is an efficient and commonly used algorithm to order the elements of a list. We choose one element of the list to be the **pivot** element and partition the remaining elements into two lists: one of elements less than the pivot and one of elements greater than the pivot. We recursively sort the two lists, which gives us a sorted list of all the elements less than the pivot and all the elements greater than the pivot, which we can then combine with the pivot for a completely sorted list.

First, implement the `quicksort_list` function. Choose the first element of the list as the pivot. You may assume that all elements are distinct.

```
def quicksort_list(lst):
    """
    >>> quicksort_list([3, 1, 4])
    [1, 3, 4]
    """

    if _____:
        _____

    pivot = lst[0]

    less = _____

    greater = _____

    return _____
```

5. We can also use quicksort to sort linked lists! Implement the `quicksort_link` function, without constructing additional `Link` instances.

You can assume that the `extend_links` function is already defined. It takes two linked lists and mutates the first so that the ending node points to the second. `extend_link` returns the head of the first linked list.

```
>>> l1, l2 = Link(1, Link(2)), Link(3, Link(4))
>>> l3 = extend_links(l1, l2)
>>> l3
Link(1, Link(2, Link(3, Link(4))))
>>> l1 is l3
True
```

```
def quicksort_link(link):
```

```
    """
```

```
    >>> s = Link(3, Link(1, Link(4)))
```

```
    >>> quicksort_link(s)
```

```
    Link(1, Link(3, Link(4)))
```

```
    """
```

```
    if _____:
```

```
        return link
```

```
    pivot, _____ = _____
```

```
    less, greater = _____
```

```
    while link is not Link.empty:
```

```
        curr, rest = link, link.rest
```

```
        if _____:
```

```
            _____
```

```
        else:
```

```
            _____
```

```
        link = _____
```

```
    less = _____
```

```
    greater = _____
```

```
    _____
```

```
    return _____
```

6. Implement `widest_level`, which takes a `Tree` instance and returns the elements at the depth with the most elements.

```
def widest_level(t):
    """
    >>> sum([[1], [2]], [])
    [1, 2]
    >>> t = Tree(3, [Tree(1, [Tree(1), Tree(5)]),
    ...             Tree(4, [Tree(9, [Tree(2)])])])
    >>> widest_level(t)
    [1, 5, 9]
    """
    levels = []
    x = [t]

    while _____:
        _____

        _____ = sum(_____, [])

    return max(levels, key=_____)
```

7. Complete `redundant_map`, which takes a tree `t` and a function `f`, and applies `f` to the node (2^d) times, where d is the depth of the node. The root has a depth of 0.

```
def redundant_map(t, f):
    """
    >>> double = lambda x: x*2
    >>> tree = Tree(1, [Tree(1), Tree(2, [Tree(1, [Tree(1)])])])
    >>> print_levels(redundant_map(tree, double))
    [2] # 1 * 2 ^ (1) ; Apply double one time
    [4, 8] # 1 * 2 ^ (2), 2 * 2 ^ (2) ; Apply double two times
    [16] # 1 * 2 ^ (2 ^ 2) ; Apply double four times
    [256] # 1 * 2 ^ (2 ^ 3) ; Apply double eight times
    """
    t.root = _____

    new_f = _____

    t.branches = _____

    return t
```