3.11 Sum-of-minterms form

Sum-of-minterms

Different equations may represent the same function. Ex: y = a + b, and y = a + a'b, represent the same function. The samer obvious, so a standard equation form is desirable.

- A canonical form of a Boolean equation is a standard equation form for a function.
- **Sum-of-minterms** form is a canonical form of a Boolean equation where the right-side expression is a sum-of-product product a unique minterm.
- A *minterm* is a product term having exactly one literal for every function variable.
- A *literal* is a variable appearance, in true or complemented form, in an expression, such as b, or b'.

For a function of variables a and b, y = ab + a'b + a'b' is in sum-of-minterms form, but y = ab + a' is not because the second missing variable b.

PARTICIPATION ACTIVITY	3.11.1: Minterms.	
Given a function of a, b, c.		
1) Does abc have 3 literals?		
O Yes		
O No		
2) Does ab'c have 4 literals?		
O Yes		
O No		

- 3) Is bc' a product term?
 - O Yes
 - O No
- 4) Is bc' a minterm?
 - O Yes
 - O No
- 5) Is ab'c a minterm?
 - O Yes
 - O No
- 6) Is a(b + c') a minterm?
 - O Yes
 - O No

PARTICIPATION ACTIVITY

3.11.2: Sum-of-minterms form.

Given a function of a, b, c, indicate if the equation is in sum-of-minterms form.

- 1) y = abc + a'b'c'
 - O Yes
 - O No
- 2) y = ab + abc
 - O Yes
 - O No
- 3) y = a(b + c)

O Yes O No		
4) y = abc		_
O Yes O No		
5) y = acO YesO No		•
6) y = abc + cb'a O Yes		•
O No7) y = abc + abcO Yes		_
O No		

Transforming to sum-of-minterms

A sum-of-products equation can be transformed to sum-of-minterms by multiplying each product term by (v + v') for any r to create minterm (removing redundant minterms). v + v' is 1, so multiplying a term by (v + v') doesn't change a product term by:

y = ab + a'	sum-of-products, but not sum-of-minterms
y = ab + a'(b + b')	
y = ab + a'b + a'b'	sum-of-minterms

An equation not initially in sum-of-products form can first be multiplied out. Thus, transforming an equation to sum-of-mint

- Initially multiplying out to sum-of-products
- Transform each product term to a minterm
- Remove redundant minterms

PARTICIPATION ACTIVITY

3.11.3: Transforming to sum-of-minterms.

Start

2x speed

Given variables a, b, c. Convert y = a(b + bc') to sum-of-minterms.

$$y = a(b + bc')$$

$$=ab(1) + abc'$$

$$= ab(c + c') + abc'$$

PARTICIPATION ACTIVITY

3.11.4: Transforming an equation already in sum-of-products form to sum-ofminterms.



Given variables a, b. Order the steps to transform y = ab + a' to sum of minterms.

$$v = ab + a'b + a'b'$$

$$v = ab + a'(1)$$

$$y = ab + a'b + a'b'$$
 $y = ab + a'(1)$ $y = ab + a'(b + b')$ $y = ab + a'$

Original equation

- (1)
- (2)
- (3)

Reset

PARTICIPATION ACTIVITY

3.11.5: Transforming a general equation to sum-of-minterms form.

Given variables a, b, c. Order the steps to transform y = (a + c)b to sum-of-minterms.

$$y = ab + bc$$
 $y = a'bc + abc' + abc$ $y = ab(1) + bc(1)$ $y = abc + abc' + abc + a'bc$

$$y = ab(c + c') + bc(a + a')$$
 $y = (a + c)b$

Original equation

- (1)
- (2)
- (3)

(4)

(5)

Reset

Note: Transforming directly from ab to ab(c + c') is a common shortcut. The intermediate step, ab to ab(1), is often omitted

PARTICIPATION ACTIVITY

3.11.6: Transforming to sum-of-minterms form.

Given variables a, b, c. Transform each equation to sum-of-minterms form. Type only the?

- 1) y = a'b
 - y = a'b(1)
 - y = a'b(c + c')
 - y = a'bc + ?

Check

Show answer

- 2) y = ac
 - y = ac(1)
 - y = ac(b + ?)

Check

Show answer

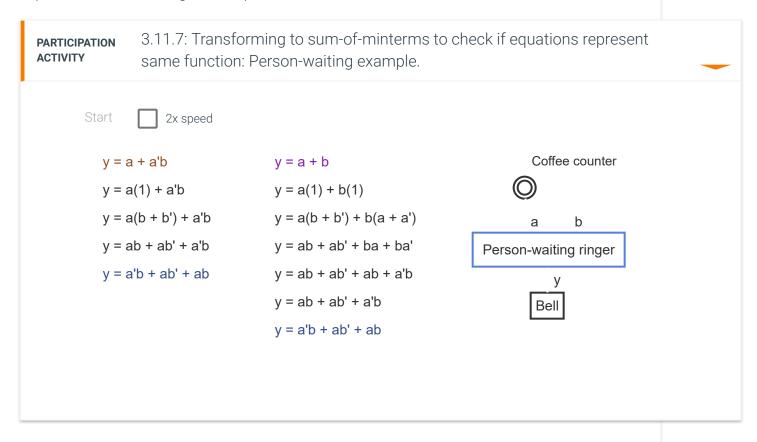
3) y = a'c'

$$y = a'c'(b + ?)$$

Check Show answer

Example: Determining if two equations represent the same function

Because sum-of-minterms is canonical, one can determine whether two equations represent the same function by transfor sum-of-minterms equations and checking if the equations are the same.



Compact function notation: Minterm numbers

A compact function notation represents each minterm by a number. Given that ab'c is 1 if a/b/c are 1/0/1, that minterm is m_5 because 101 in binary is 5 in decimal. A 3-variable function thus has minterms numbered 0 to 7. Ex: f(a,b,c) = a'b'c' + ab'

written compactly as f(a,b,c) = m0 + m5 + m7. An alternative notation is $f(a,b,c) = \sum (0, 5, 7)$.

PARTICIPATION ACTIVITY

3.11.8: Numbered minterms.

Match the minterms.

m5 m1 m2 m0 m6

a'bc'

a'b'c'

a'b'c

ab'c

abc'

Reset

PARTICIPATION ACTIVITY

3.11.9: Compact function notation.

- 1) Given f(a, b, c) = a'bc + abc, the compact notation is: f(abc) = ?
 - Om3+m7
 - Om4+m0

Cannot determine

2) Given f(a, b, c) = ab, the compact notation is: f(abc) = ?

- **O** m3
- Om6+m7
- O Cannot determine

The compact form makes comparing equations for equivalence especially easy.

CHALLENGE ACTIVITY 3.11.1: Transform the equation to a sum-of-minterms.

Start

Video: How to use this activity

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