multinomial example constrained premetes in Multinomial (degrees of fredom) [sum to unity] -HOW (K1) MSUMMelian Exported family ref. Q: why do ne go for exponential family reps? 0 - pata and peremetes cleanly grouped into 2 terms monet genesting fraction. $\frac{dA}{dm} = \mathbb{E}[T(x)] \qquad \frac{d^2A}{dm^2} \cdot Var[T(x)]$ - Gives standard operator that yield not only moments (from derivatives of log-normaliser) EX: Moments important -> unabeteise 3: Relationship between moment and natural parametes (*) very- Review moment out canonical pour relation. mult for exponential family - By differes between distrin exp. family at turn of M and I(.) i.e. consider perent and suffice start. - 110 data - log-likelihood - optimise (set 1st orde monet to 0) - monent metching EX: Exponential family exposes the relationship between olden and proceeds through (in a linearly dependent fashion) (through M) Gives into about transformations of older or forms of data ve red to noting about to present miqueness and idulity of distri-- E.g. only store sufficient statistic of data

```
-3 ways of unaptualising relation between: largerelacies)
  X (data) I(x) (suff. statiulic) & (param)
· Banjesian: - Draw enclusions on parameters given data
           - expending of parametes from data
           -use posterior plott(x), x)
Frequentist - Data greated from mknown true value of param.
           - parametes impact data only through suff stat p(x/T(x), 0)
- A influence flows through I(.) for both Bayesian, frequentist
(due to exponential family)
Negran factorisation theorem: 663 > MILI - check you udestand eq.
- exposes sufficiency of 1(x) for paramete 0.
- 1(x) d-separates X and O
(*) pusity estimation for single i.v. for many diff distri family
   -use sufficient statistic, moment notching, exp. family
· More onto 2 nodes
-genealised instance - GUIM
ex: Builds on knowledge of exponential family
- DISCIM-logistic regression; SVMS
 LOA - No it's generative
- Logistic regression - p(y=1/x) = 110-012
Trese cre GUIMS
 - But signaid -) non linearity (take care of by blanket function)
 -contains linear rel. , so ve use linear techniques with above.
 Commonality ():- Itp (Y)=M=f(BTX)
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- O(YIf(X)) - anditional dustry of X -> use exponential family - fl-) is a response function -> the x treated in a linear way (dot product) Q(4): well you inclusted formulation of GVIM (*) () Different choices of p() and f() - convall of 2 node GMS. when pegession that you Logistic nolested MRFS: No y; but exponential family distr. tuse as GUMS RBMS UR. S GUM (wort.) -simple modelling principle: (for mony metant.) Begin from data &

Assure set of parametes & (10 be estimated) & 10 form signed & 4. (*) begin from data x (4) signal & turned into mean paramete of und district output (a response function fl) (*) now pountes and cononical parametes related by 4 (muse transform for relating distribution metand perans and convolital fund. form) (*) use exponential family to get y. - mechanical pipeline (x) work in exponential tond -> lots of lay results · Ex: clear realismship between fl.) and 4(.) - allows concellation' f=4-1(.) - Ambylical simplif (?) was

me for GLIMS -> natural response

-f(-) and y(-) "ancel" -> allows simplified def. of cond. likelihood of output gives input.

wer : eneck this reasoning: - fl- and 4-1(-)

Yields while leaving for constitut GUM and stocketic gradient ascut

@ HOW is 4(-) chosen?

- Given a distri messarce, use default

- conspecify any (?)

-some don't choose 4(-)

(*) S.G.A can be used for any GUIM MORE! (SLOW)

-Baten rearring for GUIM

-Best is Newton's wethool

- requires computation of Hessian

of 4 function

- we already have a library of consnical response functions

IRUS / Menter - Rephson

- Regniles Hessian and gradient of 1055.

- refrance update rule to see now it relates to US loss.

Ext: Spirit is exponedial family and GUIMS use mivesally locks for GM).

of logistic, inneer.

MLE for geneal BNS:-

⁽x) Assume grobal moup of paam; nocus fully observed, accompare BN by decomposing log-likelihood mes a sum of local terms, one per node.

peromposable likelihood of a	3N	
-graphical illustration		
- gungates arelytic decomp	nostion juse of Gula	ulexp. nethods
Ex: flow about 2 parents		umlexp?
- multiplexe function	- ADI	ditive XIXZ
R 2(X2,i) 1=3	- MUH	tiplexer - (previously pop.)
- combine inputs asymmetrical	hy	
$\mathbb{C}\left(\prod_{i=3}^{R} \chi_{i}^{\partial(\chi_{I},i)}\right) \longrightarrow 51ill \ 0$	GUM	
MLE for BIVS with tabuler	CPDS	
- Get simple estimetas (via.	sere poudure)	
5.2020 lecture 5 is a hybrid - so this is technically S.20	of 5.2019 us and 1	rest.)
- POGMS (partially observed GA		
ex: loc useful a prectical	e.g. speech HMMs	(latert/mobs words)
Situations	biologev.	(lotest clustes)
mixture models		
-ovsere x as 2d w-ord. , no	label (2)	
-estmate plz12) generatively	via p(x) p(x/2)	
pecided to pause here: conclu	sed in of 16 5.20	19