#### **GENERAL INFO**

All bnns follow a similar architecture that consists of an input layer with 4 bit features, a hidden layer with 40 neurons and an output layer followed by argmax. The inputs of first layer of the model are not binarized, as that does not leave enough representational ability to enable classification. The outputs of the last layer are also not binarized as they are compared to determine the most propable class.

Designs and models labeled "bnn" are fully connected. Weights and hidden neuron activations are either 1 or -1. Designs and models labeled "tnn" have weights in  $\{-1, 0, 1\}$ . Hidden activations are left as binary, so they are ternary weight networks and not full ternary networks. Instead of using arithmetic with ternary weights they are implemented as sparse bnns, where weights with a value of 0 mean a missing connection.

The first layer is implemented as additions and subtractions of the input features. The second layer is implemented as the sum of the binarized activations xnored by the weights.

Models have been trained with binary and ternary weights for six small datasets with sensor features. For each of the following designs the model of each dataset has been implemented and has been tested to make sure the verilog design picks the same class as the model in python for the first 1000 samples of the dataset. They have been synthesized and the resuting area and power are given for each. If a design is based on a previous design the metrics for both are shown for comparison.

Since bnns are easier to try things with some designs for bnns have no tnn equivelant yet.

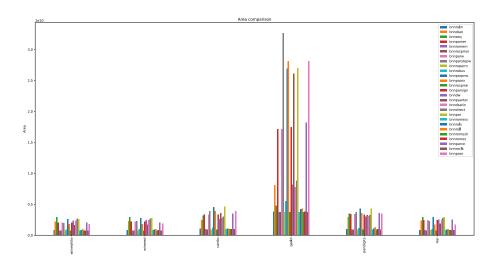
When a design is derived from an earlier design it will be annotated as **EARLIER DESIGN** -> **NEW DESIGN**.

Due to a self-imposed deadline only the descriptions for bnn designs are completed. The descriptions for tnn designs will follow soon.

METRICS
Area in microns

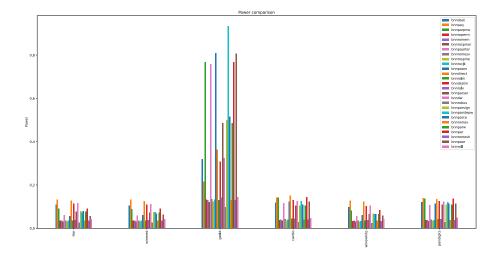
|          | gasId       | winewhite  | cardio     | pendigits  | Har        | winered    |
|----------|-------------|------------|------------|------------|------------|------------|
| bnndw    | 8186903514  | 2398069796 | 2625544276 | 2989958945 | 2538763759 | 2451240647 |
| bnnpaar  | 28155004994 | 1801300497 | 3873514668 | 3542788838 | 1742276623 | 1855123140 |
| bnndsat  | 8104696944  | 2243047476 | 2476688256 | 2978862895 | 2401863926 | 2301503726 |
| bnnrobus | 5539426651  | 955878036  | 1244282486 | 1192648308 | 997044886  | 966295906  |

|             | gasId       | winewhite  | cardio     | pendigits  | Har        | winered    |
|-------------|-------------|------------|------------|------------|------------|------------|
| bnnromem    | 3787005725  | 795724384  | 973538254  | 954620558  | 815933049  | 795551471  |
| bnnromesx   | 3784003792  | 797892993  | 1002634724 | 947374667  | 837521356  | 812703088  |
| bnnparstepw | 32698398388 | 1999572812 | 3928792766 | 3709266179 | 2315518878 | 2278159189 |
| bnnpaarter  | 26137614509 | 1665255587 | 3596909349 | 3222330307 | 1872808096 | 1747020576 |
| bnnparpnw   | 26940613850 | 2586857731 | 4581533966 | 4301046264 | 2915795216 | 2779674503 |
| bnnpaarx    | 28161515912 | 1819920659 | 3878707190 | 3551930192 | 1733307035 | 1843638582 |
| bnnparser   | 17136617736 | 2036496895 | 3321122892 | 3396546062 | 2425075600 | 2186536366 |
| bnnrospinor | 3710576970  | 747786913  | 934543087  | 881331046  | 775932821  | 757033635  |
| bnnpar      | 26976191700 | 2600670967 | 4671425747 | 4294613522 | 2939539015 | 2782322518 |
| bnndsatin   | 7747969288  | 2356646791 | 2810682089 | 3109779691 | 2545317224 | 2429171177 |
| bnnroll     | 4296589691  | 1034974561 | 1118415523 | 1313186365 | 1030487839 | 1020139925 |
| bnnparsign  | 17509279782 | 2047349412 | 3327450493 | 3338288839 | 2451830762 | 2245461263 |
| bnnroclk    | 3740279945  | 757164887  | 978063287  | 944926916  | 813471167  | 781711587  |
| bnnroperm   | 3767065181  | 785042623  | 956446441  | 935021870  | 814428053  | 787104215  |
| bnnrospine  | 3731008262  | 748739199  | 930476830  | 907653792  | 781939782  | 760587951  |
| bnnromesh   | 3762552965  | 778943884  | 967400533  | 943117202  | 811382778  | 799002613  |
| bnndirect   | 8862217257  | 2731200293 | 3049513878 | 3293137497 | 2763413176 | 2711150360 |
| bnnparw     | 17136617736 | 2036496895 | 3321122892 | 3396546062 | 2425075600 | 2186536366 |
| bnnrolx     | 4212096283  | 864705835  | 1109597201 | 1069429557 | 914303937  | 885090188  |
| bnnromex    | 3797082992  | 796969544  | 975525744  | 966093815  | 822660672  | 810091571  |
| bnnseq      | 4767284030  | 2974950246 | 3146979597 | 3471397032 | 2954896914 | 2957271954 |
| bnnrolin    | 3854120055  | 799945409  | 1085099120 | 1036541150 | 829139916  | 804058285  |
| bnnparce    | 18182298639 | 2047575794 | 3484390096 | 3573660077 | 2499410773 | 2076451308 |

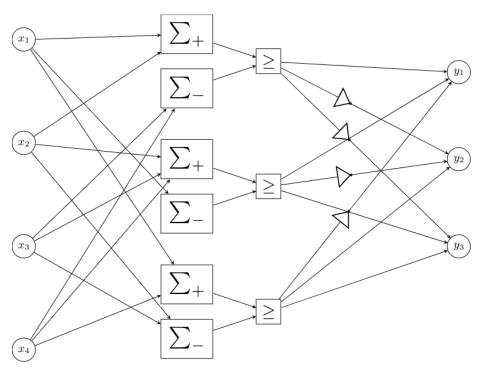


Power in Watt

|             | gasId  | winewhite | cardio | pendigits | Har    | winered |
|-------------|--------|-----------|--------|-----------|--------|---------|
| bnndw       | 0.3256 | 0.1062    | 0.1249 | 0.1231    | 0.1164 | 0.1121  |
| bnnpaar     | 0.8076 | 0.0598    | 0.1241 | 0.1146    | 0.0572 | 0.0626  |
| bnndsat     | 0.3189 | 0.0985    | 0.1187 | 0.1216    | 0.1092 | 0.1045  |
| bnnrobus    | 0.0979 | 0.0252    | 0.0294 | 0.0297    | 0.0261 | 0.0257  |
| bnnromem    | 0.13   | 0.0349    | 0.0408 | 0.0382    | 0.0351 | 0.0352  |
| bnnromesx   | 0.1355 | 0.0354    | 0.042  | 0.0404    | 0.0369 | 0.0359  |
| bnnparstepw | 0.9352 | 0.0658    | 0.1255 | 0.1203    | 0.0737 | 0.0753  |
| bnnpaarter  | 0.7597 | 0.0559    | 0.116  | 0.1073    | 0.0608 | 0.0596  |
| bnnparpnw   | 0.7683 | 0.0826    | 0.1428 | 0.1371    | 0.0916 | 0.09    |
| bnnpaarx    | 0.809  | 0.0612    | 0.1244 | 0.115     | 0.0565 | 0.0619  |
| bnnparser   | 0.4869 | 0.0667    | 0.1054 | 0.1096    | 0.0776 | 0.0723  |
| bnnrospinor | 0.1218 | 0.0306    | 0.0362 | 0.0341    | 0.0315 | 0.0308  |
| bnnpar      | 0.7677 | 0.0846    | 0.1453 | 0.1368    | 0.0921 | 0.0907  |
| bnndsatin   | 0.3076 | 0.1028    | 0.1303 | 0.1264    | 0.1145 | 0.1089  |
| bnnroll     | 0.1435 | 0.0428    | 0.0469 | 0.0506    | 0.0436 | 0.0435  |
| bnnparsign  | 0.4991 | 0.068     | 0.1062 | 0.1089    | 0.0788 | 0.0746  |
| bnnroclk    | 0.1318 | 0.0344    | 0.0406 | 0.0392    | 0.0363 | 0.0355  |
| bnnroperm   | 0.1317 | 0.0339    | 0.0391 | 0.0385    | 0.0352 | 0.0347  |
| bnnrospine  | 0.1244 | 0.0309    | 0.036  | 0.0351    | 0.0317 | 0.0309  |
| bnnromesh   | 0.1296 | 0.0341    | 0.0401 | 0.0387    | 0.0353 | 0.0348  |
| bnndirect   | 0.3645 | 0.1226    | 0.1508 | 0.1357    | 0.1288 | 0.1257  |
| bnnparw     | 0.4869 | 0.0667    | 0.1054 | 0.1096    | 0.0776 | 0.0723  |
| bnnrolx     | 0.1424 | 0.0375    | 0.0455 | 0.0435    | 0.039  | 0.0389  |
| bnnromex    | 0.1313 | 0.0353    | 0.0409 | 0.0389    | 0.0358 | 0.0356  |
| bnnseq      | 0.2168 | 0.1286    | 0.1431 | 0.139     | 0.1327 | 0.1317  |
| bnnrolin    | 0.1313 | 0.0349    | 0.0456 | 0.0426    | 0.0363 | 0.0357  |
| bnnparce    | 0.5161 | 0.0658    | 0.1105 | 0.1155    | 0.079  | 0.0677  |



### **BNNPAR**



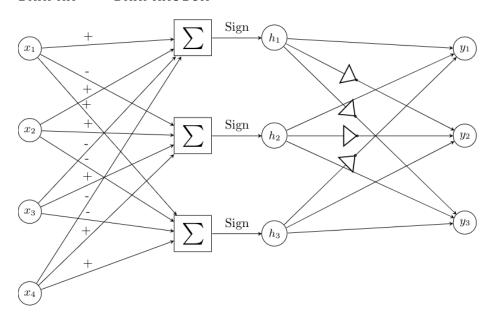
In bnnpar the arithmetic operations for each neuron are written out in verilog. For first layer neurons the features that correspond to positive weights are split from those that correspond to negative weights, the sum of each is calculated seperately and the two sums are compared to get the sign of the total sum, which is the output of the neuron. Here is an example:

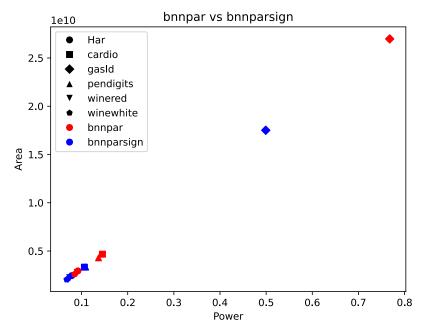
```
assign positives[0] = + feature_array[1] + feature_array[2] + ... + feature_array[10];
assign negatives[0] = + feature_array[0] + feature_array[3] + feature_array[5];
assign hidden[0] = positives[0] >= negatives[0];
```

For second layer neurons the hidden features that correspond to positive weights are summed as is and those that correspond to negative weights the inverse is added to the sum. This is equivelant to adding the result of the xnor of the activation with the weight. Example ("hidden\_n" the inverse of the array of hidden features, which is "hidden"):

```
assign scores[0*SUM_BITS+:SUM_BITS] = + hidden_n[0] + hidden[1] + hidden[2] + ... + hidden_n
```

# BNNPAR -> BNNPARSIGN





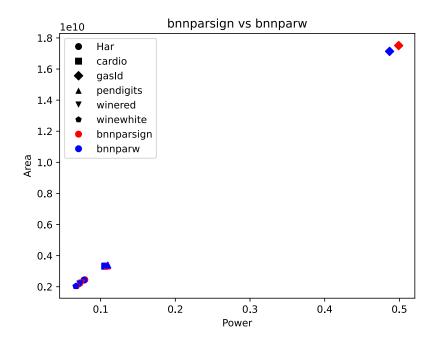
|                                    | bnnpar<br>area                     | bnnparsign<br>area | area<br>change                       | bnnpar<br>power                 | bnnparsign<br>power | power<br>change                      |
|------------------------------------|------------------------------------|--------------------|--------------------------------------|---------------------------------|---------------------|--------------------------------------|
| Har<br>cardio<br>gasId<br>pendigit | 29.4<br>46.71<br>269.76<br>s 42.95 | 33.27<br>175.09    | -16.6%<br>-28.8%<br>-35.1%<br>-22.3% | 92.1<br>145.3<br>767.7<br>136.8 | 106.2<br>499.1      | -14.4%<br>-26.9%<br>-35.0%<br>-20.4% |
| winered<br>winewhit                | 27.82                              |                    | -19.3%<br>-21.3%                     | 90.7<br>84.6                    |                     | -17.8%<br>-19.6%                     |

The difference from bnnpar is all the input features are added together in the first layer instead of split in positives and negatives. Features that correspond to weights of the neuron that are 1 are added and those of weights that are -1 are subtracted. Example:

```
wire signed [8:0] intra_0;
assign intra_0 = - feature_array[0] + feature_array[1] + ... + feature_array[10];
assign hidden[0] = intra_0 >= 0;
```

It results to a significant improvement compared to spliting the features. I expected the oposite to happen, thinking that only using additions would lead to more partial results being same between neurons and thus increasing sharing hardware. I assume the reason it is better is that having all variables in the same expression per neuron allows for more posibilities in rearanging them to share subexpressions.

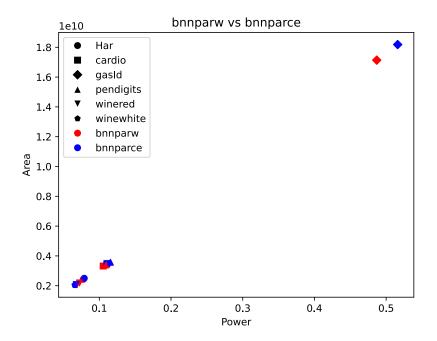
### **BNNPARSIGN -> BNNPARW**



|          | bnnparsign<br>area | bnnparw<br>area | area<br>change | bnnparsign<br>power | bnnparw<br>power | power<br>change |
|----------|--------------------|-----------------|----------------|---------------------|------------------|-----------------|
| Har      | 24.52              | 24.25           | -1.1%          | 78.8                | 77.6             | -1.5%           |
| cardio   | 33.27              | 33.21           | -0.2%          | 106.2               | 105.4            | -0.8%           |
| gasId    | 175.09             | 171.37          | -2.1%          | 499.1               | 486.9            | -2.4%           |
| pendigit | s 33.38            | 33.97           | +1.8%          | 108.9               | 109.6            | +0.6%           |
| winered  | 22.45              | 21.87           | -2.6%          | 74.6                | 72.3             | -3.1%           |
| winewhit | e 20.47            | 20.36           | -0.5%          | 68                  | 66.7             | -1.9%           |

Bnnparw differs with bnnparsign only in the number of bits that are used for the result of the operations of the hidden neurons. In bnnparsign all total sums have the maximum width a series of sums and subtractions of as many 5-bit integers as the inputs could take. In bnnparw each neuron gets assigned the minimum bitwidth needed to fit all the results it encounters in evaluating all the samples of the dataset. The bitwidth used for the operations is thus reduced. Unfortunately this truncation can block datapath extraction, leading the results to be worse for pendigits. Bnnparpnw is the equivelant for bnnpar, where the minimum bitwidth for the positive and negative components of the neuron sum is used.

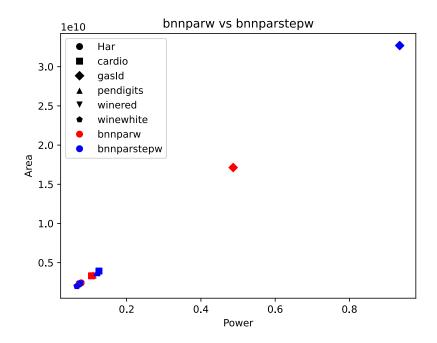
### BNNPARW -> BNNPARCE



|           | bnnparw | bnnparce | area   | bnnparw | bnnparce | power  |
|-----------|---------|----------|--------|---------|----------|--------|
|           | area    | area     | change | power   | power    | change |
| Har       | 24.25   | 24.99    | +3.1%  | 77.6    | 79       | +1.8%  |
| cardio    | 33.21   | 34.84    | +4.9%  | 105.4   | 110.5    | +4.8%  |
| gasId     | 171.37  | 181.82   | +6.1%  | 486.9   | 516.1    | +6.0%  |
| pendigits | 33.97   | 35.74    | +5.2%  | 109.6   | 115.5    | +5.4%  |
| winered   | 21.87   | 20.76    | -5.1%  | 72.3    | 67.7     | -6.4%  |
| winewhite | 20.36   | 20.48    | +0.6%  | 66.7    | 65.8     | -1.3%  |

For each hidden neuron the average of the maximum and minimum value it's total sum can take is subtracted from the sum in order to make the range of values centered on zero and thus reduce the bitwidth needed for it. Example: if the highest value the total of the neuron takes is 300 and the lowest is -100, we need a 10 bit signed integer to fit all values. If we subtract their average(100) the values will be in the range -200 to 200, so they fit in a 9 bit signed integer. RESULTS Subtracting the closest power of two that gets the range of values to a reduced bitwidth may do better.

### BNNPARW -> BNNPARSTEPW



|   | bnnparw<br>area | bnnparstepw<br>area                        | area<br>change                                       | bnnparw<br>power                                | bnnparstepw<br>power                            | power<br>change                                      |
|---|-----------------|--|--|---|---|--|
| Har<br>cardio<br>gasId<br>pendigits<br>winered<br>winewhite | 21.87           | 23.16<br>39.29<br>326.98<br>37.09<br>22.78 | -4.5%<br>+18.3%<br>+90.8%<br>+9.2%<br>+4.2%<br>-1.8% | 77.6<br>105.4<br>486.9<br>109.6<br>72.3<br>66.7 | 73.7<br>125.5<br>935.2<br>120.3<br>75.3<br>65.8 | -5.0%<br>+19.1%<br>+92.1%<br>+9.8%<br>+4.1%<br>-1.3% |

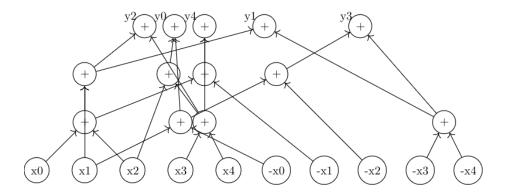
For each hidden neuron we add/subtract the features in order for each sample of the dataset. For each step of the process we find what the minimum bitwidth to hold each of the values is. For example we will need 5 bits for the just the first feature, 6 for feature 1 + feature 2, 7 bits for feature 1 + feature 2 - feature 3 and so on.

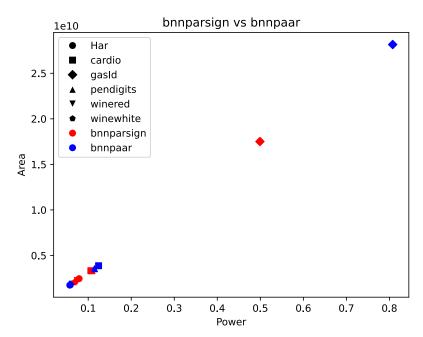
Sometimes due to the order of additions and subtractions the width needed at a later step is less than the one of an earlier step. This is because every sample for which there would be an overflow in the earlier step with the smaller width would at some following feature underflow back in the range it supports. This has been taken into

account.

I expected this one to do worse than bnnparw and it did. Truncating subexpressions impeded datapath extraction and so the results were negative for most datasets, althoughh Har and winewhite improved a bit.

## BNNPARSIGN -> BNNPAAR, BNNPAARX, BNNPAARTER





|          | bnnparsign<br>area | bnnpaar<br>area | area<br>change | bnnparsign<br>power | bnnpaar<br>power | power<br>change |
|----------|--------------------|-----------------|----------------|---------------------|------------------|-----------------|
| Har      | 24.52              | 17.42           | -29.0%         | 78.8                | 57.2             | -27.4%          |
| cardio   | 33.27              | 38.74           | +16.4%         | 106.2               | 124.1            | +16.9%          |
| gasId    | 175.09             | 281.55          | +60.8%         | 499.1               | 807.6            | +61.8%          |
| pendigit | s 33.38            | 35.43           | +6.1%          | 108.9               | 114.6            | +5.2%           |
| winered  | 22.45              | 18.55           | -17.4%         | 74.6                | 62.6             | -16.1%          |
| winewhit | e 20.47            | 18.01           | -12.0%         | 68                  | 59.8             | -12.1%          |

Since bnnstepw didn't work I thought finding the order of operations Design Compiler uses after optimization and truncating widths there may fare better. I first tried to get the arithmetic operations that are used after optimization from the analysis of datapath extraction report it provides. It turned out to be harder than expected and having to synthesize twice is suboptimal so I searched for an algorithm to do a similar arithmetic optimization beforehand.

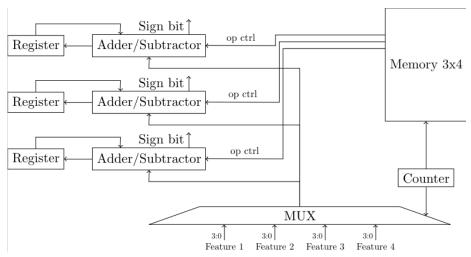
Paar's algorithm, found in [1] is used. It is explained well in that paper so I won't repeat the explanation here. Paar's algorithm considers the case where elements are only added, so to make it work for our case where there are also subtractions the negatives of input features are treated as seperate additional elements, so the operations for all neurons can be written with additions only.

By running it on the weight matrix of the first layer we get a series of additions between pairs of input features and/or intermediate results that calculate the total sum of each neuron. The additions are implemented in the same order in the design with an array to hold the intermediate results. Bitwidths for intermediate and final results were left at the default width from bnnparsign, custom widths were not implemented. Designs that have only the first layer implementing the operations found from the algorithm are called bnnpaar and those that have both layers are bnnpaarx.

Paar's algorithm was also expanded to work with subtractions. The implementation will be described seperately. Since it also uses subtraction it gives shorter series of operations. Designs using the ternary expansion in the first layer are called bnnpaarter.

I expected the results to be worse for all designs since Design Compiler would use the best available heuristics, so the fact hardcoding the order of operations with Paar's algorithm and the ternary expansion had up to 30% area reduction for some designs, even though it was worse for cardio and gasId, makes me suspect I have somehow crippled the datapath extraction of bnnparsign, though I don't see what could be a problem.

## **BNNSEQ**



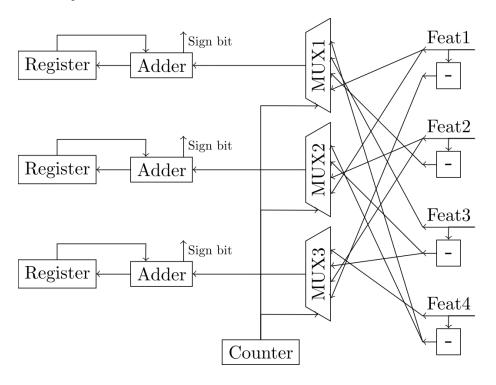
This implements the layers sequentialy in regards to the inputs of the layer, meaning each neuron has an accumulator and each cycle it is active it adds/subtracts the an input feature. All neurons update on the the same feature on the same cycle. Features get chosen to be the current sample in order. In the first layer a counter and multiplexer is used to pick the current sample. Features are picked in order. The column of binary weights that corresponds to the feature also gets picked from the weight matrix. Each accumulator receives as input the current feature and the weight bit of it's neuron and feature and depending on the weight bit either adds or subtracts the feature from it's running total.

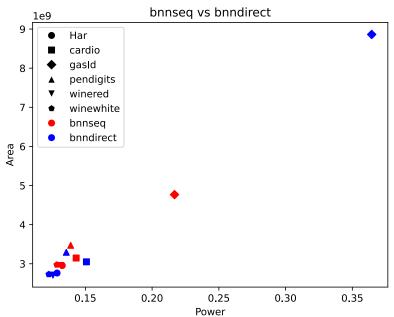
Once the counter reaches the last feature a flag that signals the first layer is done is set. This enables the second layer to start accumulating and freezes the first layer. Instead of choosing the weight bit that corresponds to each hidden feature and neuron and adding their xnor the second layer hardcodes the vector from which a neuron recieves it's inputs so it has the output of the previous layer in the position of an activation if the activation's weight with the neuron is 1 and it's inverse otherwise.

That way the accumulators of the second layer are simply counters with an enable signal that is set to the bit they would have to add. The results of the second layer are passed to an argmax module that returns the predicted class.

A design where shift registers where used to hold the weights instead of indexing a constant array with the counter was also attempted but turned out to be far worse.

## BNNSEQ -> BNNDIRECT



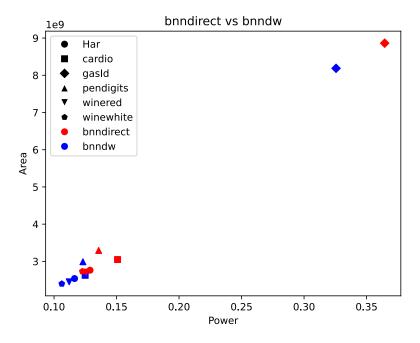


|           | bnnseq | bnndirect | area   | bnnseq | bnndirect | power  |
|-----------|--------|-----------|--------|--------|-----------|--------|
|           | area   | area      | change | power  | power     | change |
| Har       | 29.57  | 27.63     | -6.5%  | 132.7  | 128.8     | -2.9%  |
| cardio    |        | 30.5      | -3.1%  | 143.1  | 150.8     | +5.4%  |
| gasId     |        | 88.62     | +85.9% | 216.8  | 364.5     | +68.1% |
| pendigits |        | 32.93     | -5.1%  | 139    | 135.7     | -2.4%  |
| winered   |        | 27.11     | -8.3%  | 131.7  | 125.7     | -4.6%  |
| winewhite |        | 27.31     | -8.2%  | 128.6  | 122.6     | -4.7%  |

The difference of bnndirect with bnnseq is it also uses a hardcoded input vector for each neuron in the first layer instead of just the second. For each 4-bit input feature and every neuron a 5-bit signed segment of the neuron's custom input vector is set to either the feature or the negative of the feature.

It improves area and power except in the case of gasId, which has an order of magnitude more input features than other datasets and thus scales differently.

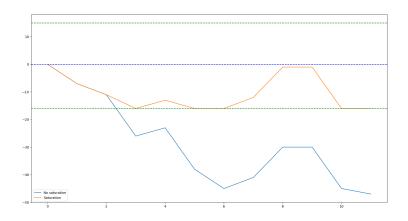
### **BNNDIRECT -> BNNDW**

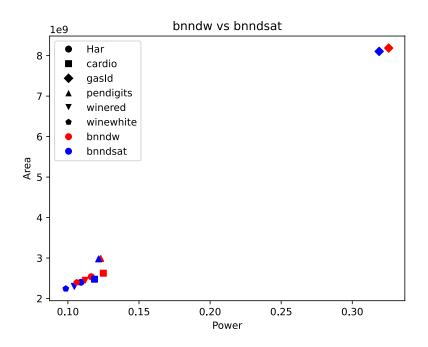


| bnı   | ndirect   | bnndw   | area   | bnndirect  | bnndw                   | power  |
|---|---|---|--|--|-------------------------|--|
|   | area  | area  | change   | power  | power                   | change   |
| Har<br>cardio<br>gasId<br>pendigits<br>winered<br>winewhite | 27.63<br>30.5<br>88.62<br>32.93<br>27.11<br>27.31 | 25.39<br>26.26<br>81.87<br>29.9<br>24.51<br>23.98 | -8.1%<br>-13.9%<br>-7.6%<br>-9.2%<br>-9.6%<br>-12.2% | 128.8<br>150.8<br>364.5<br>135.7<br>125.7<br>122.6 | 325.6<br>123.1<br>112.1 | -9.6%<br>-17.2%<br>-10.7%<br>-9.3%<br>-10.8%<br>-13.4% |

Bnndw is bnndirect with first layer accumulators getting their bitwidth set to the minimum needed similarly to bnnparw. The gains are more pronounced than the parallel case since the registers take up a significant portion of the resources and each bit shaved off an accumulator's range removes a flip-flop.

# BNNDW -> BNNDSAT





|           | bnndw area | bnndsat area | area change | bnndw power | bnndsat power | power change |
|-----------|------------|--------------|-------------|-------------|---------------|--------------|
| Har       | 25.39      | 24.02        | -5.4%       | 116.4       | 109.2         | -6.2%        |
| cardio    | 26.26      | 24.77        | -5.7%       | 124.9       | 118.7         | -5.0%        |
| gasId     | 81.87      | 81.05        | -1.0%       | 325.6       | 318.9         | -2.1%        |
| pendigits | 29.9       | 29.79        | -0.4%       | 123.1       | 121.6         | -1.2%        |

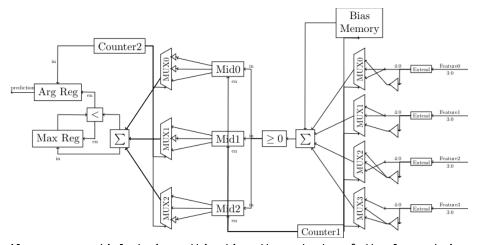
|           | bnndw area | bnndsat area | area change | bnndw power | bnndsat power | power change |
|-----------|------------|--------------|-------------|-------------|---------------|--------------|
| winered   | 24.51      | 23.02        | -6.1%       | 112.1       | 104.5         | -6.8%        |
| winewhite | 23.98      | 22.43        | -6.5%       | 106.2       | 98.5          | -7.3%        |

In bnndsat saturation is used in combination with bnndw's truncation to reduce the number of registers farther. Using the DW\_addsub\_dx module from designware the result of adding a sample to the value of the accumulator is set to the maximum value the accumulator can hold in the case it would otherwise overflow and similarly to the minimum value it can fit in case of underflow.

The bitwidth needed to have the final value after all samples are added have the correct sign using saturation is shrunk for many neurons. For neurons where saturation doesn't reduce the number of bits in the accumulator simple truncation is used instead to avoid the overhead.

(Note: for some reason the simulation module of DW\_addsub\_dx slowed simulation with iverilog by two orders of magnitude.)

### BNNROLIN

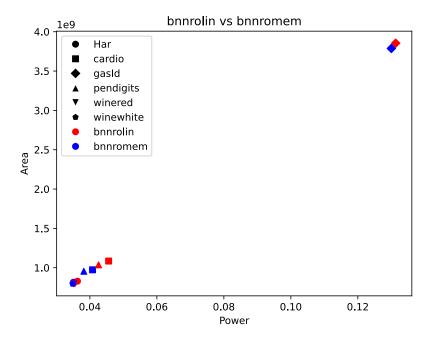


Also a sequential design, this time the outputs of the layer being the dynamic dimension instead of the inputs as in bnnseq. This means that each layer has a single adder tree that computes the output of a single neuron of the layer per cycle.

In the first layer a custom input vector per neuron is used again like bnndirect. The adder sums the entire vector of the neuron and the sign of the result is stored to a register corresponding to the layers output. Instead of having the negative of the input feature in positions of the vector that have weight -1 the inverse of it's 5-bit expansion is used. With the idea that the negative in 2's compliment is the inverse plus 1, we add a correction term equal to the number of negative weights of the neuron to the sum to get the correct result. The correction terms are stored at an array of constants and are indexed by the counter like the input vectors. This was measured to be more efficient.

After the counter of the first layer reaches the last neuron the next layer is activated in a similar fashion with previous sequential designs. Unlike the first layer the second doesn't need to store the outputs of all it's neurons. Since it is the last layer we can store only the largest value seen thus far in a register and only overwrite it when the result of the current neuron is larger. Along with this the value of the counter (which corresponds to the index of the neuron) is also written into a register each time the current result is larger than the previous best. This way the argmax is calculated at the same time as the output neurons.

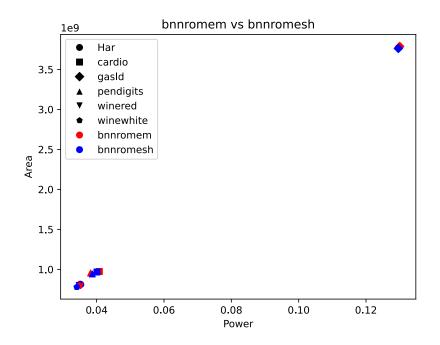
### BNNROLIN -> BNNROMEM



| k         | onnrolin<br>area | bnnromem<br>area | area<br>change | bnnrolin<br>power | bnnromem<br>power | power<br>change |
|-----------|------------------|------------------|----------------|-------------------|-------------------|-----------------|
| Har       | 8.29             | 8.16             | -1.6%          | 36.3              | 35.1              | -3.3%           |
| cardio    | 10.85            | 9.74             | -10.2%         | 45.6              | 40.8              | -10.5%          |
| gasId     | 38.54            | 37.87            | -1.7%          | 131.3             | 130               | -1.0%           |
| pendigits | 10.37            | 9.55             | -7.9%          | 42.6              | 38.2              | -10.3%          |
| winered   | 8.04             | 7.96             | -1.0%          | 35.7              | 35.2              | -1.4%           |
| winewhite | . 8              | 7.96             | -0.5%          | 34.9              | 34.9              | +0.0%           |

Instead of hardcoding a custom input vector for each neuron the row of weights that correspond to each neuron are indexed from the weight matrix by the counter and the 5-bit expansion of each input feature is xnored by it's weight bit.

## BNNROMEM -> BNNROMESH

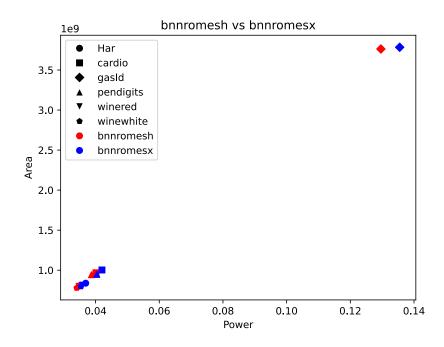


|               | bnnromem     | bnnromesh                               | area           | bnnromem     | bnnromesh | power  |
|---------------|--------------|---|----------------|--------------|-----------|--------|
|               | area         | area                                    | change         | power        | power     | change |
| Har<br>cardio | 8.16<br>9.74 | • | -0.6%<br>-0.7% | 35.1<br>40.8 |           | +0.6%  |

| br        | nromem | bnnromesh | area   | bnnromem | bnnromesh | power  |
|-----------|--------|-----------|--------|----------|-----------|--------|
|           | area   | area      | change | power    | power     | change |
| gasId     | 37.87  | 37.63     | -0.6%  | 130      | 0.10      | -0.3%  |
| pendigits | 9.55   | 9.43      | -1.3%  | 38.2     |           | +1.3%  |
| winered   | 7.96   | 7.99      | +0.4%  | 35.2     |           | -1.1%  |
| winewhite | 7.96   | 7.79      | -2.1%  | 34.9     |           | -2.3%  |

Instead of a decoder from the counter to index the register bit the current result of the first layer should be written to, bnnromesh stores the value at the end of a shifting register. At each cycle the register array shifts right once, so when the last neuron's result is written at the left-most position the first neuron's result reaches the right-most position and all the results are stored in order.

### BNNROMESH -> BNNROMESX



|        | bnnromesh<br>area | bnnromesx<br>area | area<br>change | bnnromesh<br>power | bnnromesx<br>power | power<br>change |
|--------|-------------------|-------------------|----------------|--------------------|--------------------|-----------------|
| Har    | 8.11              | 8.38              | +3.3%          | 35.3               | 36.9               | +4.5%           |
| cardio | 9.67              | 10.03             | +3.7%          | 40.1               | 42                 | +4.7%           |

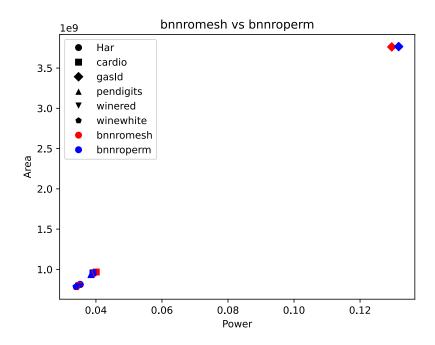
| bn        | nromesh | bnnromesx | area   | bnnromesh | bnnromesx | power  |
|-----------|---------|-----------|--------|-----------|-----------|--------|
|           | area    | area      | change | power     | power     | change |
| gasId     | 37.63   | 37.84     | +0.6%  | 129.6     | 135.5     | +4.6%  |
| pendigits | 9.43    | 9.47      | +0.4%  | 38.7      | 40.4      | +4.4%  |
| winered   | 7.99    | 8.13      | +1.8%  | 34.8      | 35.9      | +3.2%  |
| winewhite | 7.79    | 7.98      | +2.4%  | 34.1      | 35.4      | +3.8%  |

This design was implemented mostly out of curiosity and not because it would help much.

Since the counter is not used to index the position the result is stored, the sequence of values it takes doesn't have to be linear(0, 1, 2..). Instead of a 6-bit counter we can use any FSM that gives a sequence of 40 unique 6-bit values in it's place, given that we replace the array of weights we indexed with the counter's values with a lookup table with the new sequence's values as indexes. The smallest such FSM is a linear-feedback shift register with a single xor gate for the two most significant bits, so that is implemented.

The gain from removing a 6-bit add-1 circuit is negligable and I don't think the lookup table was implemented as well as it could so the results were negative.

### BNNROMESH -> BNNROPERM



|          | bnnromesh | bnnroperm | area   | bnnromesh | bnnroperm | power  |
|----------|-----------|-----------|--------|-----------|-----------|--------|
|          | area      | area      | change | power     | power     | change |
| Har      | 8.11      | 8.14      | +0.4%  | 35.3      | 35.2      | -0.3%  |
| cardio   | 9.67      | 9.56      | -1.1%  | 40.1      | 39.1      | -2.5%  |
| gasId    | 37.63     | 37.67     | +0.1%  | 129.6     | 131.7     | +1.6%  |
| pendigit | 7.99      | 9.35      | -0.8%  | 38.7      | 38.5      | -0.5%  |
| winered  |           | 7.87      | -1.5%  | 34.8      | 34.7      | -0.3%  |
| winewhit |           | 7.85      | +0.8%  | 34.1      | 33.9      | -0.6%  |

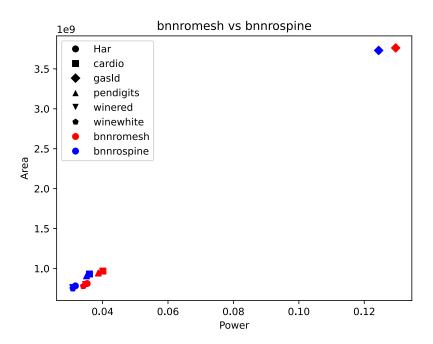
This design was also implemented mostly out of curiosity.

I had a vague notion that the logic that implements the decoder from the counter to the weights would be simpler if weight rows with "more similar" bits corresponded to counter values with "more similar" bits. To try to test that I made a graph of the hamming distances of the neuron weights and got an aproximate solution to TSP on it to get a sequence of neurons that minimises the number of bit changes between neighbouring neurons. I then got a similar sequence for the values of the counter (i.e. numbers 0-39) and permuted the rows of the weight matrix so the i-th neuron in the sequence maps to the i-th value in

the counter sequence. The columns of the second layer's weight matrix had the same permutation applied to them so the second layer's results are not affected.

The area increased in half the datasets and decreased in the other half, so it doesn't seem to be better than a random permutation.

## **BNNROMESH -> BNNROSPINE**



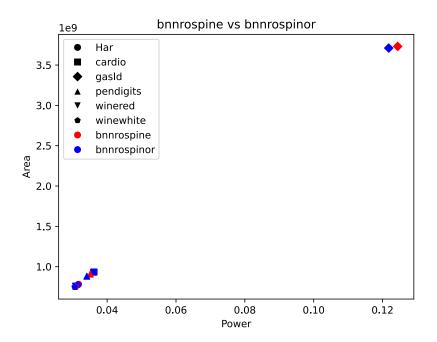
|                     | bnnromesh<br>area | bnnrospine<br>area | area<br>change | bnnromesh<br>power | bnnrospine<br>power | power<br>change  |
|---------------------|-------------------|--------------------|----------------|--------------------|---------------------|------------------|
| Har<br>cardio       | 8.11<br>9.67      |                    | -3.6%<br>-3.8% | 35.3<br>40.1       | • • • • •           | -10.2%<br>-10.2% |
| gasId               | 37.63             | 37.31              | -0.9%          | 129.6              | 124.4               | -4.0%            |
| pendigit<br>winered | ts 9.43<br>7.99   | 9.08<br>7.61       | -3.7%<br>-4.8% | 38.7<br>34.8       | 35.1<br>30.9        | -9.3%<br>-11.2%  |
| winewhit            | te 7.79           | 7.49               | -3.9%          | 34.1               | 30.9                | -9.4%            |

The shifting regiter that stores the 1st layer's outputs gets initialised with a 1 in the left-most position and 0s in all other positions. A circuit that outputs a one-hot vector where only the bit in

the position of the left-most nonzero bit in the shifting register is set to 1 is added. That implements a one-hot shifting register that encodes the index of the currently calculated neuron without using additional memory elements.

Using the bits of the one-hot vector as select signals for the weight rows the counter and it's encoder can be removed, leading in efficiency gains.

### BNNROSPINE -> BNNROSPINOR



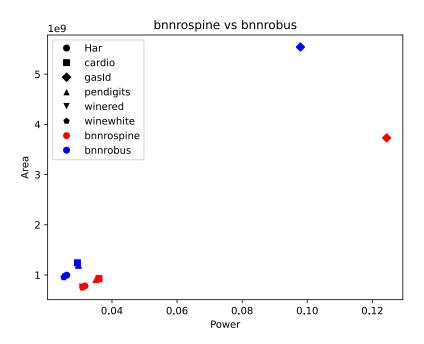
|                               | bnnrospine | bnnrospino           | r area                  | bnnrospine           | bnnrospinor          | power  |
|-------------------------------|------------|----------------------|-------------------------|----------------------|----------------------|--------|
|                               | area       | area                 | change                  | power                | power                | change |
| Har                           | 7.82       | 7.76                 | -0.8%                   | 31.7                 | 31.5                 |        |
| cardio                        | 9.3        | 9.35                 | +0.5%                   | 36                   | 36.2                 |        |
| gasId                         | 37.31      | 37.11                | -0.5%                   | 124.4                | 121.8                | -2.1%  |
| pendigi<br>winered<br>winewhi | 7.61       | 8.81<br>7.57<br>7.48 | -3.0%<br>-0.5%<br>-0.1% | 35.1<br>30.9<br>30.9 | 34.1<br>30.8<br>30.6 | -0.3%  |

Instead of the lookup table used for weights in bnnrospine, the current weight that corresponds to a given input feature is calculated by a

NOR of the bits of the one-hot vector in positions where the weight column of the feature would be -1.

Except for cardio, it is an improvement.

### **BNNROSPINE -> BNNROBUS**



|          | bnnrospine<br>area | bnnrobus<br>area | area<br>change | bnnrospine<br>power | bnnrobus<br>power | power<br>change |
|----------|--------------------|------------------|----------------|---------------------|-------------------|-----------------|
| Har      | 7.82               | 9.97             | +27.5%         | 31.7                | 26.1              | -17.7%          |
| cardio   | 9.3                | 12.44            | +33.8%         | 36                  | 29.4              | -18.3%          |
| gasId    | 37.31              | 55.39            | +48.5%         | 124.4               | 97.9              | -21.3%          |
| pendigit | ts 9.08            | 11.93            | +31.4%         | 35.1                | 29.7              | -15.4%          |
| winered  | 7.61               | 9.66             | +26.9%         | 30.9                | 25.7              | -16.8%          |
| winewhit | te 7.49            | 9.56             | +27.6%         | 30.9                | 25.2              | -18.4%          |

Every input feature gets the current weight bit from an open bus to which a tristate buffer for each entry in the feature's column in the weight matrix is connected. Each buffer in a bus corresponds to a neuron and is controlled by that neuron's select signal from the one-hot vector.

Decent improvements in power are achieved at the cost of significantly larger areas. At least the power for pendigits got under 30 mW, which I'm happy about.

## TODO: Descriptions for tnn designs

[1] Banik, S., Funabiki, Y., Isobe, T. (2019). More Results on Shortest Linear Programs. In: Attrapadung, N., Yagi, T. (eds) Advances in Information and Computer Security. IWSEC 2019. Lecture Notes in Computer Science(), vol 11689. Springer, Cham. https://doi.org/10.1007/978-3-030-26834-3\_7