**EECS 168** 

## Introduction to VLSI Design

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Quiz 1

Name: _			
tudent ID			

- 1. (10pts)
- (a) Explain the Moore's law.

Semiconductor technology will double its effectiveness every 18 months.

(b) List 3 reliability issues.

EM, TDDB, HCI, BTI

2. (10pts) Give the conditions of linear region and saturation region for both NMOS and PMOS transistors.

	NMOS	PMOS
linear	$V_{gs} > V_t, V_{ds} < V_{gs} - V_t$	$V_{sg} >  V_t , V_{sd} < V_{sg} -  V_t $
saturation	$V_{gs} > V_t, V_{ds} \ge V_{gs} - V_t$	$V_{sg} >  V_t , V_{sd} \ge V_{sg} -  V_t $

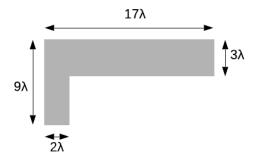
3. (10pts) Give the typical design abstraction levels for VLSI design.

higher system level register-transfer level gate level circuit level

device level

TOWCI

4. (15 pts). Compute the parasitic resistance of the following metal1 wire, where the sheet resistance  $(R_{\square})$  of metall is  $0.08\Omega/\square$ ,  $R_{corner} = R_{\square} \left(0.46 + 0.1 \cdot \frac{W_{large}}{W_{corner}}\right)$ 



$$\begin{split} R_{corner} &= R_{\square} \left( 0.46 + 0.1 \cdot \frac{W_{large}}{W_{small}} \right) \\ R &= R_{\square} \cdot \frac{L_1}{W_1} + R_{corner} + R_{\square} \cdot \frac{L_2}{W_2} \\ &= R_{\square} \left( \frac{17\lambda - 2\lambda}{3\lambda} \right) + R_{\square} \left( 0.46 + 0.1 \cdot \frac{3\lambda}{2\lambda} \right) + R_{\square} \left( \frac{9\lambda - 3\lambda}{2\lambda} \right) \\ &= R_{\square} (5 + 0.61 + 3) \\ &= 8.61 R_{\square} \\ &= 0.6888 \Omega \end{split}$$

5. (20 pts). Assuming  $V_{gs}$  is 3V, compute the drain current through an n-type transistor at a  $V_{ds}$  of 1.8V, where W/L is 6/2, k' is 73 $\mu$ A/V<sup>2</sup>, and  $V_t$  is 0.7V.

$$\frac{V_{gs} > V_t}{V_{ds} < V_{gs} - V_t} \bigg\} \Longrightarrow \text{linear region}$$

$$V_{ds} > V_{t}$$

$$V_{ds} < V_{gs} - V_{t}$$

$$\Rightarrow \text{ linear region}$$

$$I_{d} = k' \frac{W}{L} \left[ (V_{gs} - V_{t}) V_{ds} - \frac{1}{2} V_{ds}^{2} \right]$$

$$= 73 \times \frac{6}{2} \times \left[ (3 - 0.7) \times 1.8 - \frac{1}{2} \times 1.8^{2} \right]$$

$$= 551.88 \text{ uA}$$

6. (20 pts). Predict how linear and saturation drain current of an MOSFET would change for a 90nm ( $\lambda = 45$  nm) process from 180nm: (a) ideal scaling and (b) fixed-voltage scaling. Assume that S = 0.5,  $k' = \frac{\mu_{eff} \varepsilon_{ox}}{t_{ox}}$ .

Parameter	ideal scaling	fixed-voltage scaling
$W, L, t_{ox}$	S	S
$V_{gs}, V_{ds}, V_t$	S	1
$\mu_{eff}$ , $\varepsilon_{ox}$	1	1

lengths and widths: 
$$\frac{\widehat{W}}{W} = S, \frac{\widehat{L}}{L} = S$$
 oxide thickness:  $\frac{\widehat{t}_{ox}}{t_{ox}} = S$ 

transistor conductance: 
$$k' = \frac{\mu_{eff} \varepsilon_{ox}}{t_{ox}} \rightarrow \frac{\hat{k}'}{k'} = \frac{1}{S}$$

(a) ideal scaling

voltage: 
$$\frac{\hat{V}}{V} = S$$

saturation drain current:

$$\frac{\hat{I}_d}{I_d} = \left(\frac{1/2}{1/2}\right) \left(\frac{\hat{k}}{k'}\right) \left(\frac{\hat{W}/\hat{L}}{W/L}\right) \left[\frac{(\hat{V}_{gs} - \hat{V}_t)^2}{(V_{gs} - V_t)^2}\right] = \frac{1}{S} \left(\frac{S}{S}\right) S^2 = S = 0.5$$

linear drain current:

$$\frac{\hat{I}_d}{I_d} = \left(\frac{\hat{k}}{k'}\right) \left(\frac{\widehat{W}/\widehat{L}}{W/L}\right) \left[\frac{(\hat{V}_{gs} - \hat{V}_t)\hat{V}_{ds} - (1/2)\hat{V}_{ds}^2}{(V_{qs} - V_t)V_{ds} - (1/2)V_{ds}^2}\right] = \frac{1}{S} \left(\frac{S}{S}\right) S^2 = S = 0.5$$

(b) fixed-voltage scaling

voltage: 
$$\frac{\hat{V}}{V} = 1$$

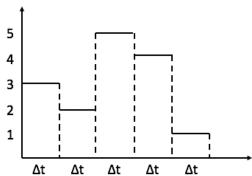
saturation drain current:

$$\frac{\hat{I}_d}{I_d} = \left(\frac{1/2}{1/2}\right) \left(\frac{\hat{k}}{k'}\right) \left(\frac{\widehat{W}/\widehat{L}}{W/L}\right) \left[\frac{\left(\hat{V}_{gs} - \hat{V}_t\right)^2}{\left(V_{gs} - V_t\right)^2}\right] = \frac{1}{S} \left(\frac{S}{S}\right) 1^2 = \frac{1}{S} = 2$$

linear drain currents

$$\frac{\hat{I}_d}{I_d} = \left(\frac{\hat{k}}{k'}\right) \left(\frac{\widehat{W}/\widehat{L}}{W/L}\right) \left[\frac{(\widehat{V}_{gs} - \widehat{V}_t)\widehat{V}_{ds} - (1/2)\widehat{V}_{ds}^2}{(V_{as} - V_t)V_{ds} - (1/2)V_{ds}^2}\right] = \frac{1}{S} \left(\frac{S}{S}\right) 1^2 = \frac{1}{S} = 2$$

7. (15 pts). The TTF (time to failure in years) of a system is changing with time as the graph shows, then what is the effective TTF for the system over the total time period?  $\Delta t = 1$ 



Compute the failure rate for each period:

The infinite the fall 
$$\Delta t_1 \colon \lambda_1 = \frac{1}{3}$$

$$\Delta t_2 \colon \lambda_2 = \frac{1}{2}$$

$$\Delta t_3 \colon \lambda_3 = \frac{1}{5}$$

$$\Delta t_4 \colon \lambda_4 = \frac{1}{4}$$

$$\Delta t_5 \colon \lambda_5 = 1$$

$$\lambda_{avg} = \frac{\left(\frac{1}{3} + \frac{1}{2} + \frac{1}{5} + \frac{1}{4} + 1\right)}{5} = \frac{137}{300}$$

$$MTTF = \frac{1}{300} = \frac{300}{300} \approx 2.19$$