
cycleke (菜鸡) 的 XCPC 模板



icpc International Collegiate
Programming Contest



哈爾濱工業大學

cycleke

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1 数学

1.1 素数

素数的数目有近似 $\pi(x) \sim \frac{x}{\ln(x)}$, 判定如下:

```

1 inline ll mmul(const ll &a, const ll &b, const ll &mod) {
2     ll k = (ll)((1.0L * a * b) / (1.0L * mod)), t = a * b - k * mod;
3     for (t -= mod; t < 0; t += mod) {}
4     return t;
5 }
6 inline ll mpow(ll a, ll b, const ll &mod) {
7     ll res = 1;
8     for (; b >= 1, a = mmul(a, a, mod)) (b & 1) && (res = mmul(res, a, mod));
9     return res;
10 }
11
12 inline bool check(const ll &x, const ll &p) {
13     if (!(x % p) || mpow(p % x, x - 1, x) ^ 1) return false;
14     for (ll k = x - 1, t; ~k & 1;) {
15         if (((t = mpow(p % x, k >= 1, x)) ^ 1) && (t ^ (x - 1))) return false;
16         if (!(t ^ (x - 1))) return true;
17     }
18     return true;
19 }
20
21 inline bool Miller_Rabin(const ll &x) {
22     if (x < 2) return false;
23     static const int p[12] = {2, 3, 5, 7, 11, 13, 17, 19, 61, 2333, 4567, 24251};
24     for (int i = 0; i < 12; ++i) {
25         if (!(x ^ p[i])) return true;
26         if (!check(x, p[i])) return false;
27     }
28     return true;
29 }

```

1.2 Pollard Rho

```

1 mt19937_64 rnd(chrono::high_resolution_clock::now().time_since_epoch().count());
2 inline ll rand64(ll x) { return rnd() % x + 1; }
3
4 inline ll Pollard_rho(const ll &x, const int &y) {
5     ll v0 = rand64(x), v = v0, d, s = 1;
6     for (int t = 0, k = 1;;) {
7         v = (mmul(v, v, x) + y) % x, s = mmul(s, abs(v - v0), x);
8         if (!(v ^ v0) || !s) return x;
9         if (++t == k) {
10             if ((d = __gcd(s, x)) ^ 1) return d;
11             v0 = v, k <= 1;
12         }
13     }
14 }
15
16 vector<ll> factor;
17 void findfac(ll n) {
18     if (Miller_Rabin(n)) {
19         factor.push_back(n);
20         return;
21     }
22     ll p = n;
23     while (p >= n) p = Pollard_rho(p, rand64(n));
24     findfac(p), findfac(n / p);
25 }

```

1.3 欧拉函数

欧拉函数的性质：

- 欧拉函数是积性函数；
- $n = \sum_{d|n} \varphi(d)$;
- 若 $n = p^k$ ，其中 p 是质数，那么 $\varphi(n) = p^k - p^{k-1}$;
- 若 $\gcd(a, m) = 1$ ，则 $a^{\varphi(m)} \equiv 1 \pmod{m}$;

$$\text{拓展欧拉定理: } a^b \equiv \begin{cases} a^{b \bmod \varphi(p)} & \gcd(a, p) = 1 \\ a^b & \gcd(a, p) \neq 1, b < \varphi(p) \quad (\bmod p) \\ a^{b \bmod \varphi(p) + \varphi(p)} & \gcd(a, p) \neq 1, b \geq \varphi(p) \end{cases}$$

```

1 int euler_phi(int n) {
2     int ans = n;
3     for (int i = 2; i * i <= n; i++)
4         if (n % i == 0) {
5             ans = ans / i * (i - 1);
6             while (n % i == 0) n /= i;
7         }
8     if (n > 1) ans = ans / n * (n - 1);
9     return ans;
10 }

```

1.4 线性筛

lpf 为最小质因子的标号；mu 为莫比乌斯函数；phi 为欧拉函数；e 为质因子最高次幂，d 为因数个数；f 为因数之和，g 为最小质因子的幂和，即 $p + p^1 + p^2 + \dots + p^k$ 。理论上积性函数都可以线性筛。

```

1 const int MAXN = 1e7 + 5;
2 int prime[MAXN / 15], prime_cnt;
3 int lpf[MAXN], e[MAXN], d[MAXN], mu[MAXN], phi[MAXN];
4 void sieve() {
5     prime[lpf[1] = 0] = 1, e[1] = 0, d[1] = 1, mu[1] = 1, phi[1] = 1;
6     for (int i = 2; i < MAXN; ++i) {
7         if (!lpf[i]) {
8             prime[lpf[i] = ++prime_cnt] = i;
9             mu[i] = -1, phi[i] = i - 1;
10            e[i] = 1, d[i] = 2;
11            g[i] = f[i] = i + 1;
12        }
13        for (int j = 1, x; j <= lpf[i] && (x = i * prime[j]) < MAXN; ++j) {
14            lpf[x] = j;
15            if (j < lpf[i]) {
16                mu[x] = -mu[i], phi[x] = phi[i] * (prime[j] - 1);
17                e[x] = 1, d[x] = d[i] * 2;
18                g[x] = 1 + prime[j], f[x] = f[i] * f[prime[j]];
19            } else { // i % prime[j] == 0
20                mu[x] = 0, phi[x] = phi[i] * prime[j];
21                e[x] = e[i] + 1, d[x] = d[i] / e[x] * (e[x] + 1);
22                g[x] = g[i] * prime[j] + 1, f[x] = f[i] / g[i] * g[x];
23            }
24        }
25    }
26 }

```

1.5 拓展欧几里得算法

```

1 int exgcd(int a, int b, int &x, int &y) {
2     if (b == 0) return x = 1, y = 0, a;
3     int g = exgcd(b, a % b, y, x);
4     y -= a / b * x;
5     return g;
6 }

```

1.6 莫比乌斯反演

常见积性函数 ($f(ab) = f(a)f(b), (a, b) = 1$):

- 单位函数: $\epsilon(n) = [n = 1]$ (完全积性)
- 恒等函数: $\text{id}_k(n) = n^k$, $\text{id}_1(n)$ 通常简记作 $\text{id}(n)$ (完全积性)。
- 常数函数: $1(n) = 1$ (完全积性)
- 除数函数: $\sigma_k(n) = \sum_{d|n} d^k$, $\sigma_0(n)$ 通常简记作 $d(n)$ 或 $\tau(n)$, $\sigma_1(n)$ 通常简记作 $\sigma(n)$ 。
- 欧拉函数: $\varphi(n) = \sum_{i=1}^n [\text{gcd}(i, n) = 1]$
- 莫比乌斯函数: $\mu(n) = \begin{cases} 1 & n = 1 \\ 0 & \exists d > 1, d^2 | n, \text{ 其中 } \omega(n) \text{ 表示 } n \text{ 的本质不同质因子个数, 它是一个加性函数 } (\omega(ab) = \omega(a) + \omega(b))。 \\ (-1)^{\omega(n)} & \text{otherwise} \end{cases}$

Dirichlet 卷积满足交换率、结合率和分配率, 常见 Dirichlet 卷积:

- $\epsilon = \mu * 1$
- $\varphi = \text{id} * \mu$
- $f \cdot d = f * f$ (f 为完全积性)
- $d = 1 * 1$
- $\text{id} = \varphi * 1$
- $\sigma = \text{id} * 1$
- $\text{id}_{k+1} = (\text{id}_k \cdot \varphi) * \text{id}_k$

莫比乌斯反演: $f = g * 1 \iff g = \mu * f$ 。

拓展: 对于数论函数 f, g 和完全积性函数 t 且 $t(1) = 1$:

$$f(n) = \sum_{i=1}^n t(i)g\left(\left\lfloor \frac{n}{i} \right\rfloor\right) \iff g(n) = \sum_{i=1}^n \mu(i)t(i)f\left(\left\lfloor \frac{n}{i} \right\rfloor\right)$$

常用结论:

- $\sum_{i=x}^n \sum_{j=y}^m [\text{gcd}(i, j) = k] = \sum_{d=1}^{\lfloor \frac{n}{kd} \rfloor} \mu(d) \lfloor \frac{n}{kd} \rfloor \lfloor \frac{m}{kd} \rfloor$
- $d(ij) = \sum_{x|i} \sum_{y|j} [\text{gcd}(x, y) = 1] = \sum_{p|i, p|j} \mu(p) d\left(\frac{i}{p}\right) d\left(\frac{j}{p}\right)$

1.7 杜教筛

设 $S(n) = \sum_{i=1}^n f(i)$, 则 $\sum_{i=1}^n (f * g)(i) = \sum_{i=1}^n g(i)S(\lfloor \frac{n}{i} \rfloor) \Rightarrow g(1)S(n) = \sum_{i=1}^n (f * g)(i) - \sum_{i=2}^n g(i)S(\lfloor \frac{n}{i} \rfloor)$ 。
直接分块复杂度 $O(n^{\frac{3}{4}})$, 预处理出前 $O(n^{\frac{2}{3}})$ 项复杂度为 $O(n^{\frac{2}{3}})$ 。常用结论:

- 莫比乌斯函数前缀和: $S(n) = \sum_{i=1}^n \epsilon(i) - \sum_{i=2}^n S(\lfloor \frac{n}{i} \rfloor)$
- 欧拉函数前缀和: $S(n) = \sum_{i=1}^n \text{id}(i) - \sum_{i=2}^n S(\lfloor \frac{n}{i} \rfloor)$

```

1 map<int, int> mp_mu;
2
3 int S_mu(int n) {
4     if (n < MAXN) return sum_mu[n];
5     if (mp_mu[n]) return mp_mu[n];
6     int ret = 1;
7     for (int i = 2, j; i <= n; i = j + 1) {
8         j = n / (n / i);
9         ret -= S_mu(n / i) * (j - i + 1);
10    }
11    return mp_mu[n] = ret;
12 }
13
14 // 使用莫比乌斯反演
15 ll S_phi(int n) {
16     ll res = 0;
17     for (int i = 1, j; i <= n; i = j + 1) {
18         j = n / (n / i);
19         res += 1LL * (S_mu(j) - S_mu(i - 1)) * (n / i) * (n / i);
20     }
21     return (res - 1) / 2 + 1;
22 }

```

1.8 Min_25 筛

要求：积性函数 $f(p)$ 是一个关于 p 的项数较少的多项式或可以快速求值； $f(p^c)$ 可以快速求值。时间复杂度： $O\left(\frac{n^{\frac{3}{4}}}{\log n}\right)$ 。部分符号和结论：

- $F_{\text{prime}}(n) = \sum_{2 \leq p \leq n} f(p)$
- $F_k(n) = \sum_{i=2}^n [p_k \leq \text{lpf}(i)] f(i)$ ，答案为 $F_1(n) + f(1)$
- $F_k(n) = \sum_{\substack{k \leq i \\ p_i^2 \leq n}} \sum_{\substack{c \geq 1 \\ p_i^{c+1} \leq n}} (f(p_i^c) F_{k+1}(n/p_i^c) + f(p_i^{c+1})) + F_{\text{prime}}(n) - F_{\text{prime}}(p_{k-1})$
- 若 $f(p) = \sum p^{s_i}$ ，设 $g(p) = p^s$, $G_k(n) = \sum_{i=1}^n [p_k < \text{lpf}(i) \vee \text{isprime}(i)] g(i)$
- $G_k(n) = G_{k-1}(n) - [p_k^2 \leq n] g(p_k) (G_{k-1}(n/p_k) - G_{k-1}(p_{k-1}))$, $G_0 = \sum_{i=2}^n g(i)$

LOJ 例题：给定 $f(n)$ ：
$$f(n) = \begin{cases} 1 & n = 1 \\ p \oplus c & n = p^c \\ f(a)f(b) & n = ab \wedge a \perp b \end{cases}, \text{ 求 } f(n) \text{ 的和。因 } f(p) = p - 1 + 2[p = 2],$$

可以按照筛 φ 的方法来处理。

```

1 constexpr int MOD = 1e9 + 7;
2 constexpr int INV2 = MOD / 2 + 1;
3
4 template <typename X, typename Y> void inc(X &x, const Y &y) { x += y, (x >= MOD) && (x -= MOD); }
5 template <typename X, typename Y> void dec(X &x, const Y &y) { x -= y, (x < 0) && (x += MOD); }
6 template <typename X, typename Y> int sum(X x, Y y) { return x + y < MOD ? x + y : x + y - MOD; }
7 template <typename X, typename Y> int sub(X x, Y y) { return x < y ? x + MOD - y : x - y; }
8
9 constexpr int MAX_SIZE = 2e5 + 3;
10 int prime[MAX_SIZE / 10], lpf[MAX_SIZE], spri[MAX_SIZE], prime_cnt;
11
12 void sieve(int n) {
13     for (int i = 2; i <= n; ++i) {
14         if (lpf[i] == 0) {
15             prime[lpf[i] = ++prime_cnt] = i;
16             spri[prime_cnt] = sum(spri[prime_cnt - 1], i);
17         }
18         for (int j = 1, x; j <= lpf[i] && (x = i * prime[j]) <= n; ++j) lpf[x] = j;
19     }
20 }

```

```

19     }
20 }
21
22 ll g_n, lis[MAX_SIZE];
23 int G[MAX_SIZE][2], Fprime[MAX_SIZE], cnt;
24 int lim, le[MAX_SIZE], ge[MAX_SIZE];
25 #define idx(x) (x <= lim ? le[x] : ge[g_n / x])
26
27 void init(ll n) {
28     for (ll i = 1, j, x; i <= n; i = n / j + 1) {
29         j = n / i, x = j % MOD;
30         lis[++cnt] = j, idx(j) = cnt;
31         G[cnt][0] = sub(x, 1);
32         G[cnt][1] = (x + 211) * (x - 111) % MOD * INV2 % MOD;
33     }
34 }
35 void calcFPrime() {
36     for (int k = 1; k <= prime_cnt; ++k) {
37         const int p = prime[k];
38         const ll sqrp = 111 * p * p;
39         for (int i = 1; lis[i] >= sqrp; ++i) {
40             const ll x = lis[i] / p;
41             const int id = idx(x);
42             dec(G[i][0], sub(G[id][0], k - 1));
43             dec(G[i][1], 111 * p * sub(G[id][1], spri[k - 1]) % MOD);
44         }
45     }
46     // f(p) = g_1(p) - g_0(p)
47     for (int i = 1; i <= cnt; ++i) Fprime[i] = sub(G[i][1], G[i][0]);
48 }
49
50 int f_p(int p, int c) { return p ^ c; }
51 int F(int k, ll n) {
52     if (n < prime[k] || n <= 1) return 0;
53     const int id = idx(n);
54     int res = sub(Fprime[id], sub(spri[k - 1], k - 1));
55     // F_prime(p_{k-1}) = spri[k-1] - (k-1)
56     if (k == 1) res += 2; // 特殊处理 f(2)
57     for (int i = k; i <= prime_cnt && 111 * prime[i] * prime[i] <= n; ++i) {
58         ll pw = prime[i], pw2 = pw * pw;
59         for (int c = 1; pw2 <= n; ++c, pw = pw2, pw2 *= prime[i])
60             inc(res, (111 * f_p(prime[i], c) * F(i + 1, n / pw) + f_p(prime[i], c + 1)) % MOD);
61     }
62     return res;
63 }

```

新版 min25 筛，复杂度 $O\left(n^{\frac{2}{3}}\right)$ 。

```

1  /*****
2  f()函数中(31-37行)填函数在质数幂次处的表达式
3  pow_sum()函数中(38-43行)填幂和函数(如果需要更高的话可以在这里添加)
4  202-205行按要求填写
5  f_p[][0/1/2/3/...]分别代表质数个数/质数和/质数平方和/质数三次方和/...根据自己需要添加
6  例: 如果该函数在质数处表达式为f(p) =
7  p^2+3*p+1, 则表明需要质数个数/质数和/质数平方和, 即f_p[][0],f_p[][1],f_p[][2]
8  *****/
9
10 inline ll f(ll p, int e) { // return f(p^e)
11     if (p == 1 || e == 0) return 1;
12     ll res = mpow(p, e);
13     return res * res + 3 * res + 1;
14 }
15 ll pow_sum(ll n, int k) { return sum(i^k), i from 1 to n.
16     if (k == 0) return n;
17     if (k == 1) return n * (n + 1) / 2;
18     if (k == 2) return n * (n + 1) * (2 * n + 1) / 6;
19 }
20 ll n, f_p[maxn][3]; // F_prime(id(n/i))

```



```

21 int n_2, n_3, n_6; // sqrt(n), sqrt3(n), sqrt6(n);
22 ll val_id[maxn]; // give the id, return the id-th number like 'n/i' ,(val_id[1] = 1)
23 int val_id_num; // how many numbers like 'n/i'
24 int val_id_num_3; // how many numbers like 'n/i' below n/n_3;
25 int p[200000 + 100];
26 bool isp[maxn];
27 int p_sz_2, p_sz_3, p_sz_6; // pi(n_2), pi(n_3), pi(n_6)
28 void init() {
29     n_2 = (int)sqrt(n);
30     n_3 = (int)pow(n, 1.0 / 3.0);
31     n_6 = (int)pow(n, 1.0 / 6.0);
32     val_id_num = 0;
33     for (ll i = 1; i <= n; i++) {
34         val_id[++val_id_num] = i;
35         if (i < n) i = n / (n / (i + 1));
36     }
37     memset(isp, 1, sizeof isp);
38     isp[1] = 0;
39     for (int i = 2; i <= n_2; i++) {
40         if (isp[i]) {
41             p[++p_sz_2] = i;
42             if (i <= n_3) p_sz_3++;
43             if (i <= n_6) p_sz_6++;
44         }
45         for (int j = 1; j <= p_sz_2 && p[j] * i <= n_2; j++) {
46             isp[i * p[j]] = 0;
47             if (i % p[j] == 0) break;
48         }
49     }
50 }
51 inline int get_id(ll k) { // give a number like 'n/i', return the id of it
52     return k > n_2 ? val_id_num - n / k + 1 : k;
53 }
54 ll c[maxn];
55 void add(int x, ll d) { for (; x < maxn; x += x & -x) c[x] += d; }
56 ll sum(int x) {
57     ll ans = 0;
58     for (; x; x &= x - 1) ans += c[x];
59     return ans;
60 }
61
62 struct node {
63     int k_max;
64     ll val, f_val;
65 };
66 void update_bfs(int k, int type) {
67     queue<node> q;
68     while (!q.empty()) q.pop();
69     int e = 1;
70     for (ll i = p[k]; i < n / n_3; i *= p[k], ++e)
71         q.emplace(k, i, type == -1 ? f(p[k], e) : mpow(i, type));
72     while (!q.empty()) {
73         node hd = q.front(); q.pop();
74         if ((hd.val != p[hd.k_max] && type >= 0) || type == -1) {
75             ll w = n / hd.val;
76             w = n / w;
77             if (type == -1) {
78                 add(get_id(w), hd.f_val);
79                 add(val_id_num + 1, -1ll * hd.f_val);
80             } else {
81                 add(get_id(w), -1ll * hd.f_val);
82                 add(val_id_num + 1, hd.f_val);
83             }
84         }
85         for (int i = hd.k_max + 1; hd.val * p[i] < n / n_3 && i <= p_sz_2; i++) {
86             ll res = p[i];
87             for (int e = 1;; e++) {
88                 if (hd.val * res < n / n_3) {

```

```

89         q.emplace(i, hd.val * res, type == -1 ? hd.f_val * f(p[i], e) : hd.f_val * mpow(res,
90         type));
91     } else break;
92     res *= p[i];
93 }
94 }
95 }
96 void get_f_p(ll n, int times) {
97     for (int i = 1; i <= val_id_num; i++)
98         for (int j = 0; j <= times; j++)
99             f_p[i][j] = pow_sum(val_id[i], j) - 1;
100     int now;
101     for (now = 1; p[now] <= n_6; now++) {
102         for (int j = val_id_num; j >= 1; j--) {
103             ll w = val_id[j] / p[now];
104             if (w < p[now]) break;
105             ll val = 1;
106             for (int k = 0; k <= times; k++) {
107                 f_p[j][k] = f_p[j][k] - val * (f_p[get_id(w)][k] - f_p[p[now] - 1][k]);
108                 val *= p[now];
109             }
110         }
111     }
112     int nnow = now, val = 1;
113     for (int tt = 0; tt <= times; tt++) {
114         now = nnow;
115         memset(c, 0, sizeof c);
116         add(1, f_p[1][tt]);
117         for (int i = 2; val_id[i] < n / n_3; i++) add(i, f_p[i][tt] - f_p[i - 1][tt]);
118         for (; p[now] <= n_3; now++) {
119             for (int j = val_id_num; j >= 1; j--) {
120                 ll w = val_id[j] / p[now];
121                 if (val_id[j] < n / n_3) break;
122                 if (w < p[now]) break;
123                 f_p[j][tt] = w < n / n_3
124                     ? (f_p[j][tt] - (sum(get_id(w)) - sum(p[now - 1])) * mpow(p[now], tt))
125                     : f_p[j][tt] - (f_p[get_id(w)][tt] - sum(p[now - 1])) * mpow(p[now], tt);
126             }
127             update_bfs(now, tt);
128         }
129         for (int i = 1; i <= val_id_num && val_id[i] < n / n_3; i++) f_p[i][tt] = sum(i);
130         for (; now <= p_sz_2; now++) {
131             for (int j = val_id_num; j >= 1; j--) {
132                 ll w = val_id[j] / p[now];
133                 if (val_id[j] < n / n_3) break;
134                 if (w < p[now]) break;
135                 f_p[j][tt] -= (f_p[get_id(w)][tt] - f_p[p[now] - 1][tt]) * mpow(p[now], tt);
136             }
137         }
138     }
139 }
140 for (int i = 1; i <= val_id_num; i++) {
141     // if f(p) = p^2+3p+1, then write: f_p[i][0] = f_p[i][2] + 3*f_p[i][1] + f_p[i][0];
142     f_p[i][0] = f_p[i][2] + 3 * f_p[i][1] + f_p[i][0];
143 }
144 }
145 ll F[2000000 + 100];
146 void get_f_3(ll n) { // V(F_{pi(n^(1/3))+1}, n)
147     ll q = p[p_sz_3 + 1];
148     for (int now = 1; now <= val_id_num; now++) {
149         if (val_id[now] < q) {
150             F[now] = 1;
151         } else if (val_id[now] < q * q) {
152             F[now] = 1 + (f_p[now][0] - f_p[q - 1][0]);
153         } else {
154             F[now] = 1 + (f_p[now][0] - f_p[q - 1][0]);
155             for (int pp = p_sz_3 + 1; p[pp] <= (int)(sqrt(val_id[now])) && pp <= p_sz_2; pp++) {

```

```

156     F[now] += f(p[pp], 2) + (f(p[pp], 1)) * (f_p[get_id(val_id[now] / p[pp])][0] - f_p[get_id(
157     p[pp])][0]);
158 }
159 }
160 }
161 void get_f_6(ll n) { // V(F_{pi(n^(1/6))+1},n)
162     memset(c, 0, sizeof c), add(1, F[1]);
163     for (int i = 2; val_id[i] < n / n_3; i++) add(i, F[i] - F[i - 1]);
164     for (int k = p_sz_3; k > p_sz_6; k--) {
165         int now = val_id_num;
166         for (; val_id[now] >= n / n_3; now--) {
167             int e = 1;
168             ll _p = p[k];
169             while (val_id[now] / _p) {
170                 if (val_id[now] / _p >= n / n_3) {
171                     F[now] += F[get_id(val_id[now] / _p)] * f(p[k], e);
172                 } else {
173                     F[now] += sum(get_id(val_id[now] / _p)) * f(p[k], e);
174                 }
175                 _p *= p[k], e++;
176             }
177         }
178         if (k == 1) break;
179         update_bfs(k, -1); // bfs to update [lpf(i)==P{k-1}]f(i)
180     }
181     for (int i = 1; i <= val_id_num && val_id[i] < n / n_3; i++) F[i] = sum(i);
182 }
183 void get_f(ll n) {
184     for (int k = p_sz_6; k >= 1; k--) {
185         for (int now = val_id_num; now >= 1; now--) {
186             int e = 1;
187             ll _p = p[k];
188             while (val_id[now] / _p) {
189                 F[now] += F[get_id(val_id[now] / _p)] * f(p[k], e);
190                 _p *= p[k], e++;
191             }
192         }
193     }
194 }
195 int main() { // n = 1000000000; 1e10:455052511,0.83s/0.58s; 1e12:37607912018 9.224s/5.105s
196     cin >> n;
197     init();
198     get_f_p(n, 2), get_f_3(n);
199     get_f_6(n), get_f(n);
200     for (int i = 1; i <= val_id_num; i++) cout << val_id[i] << " : " << F[i] << endl;
201 }

```

1.9 类欧几里德算法

$$\text{求 } f = \sum_{i=0}^n \lfloor \frac{ai+b}{c} \rfloor, g = \sum_{i=0}^n i \lfloor \frac{ai+b}{c} \rfloor, h = \sum_{i=0}^n \lfloor \frac{ai+b}{c} \rfloor^2$$

```

1  const ll P = 998244353;
2  ll i2 = 499122177, i6 = 166374059;
3  struct data {
4      data() { f = g = h = 0; }
5      ll f, g, h;
6  }; // 三个函数打包
7  data calc(ll n, ll a, ll b, ll c) {
8      ll ac = a / c, bc = b / c, m = (a * n + b) / c, n1 = n + 1, n21 = n * 2 + 1;
9      data d;
10     if (a == 0) { // 迭代到底层
11         d.f = bc * n1 % P;
12         d.g = bc * n % P * n1 % P * i2 % P;
13         d.h = bc * bc % P * n1 % P;
14         return d;
15     }

```

```

16  if (a >= c || b >= c) { // 取模
17      d.f = n * n1 % P * i2 % P * ac % P + bc * n1 % P;
18      d.g = ac * n % P * n1 % P * n21 % P * i6 % P + bc * n % P * n1 % P * i2 % P;
19      d.h = ac * ac % P * n % P * n1 % P * n21 % P * i6 % P +
20          bc * bc % P * n1 % P + ac * bc % P * n % P * n1 % P;
21      d.f %= P, d.g %= P, d.h %= P;
22
23      data e = calc(n, a % c, b % c, c); // 迭代
24
25      d.h += e.h + 2 * bc % P * e.f % P + 2 * ac % P * e.g % P;
26      d.g += e.g, d.f += e.f;
27      d.f %= P, d.g %= P, d.h %= P;
28      return d;
29  }
30  data e = calc(m - 1, c, c - b - 1, a);
31  d.f = n * m % P - e.f, d.f = (d.f % P + P) % P;
32  d.g = m * n % P * n1 % P - e.h - e.f, d.g = (d.g * i2 % P + P) % P;
33  d.h = n * m % P * (m + 1) % P - 2 * e.g - 2 * e.f - d.f;
34  d.h = (d.h % P + P) % P;
35  return d;
36 }

```

1.10 中国剩余定理

```

1  ll inv(ll a, ll p) {
2      ll x, y;
3      exgcd(a, p, x, y);
4      return (x + p) % p;
5  }
6  ll CRT(ll n, ll *a, ll *m) {
7      ll lcm = 1, res = 0;
8      for (ll i = 0; i < n; ++i) lcm *= m[i];
9      for (ll i = 0; i < n; ++i) {
10         ll t = lcm / m[i], x = inv(t, m[i]);
11         res = (res + a[i] * t % lcm * x) % lcm;
12     }
13     return res;
14 }

```

模数不互质的情况 $\begin{cases} x \equiv a_1 \pmod{m_1} \\ x \equiv a_2 \pmod{m_2} \end{cases}$, 则转换为 $m_1 p - m_2 q = a_2 - a_1$, 最终解 (若有解) 为 $x \equiv m_1 p + a_1 \pmod{\text{lcm}(m_1, m_2)}$ 。

拓展中国剩余定理:

```

1  int exctr(int n, int *a, int *m) {
2      int M = m[0], res = a[0];
3      for (int i = 1; i < n; ++i) {
4          int a = M, b = m[i], c = (a[i] - res % b + b) % b, x, y;
5          int g = exgcd(a, b, x, y), bg = b / g;
6          if (c % g != 0) return -1;
7          x = 1LL * x * (c / g) % bg;
8          res += x * M;
9          M *= bg;
10         res = (res % M + M) % M;
11     }
12     return res;
13 }

```

1.11 原根

- 阶: 若 $(a, m) = 1$, 使 $a^l \equiv 1 \pmod{m}$ 成立的最小的 l , 称为 a 关于模 m 的阶, 记为 $\text{ord}_m a$ 。

- 原根: 若 $(g, m) = 1, \text{ord}_m g = \varphi(m)$, 则称 g 为 m 的一个原根。若 m 有原根, 则 m 一定是下列形式: $\{2, 4, p^a, 2p^a\}$ (这里 p 为奇素数, a 为正整数)。
- 求原根: 设 p_1, p_2, \dots, p_k 是 $\varphi(m)$ 的所有不同的素因数, 则 g 是 m 的原根 $\iff \forall 1 \leq i \leq k$, 有 $g^{\frac{\varphi(m)}{p_i}} \not\equiv 1 \pmod{m}$, 集合 $S = \{g^s \mid 1 \leq s \leq \varphi(m), (s, \varphi(m)) = 1\}$ 给出 m 的全部原根。

1.12 BSGS

大步小步算法用来求离散对数 $x^k \equiv a \pmod{p}$ 。求解 $a^x \equiv b \pmod{p}$ 则, 令 $x = A\lceil\sqrt{p}\rceil - B, 0 \leq A, B \leq \lceil\sqrt{p}\rceil$, 有 $a^{A\lceil\sqrt{p}\rceil} \equiv ba^B \pmod{p}$, 先枚举 A 之后在哈希表中查找 B 就行。

```

1 // Finds the primitive root modulo p
2 int generator(int p) {
3     vector<int> fact;
4     int phi = p - 1, n = phi;
5     for (int i = 2; i * i <= n; ++i) {
6         if (n % i == 0) {
7             fact.push_back(i);
8             while (n % i == 0) n /= i;
9         }
10    }
11    if (n > 1) fact.push_back(n);
12    for (int res = 2; res <= p; ++res) {
13        bool ok = true;
14        for (int factor : fact)
15            if (mpow(res, phi / factor, p) == 1) {
16                ok = false;
17                break;
18            }
19        if (ok) return res;
20    }
21    return -1;
22 }
23 vector<int> BSGS(int n, int k, int a) {
24     if (a == 0) return vector<int>({0});
25
26     int g = generator(n);
27     // Baby-step giant-step discrete logarithm algorithm
28     int sq = (int)sqrt(n + .0) + 1;
29     vector<pair<int, int>> dec(sq);
30     for (int i = 1; i <= sq; ++i)
31         dec[i - 1] = {mpow(g, i * sq * k % (n - 1), n), i};
32
33     sort(dec.begin(), dec.end());
34     int any_ans = -1;
35     for (int i = 0; i < sq; ++i) {
36         int my = mpow(g, i * k % (n - 1), n) * a % n;
37         auto it = lower_bound(dec.begin(), dec.end(), make_pair(my, 0));
38         if (it != dec.end() && it->first == my) {
39             any_ans = it->second * sq - i;
40             break;
41         }
42     }
43     if (any_ans == -1) return vector<int>();
44     // Print all possible answers
45     int delta = (n - 1) / __gcd(k, n - 1);
46     vector<int> ans;
47     for (int cur = any_ans % delta; cur < n - 1; cur += delta)
48         ans.push_back(mpow(g, cur, n));
49     sort(ans.begin(), ans.end());
50     return ans;
51 }

```

1.13 自适应 Simpson

计算 $\int_a^b f(x)dx$ 。

```

1 double simpson(double a, double b) {
2     double c = a + (b - a) / 2;
3     return (f(a) + 4 * f(c) + f(b)) * (b - a) / 6;
4 }
5 double integral(double a, double b, double eps, double A) {
6     double c = a + (b - a) / 2;
7     double L = simpson(a, c), R = simpson(c, b);
8     if (fabs(L + R - A) <= 15 * eps) return L + R + (L + R - A) / 15;
9     return integral(a, c, eps / 2, L) + integral(c, b, eps / 2, R);
10 }
11 double integral(double a, double b, double eps) {
12     return integral(a, b, eps, simpson(a, b));
13 }

```

1.14 卢卡斯定理

卢卡斯定理: $\binom{n}{m} \bmod p = \binom{\lfloor n/p \rfloor}{\lfloor m/p \rfloor} \cdot \binom{n \bmod p}{m \bmod p} \bmod p$

```

1 ll lucas(ll n, ll m, int p) {
2     ll ret = 1;
3     while (n && m) {
4         ll nn = n % p, mm = m % p;
5         if (nn < mm) return 0;
6         ret = ret * fac[nn] % p * inv_fac[mm] % p * inv_fac[nn - mm] % p;
7         n /= p, m /= p;
8     }
9     return ret;
10 }

```

拓展卢卡斯定理: 用于处理 p 不是质数的情况。

对于 $C_n^m \bmod p$, 我们将其转化为 r 个形如 $a_i \equiv C_n^m \pmod{q_i^{\alpha_i}}$ 的同余方程并分别求解; 对于 $a_i \equiv C_n^m \pmod{q_i^{\alpha_i}}$, 将 C_n^m 转化为 $\frac{n!}{m! \frac{(n-m)!}{q^z}} q^{x-y-z}$, 可求逆元; 对于 $\frac{m!}{q^y}$ 和 $\frac{(n-m)!}{q^z}$, 将其变换整理, 可递归求解。

```

1 ll calc(ll n, ll x, ll p) {
2     if (!n) return 1;
3     ll s = 1;
4     for (ll i = 1; i <= p; ++i) (i % x) && (s = s * i % p);
5     s = mpow(s, n / p, p);
6     for (ll i = n / p * p; i <= n; ++i) (i % x) && (s = s * (i % p) % p);
7     return s * calc(n / x, x, p) % p;
8 }
9
10 ll multi_lucas(ll n, ll m, ll x, ll p) {
11     ll cnt = 0;
12     for (ll i = n; i; i /= x) cnt += i / x;
13     for (ll i = m; i; i /= x) cnt -= i / x;
14     for (ll i = n - m; i; i /= x) cnt -= i / x;
15     return mpow(x, cnt, p) * calc(n, x, p) % p * inv(calc(m, x, p), p) % p *
16         inv(calc(n - m, x, p), p) % p;
17 }
18
19 ll exlucas(ll n, ll m, ll P) {
20     ll cnt = 0;
21     static ll p[20], a[20];
22     for (ll i = 2; i * i <= P; ++i) {
23         if (P % i) continue;
24         p[cnt] = i;
25         while (P % i == 0) p[cnt] *= i, P /= i;
26         a[cnt] = multi_lucas(n, m, i, p[cnt]);
27         ++cnt;
28     }
29     if (P > 1) p[cnt] = P, a[cnt] = multi_lucas(n, m, P, P), ++cnt;

```

```

30     return CRT(cnt, a, p);
31 }

```

1.15 Burnside 引理

设 A 和 B 为有限集合, $X = B^A$ 表示所有从 A 到 B 的映射。 G 是 A 上的置换群, X/G 表示 G 作用在 X 上产生的所有等价类的集合 (若 X 中的两个映射经过 G 中的置换作用后相等, 则它们在同一等价类中), 则 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$ 。

Gym 101873B: m 边形, 每边是 $n \times n$ 的矩形, 用 c 种颜色染色, 可进行水平旋转, 问不同多边形个数。

```

1 for (int i = 1; i <= m; ++i) ans = (ans + mpow(c, n * n * __gcd(i, m))) % MOD;
2 ans = 1LL * ans * mpow(m, MOD - 2) % MOD;

```

1.16 Pólya 定理

前置条件与 Burnside 引理相同, 内容修改为 $|X/G| = \frac{1}{|G|} \sum_{g \in G} |B|^{c(g)}$, 其中 $c(g)$ 表示置换 g 能拆分成不相交的循环置换的数量。

1.17 高斯解线性方程

```

1 const double EPS = 1e-9;
2 const int MAXN = MAX_NODE;
3 double a[MAXN][MAXN], x[MAXN];
4 int equ, var;
5
6 int gauss() {
7     int i, j, k, col, max_r;
8     for (k = 0, col = 0; k < equ && col < var; k++, col++) {
9         max_r = k;
10        for (i = k + 1; i < equ; i++)
11            if (fabs(a[i][col]) > fabs(a[max_r][col])) max_r = i;
12        if (fabs(a[max_r][col]) < EPS) return 0;
13
14        if (k != max_r) {
15            for (j = col; j < var; j++) swap(a[k][j], a[max_r][j]);
16            swap(x[k], x[max_r]);
17        }
18
19        x[k] /= a[k][col];
20        for (j = col + 1; j < var; j++) a[k][j] /= a[k][col];
21        a[k][col] = 1;
22
23        for (i = k + 1; i < equ; i++)
24            if (i != k) {
25                x[i] -= x[k] * a[i][col];
26                for (j = col + 1; j < var; j++) a[i][j] -= a[k][j] * a[i][col];
27                a[i][col] = 0;
28            }
29    }
30
31    for (col = equ - 1, k = var - 1; ~col; --col, --k) {
32        if (fabs(a[col][k]) > 0) {
33            for (i = 0; i < k; ++i) {
34                x[i] -= x[k] * a[i][col];
35                for (j = col + 1; j < var; j++) a[i][j] -= a[k][j] * a[i][col];
36                a[i][col] = 0;
37            }
38        }
39    }
40
41    return 1;
42 }

```

1.18 线性回归

```

1 struct LinearRecurrence {
2     using int64 = long long;
3     using vec = std::vector<int64>;
4
5     static void extend(vec &a, size_t d, int64 value = 0) {
6         if (d <= a.size()) return;
7         a.resize(d, value);
8     }
9
10    static vec BerlekampMassey(const vec &s, int64 mod) {
11        std::function<int64(int64)> inverse = [&](int64 a) {
12            return a == 1 ? 1 : (int64)(mod - mod / a) * inverse(mod % a) % mod;
13        };
14        vec A = {1}, B = {1};
15        int64 b = s[0];
16        for (size_t i = 1, m = 1; i < s.size(); ++i, m++) {
17            int64 d = 0;
18            for (size_t j = 0; j < A.size(); ++j) { d += A[j] * s[i - j] % mod; }
19            if (!(d % mod)) continue;
20            if (2 * (A.size() - 1) <= i) {
21                auto temp = A;
22                extend(A, B.size() + m);
23                int64 coef = d * inverse(b) % mod;
24                for (size_t j = 0; j < B.size(); ++j) {
25                    A[j + m] -= coef * B[j] % mod;
26                    if (A[j + m] < 0) A[j + m] += mod;
27                }
28                B = temp, b = d, m = 0;
29            } else {
30                extend(A, B.size() + m);
31                int64 coef = d * inverse(b) % mod;
32                for (size_t j = 0; j < B.size(); ++j) {
33                    A[j + m] -= coef * B[j] % mod;
34                    if (A[j + m] < 0) A[j + m] += mod;
35                }
36            }
37        }
38        return A;
39    }
40
41    static void exgcd(int64 a, int64 b, int64 &g, int64 &x, int64 &y) {
42        if (!b)
43            x = 1, y = 0, g = a;
44        else {
45            exgcd(b, a % b, g, y, x);
46            y -= x * (a / b);
47        }
48    }
49
50    static int64 crt(const vec &c, const vec &m) {
51        int n = c.size();
52        int64 M = 1, ans = 0;
53        for (int i = 0; i < n; ++i) M *= m[i];
54        for (int i = 0; i < n; ++i) {
55            int64 x, y, g, tm = M / m[i];
56            exgcd(tm, m[i], g, x, y);
57            ans = (ans + tm * x * c[i] % M) % M;
58        }
59        return (ans + M) % M;
60    }
61
62    static vec ReedsSloane(const vec &s, int64 mod) {
63        auto inverse = [&](int64 a, int64 m) {
64            int64 d, x, y;
65            exgcd(a, m, d, x, y);
66            return d == 1 ? (x % m + m) % m : -1;

```



```

67 };
68 auto L = [](const vec &a, const vec &b) {
69     int da = (a.size() > 1 || (a.size() == 1 && a[0])) ? a.size() - 1 : -1000;
70     int db = (b.size() > 1 || (b.size() == 1 && b[0])) ? b.size() - 1 : -1000;
71     return std::max(da, db + 1);
72 };
73 auto prime_power = [&](const vec &s, int64 mod, int64 p, int64 e) {
74     // linear feedback shift register mod p^e, p is prime
75     std::vector<vec> a(e), b(e), an(e), bn(e), ao(e), bo(e);
76     vec t(e), u(e), r(e), to(e, 1), uo(e), pw(e + 1);
77     ;
78     pw[0] = 1;
79     for (int i = pw[0] = 1; i <= e; ++i) pw[i] = pw[i - 1] * p;
80     for (int64 i = 0; i < e; ++i) {
81         a[i] = {pw[i]}, an[i] = {pw[i]};
82         b[i] = {0}, bn[i] = {s[0] * pw[i] % mod};
83         t[i] = s[0] * pw[i] % mod;
84         if (t[i] == 0) {
85             t[i] = 1, u[i] = e;
86         } else {
87             for (u[i] = 0; t[i] % p == 0; t[i] /= p, ++u[i])
88                 ;
89         }
90     }
91     for (size_t k = 1; k < s.size(); ++k) {
92         for (int g = 0; g < e; ++g) {
93             if (L(an[g], bn[g]) > L(a[g], b[g])) {
94                 ao[g] = a[e - 1 - u[g]];
95                 bo[g] = b[e - 1 - u[g]];
96                 to[g] = t[e - 1 - u[g]];
97                 uo[g] = u[e - 1 - u[g]];
98                 r[g] = k - 1;
99             }
100         }
101         a = an, b = bn;
102         for (int o = 0; o < e; ++o) {
103             int64 d = 0;
104             for (size_t i = 0; i < a[o].size() && i <= k; ++i) {
105                 d = (d + a[o][i] * s[k - i]) % mod;
106             }
107             if (d == 0) {
108                 t[o] = 1, u[o] = e;
109             } else {
110                 for (u[o] = 0; t[o] = d; t[o] % p == 0; t[o] /= p, ++u[o])
111                     ;
112                 int g = e - 1 - u[o];
113                 if (L(a[g], b[g]) == 0) {
114                     extend(bn[o], k + 1);
115                     bn[o][k] = (bn[o][k] + d) % mod;
116                 } else {
117                     int64 coef =
118                         t[o] * inverse(to[g], mod) % mod * pw[u[o] - uo[g]] % mod;
119                     int m = k - r[g];
120                     extend(an[o], ao[g].size() + m);
121                     extend(bn[o], bo[g].size() + m);
122                     for (size_t i = 0; i < ao[g].size(); ++i) {
123                         an[o][i + m] -= coef * ao[g][i] % mod;
124                         if (an[o][i + m] < 0) an[o][i + m] += mod;
125                     }
126                     while (an[o].size() && an[o].back() == 0) an[o].pop_back();
127                     for (size_t i = 0; i < bo[g].size(); ++i) {
128                         bn[o][i + m] -= coef * bo[g][i] % mod;
129                         if (bn[o][i + m] < 0) bn[o][i + m] += mod;
130                     }
131                     while (bn[o].size() && bn[o].back() == 0) bn[o].pop_back();
132                 }
133             }
134         }
135     }

```

```

135     }
136     return std::make_pair(an[0], bn[0]);
137 };
138
139 std::vector<std::tuple<int64, int64, int>> fac;
140 for (int64 i = 2; i * i <= mod; ++i)
141     if (mod % i == 0) {
142         int64 cnt = 0, pw = 1;
143         while (mod % i == 0) mod /= i, ++cnt, pw *= i;
144         fac.emplace_back(pw, i, cnt);
145     }
146 if (mod > 1) fac.emplace_back(mod, mod, 1);
147 std::vector<vec> as;
148 size_t n = 0;
149 for (auto &&x : fac) {
150     int64 mod, p, e;
151     vec a, b;
152     std::tie(mod, p, e) = x;
153     auto ss = s;
154     for (auto &&x : ss) x %= mod;
155     std::tie(a, b) = prime_power(ss, mod, p, e);
156     as.emplace_back(a);
157     n = std::max(n, a.size());
158 }
159 vec a(n), c(as.size(), m(as.size()));
160 for (size_t i = 0; i < n; ++i) {
161     for (size_t j = 0; j < as.size(); ++j) {
162         m[j] = std::get<0>(fac[j]);
163         c[j] = i < as[j].size() ? as[j][i] : 0;
164     }
165     a[i] = crt(c, m);
166 }
167 return a;
168 }
169
170 LinearRecurrence(const vec &s, const vec &c, int64 mod)
171     : init(s), trans(c), mod(mod), m(s.size()) {}
172
173 LinearRecurrence(const vec &s, int64 mod, bool is_prime = true) : mod(mod) {
174     vec A = is_prime ? BerlekampMassey(s, mod) : ReedsSloane(s, mod);
175     if (A.empty()) A = {0};
176     m = A.size() - 1;
177     trans.resize(m);
178     for (int i = 0; i < m; ++i) { trans[i] = (mod - A[i + 1]) % mod; }
179     std::reverse(trans.begin(), trans.end());
180     init = {s.begin(), s.begin() + m};
181 }
182
183 int64 calc(int64 n) {
184     if (mod == 1) return 0;
185     if (n < m) return init[n];
186     vec v(m), u(m << 1);
187     int msk = !!n;
188     for (int64 m = n; m > 1; m >>= 1) msk <<= 1;
189     v[0] = 1 % mod;
190     for (int x = 0; msk; msk >>= 1, x <<= 1) {
191         std::fill_n(u.begin(), m * 2, 0);
192         x |= !(n & msk);
193         if (x < m)
194             u[x] = 1 % mod;
195         else { // can be optimized by fft/ntt
196             for (int i = 0; i < m; ++i) {
197                 for (int j = 0, t = i + (x & 1); j < m; ++j, ++t) {
198                     u[t] = (u[t] + v[i] * v[j]) % mod;
199                 }
200             }
201             for (int i = m * 2 - 1; i >= m; --i) {
202                 for (int j = 0, t = i - m; j < m; ++j, ++t) {

```

```

203         u[t] = (u[t] + trans[j] * u[i]) % mod;
204     }
205 }
206 }
207 v = {u.begin(), u.begin() + m};
208 }
209 int64 ret = 0;
210 for (int i = 0; i < m; ++i) { ret = (ret + v[i] * init[i]) % mod; }
211 return ret;
212 }
213
214 vec init, trans;
215 int64 mod;
216 int m;
217 };

```

1.19 线性规划

给定 n 个约束条件, m 个未知数, 求 $\sum(a[0][i] \times x[i])$ 的最大值, 约束条件: $\sum(-a[i][j] \times x[j]) \leq a[i][0]$ 。若要求最小值, 则进行对偶: 即把目标函数的系数和约束条件右边的数交换, 然后把矩阵转置。

```

1  const int MAXN = 3e3 + 3, MAXM = 3e3 + 3, INF = ~0U >> 2;
2  int n, m, a[MAXN][MAXM], nxt[MAXM];
3  void pivot(int l, int e) {
4      a[l][e] = -1;
5      int t = MAXM - 1;
6      for (int i = 0; i <= m; ++i)
7          if (a[l][i]) nxt[t] = i, t = i;
8      nxt[t] = -1;
9      for (int i = 0; i <= n; ++i)
10         if (i != l && (t = a[i][e])) {
11             a[i][e] = 0;
12             for (int j = nxt[MAXM - 1]; ~j; j = nxt[j]) a[i][j] += a[l][j] * t;
13         }
14 }
15 int simplex() {
16     for (;;) {
17         int mi = INF, l = 0, e = 0;
18         for (int i = 1; i <= m; ++i)
19             if (a[0][i] > 0) {
20                 e = i;
21                 break;
22             }
23         if (!e) return a[0][0];
24         for (int i = 1; i <= n; ++i)
25             if (a[i][e] < 0 && a[i][0] < mi) mi = a[i][0], l = i;
26         pivot(l, e);
27     }
28 }

```

1.20 实数线性规划

求 $\max\{c\vec{x} | A\vec{x} \leq b, \vec{x} \geq 0\}$ 。

```

1  typedef vector<double> VD;
2  VD simplex(vector<VD> A, VD b, VD c) {
3      int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
4      vector<VD> D(n + 2, VD(m + 1, 0));
5      vector<int> ix(n + m);
6      for (int i = 0; i < n + m; ++i) ix[i] = i;
7      for (int i = 0; i <= n; ++i) {
8          for (int j = 0; j < m - 1; ++j) D[i][j] = -A[i][j];
9          D[i][m - 1] = 1, D[i][m] = b[i];
10         if (D[r][m] > D[i][m]) r = i;
11     }

```

```

12 for (int j = 0; j < m - 1; ++j) D[n][j] = c[j];
13 D[n + 1][m - 1] = -1;
14 for (double d;;) {
15     if (r < n) {
16         swap(ix[s], ix[r + m]);
17         D[r][s] = 1 / D[r][s];
18         vector<int> speed_up;
19         for (int j = 0; j <= m; ++j)
20             if (j != s) {
21                 D[r][j] *= -D[r][s];
22                 if (D[r][j]) speed_up.push_back(j);
23             }
24         for (int i = 0; i <= n + 1; ++i)
25             if (i != r) {
26                 for (int j : speed_up) D[i][j] += D[r][j] * D[i][s];
27                 D[i][s] *= D[r][s];
28             }
29     }
30     r = -1, s = -1;
31     for (int j = 0; j < m; ++j)
32         if ((s < 0 || ix[s] > ix[j]) &&
33             (D[n + 1][j] > EPS || (D[n + 1][j] > -EPS && D[n][j] > EPS)))
34             s = j;
35     if (s < 0) break;
36     for (int i = 0; i < n; ++i)
37         if (D[i][s] < -EPS)
38             if (r < 0 || (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -EPS ||
39                 (d < EPS && ix[r + m] > ix[i + m]))
40                 r = i;
41     if (r < 0) return VD(); //无边界
42 }
43 if (D[n + 1][m] < -EPS) return VD(); // 无解
44 VD x(m - 1);
45 for (int i = m; i < n + m; ++i)
46     if (ix[i] < m - 1) x[ix[i]] = D[i - m][m];
47 return x; // 最优值在D[n][m]
48 }

```

UOJ 板题最快榜代码:

```

1 #include <bits/stdc++.h>
2 using namespace std;
3
4 #define eps 1e-7
5 int simplex(vector<vector<double>> &a, vector<double> &b, vector<double> &c,
6             vector<int> &basic) {
7     int m = b.size(), n = c.size();
8     while (true) {
9         int k = -1;
10        for (int j = 0; j < n; ++j)
11            if (c[j] < -eps) {
12                k = j;
13                break;
14            }
15        if (k == -1) {
16            double ans = 0;
17            for (int i = 0; i < m; ++i) ans += c[basic[i]] * b[i];
18            return 0;
19        }
20        int l = -1;
21        for (int i = 0; i < m; ++i)
22            if (a[i][k] > eps) {
23                if (l == -1)
24                    l = i;
25                else {
26                    double ti = b[i] / a[i][k], tl = b[l] / a[l][k];
27                    if (ti < tl - eps || (ti < tl + eps && basic[i] < basic[l])) l = i;
28                }
29            }
30    }
31 }

```

```

30     if (l == -1) return -1;
31     basic[l] = k;
32     double tmp = 1 / a[l][k];
33     for (int j = 0; j < n; ++j) a[l][j] *= tmp;
34     b[l] *= tmp;
35     for (int i = 0; i < m; ++i)
36         if (i != l) {
37             tmp = a[i][k];
38             for (int j = 0; j < n; ++j) a[i][j] -= tmp * a[l][j];
39             b[i] -= tmp * b[l];
40         }
41     tmp = c[k];
42     for (int j = 0; j < n; ++j) c[j] -= tmp * a[l][j];
43 }
44 }
45
46 int main() {
47     ios::sync_with_stdio(false);
48     int n, m, T;
49     cin >> n >> m >> T;
50     vector<double> c(n + m, 0);
51     for (int i = 0; i < n; ++i) {
52         cin >> c[i];
53         c[i] *= -1;
54     }
55     auto C = c;
56     vector<vector<double>> a(m, vector<double>(n + m, 0));
57     vector<double> b(m);
58     vector<int> basic(m, -1), tmp;
59     for (int i = 0; i < m; ++i) {
60         for (int j = 0; j < n; ++j) cin >> a[i][j];
61         a[i][i + n] = 1;
62         cin >> b[i];
63         if (b[i] > -eps)
64             basic[i] = i + n;
65         else
66             tmp.push_back(i);
67     }
68     if (!tmp.empty()) {
69         sort(tmp.begin(), tmp.end(), [&](int i, int j) { return b[i] > b[j]; });
70         vector<vector<double>> A;
71         vector<double> B, C(n + m + 1, 0);
72         vector<int> Basic;
73         for (int i : tmp) {
74             vector<double> foo;
75             for (int j = 0; j < n + m; ++j) foo.push_back(-a[i][j]);
76             foo.push_back(1);
77             double bar = -b[i];
78             for (int i = 0; i < A.size(); ++i) {
79                 double tmp = foo[Basic[i]];
80                 for (int j = 0; j <= n + m; ++j) foo[j] -= tmp * A[i][j];
81                 bar -= tmp * B[i];
82             }
83             for (int j = n + m; j >= 0; --j)
84                 if (-eps < foo[j] - 1 && foo[j] - 1 < eps) {
85                     Basic.push_back(j);
86                     break;
87                 }
88             for (int i = 0; i < A.size(); ++i) {
89                 double tmp = A[i][Basic.back()];
90                 for (int j = 0; j <= n + m; ++j) A[i][j] -= tmp * foo[j];
91                 B[i] -= tmp * bar;
92             }
93             A.push_back(foo);
94             B.push_back(bar);
95         }
96         for (int i = 0; i < A.size(); ++i)
97             if (Basic[i] == n + m) {

```

```

98     for (int j = 0; j < n + m; ++j) C[j] = -A[i][j];
99     }
100     for (int i = 0; i < m; ++i)
101     if (b[i] > -eps) {
102         A.push_back(a[i]);
103         A[A.size() - 1].push_back(0);
104         B.push_back(b[i]);
105         Basic.push_back(basic[i]);
106     }
107     simplex(A, B, C, Basic);
108     bool flag = true;
109     for (int i = 0; i < m; ++i)
110     if (Basic[i] == n + m) {
111         if (B[i] > eps) {
112             cout << "Infeasible\n";
113             return 0;
114         }
115         int k = -1;
116         for (int j = 0; j < n + m; ++j)
117             if (A[i][j] > eps || A[i][j] < -eps) {
118                 k = j;
119                 break;
120             }
121         if (k != -1) {
122             double tmp = 1 / A[i][k];
123             Basic[i] = k;
124             for (int j = 0; j <= n + m; ++j) A[i][j] *= tmp;
125             B[i] *= tmp;
126             for (int l = 0; l < m; ++l)
127                 if (l != i) {
128                     tmp = A[l][k];
129                     for (int j = 0; j <= n + m; ++j) A[l][j] -= tmp * A[i][j];
130                     B[l] -= tmp * B[i];
131                 }
132             } else
133             flag = false;
134             break;
135         }
136     if (flag) {
137         A.push_back(vector<double>(n + m, 0));
138         A[A.size() - 1].push_back(1);
139         B.push_back(0);
140         Basic.push_back(n + m);
141         for (int i = 0; i < A.size() - 1; ++i) {
142             double tmp = A[i].back();
143             for (int j = 0; j <= n + m; ++j) A[i][j] -= tmp * A[A.size() - 1][j];
144             B[i] -= tmp * B.back();
145         }
146     }
147     a = A;
148     b = B;
149     basic = Basic;
150     c.push_back(0);
151     for (int i = 0; i < a.size(); ++i) {
152         double tmp = c[basic[i]];
153         for (int j = 0; j <= n + m; ++j) c[j] -= tmp * a[i][j];
154     }
155 }
156 auto foo = simplex(a, b, c, basic);
157 if (foo == -1)
158     cout << "Unbounded" << endl;
159 else {
160     double res = 0;
161     vector<double> ans(n, 0);
162     for (int i = 0; i < basic.size(); ++i)
163         if (basic[i] < n) ans[basic[i]] = b[i];
164     for (int j = 0; j < n; ++j) res -= C[j] * ans[j];
165     cout << setprecision(8) << res << endl;

```

```

166     if (T == 1) {
167         for (int i = 0; i < n; ++i) cout << setprecision(8) << ans[i] << ' ';
168         cout << endl;
169     }
170 }
171 return 0;
172 }

```

CCPC Final 2017 F: 有 N 组人, 每组有 a_i 人, 可进行若干次选择, 每次选择一些至少有 M 人的组, 这些人都中奖。现在要使每个人中奖概率相等, 且中奖概率最大 $N \leq 10, M, a_i \leq 100$ 。两种 LP 写法:

```

1  const int MAXN = int(3e3);
2  const int MAXM = int(3e3);
3  const double INF = 1e20, EPS = 1e-9;
4
5  int n, m;
6  double a[MAXM][MAXN], v;
7
8  void pivot(int l, int e) {
9      int i, j;
10     a[l][e] = 1 / a[l][e];
11     for (j = 0; j <= n; ++j)
12         if (j != e) a[l][j] *= a[l][e];
13     for (i = 1; i <= m; ++i)
14         if (i != l && fabs(a[i][e]) > EPS) {
15             for (j = 0; j <= n; ++j)
16                 if (j != e) a[i][j] -= a[i][e] * a[l][j];
17             a[i][e] = -a[i][e] * a[l][e];
18         }
19     v += a[0][e] * a[l][0];
20     for (j = 1; j <= n; ++j)
21         if (j != e) a[0][j] -= a[0][e] * a[l][j];
22     a[0][e] = -a[0][e] * a[l][e];
23 }
24
25 double simplex() {
26     int e, l, i;
27     double mn;
28     v = 0;
29     while (true) {
30         for (e = 1; e <= n; ++e)
31             if (a[0][e] > EPS) break;
32         if (e > n) return v;
33         for (i = 1, mn = INF; i <= m; ++i)
34             if (a[i][e] > EPS && mn > a[i][0] / a[i][e])
35                 mn = a[i][0] / a[i][e], l = i;
36         if (mn == INF) return INF;
37         pivot(l, e);
38     }
39 }
40
41 void solve() {
42     static int n, m, g[10];
43     static vector<int> con[10], able;
44     scanf("%d %d", &n, &m);
45     for (int i = 0; i < n; ++i) {
46         scanf("%d", g + i);
47         con[i].clear();
48     }
49     if (n == 1) {
50         printf("%.10f\n", m >= g[0] ? 1. : 0.);
51         return;
52     }
53     able.clear();
54     for (int s = 0, S = 1 << n; s < S; ++s) {
55         int sum = 0;
56         for (int i = 0; i < n; ++i)
57             if (s >> i & 1) sum += g[i];

```

```

58     if (sum > m) continue;
59     able.push_back(s);
60     for (int i = 0; i < n; ++i)
61         if (s >> i & 1) con[i].push_back(able.size());
62 }
63 ::n = able.size();
64 ::m = 0;
65 static random_device rd;
66 mt19937 gen(rd());
67 shuffle(able.begin(), able.end(), gen);
68 for (int step = 0; step < n; ++step) {
69     int f = ++::m;
70     for (int i = 0; i <= ::n; ++i) a[f][i] = 0;
71     for (int x : con[step]) ++a[f][x];
72     if (step + 1 < n) {
73         for (int x : con[step + 1]) --a[f][x];
74     } else {
75         for (int x : con[0]) --a[f][x];
76     }
77 }
78
79 ++::m;
80 a[::m][0] = 1;
81 for (int i = 1; i <= ::n; ++i) a[::m][i] = 1;
82
83 ++::m;
84 a[::m][0] = -1;
85 for (int i = 1; i <= ::n; ++i) a[::m][i] = -1;
86
87 for (int i = 0; i <= ::n; ++i) a[0][i] = 0;
88 for (int x : con[0]) ++a[0][x];
89 printf("%.10f\n", simplex());
90 }

```

```

1  const int MAXN = 3000;
2  const int MAXM = 3000;
3  const db EPS = 1e-9;
4  const db INF = 1e200;
5
6  namespace LP {
7  db a[MAXM][MAXN];
8  int idA[MAXN], idB[MAXN];
9  int m, n;
10
11 void put_out(int x) {
12     if (x == 0)
13         printf("Infeasible\n");
14     else
15         printf("Unbounded\n");
16     exit(0);
17 }
18 void pivot(int xA, int xB) {
19     swap(idA[xA], idB[xB]);
20     static int next[MAXN];
21     int i, j, last = MAXN - 1;
22     db tmp = -a[xB][xA];
23     a[xB][xA] = -1.0;
24     for (j = 0; j <= n; j++)
25         if (fabs(a[xB][j]) > EPS) a[xB][last = next[last] = j] /= tmp;
26     next[last] = -1;
27
28     for (i = 0; i <= m; i++)
29         if (i != xB && fabs(tmp = a[i][xA]) > EPS)
30             for (a[i][xA] = 0.0, j = next[MAXN - 1]; ~j; j = next[j])
31                 a[i][j] += tmp * a[xB][j];
32 }
33 db calc() {
34     int xA, xB;

```



```

35 db Max, tmp;
36 while (1) {
37     xA = n + 1, idA[xA] = n + m + 1;
38     for (int i = 1; i <= n; i++)
39         if (a[0][i] > EPS && idA[i] < idA[xA]) xA = i;
40
41     if (xA == n + 1) return a[0][0];
42     xB = m + 1, idB[xB] = n + m + 1, Max = -INF;
43     for (int i = 1; i <= m; i++)
44         if (a[i][xA] < -EPS && ((tmp = a[i][0] / a[i][xA]) > Max + EPS ||
45             (tmp > Max - EPS && idB[i] < idB[xB])))
46             Max = tmp, xB = i;
47     if (xB == m + 1) put_out(1);
48     pivot(xA, xB);
49 }
50 return a[0][0];
51 }
52 db solve() {
53     for (int i = 1; i <= n; i++) idA[i] = i;
54     for (int i = 1; i <= m; i++) idB[i] = n + i;
55     static db tmp[MAXN];
56     db Min = 0.0;
57     int l;
58     for (int i = 1; i <= m; i++)
59         if (a[i][0] < Min) Min = a[i][0], l = i;
60     if (Min > -EPS) return calc();
61
62     idA[++n] = 0;
63     for (int i = 1; i <= m; i++) a[i][n] = 1.0;
64     for (int i = 0; i <= n; i++) tmp[i] = a[0][i], a[0][i] = 0.0;
65     a[0][n] = -1.0;
66
67     pivot(n, l);
68     if (calc() < -EPS) put_out(0);
69     for (int i = 1; i <= m; i++)
70         if (!idB[i]) {
71             for (int j = 1; j <= n; j++)
72                 if (fabs(a[0][j]) > EPS) {
73                     pivot(j, i);
74                     break;
75                 }
76             break;
77         }
78
79     int xA;
80     for (xA = 1; xA <= n; xA++)
81         if (!idA[xA]) break;
82     for (int i = 0; i <= m; i++) a[i][xA] = a[i][n];
83     idA[xA] = idA[n], n--;
84
85     for (int i = 0; i <= n; i++) a[0][i] = 0.0;
86     for (int i = 1; i <= m; i++)
87         if (idB[i] <= n) {
88             for (int j = 0; j <= n; j++) a[0][j] += a[i][j] * tmp[idB[i]];
89         }
90
91     for (int i = 1; i <= n; i++)
92         if (idA[i] <= n) a[0][i] += tmp[idA[i]];
93     return calc();
94 }
95 db ans[MAXN];
96 void findAns() {
97     for (int i = 1; i <= n; i++) ans[i] = 0.0;
98     for (int i = 1; i <= m; i++)
99         if (idB[i] <= n) ans[idB[i]] = a[i][0];
100 }
101 void work() {
102     for (int i = 1; i <= m; ++i)

```

```

103     for (int j = 1; j <= n; ++j) a[i][j] *= -1;
104     printf("%.10f\n", -double(solve()));
105 }
106 } // namespace LP
107
108 void solve() {
109     static int n, m, g[10];
110     static vector<int> con[10], able;
111
112     scanf("%d %d", &n, &m);
113     for (int i = 0; i < n; ++i) {
114         scanf("%d", g + i);
115         con[i].clear();
116     }
117     if (n == 1) {
118         printf("%.10f\n", m >= g[0] ? 1.0 : 0.0);
119         return;
120     }
121     able.clear();
122     for (int s = 0; s < (1 << n); ++s) {
123         int sum = 0;
124         for (int i = 0; i < n; ++i)
125             if (s >> i & 1) sum += g[i];
126         if (sum > m) continue;
127         able.push_back(s);
128         for (int i = 0; i < n; ++i)
129             if (s >> i & 1) con[i].push_back(able.size());
130     }
131
132     LP::n = able.size(), LP::m = 0;
133     for (int step = 0; step < n; ++step) {
134         int &f = ++LP::m;
135         for (int i = 0; i <= LP::n; ++i) LP::a[f][i] = 0;
136         for (int x : con[step]) ++LP::a[f][x];
137         if (step + 1 < n) {
138             for (int x : con[step + 1]) --LP::a[f][x];
139         } else {
140             for (int x : con[0]) --LP::a[f][x];
141         }
142     }
143
144     ++LP::m;
145     LP::a[LP::m][0] = 1;
146     for (int i = 1; i <= LP::n; ++i) LP::a[LP::m][i] = 1;
147
148     ++LP::m;
149     LP::a[LP::m][0] = -1;
150     for (int i = 1; i <= LP::n; ++i) LP::a[LP::m][i] = -1;
151
152     for (int i = 0; i <= LP::n; ++i) LP::a[0][i] = 0;
153     for (int x : con[0]) ++LP::a[0][x];
154
155     static db a2[MAXM][MAXN];
156     for (int i = 1; i <= LP::m; ++i)
157         for (int j = 1; j <= LP::n; ++j) a2[i][j] = LP::a[i][j];
158     for (int i = 1; i <= LP::m; ++i)
159         for (int j = 1; j <= LP::n; ++j) LP::a[j][i] = a2[i][j];
160     swap(LP::n, LP::m);
161     for (int i = 1; i <= max(LP::n, LP::m); ++i) swap(LP::a[0][i], LP::a[i][0]);
162     LP::a[0][0] = 0;
163     for (int i = 1; i <= LP::m; ++i)
164         for (int j = 1; j <= LP::n; ++j) LP::a[i][j] *= -1;
165     for (int i = 1; i <= LP::m; ++i) LP::a[i][0] *= -1;
166     for (int i = 1; i <= LP::n; ++i) LP::a[0][i] *= -1;
167
168     LP::work();
169 }

```

1.21 快速傅里叶变换

```

1  const int MAXN = 4 * 1e5 + 3;
2  const double PI = acos(-1);
3  complex<double> a[MAXN], b[MAXN];
4
5  int n, bit;
6  int rev[MAXN];
7
8  void fft(complex<double> *a, int sign) {
9      for (int i = 0; i < n; ++i)
10         if (i < rev[i]) swap(a[i], a[rev[i]]);
11     for (int j = 1; j < n; j <= 1) {
12         complex<double> wn(cos(2 * PI / (j <= 1)), sign * sin(2 * PI / (j <= 1)));
13         for (int i = 0; i < n; i += (j <= 1)) {
14             complex<double> w(1, 0), t0, t1;
15             for (int k = 0; k < j; ++k, w *= wn) {
16                 t0 = a[i + k], t1 = w * a[i + j + k];
17                 a[i + k] = t0 + t1, a[i + j + k] = t0 - t1;
18             }
19         }
20     }
21     if (sign == -1) for (int i = 0; i < n; ++i) a[i] /= n;
22 }
23
24 int main() {
25     int n, m, x;
26     cin >> n >> m;
27     for (int i = 0; i <= n; ++i) cin >> x, a[i].real(x);
28     for (int i = 0; i <= m; ++i) cin >> x, b[i].real(x);
29
30     for (::n = 1, bit = 0; ::n <= n + m; ++bit) ::n <= 1;
31     rev[0] = 0;
32     for (int i = 1; i < ::n; ++i) rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (bit - 1));
33     fft(a, 1), fft(b, 1);
34     for (int i = 0; i < ::n; ++i) a[i] *= b[i];
35     fft(a, -1);
36     for (int i = 0; i < n + m + 1; ++i) cout << int(a[i].real() + .5) << " \n"[i == n + m];
37     return 0;
38 }

```

1.22 快速数论变换

998244353 原根为 3, 1004535809 原根为 3, 786433 原根为 10, 880803841 原根为 26。

```

1  void ntt(int *x, int n, int sign) {
2      for (int i = 0; i < n; ++i)
3         if (rev[i] < i) swap(x[i], x[rev[i]]);
4      for (int j = 1; j < n; j <= 1) {
5         int gn = mpow(G, (P - 1) / (j <= 1));
6         for (int i = 0; i < n; i += (j <= 1)) {
7             for (int k = 0, g = 1; k < j; ++k, g = 1ll * g * gn % P) {
8                 int &a = x[i + j + k], &b = x[i + k], t = 1ll * g * a % P;
9                 (a = b - t) < 0 ? a += P : 0;
10                (b = b + t) >= P ? b -= P : 0;
11            }
12        }
13    }
14    if (sign == -1) {
15        reverse(x + 1, x + n);
16        for (int i = 0, inv = mpow(n, P - 2); i < n; ++i)
17            x[i] = 1ll * x[i] * inv % P;
18    }
19 }

```

1.23 快速沃尔什变换

$C_i = \sum_{j \oplus k = i} A_j B_k$, 其中 \oplus 为位运算。

```

1 void fwt(int *a, int n) {
2     for (int d = 1; d < n; d <= 1)
3         for (int m = d < 1, i = 0; i < n; i += m)
4             for (int j = 0; j < d; ++j) {
5                 int x = a[i + j], y = a[i + j + d];
6                 a[i + j] = x + y; // AND
7                 a[i + j + d] = x + y; // OR
8                 a[i + j] = x + y, a[i + j + d] = x - y; // XOR
9             }
10 }
11 void ufwf(int *a, int n) {
12     for (int d = 1; d < n; d <= 1)
13         for (int m = d < 1, i = 0; i < n; i += m)
14             for (int j = 0; j < d; ++j) {
15                 int x = a[i + j], y = a[i + j + d];
16                 a[i + j] = x - y; // AND
17                 a[i + j + d] = y - x; // OR
18                 a[i + j] = (x + y) / 2, a[i + j + d] = (x - y) / 2; // XOR
19             }
20 }

```

2 动态规划

2.1 斜率优化

树上斜率优化, 定义 dp_i 表示 i 节点传递到根节点的最短耗时, 规定 $dp_{root} = -P$, 有如下转移方程 $dp_u = dp_v + dist(u, v)^2 + P$, v 为 u 的祖先。

```

1 vector<pii> adj[MAXN];
2 ll dp[MAXN], d[MAXN];
3 int n, p, q[MAXN], head, tail;
4
5 inline ll S(int a, int b) { return (d[b] - d[a]) <= 1; }
6 inline ll G(int a, int b) { return dp[b] - dp[a] + d[b] * d[b] - d[a] * d[a]; }
7
8 void dfs(int u, int from) {
9     vector<int> dhead, dtail;
10    if (u ^ 1) {
11        while (head + 2 <= tail &&
12              S(q[head + 1], q[head]) * d[u] <= G(q[head + 1], q[head]))
13            dhead.push_back(q[head++]);
14        int v = q[head];
15        dp[u] = dp[v] + p + (d[u] - d[v]) * (d[u] - d[v]);
16    }
17    while (head + 2 <= tail &&
18          G(u, q[tail - 1]) * S(q[tail - 1], q[tail - 2]) <=
19          G(q[tail - 1], q[tail - 2]) * S(u, q[tail - 1]))
20      dtail.push_back(q[--tail]);
21    q[tail++] = u;
22    for (pii &e : adj[u]) {
23        if (e.first == from) continue;
24        d[e.first] = d[u] + e.second;
25        dfs(e.first, u);
26    }
27    --tail;
28    for (int i = dtail.size() - 1; ~i; --i) q[tail++] = dtail[i];
29    for (int i = dhead.size() - 1; ~i; --i) q[--head] = dhead[i];
30 }
31
32 void solve() {
33     cin >> n >> p;
34     for (int i = 1; i <= n; ++i) adj[i].clear();

```

```

35 for (int i = 1, u, v, w; i < n; ++i) {
36     cin >> u >> v >> w;
37     adj[u].emplace_back(v, w);
38     adj[v].emplace_back(u, w);
39 }
40 dp[1] = -p;
41 head = tail = 0;
42 dfs(1, 1);
43
44 ll ans = 0;
45 for (int i = 1; i <= n; ++i)
46     if (dp[i] > ans) ans = dp[i];
47 cout << ans << '\n';
48 }

```

2.2 整数划分

$f_{i,j}$ 表示选了 i 种不同的数字, 和为 j 的方案数。 $f_{i,j} = f_{i-1,j-1} + f_{i,j-i}$, 意义: 要么新选一个 1, 要么前面的数都加一。若每个数字最多一个, $f_{i,j} = f_{i-1,j-i} + f_{i,j-i}$ 。

求将 n 划分为若干整数的方案, 则设 g_n 为答案, 代码如下, 时间复杂度 $O(n\sqrt{n})$ 。

```

1 int f[732], g[20001];
2 void init() {
3     f[1] = 1, f[2] = 2, f[3] = 5, f[4] = 7;
4     for (int i = 5; i < 732; ++i) f[i] = 3 + 2 * f[i - 2] - f[i - 4];
5     for (int i = g[0] = 1; i <= n; ++i)
6         for (int j = 1; f[j] <= i; ++j)
7             g[i] = ((j + 1) >> 1 & 1) ? (g[i] + g[i - f[j]]) % MOD : (g[i] - g[i - f[j]] + MOD) % MOD;
8 }

```

3 数据结构

3.1 KD Tree

```

1 // 寻找近点
2 #include <bits/stdc++.h>
3 using namespace std;
4
5 const int MAXN = 2e5 + 5;
6 typedef long long ll;
7
8 namespace KD_Tree {
9
10     const int DIM = 2;
11
12     inline ll sqr(int x) { return 1LL * x * x; }
13
14     struct Point {
15         int x[DIM], id, c;
16
17         ll dist2(const Point &b) const {
18             return sqr(x[0] - b.x[0]) + sqr(x[1] - b.x[1]);
19         }
20     };
21
22     struct QNode {
23         Point p;
24         ll dis2;
25
26         QNode() {}
27         QNode(Point _p, ll _dis2) : p(_p), dis2(_dis2) {}
28
29         bool operator<(const QNode &b) const {
30             return dis2 < b.dis2 || (dis2 == b.dis2 && p.id < b.p.id);
31         }
32     };
33 }

```

```

30     }
31 } ans;
32 struct cmpx {
33     int div;
34     cmpx(int _div) : div(_div) {}
35     bool operator()(const Point &a, const Point &b) {
36         for (int i = 0; i < DIM; ++i)
37             if (a.x[(i + div) % DIM] != b.x[(i + div) % DIM])
38                 return a.x[(i + div) % DIM] < b.x[(i + div) % DIM];
39         return true;
40     }
41 };
42
43 bool cmp(const Point &a, const Point &b, int div) {
44     cmpx cp = cmpx(div);
45     return cp(a, b);
46 }
47
48 struct Node {
49     Point e;
50     Node *lc, *rc;
51     int div;
52 } node_pool[MAXN], *tail, *root;
53 void init() { tail = node_pool; }
54 Node *build(Point *a, int l, int r, int div) {
55     if (l >= r) return nullptr;
56     Node *p = tail++;
57     p->div = div;
58     int mid = (l + r) >> 1;
59     nth_element(a + l, a + mid, a + r, cmpx(div));
60     p->e = a[mid];
61     p->lc = build(a, l, mid, div ^ 1);
62     p->rc = build(a, mid + 1, r, div ^ 1);
63     return p;
64 }
65 void search(Point p, Node *x, int div) {
66     if (!x) return;
67     if (cmp(p, x->e, div)) {
68         search(p, x->lc, div ^ 1);
69         if (ans.dis2 == -1) {
70             if (x->e.c <= p.c) ans = QNode(x->e, p.dist2(x->e));
71             search(p, x->rc, div ^ 1);
72         } else {
73             QNode temp(x->e, p.dist2(x->e));
74             if (x->e.c <= p.c && temp < ans) ans = temp;
75             if (sqr(x->e.x[div] - p.x[div]) <= ans.dis2) search(p, x->rc, div ^ 1);
76         }
77     } else {
78         search(p, x->rc, div ^ 1);
79         if (ans.dis2 == -1) {
80             if (x->e.c <= p.c) ans = QNode(x->e, p.dist2(x->e));
81             search(p, x->lc, div ^ 1);
82         } else {
83             QNode temp(x->e, p.dist2(x->e));
84             if (x->e.c <= p.c && temp < ans) ans = temp;
85             if (sqr(x->e.x[div] - p.x[div]) <= ans.dis2) search(p, x->lc, div ^ 1);
86         }
87     }
88 }
89 void search(Point p) {
90     ans.dis2 = -1;
91     search(p, root, 0);
92 }
93 } // namespace KD_Tree
94
95 void solve() {
96     static KD_Tree::Point p[MAXN];
97     int n, m;

```

```

98     cin >> n >> m;
99     for (int i = 0; i < n; ++i) {
100         p[i].id = i;
101         cin >> p[i].x[0] >> p[i].x[1] >> p[i].c;
102     }
103     KD_Tree::init();
104     KD_Tree::root = KD_Tree::build(p, 0, n, 0);
105
106     for (KD_Tree::Point q; m; --m) {
107         cin >> q.x[0] >> q.x[1] >> q.c;
108         KD_Tree::search(q);
109         cout << KD_Tree::ans.p.x[0] << ' ' << KD_Tree::ans.p.x[1] << ' '
110              << KD_Tree::ans.p.c << '\n';
111     }
112 }
113 int main() {
114     ios::sync_with_stdio(false);
115     cin.tie(nullptr);
116
117     int o_o;
118     for (cin >> o_o; o_o; --o_o) solve();
119
120     return 0;
121 }
122
123 // 寻找远点
124 inline void cmin(int &a, int b) { b < a ? a = b : 1; }
125 inline void cmax(int &a, int b) { a < b ? a = b : 1; }
126 inline int ibs(int a) { return a < 0 ? -a : a; }
127 struct D {
128     int d[2], mx0, mx1, mi0, mi1;
129     D *l, *r;
130 } t[N], *rt;
131 int cpd, ans;
132 inline bool cmp(const D &a, const D &b) {
133     return (a.d[cpd] ^ b.d[cpd]) ? a.d[cpd] < b.d[cpd]
134         : a.d[cpd ^ 1] < b.d[cpd ^ 1];
135 }
136 inline void kd_upd(D *u) {
137     if (u->l) {
138         cmax(u->mx0, u->l->mx0);
139         cmax(u->mx1, u->l->mx1);
140         cmin(u->mi0, u->l->mi0);
141         cmin(u->mi1, u->l->mi1);
142     }
143     if (u->r) {
144         cmax(u->mx0, u->r->mx0);
145         cmax(u->mx1, u->r->mx1);
146         cmin(u->mi0, u->r->mi0);
147         cmin(u->mi1, u->r->mi1);
148     }
149 }
150 D *kd_bld(int l, int r, int d) {
151     int m = l + r >> 1;
152     cpd = d;
153     std::nth_element(t + l + 1, t + m + 1, t + r + 1, cmp);
154     t[m].mx0 = t[m].mi0 = t[m].d[0];
155     t[m].mx1 = t[m].mi1 = t[m].d[1];
156     if (l ^ m) t[m].l = kd_bld(l, m - 1, d ^ 1);
157     if (r ^ m) t[m].r = kd_bld(m + 1, r, d ^ 1);
158     kd_upd(t + m);
159     return t + m;
160 }
161 inline void kd_ins(D *ne) {
162     int cd = 0;
163     D *u = rt;
164     while (true) {
165         cmax(u->mx0, ne->mx0), cmin(u->mi0, ne->mi0);

```

```

166     cmax(u->mx1, ne->mx1), cmin(u->mi1, ne->mi1);
167     if (ne->d[cd] < u->d[cd]) {
168         if (u->l)
169             u = u->l;
170         else {
171             u->l = ne;
172             return;
173         }
174     } else {
175         if (u->r)
176             u = u->r;
177         else {
178             u->r = ne;
179             return;
180         }
181     }
182     cd ^= 1;
183 }
184 }
185 inline int dist(int x, int y, D *u) {
186     int r = 0;
187     if (x < u->mi0)
188         r = u->mi0 - x;
189     else if (x > u->mx0)
190         r = x - u->mx0;
191     if (y < u->mi1)
192         r += u->mi1 - y;
193     else if (y > u->mx1)
194         r += y - u->mx1;
195     return r;
196 }
197 inline void kd_quy(D *u, const int &x, const int &y) {
198     int dl, dr, d0;
199     d0 = abs(u->d[0] - x) + abs(u->d[1] - y);
200     if (d0 < ans) ans = d0;
201     dl = u->l ? dist(x, y, u->l) : inf;
202     dr = u->r ? dist(x, y, u->r) : inf;
203     if (dl < dr) {
204         if (dl < ans) kd_quy(u->l, x, y);
205         if (dr < ans) kd_quy(u->r, x, y);
206     } else {
207         if (dr < ans) kd_quy(u->r, x, y);
208         if (dl < ans) kd_quy(u->l, x, y);
209     }
210 }

```

3.2 zkw 线段树

```

1  int tree[MAXN * 2], pre;
2
3  void init(int n, int *a) {
4      memset(tree, 0, sizeof(tree));
5      for (pre = 1; pre <= n; pre <= 1) {}
6      for (int i = 1; i <= n; ++i) tree[i + pre] = a[i];
7      for (int i = pre; i; --i) tree[i] = max(tree[i << 1], tree[i << 1 | 1]);
8  }
9
10 void update(int pos, const int &val) {
11     tree[pos + pre] = val;
12     for (pos >= 1; pos; pos >= 1)
13         tree[pos] = max(tree[pos << 1], tree[pos << 1 | 1]);
14 }
15
16 int query(int s, int t) {
17     int res = 0;
18     for (s += pre - 1, t += pre + 1; s ^ t ^ 1; s >>= 1, t >>= 1) {

```



```

19     if (~s & 1) res = max(res, tree[s ^ 1]);
20     if (t & 1) res = max(res, tree[t ^ 1]);
21 }
22 return res;
23 }

```

3.3 Splay

```

1 struct Node {
2     long long sum;
3     int id, val, lazy, size;
4     Node *fa, *ch[2];
5 } node_pool[MAXN], *pool_it, *root, *nil;
6
7 Node *newnode(int id, int val) {
8     pool_it->id = id;
9     pool_it->lazy = 0;
10    pool_it->size = 1;
11    pool_it->sum = pool_it->val = val;
12    pool_it->fa = pool_it->ch[0] = pool_it->ch[1] = nil;
13    return pool_it++;
14 }
15
16 void maintain(Node *u) {
17     if (u == nil) { return; }
18     u->size = u->ch[0]->size + u->ch[1]->size + 1;
19     u->sum = u->ch[0]->sum + u->ch[1]->sum + u->val;
20 }
21
22 void push_down(Node *u) {
23     if (u->lazy) {
24         if (u->ch[0] != nil) {
25             u->ch[0]->val += u->lazy;
26             u->ch[0]->sum += 1LL * u->ch[0]->size * u->lazy;
27             u->ch[0]->lazy += u->lazy;
28         }
29         if (u->ch[1] != nil) {
30             u->ch[1]->val += u->lazy;
31             u->ch[1]->sum += 1LL * u->ch[1]->size * u->lazy;
32             u->ch[1]->lazy += u->lazy;
33         }
34         u->lazy = 0;
35     }
36 }
37
38 inline void rot(Node *u) {
39     Node *f = u->fa, *ff = f->fa;
40     int d = u == f->ch[1];
41     push_down(f);
42     push_down(u);
43     if ((f->ch[d] = u->ch[d ^ 1]) != nil) f->ch[d]->fa = f;
44     if ((u->fa = ff) != nil) ff->ch[f == ff->ch[1]] = u;
45     f->fa = u;
46     u->ch[d ^ 1] = f;
47     maintain(f);
48     maintain(u);
49 }
50
51 void splay(Node *u, Node *target) {
52     for (Node *f; u->fa != target; rot(u))
53         if ((f = u->fa)->fa != target) {
54             ((u == f->ch[1]) ^ (f == f->fa->ch[1])) ? rot(u) : rot(f);
55         }
56     if (target == nil) root = u;
57 }
58

```

```

59 inline void insert(int id, int val) {
60     if (root == nil) {
61         root = newnode(id, val);
62         return;
63     }
64     Node *u = root;
65     while (u != nil) {
66         int d = id >= u->id;
67         ++u->size;
68         push_down(u);
69         u->sum += val;
70         if (u->ch[d] != nil) {
71             u = u->ch[d];
72         } else {
73             u->ch[d] = newnode(id, val);
74             u->ch[d]->fa = u;
75             u = u->ch[d];
76             break;
77         }
78     }
79     splay(u, nil);
80 }
81
82 inline Node *find_pred(int id) {
83     Node *u = root, *ret = nil;
84     while (u != nil) {
85         push_down(u);
86         if (u->id < id) {
87             ret = u;
88             u = u->ch[1];
89         } else {
90             u = u->ch[0];
91         }
92     }
93     return ret;
94 }
95
96 inline Node *find_succ(int id) {
97     Node *u = root, *ret = nil;
98     while (u != nil) {
99         push_down(u);
100        if (u->id > id) {
101            ret = u;
102            u = u->ch[0];
103        } else {
104            u = u->ch[1];
105        }
106    }
107    return ret;
108 }
109
110 Node *find_kth(int k) {
111     Node *u = root;
112     while (u != nil) {
113         push_down(u);
114         if (u->ch[0]->size + 1 == k) {
115             splay(u, nil);
116             return u;
117         }
118         if (u->ch[0]->size >= k) {
119             u = u->ch[0];
120         } else {
121             k -= u->ch[0]->size + 1;
122             u = u->ch[1];
123         }
124     }
125     return nil;
126 }

```

```

127
128 Node *range(int l, int r) {
129     Node *pred = find_pred(l);
130     Node *succ = find_succ(r);
131
132     splay(pred, nil);
133     splay(succ, root);
134     push_down(pred);
135     push_down(succ);
136     return root->ch[1]->ch[0];
137 }
138
139 void init() {
140     pool_it = node_pool;
141     nil = pool_it++;
142     nil->ch[0] = nil->ch[1] = nil->fa = nil;
143     nil->id = -1, nil->val = 0;
144     root = nil;
145
146     insert(INT_MIN, 0), insert(INT_MAX, 0);
147 }

```

3.4 LCT

```

1 struct LCT {
2     struct node {
3         int val, add;
4         node *fa, *ch[2];
5         void modify(const int &x) {
6             val += x, add += x;
7         }
8     } node_mset[MaxS], *cnode, *null;
9     LCT() {
10         cnode = node_mset, null = cnode++;
11         *null = (node){0, 0, null, {null, null}};
12     }
13     inline node *newnode() {
14         *cnode = (node){0, 0, null, {null, null}};
15         return cnode++;
16     }
17     inline bool isrt(node *u) const {
18         return (u->fa->ch[0] != u) && (u->fa->ch[1] != u);
19     }
20     inline bool which(node *u) const { return u->fa->ch[1] == u; }
21     void push_down(node *u) {
22         if (!isrt(u)) push_down(u->fa);
23         if (u->add) {
24             u->ch[0]->modify(u->add);
25             u->ch[1]->modify(u->add);
26             u->add = 0;
27         }
28     }
29     inline void rotate(node *u) {
30         node *f = u->fa;
31         int d = which(u);
32         f->ch[d] = u->ch[d ^ 1];
33         f->ch[d]->fa = f;
34         u->ch[d ^ 1] = f;
35         u->fa = f->fa;
36         if (!isrt(f)) f->fa->ch[which(f)] = u;
37         f->fa = u;
38     }
39     inline void splay(node *u) {
40         push_down(u);
41         for (node *f; !isrt(u); rotate(u))
42             if (!isrt(f = u->fa)) rotate(which(u) == which(f) ? f : u);

```

```

43 }
44 inline void access(node *x) {
45     for (node *y = null; x != null; x = x->fa) {
46         splay(x);
47         x->ch[1] = y;
48         y = x;
49     }
50 }
51 inline void cut(node *u) {
52     access(u), splay(u);
53     u->ch[0]->fa = null;
54     u->ch[0] = null;
55 }
56 inline void link(node *u, node *v) {
57     cut(u), u->fa = v;
58 }
59 } tree;

```

4 字符串

4.1 KMP

```

1 void get_next(char *S, int *nxt, int n) {
2     nxt[0] = -1;
3     int j = -1;
4     for (int i = 1; i < n; ++i) {
5         while ((~j) && S[j + 1] != S[i]) j = nxt[j];
6         nxt[i] = (S[j + 1] == S[i]) ? (++j) : j;
7     }
8 }
9
10 int pattern(char *S, char *T, int *nxt, int n, int m) {
11     int j = -1;
12     for (int i = 0; i < m; ++i) {
13         while ((~j) && S[j + 1] != T[i]) j = nxt[j];
14         j += S[j + 1] == T[i];
15         if (j == n - 1) return i - n + 1;
16     }
17     return -1;
18 }

```

4.2 拓展 KMP

next[i]: $x[i..m-1]$ 与 $x[0..m-1]$ 的最长公共前缀, extend[i]: $y[i..n-1]$ 与 $x[0..m-1]$ 的最长公共前缀

```

1 void prework(char x[], int m, int next[]) {
2     next[0] = m;
3     int j = 0;
4     while (j + 1 < m && x[j] == x[j + 1]) ++j;
5     next[1] = j;
6     int k = 1;
7     for (int i = 2; i < m; ++i) {
8         int p = next[k] + k - 1;
9         int L = next[i - k];
10        if (i + L < p + 1)
11            next[i] = L;
12        else {
13            j = max(0, p - i + 1);
14            while (i + j < m && x[i + j] == x[j]) j++;
15            next[i] = j, k = i;
16        }
17    }
18 }

```

```

19 void exkmp(char x[], int m, char y[], int n, int next[], int extend[]) {
20     prework(x, m, next);
21     int j = 0;
22     while (j < n && j < m && x[j] == y[j]) ++j;
23     extend[0] = j;
24     int k = 0;
25     for (int i = 1; i < n; ++i) {
26         int p = extend[k] + k - 1;
27         int L = next[i - k];
28         if (i + L < p + 1)
29             extend[i] = L;
30         else {
31             j = max(0, p - i + 1);
32             while (i + j < n && j < m && y[i + j] == x[j]) j++;
33             extend[i] = j, k = i;
34         }
35     }
36 }

```

4.3 AC 自动机

```

1 int tr[MAX_NODE][26], fail[MAX_NODE], dep[MAX_NODE], node_c;
2
3 int add_char(int u, int id) {
4     if (tr[u][id] < 0) tr[u][id] = node_c++;
5     return tr[u][id];
6 }
7 void build_acam() {
8     queue<int> que;
9     fail[0] = 0;
10    for (int i = 0; i < 26; ++i)
11        if (~tr[0][i]) {
12            que.push(tr[0][i]);
13            fail[tr[0][i]] = 0;
14        } else {
15            tr[0][i] = 0;
16        }
17    while (!que.empty()) {
18        int u = que.front(), f = fail[u];
19        que.pop();
20        for (int i = 0; i < 26; ++i)
21            if (~tr[u][i]) {
22                que.push(tr[u][i]);
23                fail[tr[u][i]] = tr[f][i];
24            } else {
25                tr[u][i] = tr[f][i];
26            }
27    }
28    for (int i = 1; i < node_c; ++i) adj[fail[i]].push_back(i);
29 }

```

4.4 各种哈希

- 树哈希：将子树当作集合哈希，加入深度的影响。
- 集合哈希：可以使用元素的哈希值映射为高进制的某一位，也可以使用质数的积；

```

1 const unsigned int KEY = 6151;
2 const unsigned int MOD = 1610612741;
3 // 64 位哈希参数 KEY 随意 MOD 461168601842738784711
4 unsigned int hash[MAXN], p[MAXN];
5
6 unsigned int get_hash(int l, int r) { return (hash[r] + MOD - 1ULL * hash[l - 1] * p[r - l + 1] %
    MOD) % MOD; }

```

```

7
8 void init(char *s, int n) {
9     p[0] = 1;
10    for (int i = 1; i <= n; ++i) {
11        p[i] = p[i - 1] * KEY % MOD;
12        hash[i] = (1LL * hash[i - 1] * KEY + s[i]) % MOD;
13    }
14 }

```

CCPC 秦皇岛 2020 J: 两次哈希

```

1  const int MAXN = 3e5 + 3;
2  const int MAX_PRIME = 8960453 + 3;
3  const int MOD = 998244353;
4  const ll BASE = 709;
5  const ll HASH_MOD = 46116860184273874711;
6
7  char s[MAXN];
8  int fac[MAXN], inv[MAXN], fac_inv[MAXN], prime[MAXN * 2];
9  ll ha[MAXN], p[MAXN], pref[MAXN], suff[MAXN], value[MAXN * 2];
10 pair<ll, int> bin[MAXN];
11
12 int cnt[MAXN], pidx[MAXN], sidx[MAXN];
13 bitset<MAX_PRIME> mark;
14
15 ll fmul(ll a, ll b) {
16     ll k = (ll)((1.1 * a * b) / (1.1 * HASH_MOD)), t = a * b - k * HASH_MOD;
17     for (t -= HASH_MOD; t < 0; t += HASH_MOD) {}
18     return t;
19 }
20 ll getRange(int l, int r) {
21     return (ha[r] - fmul(ha[l - 1], p[r - l + 1]) + HASH_MOD) % HASH_MOD;
22 }
23
24 int gao(int n, int d) {
25     int tot = 0;
26     for (int l = 1, r = d; r <= n; l += d, r += d) value[tot++] = getRange(l, r);
27     int bunch = n / d, rest = n % d;
28     if (rest) {
29         for (int r = n, l = n - d + 1; l >= 1; l -= d, r -= d)
30             value[tot++] = getRange(l, r);
31         sort(value, value + tot);
32         tot = unique(value, value + tot) - value;
33         pref[0] = pref[1] = suff[n] = suff[n + 1] = 1;
34         for (int i = d; i <= n; i += d) {
35             int idx = lower_bound(value, value + tot, getRange(i - d + 1, i)) - value;
36             pidx[i] = idx;
37             pref[i] = fmul(pref[i - d], prime[idx]);
38         }
39         for (int i = n - d + 1; i >= 1; i -= d) {
40             int idx = lower_bound(value, value + tot, getRange(i, i + d - 1)) - value;
41             sidx[i] = idx;
42             suff[i] = fmul(suff[i + d], prime[idx]);
43         }
44         int sc = 0, cur = fac[bunch];
45         memset(cnt, 0, tot * sizeof(int));
46         for (int l = 1, r = rest; r <= n; l += d, r += d) {
47             if (r + d <= n) {
48                 ++cnt[sidx[r + 1]];
49                 cur = 1ll * cur * inv[cnt[sidx[r + 1]]] % MOD;
50             }
51             bin[sc++] = {fmul(pref[l - 1], suff[r + 1]), 1};
52         }
53         sort(bin, bin + sc);
54         mark[bin[0].second] = 1;
55         for (int i = 1; i < sc; ++i)
56             mark[bin[i].second] = bin[i].first != bin[i - 1].first;
57
58         int res = 0;

```

```

59     for (int l = 1, r = rest; r <= n; l += d, r += d) {
60         if (l - 1 >= 1) {
61             ++cnt[pidx[l - 1]];
62             cur = 1ll * cur * inv[cnt[pidx[l - 1]]] % MOD;
63         }
64         if (mark[l]) {
65             res += cur;
66             if (res >= MOD) res -= MOD;
67         }
68         if (r + 1 <= n) {
69             cur = 1ll * cur * cnt[sidx[r + 1]] % MOD;
70             --cnt[sidx[r + 1]];
71         }
72     }
73     return res;
74 } else {
75     sort(value, value + tot);
76     ll pre = value[0];
77     int res = fac[bunch], cnt = 1;
78     for (int i = 1; i < tot; ++i) {
79         if (value[i] != pre) {
80             if (cnt > 1) res = 1ll * res * fac_inv[cnt] % MOD;
81             cnt = 1, pre = value[i];
82         } else {
83             ++cnt;
84         }
85     }
86     if (cnt > 1) res = 1ll * res * fac_inv[cnt] % MOD;
87     return res;
88 }
89 }
90
91 void solve() {
92     cin >> (s + 1);
93     int n = strlen(s + 1);
94     for (int i = 1; i <= n; ++i)
95         ha[i] = (fmul(ha[i - 1], BASE) + s[i]) % HASH_MOD;
96
97     int ans = 0;
98     for (int d = 1; d <= n; ++d) {
99         ans += gao(n, d);
100         if (ans >= MOD) ans -= MOD;
101     }
102     cout << ans << "\n";
103 }
104
105 void prework() {
106     p[0] = 1;
107     for (int i = 1; i < MAXN; ++i) p[i] = fmul(p[i - 1], BASE);
108     fac[0] = fac[1] = 1;
109     fac_inv[0] = fac_inv[1] = inv[1] = 1;
110     for (int i = 2; i < MAXN; ++i) {
111         fac[i] = 1ll * fac[i - 1] * i % MOD;
112         inv[i] = 1ll * (MOD - MOD / i) * inv[MOD % i] % MOD;
113         fac_inv[i] = 1ll * fac_inv[i - 1] * inv[i] % MOD;
114     }
115
116     int pc = 0;
117     for (int i = 2; i < MAX_PRIME; ++i) {
118         if (!mark[i]) prime[pc++] = i;
119         for (int j = 0; j < pc; ++j) {
120             int t = i * prime[j];
121             if (t >= MAX_PRIME) break;
122             mark[t] = 1;
123             if (i % prime[j] == 0) break;
124         }
125     }
126 }

```

```

127
128 int main(int argc, char *argv[]) {
129     ios::sync_with_stdio(false);
130     cin.tie(nullptr), cout.tie(nullptr);
131
132     prework();
133     int T; cin >> T;
134     for (int step = 1; step <= T; ++step) {
135         cout << "Case #" << step << ": ";
136         solve();
137     }
138
139     return 0;
140 }

```

4.5 mancher

```

1 void mancher(char *s, int n) {
2     static char str[2 * MAX_LENGTH];
3     str[0] = '~', str[1] = '!';
4     int len = 2;
5     for (int i = 0; i < n; ++i) {
6         str[len++] = s[i], str[len++] = '!';
7     }
8     str[len] = 0;
9     for (int i = 1, id = 0, mx = 0; i < len; ++i) {
10        p[i] = i < mx ? min(p[2 * id - i], mx - i) : 1;
11        while (str[i + p[i]] == str[i - p[i]]) ++p[i];
12        if (mx < i + p[i]) id = i, mx = i + p[i];
13    }
14 }

```

4.6 回文树

- $ch[chr][x]$: x 两边添加字符 chr 后的回文串结点;
- $fail[x]$: x 代表的回文串的最长回文后缀;
- $l[x]$: x 代表的回文串的长度;
- $cnt[x]$: x 代表的回文串的出现次数。

```

1 struct PT {
2     char s[MAXL];
3     int fail[MAXL], ch[26][MAXL], l[MAXL], dep[MAXL], cnt[MAXL], lst, nc, n;
4     void init() {
5         l[0] = 0, l[1] = -1;
6         fail[0] = fail[1] = 1;
7         for (int i = 0; i < 26; ++i)
8             for (int j = 0; j < nc; ++j) ch[i][j] = 0;
9         for (int i = 2; i < nc; ++i) l[i] = 0, fail[i] = 0;
10
11         lst = 0, nc = 2, n = 0, s[0] = '#';
12     }
13
14     int insert(char c) {
15         int id = c - 'a';
16         s[++n] = c;
17         while (s[n - l[lst] - 1] != s[n]) { lst = fail[lst]; }
18         if (ch[id][lst] == 0) {
19             l[nc] = l[lst] + 2;
20             int f = fail[lst];
21             while (s[n - l[f] - 1] != s[n]) { f = fail[f]; }

```



```

22     fail[nc] = ch[id][f];
23     dep[nc] = dep[fail[nc]] + 1;
24     ch[id][lst] = nc;
25     ++nc;
26 }
27 ++cnt[lst = ch[id][lst]];
28 return lst;
29 }
30
31 void count() { for (int i = nc - 1; ~i; --i) cnt[fail[i]] += cnt[i]; }
32 } pt;
33
34 // 求最长双回文串
35 char S[MAXL];
36 int len[MAXL];
37 int main() {
38     ios::sync_with_stdio(false);
39     cin.tie(0);
40     cout.tie(0);
41
42     cin >> S;
43     int n = strlen(S);
44     pt.init();
45     for (int i = 0; i < n; ++i) { len[i] = pt.l[pt.insert(S[i])]; }
46     pt.init();
47     int ans = 0;
48     for (int i = n - 1; i; --i) {
49         ans = max(ans, len[i - 1] + pt.l[pt.insert(S[i])]);
50     }
51     cout << ans << "\n";
52
53     return 0;
54 }

```

4.7 后缀数组 (倍增)

```

1  #include <bits/stdc++.h>
2  using namespace std;
3
4  const int MAXN = 1e5 + 3;
5
6  template <int MAX_LENGTH> class SuffixArray {
7  public:
8      int n, sa[MAX_LENGTH], rank[MAX_LENGTH], height[MAX_LENGTH];
9
10     void compute(char *s, int n, int m) {
11         int i, p, w, j, k;
12         this->n = n;
13         if (n == 1) {
14             sa[0] = rank[0] = height[0] = 0;
15             return;
16         }
17         memset(cnt, 0, m * sizeof(int));
18         for (i = 0; i < n; ++i) ++cnt[rank[i] = s[i]];
19         for (i = 1; i < m; ++i) cnt[i] += cnt[i - 1];
20         for (i = n - 1; ~i; --i) sa[--cnt[rank[i]]] = i;
21         for (w = 1; w < n; w <= 1, m = p) {
22             for (p = 0, i = n - 1; i >= n - w; --i) id[p++] = i;
23             for (i = 0; i < n; ++i)
24                 if (sa[i] >= w) id[p++] = sa[i] - w;
25             memset(cnt, 0, m * sizeof(int));
26             for (i = 0; i < n; ++i) ++cnt[px[i] = rank[id[i]]];
27             for (i = 1; i < m; ++i) cnt[i] += cnt[i - 1];
28             for (i = n - 1; ~i; --i) sa[--cnt[px[i]]] = id[i];
29             memcpy(old_rank, rank, n * sizeof(int));
30             for (i = p = 1, rank[sa[0]] = 0; i < n; ++i)

```

```

31     rank[sa[i]] = cmp(sa[i], sa[i - 1], w) ? p - 1 : p++;
32 }
33 for (i = 0; i < n; ++i) rank[sa[i]] = i;
34 for (i = k = height[rank[0]] = 0; i < n; height[rank[i++]] = k)
35     if (rank[i])
36         for (k > 0 ? --k : 0, j = sa[rank[i] - 1]; s[i + k] == s[j + k]; ++k) {}
37 }
38
39 void init_st_table(int n) {
40     int lgn = lg[n];
41     for (int i = 0; i < n; ++i) table[0][i] = height[i];
42     for (int i = 1; i <= lgn; ++i)
43         for (int j = 0, l = 1 << (i - 1); j + l < n; ++j)
44             table[i][j] = min(table[i - 1][j], table[i - 1][j + l]);
45 }
46
47 int lcp(int i, int j) {
48     if (i > j) swap(i, j);
49     ++i;
50     int lgl = lg[j - i + 1];
51     return min(table[lgl][i], table[lgl][j - (1 << lgl) + 1]);
52 }
53
54 private:
55     int table[17][MAX_LENGTH], lg[MAX_LENGTH];
56     int old_rank[MAX_LENGTH], id[MAX_LENGTH], px[MAX_LENGTH], cnt[MAX_LENGTH];
57
58     bool cmp(int x, int y, int w) {
59         return old_rank[x] == old_rank[y] && old_rank[x + w] == old_rank[y + w];
60     }
61 };
62
63 char s[MAXN];
64 SuffixArray<MAXN> sa;
65
66 int main(int argc, char *argv[]) {
67     int n = fread(s, 1, MAXN, stdin);
68     while (s[n - 1] - 97u > 25) --n;
69     for (int i = 0; i < n; ++i) s[i] -= 'a';
70     s[n] = '$';
71     sa.compute(s, n, 26);
72     for (int i = 0; i < n; ++i) printf("%d%c", sa.sa[i] + 1, " \n"[i == n - 1]);
73     for (int i = 1; i < n; ++i) printf("%d%c", sa.height[i], " \n"[i == n - 1]);
74     return 0;
75 }

```

4.8 后缀数组 (SAIS)

UOJ 板题最快算法，字符串必须为正数，BUFFER_SIZE 要随 MAX_LENGTH 同步变化，1e6 为 25。

```

1  #include <bits/stdc++.h>
2
3  const int BUFFER_SIZE = 1u << 23 | 1;
4  char buffer[BUFFER_SIZE], *buffer_ptr = buffer;
5  #define alloc(x, type, len)                                     \
6      type *x = (type *)buffer_ptr;                             \
7      buffer_ptr += (len) * sizeof(type);                       \
8  #define clear_buffer()                                         \
9      memset(buffer, 0, buffer_ptr - buffer), buffer_ptr = buffer;
10
11 template <int MAX_LENGTH> class SuffixArray {
12     #define L_TYPE true
13     #define S_TYPE false
14 public:
15     int sa[MAX_LENGTH], rank[MAX_LENGTH], height[MAX_LENGTH];
16     void compute(int n, int m, int *s) {
17         sais(n, m, s, sa);

```

```

18     for (int i = 0; i < n; ++i) rank[sa[i]] = i;
19     for (int i = 0, h = 0; i < n; ++i) {
20         if (rank[i]) {
21             int j = sa[rank[i] - 1];
22             while (s[i + h] == s[j + h]) ++h;
23             height[rank[i]] = h;
24         } else {
25             h = 0;
26         }
27         if (h) --h;
28     }
29 }
30
31 private:
32     int l_bucket[MAX_LENGTH], s_bucket[MAX_LENGTH];
33
34     void induce(int n, int m, int *s, bool *type, int *sa, int *bucket,
35                 int *l_bucket, int *s_bucket) {
36         memcpy(l_bucket + 1, bucket, m * sizeof(int));
37         memcpy(s_bucket + 1, bucket + 1, m * sizeof(int));
38         sa[l_bucket[s[n - 1]]++] = n - 1;
39         for (int i = 0; i < n; ++i) {
40             int t = sa[i] - 1;
41             if (t >= 0 && type[t] == L_TYPE) sa[l_bucket[s[t]]++] = t;
42         }
43         for (int i = n - 1; i >= 0; --i) {
44             int t = sa[i] - 1;
45             if (t >= 0 && type[t] == S_TYPE) sa[--s_bucket[s[t]]] = t;
46         }
47     }
48     void sais(int n, int m, int *s, int *sa) {
49         alloc(type, bool, n + 1);
50         alloc(bucket, int, m + 1);
51         type[n] = false;
52         for (int i = n - 1; i >= 0; --i) {
53             ++bucket[s[i]];
54             type[i] = s[i] > s[i + 1] || (s[i] == s[i + 1] && type[i + 1] == L_TYPE);
55         }
56         for (int i = 1; i <= m; ++i) {
57             bucket[i] += bucket[i - 1];
58             s_bucket[i] = bucket[i];
59         }
60         memset(rank, -1, n * sizeof(int));
61
62         alloc(lms, int, n + 1);
63         int n1 = 0;
64         for (int i = 0; i < n; ++i) {
65             if (!type[i] && (i == 0 || type[i - 1])) lms[rank[i] = n1++] = i;
66         }
67         lms[n1] = n;
68         memset(sa, -1, n * sizeof(int));
69         for (int i = 0; i < n1; ++i) sa[--s_bucket[s[lms[i]]]] = lms[i];
70         induce(n, m, s, type, sa, bucket, l_bucket, s_bucket);
71         int m1 = 0;
72         alloc(s1, int, n + 1);
73         for (int i = 0, t = -1; i < n; ++i) {
74             int r = rank[sa[i]];
75             if (r != -1) {
76                 int len = lms[r + 1] - sa[i] + 1;
77                 m1 += t == -1 || len != lms[rank[t] + 1] - t + 1 ||
78                     memcmp(s + t, s + sa[i], len * sizeof(int)) != 0;
79                 s1[r] = m1;
80                 t = sa[i];
81             }
82         }
83         alloc(sa1, int, n + 1);
84         if (n1 == m1) {
85             for (int i = 0; i < n1; ++i) sa1[s1[i] - 1] = i;

```

```

86     } else {
87         sais(n1, m1, s1, sa1);
88     }
89     memset(sa, -1, n * sizeof(int));
90     memcpy(s_bucket + 1, bucket + 1, m * sizeof(int));
91     for (int i = n1 - 1; i >= 0; --i) {
92         int t = lms[sa1[i]];
93         sa[--s_bucket[s[t]]] = t;
94     }
95     induce(n, m, s, type, sa, bucket, l_bucket, s_bucket);
96 }
97 #undef S_TYPE
98 #undef L_TYPE
99 };
100
101 const int MAXN = 1e5 + 5;
102 SuffixArray<MAXN> sa;
103 char str[MAXN];
104 int s[MAXN];
105
106 int main() {
107     int n = fread(str, 1, MAXN, stdin);
108     while (str[n - 1] - 97u > 25) --n;
109     for (int i = 0; i < n; ++i) s[i] = str[i] - 'a' + 1;
110     sa.compute(n, 26, s);
111     for (int i = 0; i < n; ++i) printf("%d%c", sa.sa[i] + 1, " \n"[i == n - 1]);
112     for (int i = 1; i < n; ++i) printf("%d%c", sa.height[i], " \n"[i == n - 1]);
113     return 0;
114 }

```

4.9 后缀自动机

SPOJ Lexicographical Substring Search: 求字典序第 k 大子串

```

1  #include <bits/stdc++.h>
2  using namespace std;
3
4  const int MAXN = 90000 + 3;
5  const int ALPHABET = 26;
6
7  struct Node {
8      int len, cnt;
9      Node *link, *next[ALPHABET];
10     void init(int len = 0) {
11         link = nullptr;
12         this->len = len, cnt = 0;
13         memset(next, 0, sizeof(next));
14     }
15 };
16
17 template <int MAX_LENGTH> class SAM {
18 public:
19     Node *last, *root;
20
21     void init() {
22         pool_ptr = pool;
23         last = root = new_node(0);
24     }
25
26     void extend(int chr) {
27         Node *p = last, *np = new_node(p->len + 1);
28         for (last = np; p && !p->next[chr]; p = p->link) p->next[chr] = np;
29         if (!p) {
30             np->link = root;
31         } else {
32             Node *q = p->next[chr];
33             if (q->len == p->len + 1) {

```

```

34     np->link = q;
35 } else {
36     Node *nq = new_node(p->len + 1);
37     memcpy(nq->next, q->next, sizeof(q->next));
38     nq->link = q->link, q->link = np->link = nq;
39     for (; p && p->next[chr] == q; p = p->link) p->next[chr] = nq;
40 }
41 }
42 }
43
44 void toposort() {
45     int size = pool_ptr - pool;
46     memset(cnt, 0, size * sizeof(int));
47     for (Node *it = pool; it < pool_ptr; ++it) ++cnt[it->len];
48     for (int i = 1; i < size; ++i) cnt[i] += cnt[i - 1];
49     for (Node *it = pool; it < pool_ptr; ++it) order[--cnt[it->len]] = it;
50     for (int i = size - 1; ~i; --i) {
51         Node *u = order[i];
52         for (int j = 0; j < ALPHABET; ++j)
53             u->cnt += u->next[j] ? u->next[j]->cnt + 1 : 0;
54     }
55 }
56
57 void find_kth(int k, char *str) {
58     char *ptr = str;
59     Node *u = root;
60     while (k) {
61         for (int j = 0; j < ALPHABET; ++j) {
62             if (!u->next[j]) continue;
63             if (u->next[j]->cnt + 1 < k) {
64                 k -= u->next[j]->cnt + 1;
65                 continue;
66             }
67             --k, *ptr++ = j + 'a';
68             u = u->next[j];
69             break;
70         }
71     }
72     *ptr = 0;
73 }
74
75 private:
76     int cnt[MAX_LENGTH * 2];
77     Node pool[MAX_LENGTH * 2], *pool_ptr, *order[MAX_LENGTH * 2];
78
79     Node *new_node(int len) {
80         pool_ptr->init(len);
81         return pool_ptr++;
82     }
83 };
84
85 SAM<MAXN> sam;
86 char str[MAXN];
87
88 int main(int argc, char *argv[]) {
89     ios::sync_with_stdio(false);
90     cin.tie(nullptr), cout.tie(nullptr);
91
92     cin >> str;
93     sam.init();
94     for (char *it = str; *it; ++it) sam.extend(*it - 'a');
95     sam.toposort();
96
97     int q, k;
98     for (cin >> q; q; --q) cin >> k, sam.find_kth(k, str), puts(str);
99
100     return 0;
101 }

```

5 图论

5.1 Tarjan

对于无向图求边双连通，则添加两条有向边；若有重边，则在 $v == from$ 处添加计数器。

```

1  vector<int> adj[MAXN];
2  bitset<MAXN> instk, cut;
3  int bridges, dfs_clk, top, scc, n, m, d;
4  int dfn[MAXN], stk[MAXN], bel[MAXN], sz[MAXN];
5
6  int tarjan(int u, int from) {
7      int low = dfn[u] = ++dfs_clk;
8      stk[top++] = u, instk[u] = 1;
9
10     int son = 0;
11     for (int v : adj[u]) {
12         if (v == from) continue;
13         if (!dfn[v]) {
14             ++son;
15             int low_v = tarjan(v, u);
16             (low_v < low) && (low = low_v);
17             (low_v > dfn[u]) && (++bridges);
18             (u != from && low_v >= dfn[u]) && (cut[u] = 1);
19         } else if (instk[v] && low > dfn[v]) {
20             low = dfn[v];
21         }
22     }
23     (u == from && son > 1) && (cut[u] = 1);
24
25     if (low == dfn[u]) {
26         int v, sz = 0;
27         sz[++scc] = 0;
28         do {
29             ++sz;
30             v = stk[--top];
31             instk[v] = 0, bel[v] = scc;
32         } while (u ^ v);
33     }
34     return low;
35 }

```

5.2 Hopcroft 算法

pos 表示左边的点匹配右边哪一个，neg 反之，时间复杂度 $O(m\sqrt{n})$ 。

```

1  vector<int> adj[MAXN];
2  int nl, nr, pos[MAXN], neg[MAXN], lx[MAXN], ly[MAXN];
3
4  bool dfs(int x) {
5      int c = lx[x] + 1;
6      lx[x] = -1;
7      for (int y : adj[x]) {
8          if (ly[y] != c) continue;
9          ly[y] = -1;
10         if (~neg[y] && !dfs(neg[y])) continue;
11         pos[neg[y] = x] = y;
12         return true;
13     }
14     return false;
15 }
16
17 int match() {
18     int cnt = 0;
19     memset(pos, -1, sizeof(int) * nl);
20     memset(neg, -1, sizeof(int) * nr);

```

```

21 for (int x = 0; x < nl; ++x)
22     for (int y : adj[x]) {
23         if (~neg[y]) continue;
24         pos[neg[y] = x] = y, ++cnt;
25         break;
26     }
27 for (;;) {
28     static int q[MAXN];
29     int l = 0, r = 0, ok = 0;
30     memset(lx, -1, sizeof(int) * nl);
31     memset(ly, -1, sizeof(int) * nr);
32     for (int x = 0; x < nl; ++x)
33         if (pos[x] < 0) lx[q[r++] = x] = 0;
34     while (l < r) {
35         int x = q[l++];
36         for (int y : adj[x]) {
37             if (~ly[y]) continue;
38             ly[y] = lx[x] + 1;
39             if (~neg[y] && ~lx[neg[y]]) continue;
40             (~neg[y]) ? lx[q[r++] = neg[y]] = ly[y] + 1 : ok = 1;
41         }
42     }
43     if (!ok) return cnt;
44     for (int x = 0; x < nl; ++x)
45         if (pos[x] < 0 && dfs(x)) ++cnt;
46 }
47 }

```

5.3 KM 算法

点为 $1..n$ (左为 $1..nl$, 右为 $1..nr$), lk 表示左边的点匹配右边哪一个。

最大费用流时 NOT = 0, 最大费用流最大流时 NOT = -1ll * MAXN * ALPHA。

```

1  const int MAXN = 400 + 3;
2  const int ALPHA = 1e9 + 10;
3  const ll NOT = 0;
4  const ll INF = 3ll * MAXN * ALPHA;
5  struct KM {
6      int n, nl, nr, lk[MAXN], pre[MAXN];
7      ll lx[MAXN], ly[MAXN], w[MAXN][MAXN], slack[MAXN];
8      bitset<MAXN> vy;
9
10     void init(int n) {
11         this->n = n;
12         memset(lk, 0, sizeof(int) * (n + 1));
13         memset(pre, 0, sizeof(int) * (n + 1));
14         memset(lx, 0, sizeof(ll) * (n + 1));
15         memset(ly, 0, sizeof(ll) * (n + 1));
16         memset(slack, 0, sizeof(ll) * (n + 1));
17         for (int i = 0; i <= n; ++i) fill(w[i], w[i] + n + 1, NOT);
18     }
19
20     void add_edge(int x, int y, ll z) {
21         if (w[y][x] < z) w[y][x] = z;
22     }
23
24     ll match() {
25         for (int i = 1; i <= n; ++i)
26             for (int j = 1; j <= n; ++j) lx[i] = max(lx[i], w[i][j]);
27         for (int i = 1, py = p, x; i <= n; ++i) {
28             for (int j = 1; j <= n; ++j) slack[j] = INF, vy[j] = 0;
29             for (lk[py] = 0; i; lk[py] = py, py = p) {
30                 ll delta = INF;
31                 vy[py] = 1, x = lk[py];
32                 for (int y = 1; y <= n; ++y) {
33                     if (vy[y]) continue;
34                     if (lx[x] + ly[y] - w[x][y] < slack[y])

```

```

35     slack[y] = lx[x] + ly[y] - w[x][y], pre[y] = py;
36     if (slack[y] < delta) delta = slack[y], p = y;
37 }
38 for (int y = 0; y <= n; ++y)
39     if (vy[y]) {
40         lx[lk[y]] -= delta, ly[y] += delta;
41     } else {
42         slack[y] -= delta;
43     }
44 }
45 for (; py; py = pre[py]) lk[py] = lk[pre[py]];
46 }
47
48 ll ans = 0;
49 for (int i = 1; i <= n; ++i) {
50     ans += lx[i] + ly[i];
51     if (w[lk[i]][i] == NOT) ans -= NOT;
52 }
53 return ans;
54 }
55 } km;
56
57 int main() {
58     int nl, nr, m;
59     cin >> nl >> nr >> m;
60     km.init(max(nl, nr));
61     for (int x, y, z; m; --m) {
62         cin >> x >> y >> z;
63         km.add_edge(x, y, z);
64     }
65     cout << km.match() << "\n";
66     for (int i = 1; i <= nl; ++i)
67         cout << (km.w[km.lk[i]][i] == NOT ? 0 : km.lk[i]) << " \n"[i == nl];
68
69     return 0;
70 }

```

5.4 一般图最大匹配

```

1  class GeneralMatch {
2  public:
3      int n;
4      vector<vector<int>>> g;
5      vector<int> match, aux, label, orig, parent;
6      queue<int> q;
7      int aux_time;
8
9      GeneralMatch(int n)
10         : match(n, -1), aux(n, -1), label(n), orig(n), parent(n, -1),
11           aux_time(-1) {
12         this->n = n;
13         g.resize(n);
14     }
15
16     void add_edge(int u, int v) {
17         g[u].push_back(v);
18         g[v].push_back(u);
19     }
20
21     int find(int x) { return x == orig[x] ? x : orig[x] = find(orig[x]); }
22
23     int lca(int u, int v) {
24         ++aux_time;
25         u = find(u), v = find(v);
26         for (;;) swap(u, v) {
27             if (~u) {

```



```

28     if (aux[u] == aux_time) return u;
29     aux[u] = aux_time;
30     if (match[u] == -1) {
31         u = -1;
32     } else {
33         u = find(parent[match[u]]);
34     }
35 }
36 }
37 }
38
39 void blossom(int u, int v, int o) {
40     while (find(u) != o) {
41         parent[u] = v;
42         v = match[u];
43         q.push(v);
44         label[v] = 0;
45         orig[u] = orig[v] = o;
46         u = parent[v];
47     }
48 }
49
50 int bfs(int x) {
51     iota(orig.begin(), orig.end(), 0);
52     fill(label.begin(), label.end(), -1);
53     while (!q.empty()) q.pop();
54     q.push(x);
55     label[x] = 0;
56     while (!q.empty()) {
57         int u = q.front();
58         q.pop();
59         for (int v : g[u]) {
60             if (label[v] == -1) {
61                 parent[v] = u;
62                 label[v] = 1;
63                 if (match[v] == -1) {
64                     while (v != -1) {
65                         int pv = parent[v];
66                         int next_v = match[pv];
67                         match[v] = pv;
68                         match[pv] = v;
69                         v = next_v;
70                     }
71                     return 1;
72                 }
73                 q.push(match[v]);
74                 label[match[v]] = 0;
75             } else if (label[v] == 0 && find(u) != find(v)) {
76                 int o = lca(u, v);
77                 blossom(u, v, o);
78                 blossom(v, u, o);
79             }
80         }
81     }
82     return 0;
83 }
84
85 int find_max_match() {
86     int res = 0;
87     for (int i = 0; i < n; ++i) {
88         if (~match[i]) continue;
89         res += bfs(i);
90     }
91     return res;
92 }
93 };

```

5.5 SAP

```

1 struct MaxFlow {
2     struct Edge {
3         int to, rest;
4     } edges[MAXM * 4];
5
6     vector<int> adj[MAXN];
7     int n, edges_c, dep[MAXN], depc[MAXN], s, t, last[MAXN];
8
9     void init(int _n) {
10         n = _n, edges_c = 0;
11         for (int i = 1; i <= n; ++i) adj[i].clear();
12     }
13
14     void add_edge(int u, int v, int cap) {
15         edges[edges_c] = {v, cap, 0};
16         adj[u].push_back(edges_c++);
17         edges[edges_c] = {u, 0, 0};
18         adj[v].push_back(edges_c++);
19     }
20
21     int dfs(int u, int flow) {
22         if (u == t || !flow) return flow;
23         int v, e, temp, res = 0;
24         for (int &i = last[u]; i < (int)adj[u].size(); ++i) {
25             e = adj[u][i], v = edges[e].to;
26             if (!edges[e].res || dep[v] != dep[u] - 1) continue;
27             temp = dfs(v, min(flow, edges[e].cap - edges[e].flow));
28             res += temp, flow -= temp;
29             edges[e].rest -= temp, edges[e ^ 1].rest += temp;
30             if (!flow || !dep[s]) return res;
31         }
32         last[u] = 0;
33         if (!(--depc[dep[u]])) dep[s] = n + 1;
34         ++depc[++dep[u]];
35         return res;
36     }
37
38     int max_flow(int s, int t) {
39         this->s = s, this->t = t;
40
41         static queue<int> que;
42         memset(dep + 1, 0, sizeof(int) * n);
43         memset(depc + 1, 0, sizeof(int) * n);
44         memset(last + 1, 0, sizeof(int) * n);
45         while (!que.empty()) que.pop();
46         dep[t] = 1, que.push(t);
47
48         while (!que.empty()) {
49             int u = que.front();
50             que.pop();
51             ++depc[dep[u]];
52             for (int i = 0, v; i < (int)adj[u].size(); ++i) {
53                 v = edges[adj[u][i]].to;
54                 if (dep[v]) continue;
55                 dep[v] = dep[u] + 1;
56                 que.push(v);
57             }
58         }
59
60         int res = 0;
61         while (dep[s] <= n) res += dfs(s, INT_MAX);
62         return res;
63     };

```

5.6 dinic

```

1 struct MaxFlow {
2     struct Edge {
3         int to, rest;
4     } edges[MAXM * 4];
5
6     vector<int> adj[MAXN];
7     int n, edges_c, dep[MAXN], s, t, last[MAXN];
8
9     void init(int _n) {
10         n = _n, edges_c = 0;
11         for (int i = 1; i <= n; ++i) adj[i].clear();
12     }
13
14     void add_edge(int u, int v, int cap) {
15         edges[edges_c] = {v, cap, 0};
16         adj[u].push_back(edges_c++);
17         edges[edges_c] = {u, 0, 0};
18         adj[v].push_back(edges_c++);
19     }
20
21     bool bfs() {
22         memset(dep + 1, -1, sizeof(int) * n);
23         static queue<int> q;
24         q.push(s);
25         dep[s] = 0;
26         while (!q.empty()) {
27             int u = q.front();
28             q.pop();
29             for (int i = 0; i < adj[u].size(); ++i) {
30                 Edge &e = edges[adj[u][i]];
31                 if ((~dep[e.to]) || !e.rest) continue;
32                 dep[e.to] = dep[u] + 1;
33                 q.push(e.to);
34             }
35         }
36         return ~dep[t];
37     }
38
39     int dfs(int u, int flow) {
40         if (u == t || flow == 0) return flow;
41         int res = 0, temp, e, v;
42         for (int &i = last[u]; i < adj[u].size(); ++i) {
43             e = adj[u][i], v = edges[e].to;
44             if (dep[v] == dep[u] + 1 && edges[e].rest) {
45                 temp = dfs(v, min(edges[e].rest, flow));
46                 res += temp, flow -= temp;
47                 edges[e].rest -= temp, edges[e ^ 1].rest += temp;
48                 if (!flow) break;
49             }
50         }
51         return flow;
52     }
53
54     int max_flow(int s, int t) {
55         this->s = s, this->t = t;
56         int res = 0;
57         while (bfs()) {
58             memset(last + 1, 0, sizeof(int) * n);
59             res += dfs(s, INF);
60         }
61         return res;
62     }
63 };

```

5.7 高标预流推进

```

1  const int N = 1e4 + 4, M = 2e5 + 5, INF = 0x3f3f3f3f;
2  int n, m, s, t;
3
4  struct qxx {
5      int nex, t, v;
6  };
7  qxx e[M * 2];
8  int h[N], cnt = 1;
9  void add_path(int f, int t, int v) { e[++cnt] = (qxx){h[f], t, v}, h[f] = cnt; }
10 void add_flow(int f, int t, int v) {
11     add_path(f, t, v);
12     add_path(t, f, 0);
13 }
14
15 int ht[N], ex[N], gap[N]; // 高度; 超额流; gap 优化
16 bool bfs_init() {
17     memset(ht, 0x3f, sizeof(ht));
18     queue<int> q;
19     q.push(t), ht[t] = 0;
20     while (q.size()) { // 反向 BFS, 遇到没有访问过的结点就入队
21         int u = q.front();
22         q.pop();
23         for (int i = h[u]; i; i = e[i].nex) {
24             const int &v = e[i].t;
25             if (e[i ^ 1].v && ht[v] > ht[u] + 1) ht[v] = ht[u] + 1, q.push(v);
26         }
27     }
28     return ht[s] != INF; // 如果图不连通, 返回 0
29 }
30 struct cmp {
31     bool operator()(int a, int b) const { return ht[a] < ht[b]; }
32 }; // 伪装排序函数
33 priority_queue<int, vector<int>, cmp> pq; // 将需要推送的结点以高度高的优先
34 bool vis[N]; // 是否在优先队列中
35 int push(int u) { // 尽可能通过能够推送的边推送超额流
36     for (int i = h[u]; i; i = e[i].nex) {
37         const int &v = e[i].t, &w = e[i].v;
38         if (!w || ht[u] != ht[v] + 1) continue;
39         int k = min(w, ex[u]); // 取到剩余容量和超额流的最小值
40         ex[u] -= k, ex[v] += k, e[i].v -= k, e[i ^ 1].v += k; // push
41         if (v != s && v != t && !vis[v])
42             pq.push(v), vis[v] = 1; // 推送之后, v 必然溢出, 则入堆, 等待被推送
43         if (!ex[u]) return 0; // 如果已经推送完就返回
44     }
45     return 1;
46 }
47 void relabel(int u) { // 重贴标签 (高度)
48     ht[u] = INF;
49     for (int i = h[u]; i; i = e[i].nex)
50         if (e[i].v) ht[u] = min(ht[u], ht[e[i].t]);
51     ++ht[u];
52 }
53 int hlpp() { // 返回最大流
54     if (!bfs_init()) return 0; // 图不连通
55     ht[s] = n;
56     memset(gap, 0, sizeof(gap));
57     for (int i = 1; i <= n; i++)
58         if (ht[i] != INF) gap[ht[i]]++; // 初始化 gap
59     for (int i = h[s]; i; i = e[i].nex) {
60         const int v = e[i].t, w = e[i].v; // 队列初始化
61         if (!w) continue;
62         ex[s] -= w, ex[v] += w, e[i].v -= w, e[i ^ 1].v += w; // 注意取消 w 的引用
63         if (v != s && v != t && !vis[v]) pq.push(v), vis[v] = 1; // 入队
64     }
65     while (pq.size()) {
66         int u = pq.top();

```

```

67     pq.pop(), vis[u] = 0;
68     while (push(u)) { // 仍然溢出
69         // 如果 u 结点原来所在的高度没有结点了, 相当于出现断层
70         if (!--gap[ht[u]])
71             for (int i = 1; i <= n; i++)
72                 if (i != s && i != t && ht[i] > ht[u] && ht[i] < n + 1) ht[i] = n + 1;
73         relabel(u);
74         ++gap[ht[u]]; // 新的高度, 更新 gap
75     }
76 }
77 return ex[t];
78 }

```

5.8 最小费用流

```

1  class MinCostFlow {
2  public:
3      struct Result {
4          int flow, cost;
5      };
6      struct Edge {
7          int to, next, rest, cost;
8      };
9
10     vector<bool> inq;
11     vector<int> head, dist, from, flow;
12     vector<Edge> edges;
13
14     MinCostFlow(int n, int m) : inq(n), head(n, -1), dist(n), from(n), flow(n) {
15         edges.reserve(2 * m);
16     }
17
18     void add_edge(int u, int v, int capacity, int cost) {
19         internal_add_edge(u, v, capacity, cost);
20         internal_add_edge(v, u, 0, -cost);
21     }
22
23     void internal_add_edge(int u, int v, int capacity, int cost) {
24         edges.push_back((Edge){v, head[u], capacity, cost});
25         head[u] = edges.size() - 1;
26     }
27
28     Result augment(int source, int sink) {
29         fill(dist.begin(), dist.end(), INT_MAX);
30         dist[source] = 0;
31         flow[source] = INT_MAX;
32         queue<int> q;
33         q.push(source);
34         while (!q.empty()) {
35             int u = q.front();
36             q.pop();
37             inq[u] = false;
38             for (int it = head[u]; ~it; it = edges[it].next) {
39                 auto &e = edges[it];
40                 int v = e.to;
41                 if (e.rest > 0 && dist[u] + e.cost < dist[v]) {
42                     from[v] = it;
43                     dist[v] = dist[u] + e.cost;
44                     flow[v] = min(e.rest, flow[u]);
45                     if (!inq[v]) {
46                         q.push(v);
47                         inq[v] = true;
48                     }
49                 }
50             }
51         }
52     }
53 }

```

```

52
53     if (dist[sink] == INT_MAX) return {0, 0};
54     int min_flow = flow[sink];
55     for (int u = sink; u != source; u = edges[from[u] ^ 1].to) {
56         edges[from[u]].rest -= min_flow;
57         edges[from[u] ^ 1].rest += min_flow;
58     }
59     return {min_flow, dist[sink]};
60 }
61
62 Result min_cost_flow(int source, int sink) {
63     int flow = 0, cost = 0;
64     for (;;) {
65         auto result = augment(source, sink);
66         if (!result.flow) break;
67         flow += result.flow, cost += result.cost;
68     }
69     return {flow, cost};
70 }
71 };

```

5.9 上下界费用流

```

1  const int MAXN = 53;
2  const int MAX_NODE = 113;
3  const int MAX_EDGE = 1e5 + 5;
4  const int INF = 0x3f3f3f3f;
5
6  int n, s, t, ss, tt, tote;
7  int R[MAXN], C[MAXN], board[MAXN][MAXN];
8
9  struct Edge {
10     int to, cap, flow, cost;
11 } edges[MAX_EDGE];
12 vector<int> adj[MAX_NODE];
13
14 int from[MAX_NODE], in[MAX_NODE];
15 void add_edge(int from, int to, int l, int r, int cost) {
16     in[to] += l, in[from] -= l;
17     edges[tote] = (Edge){to, r - l, 0, cost};
18     adj[from].push_back(tote++);
19     edges[tote] = (Edge){from, 0, 0, -cost};
20     adj[to].push_back(tote++);
21 }
22
23 bool spfa(int s, int t) {
24     static queue<int> q;
25     static bool inq[MAX_NODE];
26     static int dist[MAX_NODE];
27     memset(inq + 1, 0, sizeof(bool) * tt);
28     memset(dist + 1, 0x3f, sizeof(int) * tt);
29     memset(from + 1, -1, sizeof(int) * tt);
30     dist[0] = 0, from[0] = -1;
31     q.push(0);
32     while (!q.empty()) {
33         int u = q.front();
34         q.pop();
35         inq[u] = false;
36         for (int e : adj[u]) {
37             if (edges[e].cap == edges[e].flow) continue;
38             int v = edges[e].to, d = dist[u] + edges[e].cost;
39             if (d >= dist[v]) continue;
40             dist[v] = d;
41             from[v] = e;
42             if (!inq[v]) {
43                 q.push(v);

```

```

44     inq[v] = true;
45 }
46 }
47 }
48 return dist[t] < INF;
49 }
50
51 pair<int, int> min_cost_max_flow(int s, int t) {
52     int flow = 0, cost = 0;
53     while (spfa(s, t)) {
54         int mi = INF;
55         for (int it = from[t]; ~it; it = from[edges[it ^ 1].to])
56             mi = min(mi, edges[it].cap - edges[it].flow);
57         flow += mi;
58         for (int it = from[t]; ~it; it = from[edges[it ^ 1].to]) {
59             edges[it].flow += mi, edges[it ^ 1].flow -= mi;
60             cost += mi * edges[it].cost;
61         }
62     }
63     return make_pair(flow, cost);
64 }
65
66 void solve() {
67     tote = 0;
68     s = 2 * n + 1, t = 2 * n + 2, ss = 0, tt = 2 * n + 3;
69     for (int i = 0; i <= tt; ++i) adj[i].clear(), in[i] = 0;
70
71     memset(R + 1, 0, sizeof(int) * n);
72     memset(C + 1, 0, sizeof(int) * n);
73
74     for (int i = 1; i <= n; ++i)
75         for (int j = 1; j <= n; ++j) {
76             cin >> board[i][j];
77             R[i] += board[i][j];
78             C[j] += board[i][j];
79         }
80
81     for (int i = 1; i <= n; ++i) {
82         add_edge(s, i, R[i], R[i], 0);
83         add_edge(s, i + n, C[i], C[i], 0);
84     }
85
86     for (int i = 1, l, r; i <= n; ++i) {
87         cin >> l >> r;
88         add_edge(i, t, l, r, 0);
89     }
90     for (int i = 1, l, r; i <= n; ++i) {
91         cin >> l >> r;
92         add_edge(i + n, t, l, r, 0);
93     }
94
95     for (int step = n * n / 2, x1, y1, x2, y2; step; --step) {
96         cin >> x1 >> y1 >> x2 >> y2;
97         if (board[x1][y1] == board[x2][y2]) continue;
98         if (board[x2][y2]) swap(x1, x2), swap(y1, y2);
99         if (x1 == x2)
100             add_edge(y1 + n, y2 + n, 0, 1, 1);
101         else
102             add_edge(x1, x2, 0, 1, 1);
103     }
104     add_edge(t, s, 0, INF, 0);
105     int sum = 0;
106     for (int i = 1; i < tt; ++i) {
107         if (in[i] > 0) {
108             sum += in[i];
109             add_edge(ss, i, 0, in[i], 0);
110         } else if (in[i] < 0) {
111             add_edge(i, tt, 0, -in[i], 0);

```

```
112     }
113 }
114
115 pair<int, int> ans = min_cost_max_flow(ss, tt);
116 if (sum != ans.first) {
117     cout << "-1\n";
118 } else {
119     cout << ans.second << '\n';
120 }
121 }
```

6 计算几何

7 Java

7.1 进制转换

```
1 import java.io.*;
2 import java.util.*;
3 import java.math.*;
4
5 public class Main {
6     public static void main(String[] args) {
7         InputStream inputStream = System.in;
8         OutputStream outputStream = System.out;
9         Scanner in = new Scanner(inputStream);
10        PrintWriter out = new PrintWriter(outputStream);
11        Solver solver = new Solver();
12        int testCount = Integer.parseInt(in.next());
13        for (int i = 1; i <= testCount; i++)
14            solver.solve(i, in, out);
15        out.close();
16    }
17
18    static class Solver {
19        public void solve(int testNumber, Scanner in, PrintWriter out) {
20            int a = in.nextInt();
21            int b = in.nextInt();
22            String num = in.next();
23
24            BigInteger value = BigInteger.ZERO;
25            for (int i = 0; i < num.length(); ++i) {
26                value = value.multiply(BigInteger.valueOf(a));
27                value = BigInteger.valueOf(getValue(num.charAt(i))).add(value);
28            }
29            out.println(a + " " + num);
30
31            if (value.equals(BigInteger.ZERO)) {
32                out.println(b + " 0");
33                out.println();
34                return;
35            }
36
37            out.print(b + " ");
38
39            char[] ans = new char[1000];
40            int length = 0;
41            while (!value.equals(BigInteger.ZERO)) {
42                int digit = value.mod(BigInteger.valueOf(b)).intValue();
43                value = value.divide(BigInteger.valueOf(b));
44                ans[length] = getChar(digit);
45                ++length;
46            }
47        }
48    }
49 }
```



```

48     for (int i = length - 1; i >= 0; --i) {
49         out.print(ans[i]);
50     }
51     out.println("\n");
52 }
53
54 private int getValue(char ch) {
55     if (ch >= 'A' && ch <= 'Z') {
56         return ch - 'A' + 10;
57     }
58     if (ch >= 'a' && ch <= 'z') {
59         return ch - 'a' + 36;
60     }
61     return ch - '0';
62 }
63
64 private char getChar(int x) {
65     if (x < 10) {
66         return (char) ('0' + x);
67     } else if (x < 36) {
68         return (char) ('A' + x - 10);
69     } else {
70         return (char) ('a' + x - 36);
71     }
72 }
73 }
74 }

```

8 杂项

8.1 I/O 优化

```

1  namespace FastIO {
2  struct Control {
3      int ct, val;
4      Control(int Ct, int Val = -1) : ct(Ct), val(Val) {}
5      inline Control operator()(int Val) { return Control(ct, Val); }
6  } _endl(0), _prs(1), _setprecision(2);
7
8  const int IO_SIZE = 1 << 16 | 127;
9
10 struct FastIO {
11     char in[IO_SIZE], *p, *pp, out[IO_SIZE], *q, *qq, ch[20], *t, b, K, prs;
12     FastIO() : p(in), pp(in), q(out), qq(out + IO_SIZE), t(ch), b(1), K(6) {}
13     ~FastIO() { fwrite(out, 1, q - out, stdout); }
14     inline char getc() {
15         return p == pp && (pp = (p = in) + fread(in, 1, IO_SIZE, stdin), p == pp)
16             ? (b = 0, EOF)
17             : *p++;
18     }
19     inline void putc(char x) {
20         q == qq && (fwrite(out, 1, q - out, stdout), q = out), *q++ = x;
21     }
22     inline void puts(const char str[]) {
23         fwrite(out, 1, q - out, stdout), fwrite(str, 1, strlen(str), stdout),
24         q = out;
25     }
26     inline void getline(string &s) {
27         s = "";
28         for (char ch; (ch = getc()) != '\n' && b;) s += ch;
29     }
30 #define indef(T)
31     inline FastIO &operator>>(T &x) {
32         x = 0;
33         char f = 0, ch;

```

```

34     while (!isdigit(ch = getc()) && b) f |= ch == '-';
35     while (isdigit(ch)) x = (x << 1) + (ch << 3) + (ch ^ 48), ch = getc();
36     return x = f ? -x : x, *this;
37 }
38 indef(int);
39 indef(long long);
40
41 inline FastIO &operator>>(string &s) {
42     s = "";
43     char ch;
44     while (isspace(ch = getc()) && b) {}
45     while (!isspace(ch) && b) s += ch, ch = getc();
46     return *this;
47 }
48 inline FastIO &operator>>(double &x) {
49     x = 0;
50     char f = 0, ch;
51     double d = 0.1;
52     while (!isdigit(ch = getc()) && b) f |= (ch == '-');
53     while (isdigit(ch)) x = x * 10 + (ch ^ 48), ch = getc();
54     if (ch == '.')
55         while (isdigit(ch = getc())) x += d * (ch ^ 48), d *= 0.1;
56     return x = f ? -x : x, *this;
57 }
58 #define outdef(_T)
59 inline FastIO &operator<<(_T x) {
60     !x && (putc('0'), 0), x < 0 && (putc('-'), x = -x);
61     while (x) *t++ = x % 10 + 48, x /= 10;
62     while (t != ch) *q++ = *--t;
63     return *this;
64 }
65 outdef(int);
66 outdef(long long);
67 inline FastIO &operator<<(char ch) { return putc(ch), *this; }
68 inline FastIO &operator<<(const char str[]) { return puts(str), *this; }
69 inline FastIO &operator<<(const string &s) { return puts(s.c_str()), *this; }
70 inline FastIO &operator<<(double x) {
71     int k = 0;
72     this->operator<<(int(x));
73     putc('.');
74     x -= int(x);
75     prs && (x += 5 * pow(10, -K - 1));
76     while (k < K) putc(int(x * 10) ^ 48), x -= int(x), ++k;
77     return *this;
78 }
79 inline FastIO &operator<<(const Control &cl) {
80     switch (cl.ct) {
81     case 0: putc('\n'); break;
82     case 1: prs = cl.val; break;
83     case 2: K = cl.val; break;
84     }
85     return *this;
86 }
87 inline operator bool() { return b; }
88 };
89 } // namespace FastIO

```

8.2 优化 STL 内存申请

```

1 // usage: vector<int, myalloc<int>> L;
2 static char space[10000000], *sp = space;
3 template <typename T> struct myalloc : allocator<T> {
4     myalloc() {}
5     template <typename T2> myalloc(const myalloc<T2> &a) {}
6     template <typename T2> myalloc<T> &operator=(const myalloc<T2> &a) {
7         return *this;

```

```

8   }
9   template <typename T2> struct rebind { typedef myalloc<T2> other; };
10  inline T *allocate(size_t n) {
11      T *result = (T *)sp;
12      sp += n * sizeof(T);
13      return result;
14  }
15  inline void deallocate(T *p, size_t n) {}
16  };

```

8.3 Emacs 配置

```

1  (defun myc++ ()
2    (c-set-style "stroustrup")
3    (setq tab-width 2)
4    (setq indent-tabs-mode nil)
5    (setq c-basic-offset 2)
6    (c-toggle-hungry-state)
7    (defun compile-and-run()
8      (interactive)
9      (setq file-name (file-name-sans-extension (file-name-nondirectory buffer-file-name)))
10     (compile
11      (format "g++ %s.cpp -o %s -Wall -Wextra -Wshadow -O2 && ./%s < in.txt"
12              file-name file-name file-name)))
13     (local-set-key (kbd "C-c C-c") 'compile-and-run)
14     (local-set-key (kbd "C-c C-k") 'kill-compilation))
15   (add-hook 'c++-mode-hook 'myc++))
16
17   (global-set-key [(meta ?o)] 'other-window)
18   (global-set-key [(meta ?)] 'hippie-expand)
19   (global-set-key [(control tab)] 'senator-completion-menu-popup)
20   (setq hippie-expand-try-functions-list
21     '(try-expand-dabbrev
22       try-expand-dabbrev-visible
23       try-expand-dabbrev-all-buffers
24       try-expand-dabbrev-from-kill
25       try-complete-file-name-partially
26       try-complete-file-name
27       try-expand-all-abbrevs
28       try-expand-list
29       try-expand-line))
30
31   (setq auto-save-mode nil)
32   (setq make-backup-files nil)
33
34   (ido-mode t)
35   (show-paren-mode 1)
36   (delete-selection-mode t)
37   (global-linum-mode t)
38   (global-auto-revert-mode t)

```

8.4 Vim 配置

```

1  syntax on
2  set tabstop=2 softtabstop=2 shiftwidth=2 expandtab smarttab autoindent
3  set incsearch ignorecase smartcase hlsearch
4  set ruler laststatus=2 showcmd showmode
5  set nobackup noswapfile noundofile autowrite noerrorbells
6  set wrap breakindent encoding=utf-8 number title cursorline
7
8  autocmd filetype c noremap <F5> :w <bar> exec '!gcc '.shellescape('%').' -o '.shellescape('%:r').
9    ' -std=c11 -Wall && ./'.shellescape('%:r')<CR>
10 autocmd filetype cpp noremap <F5> :w <bar> exec '!g++ '.shellescape('%').' -o '.shellescape('%:r')
11    ' -std=c++17 -Wall && ./'.shellescape('%:r')<CR>

```

```

10 autocmd filetype java noremap <F5> :w <bar> exec '!javac -encoding UTF-8 -sourcepath . -d . '.
    shellescape('%').' && java '.shellescape('%:r')<CR>
11
12 autocmd filetype c noremap <F6> :w <bar> exec '!gcc '.shellescape('%').' -o '.shellescape('%:r').
    ' -std=c11 -Wall -g && gdb '.shellescape('%:r')<CR>
13 autocmd filetype cpp noremap <F6> :w <bar> exec '!g++ '.shellescape('%').' -o '.shellescape('%:r'
    ).' -std=c++17 -Wall -g && gdb '.shellescape('%:r')<CR>
14
15 function! TrimWhitespace()
16     let l:save = winsaveview()
17     %s/\\@<!\s\+$//e
18     call winrestview(l:save)
19 endfunction
20
21 imap jk <Esc>
22 nmap t :call TrimWhitespace()<CR>
23
24 nmap <M-1> 1gt
25 nmap <M-2> 2gt
26 nmap <M-3> 3gt
27 nmap <M-4> 4gt
28 nmap <M-5> 5gt
29 nmap <M-6> 6gt
30 nmap <M-7> 7gt
31 nmap <M-8> 8gt
32 nmap <M-9> 9gt
33 nmap <M-t> :tabnew<CR>
34 nmap <M-w> :close<CR>
35 nmap <Tab> :tabnext<CR>
36 nmap <S-Tab> :tabprevious<CR>

```

8.5 对拍

*unix 下对拍:

```

1 while true; do
2     python gen.py > in.txt
3     time ./my < in.txt > out.txt
4     time ./std < in.txt > ans.txt
5     if diff out.txt ans.txt; then
6         echo AC
7     else
8         echo WA
9         exit 0
10    fi
11 done

```

Windows 下对拍:

```

1 @echo off
2 :loop
3 python gen.py > in.txt
4 my.exe < in.txt > out.txt
5 std.exe < in.txt > ans.txt
6 fc out.txt ans.txt
7 if not errorlevel 1 goto loop
8 pause
9 :end

```