ACM/ICPC Template Manaual

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Contents

1	Math	1
	1.1 杜教筛	1
	1.2 exctr	1
	1.3 Miller Rabin	1
	1.4 LinearSieve	2
	1.5 china	3
	1.6 BGSG	3
	1.7 Pollard rho	4
	1.8 LinearRecurrence	4
	1.9 类欧几里德算法	8
	1.10 gauss	9
	1.11 FFT	10
	1.12 lucas	11
	1.13 exgcd	11
	2.120 0.180 0.1 1.1 1.1 1.1 1.1 1.1 1.1 1.1 1.1 1.	
2	Dynamic Programming	11
3	Data Structure	11
	3.1 splay	11
	3.2 zkw	14
4	String	15
	4.1 hash	15
	4.2 mancher	15
	4.3 回文树	16
	4.4 exkmp	17
	4.5 kmp	18
5	Graph Theory	18
	5.1 KM	18
6	Computational Geometry	19
7	Java	19
•	7.1 进制转换	19
	7.2 out	20
	7.3 head	22
	7.4 myalloc	23
	7.5 duipai	$\frac{23}{23}$
	110 Garagean Commission Commissio	40

1 Math

1.1 杜教筛

```
map<int, int> mp_mu;
   int S_mu(int n) {
3
     if (n < MAXN) return sum_mu[n];</pre>
4
     if (mp_mu[n]) return mp_mu[n];
5
     int ret = 1;
6
     for (int i = 2, j; i \le n; i = j + 1) {
7
8
       j = n / (n / i);
9
       ret -= S_mu(n / i) * (j - i + 1);
10
11
     return mp_mu[n] = ret;
12 }
13
14 ll S_phi(int n) {
     ll res = 0:
15
16
     for (int i = 1, j; i \le n; i = j + 1) {
17
        j = n / (n / i);
       res += 1LL * (S_mu(j) - S_mu(i - 1)) * (n / i) * (n / i);
18
19
20
     return (res -1) / 2 + 1;
21 }
   1.2 exctr
   int exctr(int n, int *a, int *m) {
     int M = m[0], res = a[0];
     for (int i = 1; i < n; ++i) {</pre>
3
       int a = M, b = m[i], c = (a[i] - res \% b + b) \% b, x, y;
4
       int g = exgcd(a, b, x, y), bg = b / g;
5
       if (c % g != 0) return -1;
6
7
       x = 1LL * x * (c / g) % bg;
       res += x * M;
8
9
       M *= bg:
10
       res = (res % M + M) % M;
11
12
     return res;
13 }
   1.3 Miller Rabin
1 inline ll mod_mul(const ll &a, const ll &b, const ll &mod) {
     ll k = (ll)((1.0L * a * b) / (1.0L * mod)), t = a * b - k * mod;
3
     t -= mod;
     while (t < 0) t += mod;
4
5
     return t;
6
   inline ll mod_pow(ll a, ll b, const ll &mod) {
7
     ll res = 1:
9
     for (; b; b >>= 1, a = mod_mul(a, a, mod))
10
        (b & 1) && (res = mod_mul(res, a, mod));
11
     return res;
12 }
13
```

```
inline bool check(const ll &x, const ll &p) {
     if (!(x \% p) \mid | mod_pow(p \% x, x - 1, x) \land 1) return false;
15
      ll k = x - 1, t;
16
     while (~k & 1) {
17
        if (((t = mod_pow(p \% x, k >>= 1, x)) ^ 1) && (t ^ (x - 1))) return false;
18
19
        if (!(t \wedge (x - 1))) return true;
20
21
     return true;
22
   }
23
   inline bool Miller_Rabin(const ll &x) {
     if (x < 2) return false;
     static const int p[12] = {2, 3, 5, 7, 11, 13, 17, 19, 61, 2333, 4567, 24251};
26
      for (register int i = 0; i < 12; ++i) {</pre>
27
        if (!(x ^ p[i])) return true;
28
29
        if (!check(x, p[i])) return false;
30
31
     return true;
32 }
   1.4 LinearSieve
   const int MAXN = 1e7 + 5;
2
3 bool vis[MAXN];
4 int prime[MAXN / 10], prime_cnt;
  int fac[MAXN], e[MAXN], d[MAXN], mu[MAXN], phi[MAXN];
5
6
7
   void sieve() {
     fac[1] = 1;
8
9
     e[1] = 0;
10
     d[1] = 1;
11
     mu[1] = 1;
12
     phi[1] = 1;
13
     for (int i = 2; i < MAXN; ++i) {</pre>
        if (!vis[i]) {
14
          prime[prime_cnt++] = i;
          fac[i] = i;
16
17
          e[i] = 1;
          d[i] = 2;
18
          mu[i] = -1;
19
          phi[i] = i - 1;
20
21
        for (int j = 0; j < prime_cnt; ++j) {</pre>
22
23
          int t = prime[j] * i;
          if (t >= MAXN) { break; }
24
25
          vis[t] = true;
          fac[t] = prime[j];
26
          if (i % prime[j] == 0) {
27
            e[t] = e[i] + 1;
28
            d[t] = d[i] / (e[i] + 1) * (e[t] + 1);
29
            mu[t] = 0;
30
            phi[t] = phi[i] * prime[j];
31
32
            break:
33
          } else {
34
            e[t] = 1;
35
            d[t] = d[i] * 2;
            mu[t] = -mu[i];
36
```

```
37
            phi[t] = phi[i] * (prime[j] - 1);
38
39
40
      }
   }
41
   1.5 china
   int china(int n, int *a, int *m) {
     int lcm = 1, res = 0;
3
      for (int i = 0; i < n; ++i) lcm *= m[i];</pre>
      for (int i = 0; i < n; ++i) {
4
        int t = lcm / m[i], x, y;
5
6
        exgcd(t, m[i], x, y);
        x = (x \% m[i] + m[i]) \% m[i];
7
        res = (res + 1LL * t * x) % lcm;
8
9
10
     return res;
  }
11
   1.6 BGSG
1 // Finds the primitive root modulo p
   int generator(int p) {
3
     vector<int> fact;
4
     int phi = p - 1, n = phi;
     for (int i = 2; i * i <= n; ++i) {</pre>
5
6
        if (n \% i == 0) {
7
          fact.push_back(i);
8
          while (n \% i == 0) n /= i;
9
        }
10
     }
11
     if (n > 1) fact.push_back(n);
      for (int res = 2; res <= p; ++res) {</pre>
12
        bool ok = true;
13
        for (int factor : fact)
15
          if (mod_pow(res, phi / factor, p) == 1) {
            ok = false;
16
17
            break;
          }
18
19
20
        if (ok) return res;
21
22
     return -1;
23
   }
   // This program finds all numbers x such that x^k=a \pmod{n}
24
   vector<int> BSGS(int n, int k, int a) {
     if (a == 0) return vector<int>({0});
26
27
      int g = generator(n);
28
      // Baby-step giant-step discrete logarithm algorithm
29
30
     int sq = (int) sqrt(n + .0) + 1;
31
     vector<pair<int, int>> dec(sq);
      for (int i = 1; i <= sq; ++i)</pre>
32
        dec[i-1] = \{mod\_pow(g, i * sq * k % (n-1), n), i\};
33
34
35
     sort(dec.begin(), dec.end());
```

```
int any_ans = -1;
36
      for (int i = 0; i < sq; ++i) {
37
        int my = mod_pow(g, i * k % (n - 1), n) * a % n;
38
        auto it = lower_bound(dec.begin(), dec.end(), make_pair(my, 0));
39
40
        if (it != dec.end() && it->first == my) {
          any_ans = it->second * sq - i;
41
42
          break;
        }
43
      }
44
      if (any_ans == -1) return vector<int>();
45
      // Print all possible answers
46
47
     int delta = (n - 1) / \underline{gcd(k, n - 1)};
48
      vector<int> ans;
      for (int cur = any_ans % delta; cur < n - 1; cur += delta)</pre>
49
        ans.push_back(mod_pow(g, cur, n));
50
      sort(ans.begin(), ans.end());
51
52
      return ans;
53
   1.7 Pollard rho
   inline ll rand64(ll x) {
     return 1ll * ((rand() << 15 ^ rand()) << 30 ^ (rand() << 15 ^ rand())) % x;</pre>
2
   }
3
4
   inline ll Pollard_rho(const ll &x, const int &y) {
     ll v0 = rand64(x - 1) + 1, v = v0, d, s = 1;
6
      for (register int t = 0, k = 1;;) {
7
        if (v = (mod_mul(v, v, x) + y) \% x, s = mod_mul(s, abs(v - v0), x),
8
            !(v \wedge v0) || !s)
9
          return x;
10
11
        if (++t == k) {
          if ((d = \underline{gcd}(s, x)) \land 1) return d;
12
          v0 = v, k \ll 1;
13
14
     }
15
   }
16
17
18 ll ans;
   vector<ll> factor;
   void findfac(ll n) {
      if (Miller_Rabin(n)) {
21
        factor.push_back(n);
22
23
        return:
24
      }
25
      ll p = n;
      while (p \ge n) \{ p = Pollard\_rho(p, rand64(n - 1) + 1); \}
26
      findfac(p);
27
      findfac(n / p);
28
  }
29
   1.8 LinearRecurrence
   struct LinearRecurrence {
     using int64 = long long;
2
      using vec = std::vector<int64>;
3
4
```

```
static void extand(vec &a, size_t d, int64 value = 0) {
5
6
        if (d <= a.size()) return;</pre>
7
        a.resize(d, value);
8
9
     static vec BerlekampMassey(const vec &s, int64 mod) {
10
        std::function<int64(int64)> inverse = [&](int64 a) {
11
          return a == 1 ? 1 : (int64)(mod - mod / a) * inverse(mod % a) % mod;
12
        };
13
        vec A = \{1\}, B = \{1\};
14
        int64 b = s[0];
15
16
        for (size_t i = 1, m = 1; i < s.size(); ++i, m++) {</pre>
17
          int64 d = 0;
          for (size_t j = 0; j < A.size(); ++j) \{ d += A[j] * s[i - j] % mod; \}
18
          if (!(d %= mod)) continue;
19
          if (2 * (A.size() - 1) <= i) {
20
21
            auto temp = A;
            extand(A, B.size() + m);
22
            int64 coef = d * inverse(b) % mod;
23
            for (size_t j = 0; j < B.size(); ++j) {</pre>
24
              A[j + m] = coef * B[j] % mod;
25
              if (A[j + m] < 0) A[j + m] += mod;
26
27
28
            B = temp, b = d, m = 0;
29
          } else {
30
            extand(A, B.size() + m);
            int64 coef = d * inverse(b) % mod;
31
            for (size_t j = 0; j < B.size(); ++j) {</pre>
32
              A[j + m] -= coef * B[j] % mod;
33
34
              if (A[j + m] < 0) A[j + m] += mod;
35
36
          }
37
        }
38
        return A;
39
40
      static void exgcd(int64 a, int64 b, int64 &g, int64 &x, int64 &y) {
41
42
        if (!b)
          x = 1, y = 0, g = a;
43
        else {
44
          exgcd(b, a % b, g, y, x);
45
46
          y -= x * (a / b);
        }
47
48
      }
49
50
      static int64 crt(const vec &c, const vec &m) {
51
        int n = c.size();
        int64 M = 1, ans = 0;
52
        for (int i = 0; i < n; ++i) M *= m[i];
53
        for (int i = 0; i < n; ++i) {
54
55
          int64 x, y, g, tm = M / m[i];
56
          exgcd(tm, m[i], g, x, y);
57
          ans = (ans + tm * x * c[i] % M) % M;
        }
58
        return (ans + M) % M;
59
60
61
62
      static vec ReedsSloane(const vec &s, int64 mod) {
63
        auto inverse = [](int64 a, int64 m) {
```

```
int64 d, x, y;
64
           exgcd(a, m, d, x, y);
65
           return d == 1 ? (x % m + m) % m : -1;
66
67
         auto L = [](const vec &a, const vec &b) {
68
           int da = (a.size() > 1 || (a.size() == 1 && a[0])) ? a.size() - 1 : -1000;
69
70
           int db = (b.size() > 1 \mid | (b.size() == 1 && b[0])) ? b.size() - 1 : -1000;
           return std::max(da, db + 1);
71
72
        };
         auto prime_power = [&](const vec &s, int64 mod, int64 p, int64 e) {
73
74
           // linear feedback shift register mod p^e, p is prime
75
           std::vector<vec> a(e), b(e), an(e), bn(e), ao(e), bo(e);
76
           vec t(e), u(e), r(e), to(e, 1), uo(e), pw(e + 1);
77
78
           pw[0] = 1;
           for (int i = pw[0] = 1; i \le e; ++i) pw[i] = pw[i - 1] * p;
79
           for (int64 i = 0; i < e; ++i) {
80
             a[i] = {pw[i]}, an[i] = {pw[i]};
81
             b[i] = \{0\}, bn[i] = \{s[0] * pw[i] \% mod\};
82
             t[i] = s[0] * pw[i] % mod;
83
             if (t[i] == 0) {
84
85
               t[i] = 1, u[i] = e;
86
             } else {
87
               for (u[i] = 0; t[i] \% p == 0; t[i] /= p, ++u[i])
88
89
             }
90
           for (size_t k = 1; k < s.size(); ++k) {</pre>
91
             for (int g = 0; g < e; ++g) {
92
93
               if (L(an[g], bn[g]) > L(a[g], b[g])) {
94
                 ao[g] = a[e - 1 - u[g]];
                 bo[g] = b[e - 1 - u[g]];
95
96
                 to[g] = t[e - 1 - u[g]];
                 uo[g] = u[e - 1 - u[g]];
97
98
                 r[g] = k - 1;
               }
99
             }
100
101
             a = an, b = bn;
             for (int o = 0; o < e; ++o) {</pre>
102
               int64 d = 0;
103
               for (size_t i = 0; i < a[o].size() && i <= k; ++i) {</pre>
104
                 d = (d + a[o][i] * s[k - i]) % mod;
105
106
               if (d == 0) {
107
                 t[o] = 1, u[o] = e;
108
               } else {
109
                 for (u[o] = 0, t[o] = d; t[o] % p == 0; t[o] /= p, ++u[o])
110
111
                 int g = e - 1 - u[o];
112
                 if (L(a[g], b[g]) == 0) {
113
114
                   extand(bn[o], k + 1);
115
                   bn[o][k] = (bn[o][k] + d) \% mod;
                 } else {
116
                   int64 coef =
117
                        t[o] * inverse(to[g], mod) % mod * pw[u[o] - uo[g]] % mod;
118
119
                   int m = k - r[g];
                   extand(an[o], ao[g].size() + m);
120
121
                   extand(bn[o], bo[g].size() + m);
122
                   for (size_t i = 0; i < ao[g].size(); ++i) {</pre>
```

```
123
                      an[o][i + m] -= coef * ao[g][i] % mod;
124
                      if (an[o][i + m] < 0) an[o][i + m] += mod;
125
                    while (an[o].size() \&\& an[o].back() == 0) an[o].pop_back();
126
127
                    for (size_t i = 0; i < bo[g].size(); ++i) {</pre>
128
                      bn[o][i + m] -= coef * bo[g][i] % mod;
129
                      if (bn[o][i + m] < 0) bn[o][i + m] -= mod;
130
                    while (bn[o].size() && bn[o].back() == 0) bn[o].pop_back();
131
132
133
               }
             }
134
           }
135
           return std::make_pair(an[0], bn[0]);
136
137
138
         std::vector<std::tuple<int64, int64, int>> fac;
139
         for (int64 i = 2; i * i <= mod; ++i)</pre>
140
           if (mod % i == 0) {
141
             int64 cnt = 0, pw = 1;
142
             while (\text{mod } \% \text{ i } == 0) \text{ mod } /= \text{ i, } ++\text{cnt, } \text{pw } *= \text{ i;}
143
             fac.emplace_back(pw, i, cnt);
144
145
         if (mod > 1) fac.emplace_back(mod, mod, 1);
146
147
         std::vector<vec> as;
148
         size_t n = 0;
         for (auto &&x : fac) {
149
           int64 mod, p, e;
150
           vec a, b;
151
           std::tie(mod, p, e) = x;
152
153
           auto ss = s;
           for (auto &&x : ss) x %= mod;
154
           std::tie(a, b) = prime_power(ss, mod, p, e);
155
           as.emplace_back(a);
156
           n = std::max(n, a.size());
157
158
159
         vec a(n), c(as.size()), m(as.size());
160
         for (size_t i = 0; i < n; ++i) {</pre>
           for (size_t j = 0; j < as.size(); ++j) {</pre>
161
             m[j] = std::get<0>(fac[j]);
162
163
             c[j] = i < as[j].size() ? as[j][i] : 0;
164
165
           a[i] = crt(c, m);
166
167
         return a;
168
169
       LinearRecurrence(const vec &s, const vec &c, int64 mod)
170
           : init(s), trans(c), mod(mod), m(s.size()) {}
171
172
173
       LinearRecurrence(const vec &s, int64 mod, bool is_prime = true) : mod(mod) {
174
         vec A;
175
         if (is_prime)
176
           A = BerlekampMassey(s, mod);
177
         else
           A = ReedsSloane(s, mod);
178
179
         if (A.empty()) A = \{0\};
180
         m = A.size() - 1;
181
         trans.resize(m);
```

```
for (int i = 0; i < m; ++i) { trans[i] = (mod - A[i + 1]) % mod; }
182
        std::reverse(trans.begin(), trans.end());
183
        init = {s.begin(), s.begin() + m};
184
185
186
      int64 calc(int64 n) {
187
        if (mod == 1) return 0;
188
        if (n < m) return init[n];</pre>
189
        vec v(m), u(m \ll 1);
190
        int msk = !!n;
191
        for (int64 m = n; m > 1; m >>= 1) msk <<= 1;
192
193
        v[0] = 1 \% mod;
        for (int x = 0; msk; msk >>= 1, x <<= 1) {
194
          std::fill_n(u.begin(), m * 2, 0);
195
196
          x = !!(n \& msk);
          if(x < m)
197
            u[x] = 1 \% mod;
198
          else { // can be optimized by fft/ntt
199
200
             for (int i = 0; i < m; ++i) {
               for (int j = 0, t = i + (x \& 1); j < m; ++j, ++t) {
201
                 u[t] = (u[t] + v[i] * v[j]) % mod;
202
               }
203
             }
204
             for (int i = m * 2 - 1; i >= m; --i) {
205
206
               for (int j = 0, t = i - m; j < m; ++j, ++t) {
207
                 u[t] = (u[t] + trans[j] * u[i]) % mod;
               }
208
             }
209
210
211
          v = \{u.begin(), u.begin() + m\};
212
213
        int64 ret = 0;
214
        for (int i = 0; i < m; ++i) { ret = (ret + v[i] * init[i]) % mod; }</pre>
215
        return ret;
216
      }
217
218
      vec init, trans;
219
      int64 mod;
220
      int m;
221 };
    1.9
          类欧几里德算法
 1 / \pi f = sum((a*i+b)/c), g = sum((a*i+b)/c*i), h = sum(((a*i+b)/c)^2), for i in [0..n],
   //整除向下
 3 #include <bits/stdc++.h>
 4 #define int long long
 5 using namespace std;
 6 const int P = 998244353;
 7 int i2 = 499122177, i6 = 166374059;
    struct data {
      data() { f = g = h = 0; }
 9
      int f, g, h;
10
   }; // 三个函数打包
    data calc(int n, int a, int b, int c) {
13
      int ac = a / c, bc = b / c, m = (a * n + b) / c, n1 = n + 1, n21 = n * 2 + 1;
      data d:
14
      if (a == 0) { // 迭代到最底层
15
```

```
16
       d.f = bc * n1 \% P;
       d.g = bc * n \% P * n1 \% P * i2 \% P;
17
       d.h = bc * bc % P * n1 % P;
18
19
       return d;
20
21
     if (a >= c || b >= c) { // 取模
       d.f = n * n1 % P * i2 % P * ac % P + bc * n1 % P;
22
23
       d.g = ac * n \% P * n1 \% P * n21 \% P * i6 \% P + bc * n % P * n1 % P * i2 % P;
24
       d.h = ac * ac % P * n % P * n1 % P * n21 % P * i6 % P +
              bc * bc % P * n1 % P + ac * bc % P * n % P * n1 % P;
25
26
       d.f %= P, d.g %= P, d.h %= P;
27
       data e = calc(n, a % c, b % c, c); // 迭代
28
29
       d.h += e.h + 2 * bc % P * e.f % P + 2 * ac % P * e.g % P;
30
       d.g += e.g, d.f += e.f;
31
       d.f %= P, d.g %= P, d.h %= P;
32
33
       return d;
34
35
     data e = calc(m - 1, c, c - b - 1, a);
     d.f = n * m % P - e.f, d.f = (d.f % P + P) % P;
36
     d.g = m * n \% P * n1 \% P - e.h - e.f, d.g = (d.g * i2 % P + P) % P;
37
     d.h = n * m \% P * (m + 1) \% P - 2 * e.g - 2 * e.f - d.f;
38
39
     d.h = (d.h \% P + P) \% P;
40
     return d;
41 }
42
   int T, n, a, b, c;
43
   signed main() {
44
     scanf("%lld", &T);
45
46
     while (T--) {
47
       scanf("%lld%lld%lld%lld", &n, &a, &b, &c);
48
       data ans = calc(n, a, b, c);
       printf("%lld %lld %lld\n", ans.f, ans.h, ans.g);
49
50
51
     return 0;
52 }
   1.10
         gauss
1 const double EPS = 1e-9;
   const int MAXN = 220;
   double a[MAXN][MAXN], x[MAXN];
   int equ, var;
5
   int Gauss() {
6
     int i, j, k, col, max_r;
7
      for (k = 0, col = 0; k < equ && col < var; k++, col++) {
8
9
       max_r = k;
       for (i = k + 1; i < equ; i++)
10
          if (fabs(a[i][col]) > fabs(a[max_r][col])) max_r = i;
11
       if (fabs(a[max_r][col]) < eps) return 0;</pre>
12
13
       if (k != max_r) {
14
          for (j = col; j < var; j++) swap(a[k][j], a[max_r][j]);
15
16
          swap(x[k], x[max_r]);
17
18
```

```
x[k] /= a[k][col];
19
        for (j = col + 1; j < var; j++) a[k][j] /= a[k][col];
20
21
        a[k][col] = 1;
22
        for (i = 0; i < equ; i++)
23
          if (i != k) {
24
25
            x[i] - = x[k] * a[i][col];
            for (j = col + 1; j < var; j++) a[i][j] - = a[k][j] * a[i][col];
26
27
            a[i][col] = 0;
          }
28
29
     }
30
     return 1;
31
   }
   1.11 FFT
   const int MAXN = 4 * 1e5 + 3;
   const double PI = acos(-1);
   complex<double> a[MAXN], b[MAXN];
4
5 int n, bit;
  int rev[MAXN];
6
7
   void fft(complex<double> *a, int sign) {
9
      for (int i = 0; i < n; ++i)
10
        if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
11
12
     for (int j = 1; j < n; j <<= 1) {
        complex<double> wn(cos(2 * PI / (j << 1)), sign * sin(2 * PI / (j << 1)));
13
        for (int i = 0; i < n; i += (j << 1)) {
14
15
          complex<double> w(1, 0), t0, t1;
16
          FOR(k, 0, j) {
17
            t0 = a[i + k];
            t1 = w * a[i + j + k];
18
            a[i + k] = t0 + t1;
19
20
            a[i + j + k] = t0 - t1;
21
            w *= wn;
22
          }
23
        }
24
     }
25
     if (sign == -1)
        for (int i = 0; i < n; ++i) a[i] /= n;</pre>
26
27
   }
28
   int main() {
29
     ios::sync_with_stdio(false);
30
31
     cin.tie(0);
32
     cout.tie(0);
33
34
     int n, m, x;
35
     cin >> n >> m;
      for (int i = 0; i \le n; ++i) {
36
37
        cin >> x;
38
        a[i].real(x);
39
40
     for (int i = 0; i \le m; ++i) {
41
        cin >> x;
42
        b[i].real(x);
```

```
}
43
44
      ::n = 1;
45
46
     bit = 0;
47
     while (::n <= n + m) {
48
        ::n <<= 1;
49
       ++bit;
     }
50
     rev[0] = 0;
51
     FOR(i, 1, ::n) rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (bit - 1));
52
53
     fft(a, 1);
54
     fft(b, 1);
     FOR(i, 0, ::n) a[i] *= b[i];
55
     fft(a, -1);
56
     FOR(i, 0, n + m + 1) cout << int(a[i].real() + .5) << " ";</pre>
57
     cout << "\n";
58
59
     return 0;
60 }
   1.12 lucas
   // C(n, m) = C(n / p, m / p) * C(n % p, m % p) (mod p)
   ll lucas(ll n, ll k, int p) {
     ll ret = 1;
3
     while (n && k) {
 4
       ll nn = n \% p, kk = k \% p;
5
       if (nn < kk) return 0;</pre>
6
7
       ret = ret * f[nn] * mod_pow(f[kk] * f[nn - kk] % p, p - 2, p) % p;
8
       n /= p, k /= p;
9
10
     return res;
11 }
   1.13 exgcd
   int exgcd(int a, int b, int &x, int &y) {
     if (b == 0) return x = 1, y = 0, a;
3
     int g = exgcd(b, a \% b, y, x);
     y -= a / b * x;
4
     return g;
6 }
       Dynamic Programming
   \mathbf{2}
   3
        Data Structure
   3.1 splay
1 #include <algorithm>
2 #include <cstdio>
3 #include <cstring>
4 #include <iostream>
5
   using namespace std;
```

7 const int MAXN = 2e5 + 10;

```
8
    struct Node {
 9
       long long sum;
10
       int id, val, lazy, size;
11
       Node *fa, *ch[2];
12
    } node_pool[MAXN], *pool_it, *root, *nil;
13
14
    Node *newnode(int id, int val) {
15
       pool_it->id = id;
16
       pool_it->lazy = 0;
17
       pool_it->size = 1;
18
19
       pool_it->sum = pool_it->val = val;
       pool_it->fa = pool_it->ch[0] = pool_it->ch[1] = nil;
20
       return pool_it++;
21
22 }
23
   void maintain(Node *u) {
24
       if (u == nil) { return; }
       u\rightarrow size = u\rightarrow ch[0]\rightarrow size + u\rightarrow ch[1]\rightarrow size + 1;
26
27
       u -> sum = u -> ch[0] -> sum + u -> ch[1] -> sum + u -> val;
28 }
29
   void push_down(Node *u) {
30
31
       if (u->lazy) {
32
         if (u->ch[0] != nil) {
33
            u\rightarrow ch[0]\rightarrow val += u\rightarrow lazy;
34
            u \to ch[0] \to sum += 1LL * u \to ch[0] \to size * u \to lazy;
            u\rightarrow ch[0]\rightarrow lazy += u\rightarrow lazy;
35
36
         if (u->ch[1] != nil) {
37
38
            u->ch[1]->val += u->lazy;
39
            u \rightarrow ch[1] \rightarrow sum += 1LL * u \rightarrow ch[1] \rightarrow size * u \rightarrow lazy;
40
            u \rightarrow ch[1] \rightarrow lazy += u \rightarrow lazy;
41
         }
42
         u \rightarrow lazy = 0;
43
    }
44
45
    inline void rot(Node *u) {
46
       Node *f = u \rightarrow fa, *ff = f \rightarrow fa;
47
       int d = u == f -> ch[1];
48
       push_down(f);
49
       push_down(u);
50
       if ((f->ch[d] = u->ch[d \land 1]) != nil) f->ch[d]->fa = f;
       if ((u-)fa = ff) != nil) ff->ch[f == ff->ch[1]] = u;
52
       f\rightarrow fa = u;
53
       u\rightarrow ch[d \land 1] = f;
54
       maintain(f);
55
       maintain(u);
56
57 }
58
59
    void splay(Node *u, Node *target) {
60
       for (Node *f; u->fa != target; rot(u))
61
         if ((f = u->fa)->fa != target) {
            ((u == f->ch[1]) \land (f == f->fa->ch[1])) ? rot(u) : rot(f);
62
63
64
       if (target == nil) root = u;
65
66
```

```
inline void insert(int id, int val) {
       if (root == nil) {
68
         root = newnode(id, val);
69
 70
         return;
 71
 72
       Node *u = root;
 73
       while (u != nil) {
         int d = id >= u -> id;
 74
 75
         ++u->size;
         push_down(u);
 76
 77
         u->sum += val;
 78
         if (u->ch[d] != nil) {
            u = u \rightarrow ch[d];
 79
         } else {
 80
            u->ch[d] = newnode(id, val);
 81
            u \rightarrow ch[d] \rightarrow fa = u;
 82
 83
            u = u - > ch[d];
 84
            break;
 85
         }
       }
 86
 87
       splay(u, nil);
    }
 88
 89
    inline Node *find_pred(int id) {
 91
       Node *u = root, *ret = nil;
       while (u != nil) {
92
93
         push_down(u);
         if (u->id < id) {</pre>
94
            ret = u;
95
 96
            u = u \rightarrow ch[1];
 97
         } else {
98
            u = u -> ch[0];
99
100
101
       return ret;
102
103
104
    inline Node *find_succ(int id) {
       Node *u = root, *ret = nil;
105
       while (u != nil) {
106
107
         push_down(u);
         if (u->id > id) {
108
109
            ret = u;
110
            u = u \rightarrow ch[0];
         } else {
111
112
            u = u \rightarrow ch[1];
113
         }
       }
114
       return ret;
115
116 }
117
118
     Node *find_kth(int k) {
119
       Node *u = root;
       while (u != nil) {
120
121
         push_down(u);
122
         if (u->ch[0]->size + 1 == k) {
123
            splay(u, nil);
124
            return u;
125
         }
```

```
if (u\rightarrow ch[0]\rightarrow size >= k) {
126
127
           u = u \rightarrow ch[0];
         } else {
128
           k = u - ch[0] - size + 1;
129
130
           u = u \rightarrow ch[1];
131
132
133
       return nil;
134
    }
135
136
    Node *range(int l, int r) {
137
       Node *pred = find_pred(l);
       Node *succ = find_succ(r);
138
139
       splay(pred, nil);
140
       splay(succ, root);
141
       push_down(pred);
142
143
       push_down(succ);
       return root->ch[1]->ch[0];
144
145 }
146
147 int main() {
148
149
       // freopen("input.txt", "r", stdin);
150
       ios::sync_with_stdio(false);
151
       cin.tie(0);
152
       cout.tie(0);
153
154
155
       int n;
156
       cin >> n;
157
       pool_it = node_pool;
158
       nil = pool_it++;
159
       nil->ch[0] = nil->ch[1] = nil->fa = nil;
160
       nil->id = -1;
161
162
       nil->val = 0;
163
       root = nil;
164
       insert(-0x3fffffff, 0);
165
166
       insert(0x3fffffff, 0);
167
168
       return 0;
169
    }
    3.2 zkw
 1 int tree[MAXN * 2], pre;
 3
    void init(int n, int *a) {
       memset(tree, 0, sizeof(tree));
       for (pre = 1; pre <= n; pre <<= 1) {}</pre>
 5
       for (int i = 1; i <= n; ++i) tree[i + pre] = i;</pre>
 6
       for (int i = pre; i; --i) tree[i] = max(tree[i << 1], tree[i << 1 | 1]);</pre>
 7
    }
 8
 9
   void update(int pos, const int &val) {
10
       tree[pos += pre] = val;
```

```
for (pos >>= 1; pos; pos >>= 1)
12
        tree[pos] = max(tree[pos << 1], tree[pos << 1 | 1]);</pre>
13
   }
14
15
   int query(int s, int t) {
16
     int res = 0;
17
     for (s += pre - 1, t += pre + 1; s ^ t ^ 1; s >>= 1, t >>= 1) {
18
        if (~s & 1) res = max(res, tree[s ^ 1]);
19
20
        if (t & 1) res = max(res, tree[t ^ 1]);
21
22
     return res;
23
   }
        String
   4
   4.1 hash
1
   const unsigned int KEY = 6151;
   const unsigned int MOD = 1610612741;
4
   unsigned int hash[MAXN], p[MAXN];
5
6
   inline unsigned int get_hash(int l, int r) {
7
     return (hash[r] + MOD - 1ULL * hash[l - 1] * p[r - l + 1] % MOD) % MOD;
8
9
10
   void init(char *s, int n) {
11
12
     p[0] = 1;
13
     for (int i = 1; i \le n; ++i) {
        p[i] = p[i - 1] * KEY % MOD;
14
15
        hash[i] = (1LL * hash[i - 1] * KEY + s[i]) % MOD;
16
     }
   }
17
   4.2 mancher
   void mancher(char *s, int n) {
     str[0] = '~';
2
     str[1] = '!';
3
     for (int i = 1; i <= n; ++i) {
4
5
        str[i * 2] = s[i];
        str[i * 2 + 1] = '!';
6
7
     for (int i = 1, j = 0; i \le n; ++i) {
8
        if (p[j] + j > i) {
9
          p[i] = min(p[2 * j - i], p[j] + j - i);
10
11
        } else {
12
         p[i] = 1;
13
        while (str[i + p[i]] == str[i - p[i]]) {
14
15
         ++p[i];
16
        if (i + p[i] > j + p[j]) {
17
18
          j = i;
19
        }
20
     }
```

21 }

4.3 回文树

```
1
   //最长双回文串
 2
   struct PT {
3
     char s[MAXL];
      int fail[MAXL], ch[26][MAXL], l[MAXL], dep[MAXL], lst, nc, n;
4
      void init() {
5
6
        l[0] = 0;
        l[1] = -1;
7
8
        fail[0] = fail[1] = 1;
9
        for (int i = 0; i < 26; ++i) {
10
          for (int j = 0; j < nc; ++j) {
            ch[i][j] = 0;
11
          }
12
13
        for (int i = 2; i < nc; ++i) {</pre>
14
15
          l[i] = 0;
16
          fail[i] = 0;
17
18
19
        lst = 0;
        nc = 2;
20
21
        n = 0;
22
        s[0] = '#';
23
24
      int insert(char c) {
25
        int id = c - 'a';
26
        s[++n] = c;
27
        while (s[n - l[lst] - 1] != s[n]) {
28
29
          lst = fail[lst];
30
        if (ch[id][lst] == 0) {
31
32
          l[nc] = l[lst] + 2;
33
          int f = fail[lst];
34
          while (s[n - l[f] - 1] != s[n]) {
35
            f = fail[f];
36
          fail[nc] = ch[id][f];
37
          dep[nc] = dep[fail[nc]] + 1;
38
39
          ch[id][lst] = nc;
40
          ++nc;
41
42
        lst = ch[id][lst];
        return lst;
43
44
45
   } pt;
46
47 char S[MAXL];
  int len[MAXL];
48
49
   int main() {
     ios::sync_with_stdio(false);
50
51
     cin.tie(0);
52
     cout.tie(0);
53
54
     cin >> S;
```

```
55
      int n = strlen(S);
56
      pt.init();
      for (int i = 0; i < n; ++i) {
57
        len[i] = pt.l[pt.insert(S[i])];
58
59
60
      pt.init();
      int ans = 0;
61
      for (int i = n - 1; i; --i) {
62
        ans = \max(ans, len[i - 1] + pt.l[pt.insert(S[i])]);
63
64
65
     cout << ans << "\n";</pre>
66
67
     return 0;
68
  }
   4.4 exkmp
1 // next[i]:x[i...m-1] 与 x[0...m-1] 的最长公共前缀
   // extend[i]:y[i...n-1] 与 x[0...m-1] 的最长公共前缀
 3
   void prework(char x[], int m, int next[]) {
     next[0] = m;
4
      int j = 0;
5
      while (j + 1 < m \&\& x[j] == x[j + 1])
6
7
     next[1] = j;
8
9
      int k = 1;
10
      for (int i = 2; i < m; i++) {</pre>
11
        int p = next[k] + k - 1;
12
        int L = next[i - k];
        if (i + L 
13
14
          next[i] = L;
15
        else {
16
          j = max(0, p - i + 1);
17
          while (i + j < m \&\& x[i + j] == x[j])
18
            j++;
19
          next[i] = j;
20
          k = i;
21
        }
22
      }
23
   }
   void exkmp(char x[], int m, char y[], int n, int next[], int extend[]) {
     prework(x, m, next);
25
26
      int j = 0;
      while (j < n \&\& j < m \&\& x[j] == y[j])
27
28
        j++;
      extend[0] = j;
29
      int k = 0;
30
31
      for (int i = 1; i < n; i++) {
        int p = extend[k] + k - 1;
32
        int L = next[i - k];
33
34
        if (i + L 
          extend[i] = L;
35
        else {
36
37
          j = max(0, p - i + 1);
          while (i + j < n \&\& j < m \&\& y[i + j] == x[j])
38
39
            j++;
40
          extend[i] = j;
          k = i;
41
```

```
42
        }
43
   }
44
   4.5 kmp
   void get_next(char *S, int *nxt, int n) {
2
     nxt[0] = -1;
3
     int j = -1;
4
     for (int i = 1; i < n; ++i) {</pre>
5
        while ((\sim j) \&\& S[j + 1] != S[i]) {
6
          j = nxt[j];
        }
7
        nxt[i] = (S[j + 1] == S[i]) ? (++j) : j;
8
9
10
11
12
   int pattern(char *S, char *T, int *nxt, int n, int m) {
     int j = -1;
13
14
      for (int i = 0; i < m; ++i) {</pre>
15
        while ((\sim j) \&\& S[j + 1] != T[i]) {
16
          j = nxt[j];
17
        j += S[j + 1] == T[i];
        if (j == n - 1) {
19
          return i - n + 1;
20
21
        }
22
     }
23
     return -1;
   }
24
        Graph Theory
   5
   5.1 KM
   int n, m, match[MAXN];
   int adj[MAXN][MAXN], lx[MAXN], ly[MAXN], slack[MAXN];
   int visx[MAXN], visx_c, visy[MAXN], visy_c;
4
5
   bool dfs(int x) {
6
     visx[x] = visx_c;
7
     for (int y = 0; y < m; ++y)
        if (visy[y] ^ visy_c) {
8
9
          int t = lx[x] + ly[y] - adj[x][y];
10
          if (!t) {
            visy[y] = visy_c;
11
            if (match[y] < 0 || dfs(match[y])) return match[y] = x, true;</pre>
12
13
            (slack[y] > t) \&\& (slack[y] = t);
14
15
     return false;
16
   }
17
18
19
   int KM() {
20
     memset(match, -1, sizeof(int) * m);
21
     memset(ly, 0, sizeof(int) * m);
22
     for (int i = 0; i < n; ++i) {
```

```
23
        lx[i] = -INF;
24
        for (int j = 0; j < m; ++j) (adj[i][j] > lx[i]) && (lx[i] = adj[i][j]);
25
      for (int x = 0; x < n; ++x) {
26
27
        fill(slack, slack + m, INF);
28
        for (;;) {
29
          ++visx_c, ++visy_c;
          if (dfs(x)) break;
30
          int d = INF;
31
          for (int i = 0; i < m; ++i)
32
33
            (visy[i] \land visy\_c) \&\& (d > slack[i]) \&\& (d = slack[i]);
34
          for (int i = 0; i < n; ++i) (visx[i] == visx_c) && (lx[i] -= d);
          for (int i = 0; i < m; ++i)
35
            (visy[i] \land visy\_c) ? slack[i] -= d : ly[i] += d;
36
        }
37
      }
38
39
      int res = 0;
      for (int i = 0; i < m; ++i) (~match[i]) && (res += adj[match[i]][i]);</pre>
      return res;
41
42
  }
```

6 Computational Geometry

7 Java

7.1 进制转换

```
import java.io.*;
   import java.util.*;
3
   import java.math.*;
4
5 /**
6
    * Built using CHelper plug-in
    * Actual solution is at the top
7
8
   public class Main {
       public static void main(String[] args) {
10
11
            InputStream inputStream = System.in;
12
            OutputStream outputStream = System.out;
13
            Scanner in = new Scanner(inputStream);
            PrintWriter out = new PrintWriter(outputStream);
14
            Solver solver = new Solver();
15
            int testCount = Integer.parseInt(in.next());
16
            for (int i = 1; i <= testCount; i++)</pre>
17
                solver.solve(i, in, out);
18
            out.close();
19
       }
20
21
       static class Solver {
22
            public void solve(int testNumber, Scanner in, PrintWriter out) {
23
                int a = in.nextInt();
24
25
                int b = in.nextInt();
26
                String num = in.next();
27
                BigInteger value = BigInteger.ZERO;
28
                for (int i = 0; i < num.length(); ++i) {</pre>
29
30
                    value = value.multiply(BigInteger.valueOf(a));
```

```
value = BigInteger.valueOf(getValue(num.charAt(i))).add(value);
31
                }
32
                out.println(a + " " + num);
33
34
                if (value.equals(BigInteger.ZERO)) {
35
                    out.println(b + " 0");
36
37
                    out.println();
                    return;
38
                }
39
40
                out.print(b + " ");
41
42
                char[] ans = new char[1000];
43
                int length = 0;
44
                while (!value.equals(BigInteger.ZERO)) {
45
                    int digit = value.mod(BigInteger.valueOf(b)).intValue();
46
                    value = value.divide(BigInteger.valueOf(b));
47
                    ans[length] = getChar(digit);
48
                    ++length;
49
                }
50
51
                for (int i = length - 1; i >= 0; --i) {
52
                    out.print(ans[i]);
53
54
55
                out.println("\n");
            }
56
57
            private int getValue(char ch) {
58
                if (ch >= 'A' && ch <= 'Z') {
59
                    return ch - 'A' + 10;
60
61
                if (ch >= 'a' && ch <= 'z') {
62
                    return ch - 'a' + 36;
63
64
                return ch - '0';
65
            }
66
67
68
            private char getChar(int x) {
                if (x < 10) {
69
70
                    return (char) ('0' + x);
71
                \} else if (x < 36) {
                    return (char) ('A' + x - 10);
72
73
74
                    return (char) ('a' + x - 36);
75
76
            }
77
78
        }
79 }
   7.2 out
1
   \section{Others}
2
3
4 \subsection{FastI0}
   \begin{lstlisting}
6 namespace FastIO {
```

```
struct Control {
8
      int ct, val;
      Control(int Ct, int Val = -1) : ct(Ct), val(Val) {}
9
      inline Control operator()(int Val) { return Control(ct, Val); }
   } _endl(0), _prs(1), _setprecision(2);
11
12
13 const int IO_SIZE = 1 << 16 | 127;
14
  struct FastI0 {
15
      char in[IO_SIZE], *p, *pp, out[IO_SIZE], *q, *qq, ch[20], *t, b, K, prs;
16
      FastIO(): p(in), pp(in), q(out), qq(out + IO_SIZE), t(ch), b(1), K(6) {}
17
18
      ~FastIO() { fwrite(out, 1, q - out, stdout); }
19
      inline char getc() {
        return p == pp && (pp = (p = in) + fread(in, 1, IO_SIZE, stdin), p == pp)
20
                   ? (b = 0, EOF)
21
                   : *p++;
22
23
24
      inline void putc(char x) {
25
        q == qq \&\& (fwrite(out, 1, q - out, stdout), q = out), *q++ = x;
26
27
      inline void puts(const char str[]) {
28
        fwrite(out, 1, q - out, stdout), fwrite(str, 1, strlen(str), stdout),
29
            q = out;
30
31
      inline void getline(string &s) {
        s = "":
32
33
        for (char ch; (ch = getc()) != '\n' && b;) s += ch;
34
   #define indef(T)
35
      inline FastIO &operator>>(T &x) {
36
37
        x = 0;
        char f = 0, ch;
38
39
        while (!isdigit(ch = getc()) && b) f |= ch == '-';
        while (isdigit(ch)) x = (x << 1) + (x << 3) + (ch ^ 48), ch = getc();
40
        return x = f ? -x : x, *this;
41
42
      indef(int);
43
44
      indef(long long);
45
      inline FastIO &operator>>(string &s) {
46
       s = "":
47
48
        char ch;
49
        while (isspace(ch = getc()) && b) {}
        while (!isspace(ch) && b) s += ch, ch = getc();
50
51
        return *this;
52
      inline FastIO &operator>>(double &x) {
53
        x = 0;
54
        char f = 0, ch;
55
        double d = 0.1;
56
57
        while (!isdigit(ch = getc()) && b) f |= (ch == '-');
58
        while (isdigit(ch)) x = x * 10 + (ch ^ 48), ch = getc();
59
        if (ch == '.')
          while (isdigit(ch = getc())) x += d * (ch ^ 48), d *= 0.1;
60
        return x = f ? -x : x, *this;
61
62
   #define outdef(_T)
63
64
      inline FastIO &operator<<(_T x) {</pre>
        !x \&\& (putc('0'), 0), x < 0 \&\& (putc('-'), x = -x);
65
```

```
66
       while (x) *t++ = x % 10 + 48, x /= 10;
       while (t != ch) *q++ = *--t;
67
       return *this;
68
69
70
     outdef(int);
     outdef(long long);
71
     inline FastIO &operator<<(char ch) { return putc(ch), *this; }</pre>
72
     inline FastIO &operator<<(const char str[]) { return puts(str), *this; }</pre>
73
     inline FastIO &operator<<(const string &s) { return puts(s.c_str()), *this; }</pre>
74
     inline FastIO &operator<<(double x) {</pre>
75
76
       int k = 0;
77
       this->operator<<(int(x));</pre>
       putc('.');
78
       x = int(x);
79
       prs && (x += 5 * pow(10, -K - 1));
80
       while (k < K) putc(int(x *= 10) \land 48), x -= int(x), ++k;
81
82
       return *this;
83
     inline FastIO &operator<<(const Control &cl) {</pre>
84
       switch (cl.ct) {
85
       case 0: putc('\n'); break;
86
       case 1: prs = cl.val; break;
87
       case 2: K = cl.val; break;
88
89
90
       return *this;
91
     inline operator bool() { return b; }
92
93
   } // namespace FastIO
   7.3 head
   #include <bits/stdc++.h>
2 using namespace std;
3
4 typedef long long ll;
5 typedef unsigned long long ull;
6 typedef long double ld;
7 typedef pair<int, int> pii;
8 typedef tuple<int, int, int> tiii;
9 typedef vector<int> vi;
10 typedef vector<vi> vvi;
   typedef vector<long long> vll;
   typedef vector<pii> vpii;
13
14 #define SZ(a) int((a).size())
15 #define ALL(a) (a).begin(), (a).end()
16 #define EXIST(s, x) ((s).find(x) != (s).end())
17 #define A_EXIST(a, x) (find(ALL(a), x) != (a).end())
18 #define ZERO(a) memset((a), 0, sizeof(a))
19
20 #define FOR(i, a, b) for (int i = int(a); i < int(b); ++i)
21 #define REP(i, a, b) for (int i = int(b) - 1; i >= a; --i)
22 #define FOR2(i, a, b, j, c, d) FOR(i, a, b) FOR(j, c, d)
23 #define REP2(i, a, b, j, c, d) REP(i, a, b) REP(j, c, d)
24 #define EACH(i, s) for (auto i = (s).begin(); i != (s).end(); ++i)
25 #define debug(...) fprintf(stderr, __VA_ARGS__)
26 #define dbg(x)
                                                                                      \
```

```
27
28
          << #x " = " << (x) << endl
29
30
31 const int INF = 0x3ffffff;
   const ll LL_INF = 0x3ffffffffffffffff;
33 const int MOD = 1e9 + 7;
34 const ll HASH_KEY = 6151;
35 const ll HASH_MOD = 1610612741;
36
37 // mt19937 rdm(chrono::steady_clock::now().time_since_epoch().count());
38 // uniform_int_distribution<int> u_int(begin, end);
  // uniform_real_distribution<double> u_read(begin, end);
40 /* -- HEAD END -- */
41
42 void solve() {}
43
44 int main(int argc, char *argv[]) {
     ios::sync_with_stdio(false);
45
     cin.tie(nullptr);
46
     cout << fixed << setprecision(10);</pre>
47
48
49
     int o_o;
     for (o_o = 1; o_o; --o_o) solve();
51
52
     return 0;
53 }
   7.4 myalloc
1 // useage: vector<int. mvalloc<int>> L:
  static char space[10000000], *sp = space;
3 template <typename T> struct myalloc : allocator<T> {
     myalloc() {}
4
     template <typename T2> myalloc(const myalloc<T2> &a) {}
5
     template <typename T2> myalloc<T> &operator=(const myalloc<T2> &a) {
6
       return *this:
7
8
     template <typename T2> struct rebind { typedef myalloc<T2> other; };
9
     inline T *allocate(size_t n) {
10
       T * result = (T *) sp;
11
       sp += n * sizeof(T);
12
       return result;
13
15
     inline void deallocate(T *p, size_t n) {}
16 };
   7.5 duipai
1 #/usr/bin/bash
  while true: do
3
     python gen_data.py
4
5
     ./E < input.txt > output.txt
6
    ./E_r <input.txt > r.txt
     if diff output.txt r.txt; then
       printf AC
```

```
9 else
10 echo WA
11 exit 0
12 fi
13 done
```