
cycleke（菜鸡）的 XPCP 模板



icpc International Collegiate
Programming Contest



哈爾濱工業大學

cycleke

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1 Math

1.1 BSGS

```

1 // Finds the primitive root modulo p
2 int generator(int p) {
3     vector<int> fact;
4     int phi = p - 1, n = phi;
5     for (int i = 2; i * i <= n; ++i) {
6         if (n % i == 0) {
7             fact.push_back(i);
8             while (n % i == 0) n /= i;
9         }
10    }
11    if (n > 1) fact.push_back(n);
12    for (int res = 2; res <= p; ++res) {
13        bool ok = true;
14        for (int factor : fact)
15            if (mod_pow(res, phi / factor, p) == 1) {
16                ok = false;
17                break;
18            }
19    }
20    if (ok) return res;
21 }
22 return -1;
23 }
24 // This program finds all numbers x such that  $x^k \equiv a \pmod n$ 
25 vector<int> BSGS(int n, int k, int a) {
26     if (a == 0) return vector<int>({0});
27
28     int g = generator(n);
29     // Baby-step giant-step discrete logarithm algorithm
30     int sq = (int)sqrt(n + .0) + 1;
31     vector<pair<int, int>> dec(sq);
32     for (int i = 1; i <= sq; ++i)
33         dec[i - 1] = {mod_pow(g, i * sq * k % (n - 1), n), i};
34
35     sort(dec.begin(), dec.end());
36     int any_ans = -1;
37     for (int i = 0; i < sq; ++i) {
38         int my = mod_pow(g, i * k % (n - 1), n) * a % n;
39         auto it = lower_bound(dec.begin(), dec.end(), make_pair(my, 0));
40         if (it != dec.end() && it->first == my) {
41             any_ans = it->second * sq - i;
42             break;
43         }
44     }
45     if (any_ans == -1) return vector<int>();
46     // Print all possible answers
47     int delta = (n - 1) / __gcd(k, n - 1);
48     vector<int> ans;
49     for (int cur = any_ans % delta; cur < n - 1; cur += delta)
50         ans.push_back(mod_pow(g, cur, n));
51     sort(ans.begin(), ans.end());
52     return ans;
53 }

```

1.2 FFT

```

1  const int MAXN = 4 * 1e5 + 3;
2  const double PI = acos(-1);
3  complex<double> a[MAXN], b[MAXN];
4
5  int n, bit;
6  int rev[MAXN];
7
8  void fft(complex<double> *a, int sign) {
9      for (int i = 0; i < n; ++i)
10         if (i < rev[i]) swap(a[i], a[rev[i]]);
11
12     for (int j = 1; j < n; j <= 1) {
13         complex<double> wn(cos(2 * PI / (j << 1)), sign * sin(2 * PI / (j << 1)));
14         for (int i = 0; i < n; i += (j << 1)) {
15             complex<double> w(1, 0), t0, t1;
16             FOR(k, 0, j) {
17                 t0 = a[i + k];
18                 t1 = w * a[i + j + k];
19                 a[i + k] = t0 + t1;
20                 a[i + j + k] = t0 - t1;
21                 w *= wn;
22             }
23         }
24     }
25     if (sign == -1)
26         for (int i = 0; i < n; ++i) a[i] /= n;
27 }
28
29 int main() {
30     ios::sync_with_stdio(false);
31     cin.tie(0);
32     cout.tie(0);
33
34     int n, m, x;
35     cin >> n >> m;
36     for (int i = 0; i <= n; ++i) {
37         cin >> x;
38         a[i].real(x);
39     }
40     for (int i = 0; i <= m; ++i) {
41         cin >> x;
42         b[i].real(x);
43     }
44
45     ::n = 1;
46     bit = 0;
47     while (::n <= n + m) {
48         ::n <<= 1;
49         ++bit;
50     }
51     rev[0] = 0;
52     FOR(i, 1, ::n) rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (bit - 1));
53     fft(a, 1);
54     fft(b, 1);
55     FOR(i, 0, ::n) a[i] *= b[i];
56     fft(a, -1);
57     FOR(i, 0, n + m + 1) cout << int(a[i].real() + .5) << " ";

```

```

58     cout << "\n";
59     return 0;
60 }

```

1.3 Linear Recurrence

```

1  struct LinearRecurrence {
2      using int64 = long long;
3      using vec = std::vector<int64>;
4
5      static void extend(vec &a, size_t d, int64 value = 0) {
6          if (d <= a.size()) return;
7          a.resize(d, value);
8      }
9
10     static vec BerlekampMassey(const vec &s, int64 mod) {
11         std::function<int64(int64)> inverse = [&](int64 a) {
12             return a == 1 ? 1 : (int64)(mod - mod / a) * inverse(mod % a) % mod;
13         };
14         vec A = {1}, B = {1};
15         int64 b = s[0];
16         for (size_t i = 1, m = 1; i < s.size(); ++i, m++) {
17             int64 d = 0;
18             for (size_t j = 0; j < A.size(); ++j) { d += A[j] * s[i - j] % mod; }
19             if (!(d % mod)) continue;
20             if (2 * (A.size() - 1) <= i) {
21                 auto temp = A;
22                 extend(A, B.size() + m);
23                 int64 coef = d * inverse(b) % mod;
24                 for (size_t j = 0; j < B.size(); ++j) {
25                     A[j + m] -= coef * B[j] % mod;
26                     if (A[j + m] < 0) A[j + m] += mod;
27                 }
28                 B = temp, b = d, m = 0;
29             } else {
30                 extend(A, B.size() + m);
31                 int64 coef = d * inverse(b) % mod;
32                 for (size_t j = 0; j < B.size(); ++j) {
33                     A[j + m] -= coef * B[j] % mod;
34                     if (A[j + m] < 0) A[j + m] += mod;
35                 }
36             }
37         }
38         return A;
39     }
40
41     static void exgcd(int64 a, int64 b, int64 &g, int64 &x, int64 &y) {
42         if (!b)
43             x = 1, y = 0, g = a;
44         else {
45             exgcd(b, a % b, g, y, x);
46             y -= x * (a / b);
47         }
48     }
49
50     static int64 crt(const vec &c, const vec &m) {
51         int n = c.size();
52         int64 M = 1, ans = 0;

```

```

53     for (int i = 0; i < n; ++i) M *= m[i];
54     for (int i = 0; i < n; ++i) {
55         int64 x, y, g, tm = M / m[i];
56         exgcd(tm, m[i], g, x, y);
57         ans = (ans + tm * x * c[i] % M) % M;
58     }
59     return (ans + M) % M;
60 }
61
62 static vec ReedsSloane(const vec &s, int64 mod) {
63     auto inverse = [](int64 a, int64 m) {
64         int64 d, x, y;
65         exgcd(a, m, d, x, y);
66         return d == 1 ? (x % m + m) % m : -1;
67     };
68     auto L = [](const vec &a, const vec &b) {
69         int da = (a.size() > 1 || (a.size() == 1 && a[0])) ? a.size() - 1 : -1000;
70         int db = (b.size() > 1 || (b.size() == 1 && b[0])) ? b.size() - 1 : -1000;
71         return std::max(da, db + 1);
72     };
73     auto prime_power = [&](const vec &s, int64 mod, int64 p, int64 e) {
74         // linear feedback shift register mod p^e, p is prime
75         std::vector<vec> a(e), b(e), an(e), bn(e), ao(e), bo(e);
76         vec t(e), u(e), r(e), to(e, 1), uo(e), pw(e + 1);
77         ;
78         pw[0] = 1;
79         for (int i = pw[0] = 1; i <= e; ++i) pw[i] = pw[i - 1] * p;
80         for (int64 i = 0; i < e; ++i) {
81             a[i] = {pw[i]}, an[i] = {pw[i]};
82             b[i] = {0}, bn[i] = {s[0] * pw[i] % mod};
83             t[i] = s[0] * pw[i] % mod;
84             if (t[i] == 0) {
85                 t[i] = 1, u[i] = e;
86             } else {
87                 for (u[i] = 0; t[i] % p == 0; t[i] /= p, ++u[i])
88                     ;
89             }
90         }
91         for (size_t k = 1; k < s.size(); ++k) {
92             for (int g = 0; g < e; ++g) {
93                 if (L(an[g], bn[g]) > L(a[g], b[g])) {
94                     ao[g] = a[e - 1 - u[g]];
95                     bo[g] = b[e - 1 - u[g]];
96                     to[g] = t[e - 1 - u[g]];
97                     uo[g] = u[e - 1 - u[g]];
98                     r[g] = k - 1;
99                 }
100             }
101             a = an, b = bn;
102             for (int o = 0; o < e; ++o) {
103                 int64 d = 0;
104                 for (size_t i = 0; i < a[o].size() && i <= k; ++i) {
105                     d = (d + a[o][i] * s[k - i]) % mod;
106                 }
107                 if (d == 0) {
108                     t[o] = 1, u[o] = e;
109                 } else {
110                     for (u[o] = 0; t[o] % p == 0; t[o] /= p, ++u[o])
111                         ;

```

```

112         int g = e - 1 - u[o];
113         if (L(a[g], b[g]) == 0) {
114             extand(bn[o], k + 1);
115             bn[o][k] = (bn[o][k] + d) % mod;
116         } else {
117             int64 coef =
118                 t[o] * inverse(to[g], mod) % mod * pw[u[o] - uo[g]] % mod;
119             int m = k - r[g];
120             extand(an[o], ao[g].size() + m);
121             extand(bn[o], bo[g].size() + m);
122             for (size_t i = 0; i < ao[g].size(); ++i) {
123                 an[o][i + m] -= coef * ao[g][i] % mod;
124                 if (an[o][i + m] < 0) an[o][i + m] += mod;
125             }
126             while (an[o].size() && an[o].back() == 0) an[o].pop_back();
127             for (size_t i = 0; i < bo[g].size(); ++i) {
128                 bn[o][i + m] -= coef * bo[g][i] % mod;
129                 if (bn[o][i + m] < 0) bn[o][i + m] += mod;
130             }
131             while (bn[o].size() && bn[o].back() == 0) bn[o].pop_back();
132         }
133     }
134 }
135 }
136 return std::make_pair(an[0], bn[0]);
137 };
138
139 std::vector<std::tuple<int64, int64, int>> fac;
140 for (int64 i = 2; i * i <= mod; ++i)
141     if (mod % i == 0) {
142         int64 cnt = 0, pw = 1;
143         while (mod % i == 0) mod /= i, ++cnt, pw *= i;
144         fac.emplace_back(pw, i, cnt);
145     }
146 if (mod > 1) fac.emplace_back(mod, mod, 1);
147 std::vector<vec> as;
148 size_t n = 0;
149 for (auto &&x : fac) {
150     int64 mod, p, e;
151     vec a, b;
152     std::tie(mod, p, e) = x;
153     auto ss = s;
154     for (auto &&x : ss) x %= mod;
155     std::tie(a, b) = prime_power(ss, mod, p, e);
156     as.emplace_back(a);
157     n = std::max(n, a.size());
158 }
159 vec a(n), c(as.size()), m(as.size());
160 for (size_t i = 0; i < n; ++i) {
161     for (size_t j = 0; j < as.size(); ++j) {
162         m[j] = std::get<0>(fac[j]);
163         c[j] = i < as[j].size() ? as[j][i] : 0;
164     }
165     a[i] = crt(c, m);
166 }
167 return a;
168 }
169
170 LinearRecurrence(const vec &s, const vec &c, int64 mod)

```



```

171         : init(s), trans(c), mod(mod), m(s.size()) {}
172
173 LinearRecurrence(const vec &s, int64 mod, bool is_prime = true) : mod(mod) {
174     vec A = is_prime ? BerlekampMassey(s, mod) : ReedsSloane(s, mod);
175     if (A.empty()) A = {0};
176     m = A.size() - 1;
177     trans.resize(m);
178     for (int i = 0; i < m; ++i) { trans[i] = (mod - A[i + 1]) % mod; }
179     std::reverse(trans.begin(), trans.end());
180     init = {s.begin(), s.begin() + m};
181 }
182
183 int64 calc(int64 n) {
184     if (mod == 1) return 0;
185     if (n < m) return init[n];
186     vec v(m), u(m << 1);
187     int msk = !!n;
188     for (int64 m = n; m > 1; m >= 1) msk <<= 1;
189     v[0] = 1 % mod;
190     for (int x = 0; msk; msk >= 1, x <= 1) {
191         std::fill_n(u.begin(), m * 2, 0);
192         x |= !(n & msk);
193         if (x < m)
194             u[x] = 1 % mod;
195         else { // can be optimized by fft/ntt
196             for (int i = 0; i < m; ++i) {
197                 for (int j = 0, t = i + (x & 1); j < m; ++j, ++t) {
198                     u[t] = (u[t] + v[i] * v[j]) % mod;
199                 }
200             }
201             for (int i = m * 2 - 1; i >= m; --i) {
202                 for (int j = 0, t = i - m; j < m; ++j, ++t) {
203                     u[t] = (u[t] + trans[j] * u[i]) % mod;
204                 }
205             }
206         }
207         v = {u.begin(), u.begin() + m};
208     }
209     int64 ret = 0;
210     for (int i = 0; i < m; ++i) { ret = (ret + v[i] * init[i]) % mod; }
211     return ret;
212 }
213
214 vec init, trans;
215 int64 mod;
216 int m;
217 };

```

1.4 Linear Sieve

```

1  const int MAXN = 1e7 + 5;
2
3  bool vis[MAXN];
4  int prime[MAXN / 10], prime_cnt;
5  int fac[MAXN], e[MAXN], d[MAXN], mu[MAXN], phi[MAXN];
6  // e 质因子最高次数, d 因数个数
7  void sieve() {
8      fac[1] = 1, e[1] = 0, d[1] = 1, mu[1] = 1, phi[1] = 1;

```

```

9   for (int i = 2; i < MAXN; ++i) {
10       if (!vis[i]) {
11           prime[prime_cnt++] = i;
12           fac[i] = i, e[i] = 1, d[i] = 2, mu[i] = -1, phi[i] = i - 1;
13       }
14       for (int j = 0; j < prime_cnt; ++j) {
15           int t = prime[j] * i;
16           if (t >= MAXN) { break; }
17           vis[t] = true;
18           fac[t] = prime[j];
19           if (i % prime[j] == 0) {
20               e[t] = e[i] + 1;
21               d[t] = d[i] / (e[i] + 1) * (e[t] + 1);
22               mu[t] = 0;
23               phi[t] = phi[i] * prime[j];
24               break;
25           } else {
26               e[t] = 1;
27               d[t] = d[i] * 2;
28               mu[t] = -mu[i];
29               phi[t] = phi[i] * (prime[j] - 1);
30           }
31       }
32   }
33 }

```

1.5 Lucas

```

1  // C(n, m) = C(n / p, m / p) * C(n % p, m % p) (mod p)
2  ll lucas(ll n, ll k, int p) {
3      ll ret = 1;
4      while (n && k) {
5          ll nn = n % p, kk = k % p;
6          if (nn < kk) return 0;
7          ret = ret * f[nn] * mod_pow(f[kk] * f[nn - kk] % p, p - 2, p) % p;
8          n /= p, k /= p;
9      }
10     return res;
11 }

```

1.6 Miller Rabin

```

1  inline ll mod_mul(const ll &a, const ll &b, const ll &mod) {
2      ll k = (ll)((1.0L * a * b) / (1.0L * mod)), t = a * b - k * mod;
3      t -= mod;
4      while (t < 0) t += mod;
5      return t;
6  }
7  inline ll mod_pow(ll a, ll b, const ll &mod) {
8      ll res = 1;
9      for (; b >= 1, a = mod_mul(a, a, mod))
10         (b & 1) && (res = mod_mul(res, a, mod));
11     return res;
12 }
13
14 inline bool check(const ll &x, const ll &p) {

```

```

15  if (!(x % p) || mod_pow(p % x, x - 1, x) ^ 1) return false;
16  ll k = x - 1, t;
17  while (~k & 1) {
18      if ((t = mod_pow(p % x, k >= 1, x)) ^ 1) && (t ^ (x - 1)) return false;
19      if (!(t ^ (x - 1))) return true;
20  }
21  return true;
22 }
23
24 inline bool Miller_Rabin(const ll &x) {
25     if (x < 2) return false;
26     static const int p[12] = {2, 3, 5, 7, 11, 13, 17, 19, 61, 2333, 4567, 24251};
27     for (int i = 0; i < 12; ++i) {
28         if (!(x ^ p[i])) return true;
29         if (!check(x, p[i])) return false;
30     }
31     return true;
32 }

```

1.7 Pollard rho

```

1  inline ll rand64(ll x) {
2      return 1ll * ((rand() << 15 ^ rand()) << 30 ^ (rand() << 15 ^ rand())) % x;
3  }
4
5  inline ll Pollard_rho(const ll &x, const int &y) {
6      ll v0 = rand64(x - 1) + 1, v = v0, d, s = 1;
7      for (register int t = 0, k = 1;;) {
8          if (v = (mod_mul(v, v, x) + y) % x, s = mod_mul(s, abs(v - v0), x),
9              !(v ^ v0) || !s)
10             return x;
11         if (++t == k) {
12             if ((d = __gcd(s, x)) ^ 1) return d;
13             v0 = v, k <<= 1;
14         }
15     }
16 }
17
18 ll ans;
19 vector<ll> factor;
20 void findfac(ll n) {
21     if (Miller_Rabin(n)) {
22         factor.push_back(n);
23         return;
24     }
25     ll p = n;
26     while (p >= n) { p = Pollard_rho(p, rand64(n - 1) + 1); }
27     findfac(p);
28     findfac(n / p);
29 }

```

1.8 burnside

```

1  //  $|X/G| = \frac{1}{|G|} \sum_{g \in G} |X^g|$ 
2  // Gym - 101873B
3  // m边形, 每边是n*n的矩形, 用c种颜色染色, 可进行水平旋转, 问不同多边形个数。

```

```

4  #include <bits/stdc++.h>
5  using namespace std;
6
7  const int MOD = 1e9 + 7;
8
9  int mod_pow(int a, int b) {
10     int r = 1;
11     for (; b >= 1, a = 1LL * a * a % MOD)
12         if (b & 1) r = 1LL * a * r % MOD;
13     return r;
14 }
15
16 int main() {
17     ios::sync_with_stdio(false);
18     cin.tie(nullptr);
19
20     int n, m, c;
21     cin >> n >> m >> c;
22
23     int ans = 0;
24     for (int i = 1; i <= m; ++i)
25         ans = (ans + mod_pow(c, n * n * __gcd(i, m))) % MOD;
26     ans = 1LL * ans * mod_pow(m, MOD - 2) % MOD;
27     cout << ans << '\n';
28     return 0;
29 }

```

1.9 china

```

1  int china(int n, int *a, int *m) {
2     int lcm = 1, res = 0;
3     for (int i = 0; i < n; ++i) lcm *= m[i];
4     for (int i = 0; i < n; ++i) {
5         int t = lcm / m[i], x, y;
6         exgcd(t, m[i], x, y);
7         x = (x % m[i] + m[i]) % m[i];
8         res = (res + 1LL * t * x) % lcm;
9     }
10    return res;
11 }

```

1.10 exctr

```

1  int exctr(int n, int *a, int *m) {
2     int M = m[0], res = a[0];
3     for (int i = 1; i < n; ++i) {
4         int a = M, b = m[i], c = (a[i] - res % b + b) % b, x, y;
5         int g = exgcd(a, b, x, y), bg = b / g;
6         if (c % g != 0) return -1;
7         x = 1LL * x * (c / g) % bg;
8         res += x * M;
9         M *= bg;
10        res = (res % M + M) % M;
11    }
12    return res;
13 }

```

1.11 exgcd

```

1 int exgcd(int a, int b, int &x, int &y) {
2     if (b == 0) return x = 1, y = 0, a;
3     int g = exgcd(b, a % b, y, x);
4     y -= a / b * x;
5     return g;
6 }

```

1.12 gauss

```

1
2 const double EPS = 1e-9;
3 const int MAXN = MAX_NODE;
4 double a[MAXN][MAXN], x[MAXN];
5 int equ, var;
6
7 int gauss() {
8     int i, j, k, col, max_r;
9     for (k = 0, col = 0; k < equ && col < var; k++, col++) {
10         max_r = k;
11         for (i = k + 1; i < equ; i++)
12             if (fabs(a[i][col]) > fabs(a[max_r][col])) max_r = i;
13         if (fabs(a[max_r][col]) < EPS) return 0;
14
15         if (k != max_r) {
16             for (j = col; j < var; j++) swap(a[k][j], a[max_r][j]);
17             swap(x[k], x[max_r]);
18         }
19
20         x[k] /= a[k][col];
21         for (j = col + 1; j < var; j++) a[k][j] /= a[k][col];
22         a[k][col] = 1;
23
24         for (i = k + 1; i < equ; i++)
25             if (i != k) {
26                 x[i] -= x[k] * a[i][col];
27                 for (j = col + 1; j < var; j++) a[i][j] -= a[k][j] * a[i][col];
28                 a[i][col] = 0;
29             }
30     }
31
32     for (col = equ - 1, k = var - 1; ~col; --col, --k) {
33         if (fabs(a[col][k]) > 0) {
34             for (i = 0; i < k; ++i) {
35                 x[i] -= x[k] * a[i][col];
36                 for (j = col + 1; j < var; j++) a[i][j] -= a[k][j] * a[i][col];
37                 a[i][col] = 0;
38             }
39         }
40     }
41
42     return 1;
43 }

```

1.13 实数线性规划

```

1 // 求  $\max\{cx \mid Ax \leq b, x \geq 0\}$ 
2 typedef vector<double> VD;
3 VD simplex(vector<VD> A, VD b, VD c) {
4     int n = A.size(), m = A[0].size() + 1, r = n, s = m - 1;
5     vector<VD> D(n + 2, VD(m + 1, 0));
6     vector<int> ix(n + m);
7     for (int i = 0; i < n + m; ++i) ix[i] = i;
8     for (int i = 0; i <= n; ++i) {
9         for (int j = 0; j < m - 1; ++j) D[i][j] = -A[i][j];
10        D[i][m - 1] = 1, D[i][m] = b[i];
11        if (D[r][m] > D[i][m]) r = i;
12    }
13    for (int j = 0; j < m - 1; ++j) D[n][j] = c[j];
14    D[n + 1][m - 1] = -1;
15    for (double d;;) {
16        if (r < n) {
17            swap(ix[s], ix[r + m]);
18            D[r][s] = 1 / D[r][s];
19            vector<int> speed_up;
20            for (int j = 0; j <= m; ++j)
21                if (j != s) {
22                    D[r][j] *= -D[r][s];
23                    if (D[r][j]) speed_up.push_back(j);
24                }
25            for (int i = 0; i <= n + 1; ++i)
26                if (i != r) {
27                    for (int j : speed_up) D[i][j] += D[r][j] * D[i][s];
28                    D[i][s] *= D[r][s];
29                }
30        }
31        r = -1, s = -1;
32        for (int j = 0; j < m; ++j)
33            if ((s < 0 || ix[s] > ix[j]) &&
34                (D[n + 1][j] > EPS || (D[n + 1][j] > -EPS && D[n][j] > EPS)))
35                s = j;
36        if (s < 0) break;
37        for (int i = 0; i < n; ++i)
38            if (D[i][s] < -EPS)
39                if (r < 0 || (d = D[r][m] / D[r][s] - D[i][m] / D[i][s]) < -EPS ||
40                    (d < EPS && ix[r + m] > ix[i + m]))
41                    r = i;
42        if (r < 0) return VD(); // 无边界
43    }
44    if (D[n + 1][m] < -EPS) return VD(); // 无解
45    VD x(m - 1);
46    for (int i = m; i < n + m; ++i)
47        if (ix[i] < m - 1) x[ix[i]] = D[i - m][m];
48    return x; // 最优值在 D[n][m]
49 }

```

1.14 杜教筛

```

1 // e = mu x 1
2 // d = 1 x 1
3 // sigma = d x 1
4 // phi = mu x id
5 // id = phi x 1
6 // id^2 = (id * phi) x id

```

```

7
8 // S = sum(f)
9 // sum(fxg) = sum(g(i)S(n/i))
10 map<int, int> mp_mu;
11
12 int S_mu(int n) {
13     if (n < MAXN) return sum_mu[n];
14     if (mp_mu[n]) return mp_mu[n];
15     int ret = 1;
16     for (int i = 2, j; i <= n; i = j + 1) {
17         j = n / (n / i);
18         ret -= S_mu(n / i) * (j - i + 1);
19     }
20     return mp_mu[n] = ret;
21 }
22
23 ll S_phi(int n) {
24     ll res = 0;
25     for (int i = 1, j; i <= n; i = j + 1) {
26         j = n / (n / i);
27         res += 1LL * (S_mu(j) - S_mu(i - 1)) * (n / i) * (n / i);
28     }
29     return (res - 1) / 2 + 1;
30 }

```

1.15 类欧几里德算法

```

1 //求 f=sum((a*i+b)/c),g=sum((a*i+b)/c*i),h=sum(((a*i+b)/c)^2), for i in [0..n],
2 //整除向下
3 #include <bits/stdc++.h>
4 #define int long long
5 using namespace std;
6 const int P = 998244353;
7 int i2 = 499122177, i6 = 166374059;
8 struct data {
9     data() { f = g = h = 0; }
10    int f, g, h;
11 }; // 三个函数打包
12 data calc(int n, int a, int b, int c) {
13     int ac = a / c, bc = b / c, m = (a * n + b) / c, n1 = n + 1, n21 = n * 2 + 1;
14     data d;
15     if (a == 0) { // 迭代到最底层
16         d.f = bc * n1 % P;
17         d.g = bc * n % P * n1 % P * i2 % P;
18         d.h = bc * bc % P * n1 % P;
19         return d;
20     }
21     if (a >= c || b >= c) { // 取模
22         d.f = n * n1 % P * i2 % P * ac % P + bc * n1 % P;
23         d.g = ac * n % P * n1 % P * n21 % P * i6 % P + bc * n % P * n1 % P * i2 % P;
24         d.h = ac * ac % P * n % P * n1 % P * n21 % P * i6 % P +
25             bc * bc % P * n1 % P + ac * bc % P * n % P * n1 % P;
26         d.f %= P, d.g %= P, d.h %= P;
27
28         data e = calc(n, a % c, b % c, c); // 迭代
29
30         d.h += e.h + 2 * bc % P * e.f % P + 2 * ac % P * e.g % P;
31         d.g += e.g, d.f += e.f;

```

```

32     d.f %= P, d.g %= P, d.h %= P;
33     return d;
34 }
35 data e = calc(m - 1, c, c - b - 1, a);
36 d.f = n * m % P - e.f, d.f = (d.f % P + P) % P;
37 d.g = m * n % P * n1 % P - e.h - e.f, d.g = (d.g * i2 % P + P) % P;
38 d.h = n * m % P * (m + 1) % P - 2 * e.g - 2 * e.f - d.f;
39 d.h = (d.h % P + P) % P;
40 return d;
41 }
42
43 int T, n, a, b, c;
44 signed main() {
45     scanf("%lld", &T);
46     while (T--) {
47         scanf("%lld%lld%lld%lld", &n, &a, &b, &c);
48         data ans = calc(n, a, b, c);
49         printf("%lld %lld %lld\n", ans.f, ans.h, ans.g);
50     }
51     return 0;
52 }

```

1.16 线性规划

```

1  /*
2   * 给定 n 个约束条件, m 个未知数, 求 sum(a[0][i] * x[i]) 的最大值
3   * 约束条件: sum(-a[i][j] * x[j]) <= a[i][0]
4   * 若要求最小值, 则进行对偶: 即把目标函数的系数和约束条件右边的数交换, 然后把矩阵转置
5   */
6  const int MAXN = 3e3 + 3, MAXM = 3e3 + 3, INF = ~0U >> 2;
7  int n, m, a[MAXN][MAXM], nxt[MAXM];
8  void pivot(int l, int e) {
9      a[l][e] = -1;
10     int t = MAXM - 1;
11     for (int i = 0; i <= m; ++i)
12         if (a[l][i]) nxt[t] = i, t = i;
13     nxt[t] = -1;
14     for (int i = 0; i <= n; ++i)
15         if (i != l && (t = a[i][e])) {
16             a[i][e] = 0;
17             for (int j = nxt[MAXM - 1]; ~j; j = nxt[j]) a[i][j] += a[l][j] * t;
18         }
19 }
20 int simplex() {
21     for (;;) {
22         int mi = INF, l = 0, e = 0;
23         for (int i = 1; i <= m; ++i)
24             if (a[0][i] > 0) {
25                 e = i;
26                 break;
27             }
28         if (!e) return a[0][0];
29         for (int i = 1; i <= n; ++i)
30             if (a[i][e] < 0 && a[i][0] < mi) mi = a[i][0], l = i;
31         pivot(l, e);
32     }
33 }

```


1.17 线性规划例题 (CCPC Final 2017 F)

```

1 // 有N组人, 每组人有ai个, 可以进行若干次选择, 每次选择一些至少有M个人的组, 这些组的人都中奖。
2 // 现在要使每个人中奖概率相等, 且中奖概率最大。N <= 10, M, ai <= 100
3
4 // 写法一
5 #include <bits/stdc++.h>
6 using namespace std;
7
8 const int MAXN = int(3e3);
9 const int MAXM = int(3e3);
10 const double INF = 1e20, EPS = 1e-9;
11
12 int n, m;
13 double a[MAXM][MAXN], v;
14
15 void pivot(int l, int e) {
16     int i, j;
17     a[l][e] = 1 / a[l][e];
18     for (j = 0; j <= n; ++j)
19         if (j != e) a[l][j] *= a[l][e];
20     for (i = 1; i <= m; ++i)
21         if (i != l && fabs(a[i][e]) > EPS) {
22             for (j = 0; j <= n; ++j)
23                 if (j != e) a[i][j] -= a[i][e] * a[l][j];
24             a[i][e] = -a[i][e] * a[l][e];
25         }
26     v += a[0][e] * a[l][0];
27     for (j = 1; j <= n; ++j)
28         if (j != e) a[0][j] -= a[0][e] * a[l][j];
29     a[0][e] = -a[0][e] * a[l][e];
30 }
31
32 double simplex() {
33     int e, l, i;
34     double mn;
35     v = 0;
36     while (true) {
37         for (e = 1; e <= n; ++e)
38             if (a[0][e] > EPS) break;
39         if (e > n) return v;
40         for (i = 1, mn = INF; i <= m; ++i)
41             if (a[i][e] > EPS && mn > a[i][0] / a[i][e])
42                 mn = a[i][0] / a[i][e], l = i;
43         if (mn == INF) return INF;
44         pivot(l, e);
45     }
46 }
47
48 void solve() {
49     static int n, m, g[10];
50     static vector<int> con[10], able;
51
52     scanf("%d %d", &n, &m);
53     for (int i = 0; i < n; ++i) {
54         scanf("%d", g + i);
55         con[i].clear();
56     }
57

```

```

58     if (n == 1) {
59         printf("%.10f\n", m >= g[0] ? 1. : 0.);
60         return;
61     }
62
63     able.clear();
64     for (int s = 0, S = 1 << n; s < S; ++s) {
65         int sum = 0;
66         for (int i = 0; i < n; ++i)
67             if (s >> i & 1) sum += g[i];
68         if (sum > m) continue;
69         able.push_back(s);
70         for (int i = 0; i < n; ++i)
71             if (s >> i & 1) con[i].push_back(able.size());
72     }
73     ::n = able.size();
74     ::m = 0;
75     static random_device rd;
76     mt19937 gen(rd());
77     shuffle(able.begin(), able.end(), gen);
78     for (int step = 0; step < n; ++step) {
79         int f = ++::m;
80         for (int i = 0; i <= ::n; ++i) a[f][i] = 0;
81         for (int x : con[step]) ++a[f][x];
82         if (step + 1 < n) {
83             for (int x : con[step + 1]) --a[f][x];
84         } else {
85             for (int x : con[0]) --a[f][x];
86         }
87     }
88
89     ++::m;
90     a[::m][0] = 1;
91     for (int i = 1; i <= ::n; ++i) a[::m][i] = 1;
92
93     ++::m;
94     a[::m][0] = -1;
95     for (int i = 1; i <= ::n; ++i) a[::m][i] = -1;
96
97     for (int i = 0; i <= ::n; ++i) a[0][i] = 0;
98     for (int x : con[0]) ++a[0][x];
99     printf("%.10f\n", simplex());
100 }
101
102 int main() {
103     int o_o, case_number = 1;
104     for (scanf("%d", &o_o); case_number <= o_o; ++case_number) {
105         printf("Case #%d: ", case_number);
106         solve();
107     }
108     return 0;
109 }
110
111 // 写法二
112 #include <bits/stdc++.h>
113 using namespace std;
114
115 typedef long double db;
116 const int MAXN = 3000;

```

```

117 const int MAXM = 3000;
118 const db EPS = 1e-9;
119 const db INF = 1e200;
120
121 namespace LP {
122 db a[MAXM][MAXN];
123 int idA[MAXN], idB[MAXN];
124 int m, n;
125
126 void put_out(int x) {
127     if (x == 0)
128         printf("Infeasible\n");
129     else
130         printf("Unbounded\n");
131     exit(0);
132 }
133 void pivot(int xA, int xB) {
134     swap(idA[xA], idB[xB]);
135     static int next[MAXN];
136     int i, j, last = MAXN - 1;
137     db tmp = -a[xB][xA];
138     a[xB][xA] = -1.0;
139     for (j = 0; j <= n; j++)
140         if (fabs(a[xB][j]) > EPS) a[xB][last = next[last] = j] /= tmp;
141     next[last] = -1;
142
143     for (i = 0; i <= m; i++)
144         if (i != xB && fabs(tmp = a[i][xA]) > EPS)
145             for (a[i][xA] = 0.0, j = next[MAXN - 1]; ~j; j = next[j])
146                 a[i][j] += tmp * a[xB][j];
147 }
148 db calc() {
149     int xA, xB;
150     db Max, tmp;
151     while (1) {
152         xA = n + 1, idA[xA] = n + m + 1;
153         for (int i = 1; i <= n; i++)
154             if (a[0][i] > EPS && idA[i] < idA[xA]) xA = i;
155
156         if (xA == n + 1) return a[0][0];
157         xB = m + 1, idB[xB] = n + m + 1, Max = -INF;
158         for (int i = 1; i <= m; i++)
159             if (a[i][xA] < -EPS && ((tmp = a[i][0] / a[i][xA]) > Max + EPS ||
160                 (tmp > Max - EPS && idB[i] < idB[xB])))
161                 Max = tmp, xB = i;
162
163         if (xB == m + 1) put_out(1);
164
165         pivot(xA, xB);
166     }
167     return a[0][0];
168 }
169 db solve() {
170     for (int i = 1; i <= n; i++) idA[i] = i;
171     for (int i = 1; i <= m; i++) idB[i] = n + i;
172     static db tmp[MAXN];
173     db Min = 0.0;
174     int l;
175     for (int i = 1; i <= m; i++)

```

```

176     if (a[i][0] < Min) Min = a[i][0], l = i;
177     if (Min > -EPS) return calc();
178
179     idA[+n] = 0;
180     for (int i = 1; i <= m; i++) a[i][n] = 1.0;
181     for (int i = 0; i <= n; i++) tmp[i] = a[0][i], a[0][i] = 0.0;
182     a[0][n] = -1.0;
183
184     pivot(n, l);
185
186     if (calc() < -EPS) put_out(0);
187     for (int i = 1; i <= m; i++)
188         if (!idB[i]) {
189             for (int j = 1; j <= n; j++)
190                 if (fabs(a[0][j]) > EPS) {
191                     pivot(j, i);
192                     break;
193                 }
194             break;
195         }
196
197     int xA;
198     for (xA = 1; xA <= n; xA++)
199         if (!idA[xA]) break;
200     for (int i = 0; i <= m; i++) a[i][xA] = a[i][n];
201     idA[xA] = idA[n], n--;
202
203     for (int i = 0; i <= n; i++) a[0][i] = 0.0;
204     for (int i = 1; i <= m; i++)
205         if (idB[i] <= n) {
206             for (int j = 0; j <= n; j++) a[0][j] += a[i][j] * tmp[idB[i]];
207         }
208
209     for (int i = 1; i <= n; i++)
210         if (idA[i] <= n) a[0][i] += tmp[idA[i]];
211     return calc();
212 }
213 db ans[MAXN];
214 void findAns() {
215     for (int i = 1; i <= n; i++) ans[i] = 0.0;
216     for (int i = 1; i <= m; i++)
217         if (idB[i] <= n) ans[idB[i]] = a[i][0];
218 }
219 void work() {
220     for (int i = 1; i <= m; ++i)
221         for (int j = 1; j <= n; ++j) a[i][j] *= -1;
222     printf("%.10f\n", -double(solve()));
223 }
224 } // namespace LP
225
226 void solve() {
227     static int n, m, g[10];
228     static vector<int> con[10], able;
229
230     scanf("%d %d", &n, &m);
231     for (int i = 0; i < n; ++i) {
232         scanf("%d", g + i);
233         con[i].clear();
234     }

```

```

235
236 if (n == 1) {
237     printf("%.10f\n", m >= g[0] ? 1.0 : 0.0);
238     return;
239 }
240
241 able.clear();
242 for (int s = 0; s < (1 << n); ++s) {
243     int sum = 0;
244     for (int i = 0; i < n; ++i)
245         if (s >> i & 1) sum += g[i];
246     if (sum > m) continue;
247
248     able.push_back(s);
249     for (int i = 0; i < n; ++i)
250         if (s >> i & 1) con[i].push_back(able.size());
251 }
252
253 LP::n = able.size();
254 LP::m = 0;
255
256 for (int step = 0; step < n; ++step) {
257     int &f = ++LP::m;
258     for (int i = 0; i <= LP::n; ++i) LP::a[f][i] = 0;
259     for (int x : con[step]) ++LP::a[f][x];
260     if (step + 1 < n) {
261         for (int x : con[step + 1]) --LP::a[f][x];
262     } else {
263         for (int x : con[0]) --LP::a[f][x];
264     }
265 }
266
267 ++LP::m;
268 LP::a[LP::m][0] = 1;
269 for (int i = 1; i <= LP::n; ++i) LP::a[LP::m][i] = 1;
270
271 ++LP::m;
272 LP::a[LP::m][0] = -1;
273 for (int i = 1; i <= LP::n; ++i) LP::a[LP::m][i] = -1;
274
275 for (int i = 0; i <= LP::n; ++i) LP::a[0][i] = 0;
276 for (int x : con[0]) ++LP::a[0][x];
277
278 static db a2[MAXM][MAXN];
279 for (int i = 1; i <= LP::m; ++i)
280     for (int j = 1; j <= LP::n; ++j) a2[i][j] = LP::a[i][j];
281 for (int i = 1; i <= LP::m; ++i)
282     for (int j = 1; j <= LP::n; ++j) LP::a[j][i] = a2[i][j];
283 swap(LP::n, LP::m);
284 for (int i = 1; i <= max(LP::n, LP::m); ++i) swap(LP::a[0][i], LP::a[i][0]);
285 LP::a[0][0] = 0;
286 for (int i = 1; i <= LP::m; ++i)
287     for (int j = 1; j <= LP::n; ++j) LP::a[i][j] *= -1;
288 for (int i = 1; i <= LP::m; ++i) LP::a[i][0] *= -1;
289 for (int i = 1; i <= LP::n; ++i) LP::a[0][i] *= -1;
290
291 LP::work();
292 }
293

```

```

294 int main() {
295     int o_o;
296     scanf("%d", &o_o);
297     for (int i = 1; i <= o_o; ++i) {
298         printf("Case #%d: ", i);
299         solve();
300     }
301     return 0;
302 }

```

1.18 线性规划例题 (UOJ 板题代码)

```

1  #include <bits/stdc++.h>
2  using namespace std;
3
4  #ifdef __WIN32
5  #define LLFORMAT "I64"
6  #else
7  #define LLFORMAT "ll"
8  #endif
9
10 #define eps 1e-7
11
12 int simplex(vector<vector<double>> &a, vector<double> &b, vector<double> &c,
13             vector<int> &basic) {
14     int m = b.size(), n = c.size();
15     while (true) {
16         int k = -1;
17         for (int j = 0; j < n; ++j)
18             if (c[j] < -eps) {
19                 k = j;
20                 break;
21             }
22         if (k == -1) {
23             double ans = 0;
24             for (int i = 0; i < m; ++i) ans += c[basic[i]] * b[i];
25             return 0;
26         }
27         int l = -1;
28         for (int i = 0; i < m; ++i)
29             if (a[i][k] > eps) {
30                 if (l == -1)
31                     l = i;
32                 else {
33                     double ti = b[i] / a[i][k], t1 = b[l] / a[l][k];
34                     if (ti < t1 - eps || (ti < t1 + eps && basic[i] < basic[l])) l = i;
35                 }
36             }
37         if (l == -1) return -1;
38         basic[l] = k;
39         double tmp = 1 / a[l][k];
40         for (int j = 0; j < n; ++j) a[l][j] *= tmp;
41         b[l] *= tmp;
42         for (int i = 0; i < m; ++i)
43             if (i != l) {
44                 tmp = a[i][k];
45                 for (int j = 0; j < n; ++j) a[i][j] -= tmp * a[l][j];
46                 b[i] -= tmp * b[l];

```

```

47     }
48     tmp = c[k];
49     for (int j = 0; j < n; ++j) c[j] -= tmp * a[l][j];
50 }
51 }
52
53 int main() {
54     ios::sync_with_stdio(false);
55     int n, m, T;
56     cin >> n >> m >> T;
57     vector<double> c(n + m, 0);
58     for (int i = 0; i < n; ++i) {
59         cin >> c[i];
60         c[i] *= -1;
61     }
62     auto C = c;
63     vector<vector<double>>> a(m, vector<double>(n + m, 0));
64     vector<double> b(m);
65     vector<int> basic(m, -1), tmp;
66     for (int i = 0; i < m; ++i) {
67         for (int j = 0; j < n; ++j) cin >> a[i][j];
68         a[i][i + n] = 1;
69         cin >> b[i];
70         if (b[i] > -eps)
71             basic[i] = i + n;
72         else
73             tmp.push_back(i);
74     }
75     if (!tmp.empty()) {
76         sort(tmp.begin(), tmp.end(), [&](int i, int j) { return b[i] > b[j]; });
77         vector<vector<double>>> A;
78         vector<double> B, C(n + m + 1, 0);
79         vector<int> Basic;
80         for (int i : tmp) {
81             vector<double> foo;
82             for (int j = 0; j < n + m; ++j) foo.push_back(-a[i][j]);
83             foo.push_back(1);
84             double bar = -b[i];
85             for (int i = 0; i < A.size(); ++i) {
86                 double tmp = foo[Basic[i]];
87                 for (int j = 0; j <= n + m; ++j) foo[j] -= tmp * A[i][j];
88                 bar -= tmp * B[i];
89             }
90             for (int j = n + m; j >= 0; --j)
91                 if (-eps < foo[j] - 1 && foo[j] - 1 < eps) {
92                     Basic.push_back(j);
93                     break;
94                 }
95             for (int i = 0; i < A.size(); ++i) {
96                 double tmp = A[i][Basic.back()];
97                 for (int j = 0; j <= n + m; ++j) A[i][j] -= tmp * foo[j];
98                 B[i] -= tmp * bar;
99             }
100             A.push_back(foo);
101             B.push_back(bar);
102         }
103         for (int i = 0; i < A.size(); ++i)
104             if (Basic[i] == n + m) {
105                 for (int j = 0; j < n + m; ++j) C[j] = -A[i][j];

```

```

106     }
107     for (int i = 0; i < m; ++i)
108         if (b[i] > -eps) {
109             A.push_back(a[i]);
110             A[A.size() - 1].push_back(0);
111             B.push_back(b[i]);
112             Basic.push_back(basic[i]);
113         }
114     simplex(A, B, C, Basic);
115     bool flag = true;
116     for (int i = 0; i < m; ++i)
117         if (Basic[i] == n + m) {
118             if (B[i] > eps) {
119                 cout << "Infeasible\n";
120                 return 0;
121             }
122             int k = -1;
123             for (int j = 0; j < n + m; ++j)
124                 if (A[i][j] > eps || A[i][j] < -eps) {
125                     k = j;
126                     break;
127                 }
128             if (k != -1) {
129                 double tmp = 1 / A[i][k];
130                 Basic[i] = k;
131                 for (int j = 0; j <= n + m; ++j) A[i][j] *= tmp;
132                 B[i] *= tmp;
133                 for (int l = 0; l < m; ++l)
134                     if (l != i) {
135                         tmp = A[l][k];
136                         for (int j = 0; j <= n + m; ++j) A[l][j] -= tmp * A[i][j];
137                         B[l] -= tmp * B[i];
138                     }
139             } else
140                 flag = false;
141             break;
142         }
143     if (flag) {
144         A.push_back(vector<double>(n + m, 0));
145         A[A.size() - 1].push_back(1);
146         B.push_back(0);
147         Basic.push_back(n + m);
148         for (int i = 0; i < A.size() - 1; ++i) {
149             double tmp = A[i].back();
150             for (int j = 0; j <= n + m; ++j) A[i][j] -= tmp * A[A.size() - 1][j];
151             B[i] -= tmp * B.back();
152         }
153     }
154     a = A;
155     b = B;
156     basic = Basic;
157     c.push_back(0);
158     for (int i = 0; i < a.size(); ++i) {
159         double tmp = c[basic[i]];
160         for (int j = 0; j <= n + m; ++j) c[j] -= tmp * a[i][j];
161     }
162 }
163 auto foo = simplex(a, b, c, basic);
164 if (foo == -1)

```



```

165     cout << "Unbounded" << endl;
166     else {
167         double res = 0;
168         vector<double> ans(n, 0);
169         for (int i = 0; i < basic.size(); ++i)
170             if (basic[i] < n) ans[basic[i]] = b[i];
171         for (int j = 0; j < n; ++j) res -= C[j] * ans[j];
172         cout << setprecision(8) << res << endl;
173         if (T == 1) {
174             for (int i = 0; i < n; ++i) cout << setprecision(8) << ans[i] << ' ';
175             cout << endl;
176         }
177     }
178     return 0;
179 }

```

1.19 自适应 Simpson

```

1  // 计算  $\int_a^b f(x) dx$ 
2  double simpson(double a, double b) {
3      double c = a + (b - a) / 2;
4      return (f(a) + 4 * f(c) + f(b)) * (b - a) / 6;
5  }
6  double integral(double a, double b, double eps, double A) {
7      double c = a + (b - a) / 2;
8      double L = simpson(a, c), R = simpson(c, b);
9      if (fabs(L + R - A) <= 15 * eps) return L + R + (L + R - A) / 15;
10     return integral(a, c, eps / 2, L) + integral(c, b, eps / 2, R);
11 }
12 double integral(double a, double b, double eps) {
13     return integral(a, b, eps, simpson(a, b));
14 }

```

2 Dynamic Programming

2.1 斜率优化

```

1  // 树上斜率优化
2  // 定义dpi表示i节点传递到根节点的最短耗时,规定dproot=-P。
3  // 有如下转移方程 $dpu = dpv + dist(u, v)^2 + P$ , v is an ancestor of u.
4
5  #include <bits/stdc++.h>
6  using namespace std;
7
8  typedef long long ll;
9  typedef pair<int, int> pii;
10 const int MAXN = 1e5 + 5;
11
12 vector<pii> adj[MAXN];
13 ll dp[MAXN], d[MAXN];
14 int n, p, q[MAXN], head, tail;
15
16 inline ll S(int a, int b) { return (d[b] - d[a]) < 1; }
17 inline ll G(int a, int b) { return dp[b] - dp[a] + d[b] * d[b] - d[a] * d[a]; }
18
19 void dfs(int u, int from) {

```

```

20  vector<int> dhead, dtail;
21  if (u ^ 1) {
22      while (head + 2 <= tail &&
23             S(q[head + 1], q[head]) * d[u] <= G(q[head + 1], q[head]))
24          dhead.push_back(q[head++]);
25      int v = q[head];
26      dp[u] = dp[v] + p + (d[u] - d[v]) * (d[u] - d[v]);
27  }
28  while (head + 2 <= tail &&
29         G(u, q[tail - 1]) * S(q[tail - 1], q[tail - 2]) <=
30         G(q[tail - 1], q[tail - 2]) * S(u, q[tail - 1]))
31      dtail.push_back(q[--tail]);
32  q[tail++] = u;
33  for (pii &e : adj[u]) {
34      if (e.first == from) continue;
35      d[e.first] = d[u] + e.second;
36      dfs(e.first, u);
37  }
38  --tail;
39  for (int i = dtail.size() - 1; ~i; --i) q[tail++] = dtail[i];
40  for (int i = dhead.size() - 1; ~i; --i) q[--head] = dhead[i];
41 }
42
43 void solve() {
44     cin >> n >> p;
45     for (int i = 1; i <= n; ++i) adj[i].clear();
46     for (int i = 1, u, v, w; i < n; ++i) {
47         cin >> u >> v >> w;
48         adj[u].emplace_back(v, w);
49         adj[v].emplace_back(u, w);
50     }
51     dp[1] = -p;
52     head = tail = 0;
53     dfs(1, 1);
54
55     ll ans = 0;
56     for (int i = 1; i <= n; ++i)
57         if (dp[i] > ans) ans = dp[i];
58     cout << ans << '\n';
59 }
60
61 int main() {
62     // freopen("in.txt", "r", stdin);
63     ios::sync_with_stdio(false);
64     cin.tie(0);
65
66     int o_o;
67     for (cin >> o_o; o_o; --o_o) solve();
68
69     return 0;
70 }

```

3 Data Structure

3.1 KD-tree

```

1 // 寻找近点

```

```

2  #include <bits/stdc++.h>
3  using namespace std;
4
5  const int MAXN = 2e5 + 5;
6  typedef long long ll;
7
8  namespace KD_Tree {
9
10 const int DIM = 2;
11
12 inline ll sqr(int x) { return 1LL * x * x; }
13
14 struct Point {
15     int x[DIM], id, c;
16
17     ll dist2(const Point &b) const {
18         return sqr(x[0] - b.x[0]) + sqr(x[1] - b.x[1]);
19     }
20 };
21 struct QNode {
22     Point p;
23     ll dis2;
24
25     QNode() {}
26     QNode(Point _p, ll _dis2) : p(_p), dis2(_dis2) {}
27
28     bool operator<(const QNode &b) const {
29         return dis2 < b.dis2 || (dis2 == b.dis2 && p.id < b.p.id);
30     }
31 } ans;
32 struct cmpx {
33     int div;
34     cmpx(int _div) : div(_div) {}
35     bool operator()(const Point &a, const Point &b) {
36         for (int i = 0; i < DIM; ++i)
37             if (a.x[(i + div) % DIM] != b.x[(i + div) % DIM])
38                 return a.x[(i + div) % DIM] < b.x[(i + div) % DIM];
39         return true;
40     }
41 };
42
43 bool cmp(const Point &a, const Point &b, int div) {
44     cmpx cp = cmpx(div);
45     return cp(a, b);
46 }
47
48 struct Node {
49     Point e;
50     Node *lc, *rc;
51     int div;
52 } node_pool[MAXN], *tail, *root;
53 void init() { tail = node_pool; }
54 Node *build(Point *a, int l, int r, int div) {
55     if (l >= r) return nullptr;
56     Node *p = tail++;
57     p->div = div;
58     int mid = (l + r) >> 1;
59     nth_element(a + l, a + mid, a + r, cmpx(div));
60     p->e = a[mid];

```

```

61     p->lc = build(a, l, mid, div ^ 1);
62     p->rc = build(a, mid + 1, r, div ^ 1);
63     return p;
64 }
65 void search(Point p, Node *x, int div) {
66     if (!x) return;
67     if (cmp(p, x->e, div)) {
68         search(p, x->lc, div ^ 1);
69         if (ans.dis2 == -1) {
70             if (x->e.c <= p.c) ans = QNode(x->e, p.dist2(x->e));
71             search(p, x->rc, div ^ 1);
72         } else {
73             QNode temp(x->e, p.dist2(x->e));
74             if (x->e.c <= p.c && temp < ans) ans = temp;
75             if (sqr(x->e.x[div] - p.x[div]) <= ans.dis2) search(p, x->rc, div ^ 1);
76         }
77     } else {
78         search(p, x->rc, div ^ 1);
79         if (ans.dis2 == -1) {
80             if (x->e.c <= p.c) ans = QNode(x->e, p.dist2(x->e));
81             search(p, x->lc, div ^ 1);
82         } else {
83             QNode temp(x->e, p.dist2(x->e));
84             if (x->e.c <= p.c && temp < ans) ans = temp;
85             if (sqr(x->e.x[div] - p.x[div]) <= ans.dis2) search(p, x->lc, div ^ 1);
86         }
87     }
88 }
89 void search(Point p) {
90     ans.dis2 = -1;
91     search(p, root, 0);
92 }
93 } // namespace KD_Tree
94
95 void solve() {
96     static KD_Tree::Point p[MAXN];
97     int n, m;
98     cin >> n >> m;
99     for (int i = 0; i < n; ++i) {
100         p[i].id = i;
101         cin >> p[i].x[0] >> p[i].x[1] >> p[i].c;
102     }
103     KD_Tree::init();
104     KD_Tree::root = KD_Tree::build(p, 0, n, 0);
105
106     for (KD_Tree::Point q; m; --m) {
107         cin >> q.x[0] >> q.x[1] >> q.c;
108         KD_Tree::search(q);
109         cout << KD_Tree::ans.p.x[0] << ' ' << KD_Tree::ans.p.x[1] << ' '
110             << KD_Tree::ans.p.c << '\n';
111     }
112 }
113 int main() {
114     ios::sync_with_stdio(false);
115     cin.tie(nullptr);
116
117     int o_o;
118     for (cin >> o_o; o_o; --o_o) solve();
119 }

```

```

120     return 0;
121 }
122
123 // 寻找远点
124 inline void cmin(int &a, int b) { b < a ? a = b : 1; }
125 inline void cmax(int &a, int b) { a < b ? a = b : 1; }
126 inline int ibs(int a) { return a < 0 ? -a : a; }
127 struct D {
128     int d[2], mx0, mx1, mi0, mi1;
129     D *l, *r;
130 } t[N], *rt;
131 int cpd, ans;
132 inline bool cmp(const D &a, const D &b) {
133     return (a.d[cpd] ^ b.d[cpd]) ? a.d[cpd] < b.d[cpd]
134         : a.d[cpd ^ 1] < b.d[cpd ^ 1];
135 }
136 inline void kd_upd(D *u) {
137     if (u->l) {
138         cmax(u->mx0, u->l->mx0);
139         cmax(u->mx1, u->l->mx1);
140         cmin(u->mi0, u->l->mi0);
141         cmin(u->mi1, u->l->mi1);
142     }
143     if (u->r) {
144         cmax(u->mx0, u->r->mx0);
145         cmax(u->mx1, u->r->mx1);
146         cmin(u->mi0, u->r->mi0);
147         cmin(u->mi1, u->r->mi1);
148     }
149 }
150 D *kd_bld(int l, int r, int d) {
151     int m = l + r >> 1;
152     cpd = d;
153     std::nth_element(t + l + 1, t + m + 1, t + r + 1, cmp);
154     t[m].mx0 = t[m].mi0 = t[m].d[0];
155     t[m].mx1 = t[m].mi1 = t[m].d[1];
156     if (l ^ m) t[m].l = kd_bld(l, m - 1, d ^ 1);
157     if (r ^ m) t[m].r = kd_bld(m + 1, r, d ^ 1);
158     kd_upd(t + m);
159     return t + m;
160 }
161 inline void kd_ins(D *ne) {
162     int cd = 0;
163     D *u = rt;
164     while (true) {
165         cmax(u->mx0, ne->mx0), cmin(u->mi0, ne->mi0);
166         cmax(u->mx1, ne->mx1), cmin(u->mi1, ne->mi1);
167         if (ne->d[cd] < u->d[cd]) {
168             if (u->l)
169                 u = u->l;
170             else {
171                 u->l = ne;
172                 return;
173             }
174         } else {
175             if (u->r)
176                 u = u->r;
177             else {
178                 u->r = ne;

```

```

179         return;
180     }
181 }
182     cd ^= 1;
183 }
184 }
185 inline int dist(int x, int y, D *u) {
186     int r = 0;
187     if (x < u->mi0)
188         r = u->mi0 - x;
189     else if (x > u->mx0)
190         r = x - u->mx0;
191     if (y < u->mi1)
192         r += u->mi1 - y;
193     else if (y > u->mx1)
194         r += y - u->mx1;
195     return r;
196 }
197 inline void kd_quy(D *u, const int &x, const int &y) {
198     int dl, dr, d0;
199     d0 = ibs(u->d[0] - x) + ibs(u->d[1] - y);
200     if (d0 < ans) ans = d0;
201     dl = u->l ? dist(x, y, u->l) : inf;
202     dr = u->r ? dist(x, y, u->r) : inf;
203     if (dl < dr) {
204         if (dl < ans) kd_quy(u->l, x, y);
205         if (dr < ans) kd_quy(u->r, x, y);
206     } else {
207         if (dr < ans) kd_quy(u->r, x, y);
208         if (dl < ans) kd_quy(u->l, x, y);
209     }
210 }

```

3.2 LCT

```

1 struct LCT {
2     struct node {
3         int val, add;
4         node *fa, *ch[2];
5         void modify(const int &x) {
6             val += x;
7             add += x;
8         }
9     } node_mset[MaxS], *cnode, *null;
10    LCT() {
11        cnode = node_mset;
12        null = cnode++;
13        *null = (node){0, 0, null, {null, null}};
14    }
15    inline node *newnode() {
16        *cnode = (node){0, 0, null, {null, null}};
17        return cnode++;
18    }
19    inline bool isrt(node *u) const {
20        return (u->fa->ch[0] != u) && (u->fa->ch[1] != u);
21    }
22    inline bool which(node *u) const { return u->fa->ch[1] == u; }
23    void push_down(node *u) {

```

```

24     if (!isrt(u)) push_down(u->fa);
25     if (u->add) {
26         u->ch[0]->modify(u->add);
27         u->ch[1]->modify(u->add);
28         u->add = 0;
29     }
30 }
31 inline void rotate(node *u) {
32     node *f = u->fa;
33     int d = which(u);
34     f->ch[d] = u->ch[d ^ 1];
35     f->ch[d]->fa = f;
36     u->ch[d ^ 1] = f;
37     u->fa = f->fa;
38     if (!isrt(f)) f->fa->ch[which(f)] = u;
39     f->fa = u;
40 }
41 inline void splay(node *u) {
42     push_down(u);
43     for (node *f; !isrt(u); rotate(u))
44         if (!isrt(f = u->fa)) rotate(which(u) == which(f) ? f : u);
45 }
46 inline void access(node *x) {
47     for (node *y = null; x != null; x = x->fa) {
48         splay(x);
49         x->ch[1] = y;
50         y = x;
51     }
52 }
53 inline void cut(node *u) {
54     access(u);
55     splay(u);
56     u->ch[0]->fa = null;
57     u->ch[0] = null;
58 }
59 inline void link(node *u, node *v) {
60     cut(u);
61     u->fa = v;
62 }
63 } tree;

```

3.3 Splay

```

1  #include <algorithm>
2  #include <cstdio>
3  #include <cstring>
4  #include <iostream>
5  using namespace std;
6
7  const int MAXN = 2e5 + 10;
8
9  struct Node {
10     long long sum;
11     int id, val, lazy, size;
12     Node *fa, *ch[2];
13 } node_pool[MAXN], *pool_it, *root, *nil;
14
15 Node *newnode(int id, int val) {

```

```

16  pool_it->id = id;
17  pool_it->lazy = 0;
18  pool_it->size = 1;
19  pool_it->sum = pool_it->val = val;
20  pool_it->fa = pool_it->ch[0] = pool_it->ch[1] = nil;
21  return pool_it++;
22 }
23
24 void maintain(Node *u) {
25     if (u == nil) { return; }
26     u->size = u->ch[0]->size + u->ch[1]->size + 1;
27     u->sum = u->ch[0]->sum + u->ch[1]->sum + u->val;
28 }
29
30 void push_down(Node *u) {
31     if (u->lazy) {
32         if (u->ch[0] != nil) {
33             u->ch[0]->val += u->lazy;
34             u->ch[0]->sum += 1LL * u->ch[0]->size * u->lazy;
35             u->ch[0]->lazy += u->lazy;
36         }
37         if (u->ch[1] != nil) {
38             u->ch[1]->val += u->lazy;
39             u->ch[1]->sum += 1LL * u->ch[1]->size * u->lazy;
40             u->ch[1]->lazy += u->lazy;
41         }
42         u->lazy = 0;
43     }
44 }
45
46 inline void rot(Node *u) {
47     Node *f = u->fa, *ff = f->fa;
48     int d = u == f->ch[1];
49     push_down(f);
50     push_down(u);
51     if ((f->ch[d] = u->ch[d ^ 1]) != nil) f->ch[d]->fa = f;
52     if ((u->fa = ff) != nil) ff->ch[f == ff->ch[1]] = u;
53     f->fa = u;
54     u->ch[d ^ 1] = f;
55     maintain(f);
56     maintain(u);
57 }
58
59 void splay(Node *u, Node *target) {
60     for (Node *f; u->fa != target; rot(u))
61         if ((f = u->fa)->fa != target) {
62             ((u == f->ch[1]) ^ (f == f->fa->ch[1])) ? rot(u) : rot(f);
63         }
64     if (target == nil) root = u;
65 }
66
67 inline void insert(int id, int val) {
68     if (root == nil) {
69         root = newnode(id, val);
70         return;
71     }
72     Node *u = root;
73     while (u != nil) {
74         int d = id >= u->id;

```



```

75     ++u->size;
76     push_down(u);
77     u->sum += val;
78     if (u->ch[d] != nil) {
79         u = u->ch[d];
80     } else {
81         u->ch[d] = newnode(id, val);
82         u->ch[d]->fa = u;
83         u = u->ch[d];
84         break;
85     }
86 }
87 splay(u, nil);
88 }
89
90 inline Node *find_pred(int id) {
91     Node *u = root, *ret = nil;
92     while (u != nil) {
93         push_down(u);
94         if (u->id < id) {
95             ret = u;
96             u = u->ch[1];
97         } else {
98             u = u->ch[0];
99         }
100     }
101     return ret;
102 }
103
104 inline Node *find_succ(int id) {
105     Node *u = root, *ret = nil;
106     while (u != nil) {
107         push_down(u);
108         if (u->id > id) {
109             ret = u;
110             u = u->ch[0];
111         } else {
112             u = u->ch[1];
113         }
114     }
115     return ret;
116 }
117
118 Node *find_kth(int k) {
119     Node *u = root;
120     while (u != nil) {
121         push_down(u);
122         if (u->ch[0]->size + 1 == k) {
123             splay(u, nil);
124             return u;
125         }
126         if (u->ch[0]->size >= k) {
127             u = u->ch[0];
128         } else {
129             k -= u->ch[0]->size + 1;
130             u = u->ch[1];
131         }
132     }
133     return nil;

```

```

134 }
135
136 Node *range(int l, int r) {
137     Node *pred = find_pred(l);
138     Node *succ = find_succ(r);
139
140     splay(pred, nil);
141     splay(succ, root);
142     push_down(pred);
143     push_down(succ);
144     return root->ch[1]->ch[0];
145 }
146
147 int main() {
148
149     // freopen("input.txt", "r", stdin);
150
151     ios::sync_with_stdio(false);
152     cin.tie(0);
153     cout.tie(0);
154
155     int n;
156     cin >> n;
157
158     pool_it = node_pool;
159     nil = pool_it++;
160     nil->ch[0] = nil->ch[1] = nil->fa = nil;
161     nil->id = -1;
162     nil->val = 0;
163     root = nil;
164
165     insert(-0x3fffffff, 0);
166     insert(0x3fffffff, 0);
167
168     return 0;
169 }

```

3.4 zkw

```

1  int tree[MAXN * 2], pre;
2
3  void init(int n, int *a) {
4      memset(tree, 0, sizeof(tree));
5      for (pre = 1; pre <= n; pre <= 1) {}
6      for (int i = 1; i <= n; ++i) tree[i + pre] = a[i];
7      for (int i = pre; i; --i) tree[i] = max(tree[i << 1], tree[i << 1 | 1]);
8  }
9
10 void update(int pos, const int &val) {
11     tree[pos += pre] = val;
12     for (pos >>= 1; pos; pos >>= 1)
13         tree[pos] = max(tree[pos << 1], tree[pos << 1 | 1]);
14 }
15
16 int query(int s, int t) {
17     int res = 0;
18     for (s += pre - 1, t += pre + 1; s ^ t ^ 1; s >>= 1, t >>= 1) {
19         if (~s & 1) res = max(res, tree[s ^ 1]);

```

```

20     if (t & 1) res = max(res, tree[t ^ 1]);
21 }
22 return res;
23 }

```

4 String

4.1 AC 自动机

```

1  int ch[MAX_NODE][26], fail[MAX_NODE], dep[MAX_NODE], node_c;
2
3  int add_char(int u, int id) {
4      if (ch[u][id] < 0) ch[u][id] = node_c++;
5      return ch[u][id];
6  }
7  void build_acam() {
8      queue<int> que;
9      fail[0] = 0;
10     for (int i = 0; i < 26; ++i)
11         if (~ch[0][i]) {
12             que.push(ch[0][i]);
13             fail[ch[0][i]] = 0;
14         } else {
15             ch[0][i] = 0;
16         }
17     while (!que.empty()) {
18         int u = que.front(), f = fail[u];
19         que.pop();
20         for (int i = 0; i < 26; ++i)
21             if (~ch[u][i]) {
22                 que.push(ch[u][i]);
23                 fail[ch[u][i]][i] = ch[f][i];
24             } else {
25                 ch[u][i] = ch[f][i];
26             }
27     }
28     for (int i = 1; i < node_c; ++i) adj[fail[i]].push_back(i);
29 }

```

4.2 KMP

```

1  void get_next(char *S, int *nxt, int n) {
2      nxt[0] = -1;
3      int j = -1;
4      for (int i = 1; i < n; ++i) {
5          while ((~j) && S[j + 1] != S[i]) j = nxt[j];
6          nxt[i] = (S[j + 1] == S[i]) ? (++j) : j;
7      }
8  }
9
10 int pattern(char *S, char *T, int *nxt, int n, int m) {
11     int j = -1;
12     for (int i = 0; i < m; ++i) {
13         while ((~j) && S[j + 1] != T[i]) j = nxt[j];
14         j += S[j + 1] == T[i];
15         if (j == n - 1) return i - n + 1;
16     }
17 }

```

```

16 }
17 return -1;
18 }

```

4.3 SAM

```

1 // SPOJ Lexicographical Substring Search 求字典序第 k 大子串
2 #pragma GCC optimize(2)
3 #include <bits/stdc++.h>
4 using namespace std;
5
6 const int MAXN = 90000 + 3;
7 const int ALPHABET = 26;
8
9 struct Node {
10     int len, cnt;
11     Node *link, *next[ALPHABET];
12     void init(int len = 0) {
13         link = nullptr;
14         this->len = len, cnt = 0;
15         memset(next, 0, sizeof(next));
16     }
17 };
18
19 template <int MAX_LENGTH> class SAM {
20 public:
21     Node *last, *root;
22
23     void init() {
24         pool_ptr = pool;
25         last = root = new_node(0);
26     }
27
28     void extend(int chr) {
29         Node *p = last, *np = new_node(p->len + 1);
30         for (last = np; p && !p->next[chr]; p = p->link) p->next[chr] = np;
31         if (!p) {
32             np->link = root;
33         } else {
34             Node *q = p->next[chr];
35             if (q->len == p->len + 1) {
36                 np->link = q;
37             } else {
38                 Node *nq = new_node(p->len + 1);
39                 memcpy(nq->next, q->next, sizeof(q->next));
40                 nq->link = q->link, q->link = np->link = nq;
41                 for (; p && p->next[chr] == q; p = p->link) p->next[chr] = nq;
42             }
43         }
44     }
45
46     void toposort() {
47         int size = pool_ptr - pool;
48         memset(cnt, 0, size * sizeof(int));
49         for (Node *it = pool; it < pool_ptr; ++it) ++cnt[it->len];
50         for (int i = 1; i < size; ++i) cnt[i] += cnt[i - 1];
51         for (Node *it = pool; it < pool_ptr; ++it) order[--cnt[it->len]] = it;
52         for (int i = size - 1; ~i; --i) {

```

```

53     Node *u = order[i];
54     for (int j = 0; j < ALPHABET; ++j)
55         u->cnt += u->next[j] ? u->next[j]->cnt + 1 : 0;
56     }
57 }
58
59 void find_kth(int k, char *str) {
60     char *ptr = str;
61     Node *u = root;
62     while (k) {
63         for (int j = 0; j < ALPHABET; ++j) {
64             if (!u->next[j]) continue;
65             if (u->next[j]->cnt + 1 < k) {
66                 k -= u->next[j]->cnt + 1;
67                 continue;
68             }
69             --k, *ptr++ = j + 'a';
70             u = u->next[j];
71             break;
72         }
73     }
74     *ptr = 0;
75 }
76
77 private:
78     int cnt[MAX_LENGTH * 2];
79     Node pool[MAX_LENGTH * 2], *pool_ptr, *order[MAX_LENGTH * 2];
80
81     Node *new_node(int len) {
82         pool_ptr->init(len);
83         return pool_ptr++;
84     }
85 };
86
87 SAM<MAXN> sam;
88 char str[MAXN];
89
90 int main(int argc, char *argv[]) {
91     ios::sync_with_stdio(false);
92     cin.tie(nullptr), cout.tie(nullptr);
93
94     cin >> str;
95     sam.init();
96     for (char *it = str; *it; ++it) sam.extend(*it - 'a');
97     sam.toposort();
98
99     int q, k;
100    for (cin >> q; q; --q) cin >> k, sam.find_kth(k, str), puts(str);
101
102    return 0;
103 }

```

4.4 mancher

```

1 void mancher(char *s, int n) {
2     str[0] = '~';
3     str[1] = '!';
4     for (int i = 1; i <= n; ++i) {

```

```

5     str[i * 2] = s[i];
6     str[i * 2 + 1] = '!';
7 }
8 for (int i = 1, j = 0; i <= n; ++i) {
9     if (p[j] + j > i) {
10        p[i] = min(p[2 * j - i], p[j] + j - i);
11    } else {
12        p[i] = 1;
13    }
14    while (str[i + p[i]] == str[i - p[i]]) { ++p[i]; }
15    if (i + p[i] > j + p[j]) { j = i; }
16 }
17 }

```

4.5 后缀数组 (SAIS)

```

1 // UOJ 模板题, 最快算法
2 // 字符串必须为正数, BUFFER_SIZE 要随 MAX_LENGTH 同步变化, 1e6为25
3 #include <bits/stdc++.h>
4
5 const int BUFFER_SIZE = 1u << 23 | 1;
6 char buffer[BUFFER_SIZE], *buffer_ptr = buffer;
7 #define alloc(x, type, len)
8     type *x = (type *)buffer_ptr;
9     buffer_ptr += (len) * sizeof(type);
10 #define clear_buffer()
11     memset(buffer, 0, buffer_ptr - buffer), buffer_ptr = buffer;
12
13 template <int MAX_LENGTH> class SuffixArray {
14 #define L_TYPE true
15 #define S_TYPE false
16 public:
17     int sa[MAX_LENGTH], rank[MAX_LENGTH], height[MAX_LENGTH];
18     void compute(int n, int m, int *s) {
19         sais(n, m, s, sa);
20         for (int i = 0; i < n; ++i) rank[sa[i]] = i;
21         for (int i = 0, h = 0; i < n; ++i) {
22             if (rank[i]) {
23                 int j = sa[rank[i] - 1];
24                 while (s[i + h] == s[j + h]) ++h;
25                 height[rank[i]] = h;
26             } else {
27                 h = 0;
28             }
29             if (h) --h;
30         }
31     }
32
33 private:
34     int l_bucket[MAX_LENGTH], s_bucket[MAX_LENGTH];
35
36     void induce(int n, int m, int *s, bool *type, int *sa, int *bucket,
37                 int *l_bucket, int *s_bucket) {
38         memcpy(l_bucket + 1, bucket, m * sizeof(int));
39         memcpy(s_bucket + 1, bucket + 1, m * sizeof(int));
40         sa[l_bucket[s[n - 1]]++] = n - 1;
41         for (int i = 0; i < n; ++i) {
42             int t = sa[i] - 1;

```

```

43     if (t >= 0 && type[t] == L_TYPE) sa[l_bucket[s[t]]++] = t;
44 }
45 for (int i = n - 1; i >= 0; --i) {
46     int t = sa[i] - 1;
47     if (t >= 0 && type[t] == S_TYPE) sa[--s_bucket[s[t]]] = t;
48 }
49 }
50 void sais(int n, int m, int *s, int *sa) {
51     alloc(type, bool, n + 1);
52     alloc(bucket, int, m + 1);
53     type[n] = false;
54     for (int i = n - 1; i >= 0; --i) {
55         ++bucket[s[i]];
56         type[i] = s[i] > s[i + 1] || (s[i] == s[i + 1] && type[i + 1] == L_TYPE);
57     }
58     for (int i = 1; i <= m; ++i) {
59         bucket[i] += bucket[i - 1];
60         s_bucket[i] = bucket[i];
61     }
62     memset(rank, -1, n * sizeof(int));
63
64     alloc(lms, int, n + 1);
65     int n1 = 0;
66     for (int i = 0; i < n; ++i) {
67         if (!type[i] && (i == 0 || type[i - 1])) lms[rank[i] = n1++] = i;
68     }
69     lms[n1] = n;
70     memset(sa, -1, n * sizeof(int));
71     for (int i = 0; i < n1; ++i) sa[--s_bucket[s[lms[i]]]] = lms[i];
72     induce(n, m, s, type, sa, bucket, l_bucket, s_bucket);
73     int m1 = 0;
74     alloc(s1, int, n + 1);
75     for (int i = 0, t = -1; i < n; ++i) {
76         int r = rank[sa[i]];
77         if (r != -1) {
78             int len = lms[r + 1] - sa[i] + 1;
79             m1 += t == -1 || len != lms[rank[t] + 1] - t + 1 ||
80                 memcmp(s + t, s + sa[i], len * sizeof(int)) != 0;
81             s1[r] = m1;
82             t = sa[i];
83         }
84     }
85     alloc(sa1, int, n + 1);
86     if (n1 == m1) {
87         for (int i = 0; i < n1; ++i) sa1[s1[i] - 1] = i;
88     } else {
89         sais(n1, m1, s1, sa1);
90     }
91     memset(sa, -1, n * sizeof(int));
92     memcpy(s_bucket + 1, bucket + 1, m * sizeof(int));
93     for (int i = n1 - 1; i >= 0; --i) {
94         int t = lms[sa1[i]];
95         sa[--s_bucket[s[t]]] = t;
96     }
97     induce(n, m, s, type, sa, bucket, l_bucket, s_bucket);
98 }
99 #undef S_TYPE
100 #undef L_TYPE
101 };

```

```

102
103 const int MAXN = 1e5 + 5;
104 SuffixArray<MAXN> sa;
105 char str[MAXN];
106 int s[MAXN];
107
108 int main() {
109     int n = fread(str, 1, MAXN, stdin);
110     while (str[n - 1] - 97u > 25) --n;
111     for (int i = 0; i < n; ++i) s[i] = str[i] - 'a' + 1;
112     sa.compute(n, 26, s);
113     for (int i = 0; i < n; ++i) printf("%d%c", sa.sa[i] + 1, " \n"[i == n - 1]);
114     for (int i = 1; i < n; ++i) printf("%d%c", sa.height[i], " \n"[i == n - 1]);
115     return 0;
116 }

```

4.6 后缀数组 (倍增)

```

1 // UOJ 模板题
2 #include <bits/stdc++.h>
3 using namespace std;
4
5 const int MAXN = 1e5 + 3;
6
7 template <int MAX_LENGTH> class SuffixArray {
8 public:
9     int n, sa[MAX_LENGTH], rank[MAX_LENGTH], height[MAX_LENGTH];
10
11     void compute(char *s, int n, int m) {
12         int i, p, w, j, k;
13         this->n = n;
14         if (n == 1) {
15             sa[0] = rank[0] = height[0] = 0;
16             return;
17         }
18         memset(cnt, 0, m * sizeof(int));
19         for (i = 0; i < n; ++i) ++cnt[rank[i] = s[i]];
20         for (i = 1; i < m; ++i) cnt[i] += cnt[i - 1];
21         for (i = n - 1; ~i; --i) sa[--cnt[rank[i]]] = i;
22         for (w = 1; w < n; w <= 1, m = p) {
23             for (p = 0, i = n - 1; i >= n - w; --i) id[p++] = i;
24             for (i = 0; i < n; ++i)
25                 if (sa[i] >= w) id[p++] = sa[i] - w;
26             memset(cnt, 0, m * sizeof(int));
27             for (i = 0; i < n; ++i) ++cnt[px[i] = rank[id[i]]];
28             for (i = 1; i < m; ++i) cnt[i] += cnt[i - 1];
29             for (i = n - 1; ~i; --i) sa[--cnt[px[i]]] = id[i];
30             memcpy(old_rank, rank, n * sizeof(int));
31             for (i = p = 1, rank[sa[0]] = 0; i < n; ++i)
32                 rank[sa[i]] = cmp(sa[i], sa[i - 1], w) ? p - 1 : p++;
33         }
34         for (i = 0; i < n; ++i) rank[sa[i]] = i;
35         for (i = k = height[rank[0]] = 0; i < n; height[rank[i++]] = k)
36             if (rank[i])
37                 for (k > 0 ? --k : 0, j = sa[rank[i] - 1]; s[i + k] == s[j + k]; ++k) {}
38     }
39
40     void init_st_table(int n) {

```



```

41     int lgn = lg[n];
42     for (int i = 0; i < n; ++i) table[0][i] = height[i];
43     for (int i = 1; i <= lgn; ++i)
44         for (int j = 0, l = 1 << (i - 1); j + l < n; ++j)
45             table[i][j] = min(table[i - 1][j], table[i - 1][j + l]);
46 }
47
48 int lcp(int i, int j) {
49     if (i > j) swap(i, j);
50     ++i;
51     int lgl = lg[j - i + 1];
52     return min(table[lgl][i], table[lgl][j - (1 << lgl) + 1]);
53 }
54
55 private:
56     int table[17][MAX_LENGTH], lg[MAX_LENGTH];
57     int old_rank[MAX_LENGTH], id[MAX_LENGTH], px[MAX_LENGTH], cnt[MAX_LENGTH];
58
59     bool cmp(int x, int y, int w) {
60         return old_rank[x] == old_rank[y] && old_rank[x + w] == old_rank[y + w];
61     }
62 };
63
64 char s[MAXN];
65 SuffixArray<MAXN> sa;
66
67 int main(int argc, char *argv[]) {
68     int n = fread(s, 1, MAXN, stdin);
69     while (s[n - 1] - 97u > 25) --n;
70     for (int i = 0; i < n; ++i) s[i] -= 'a';
71     s[n] = '$';
72     sa.compute(s, n, 26);
73     for (int i = 0; i < n; ++i) printf("%d%c", sa.sa[i] + 1, " \n"[i == n - 1]);
74     for (int i = 1; i < n; ++i) printf("%d%c", sa.height[i], " \n"[i == n - 1]);
75     return 0;
76 }

```

4.7 哈希

```

1  /*
2  * 其他哈希:
3  * 集合哈希: 可以使用元素的哈希值映射为高进制的某一位, 也可以使用质数的积。
4  * 树哈希: 将子树当作集合哈希, 加入深度的影响
5  */
6
7  const unsigned int KEY = 6151;
8  const unsigned int MOD = 1610612741;
9  // 64 位哈希参数 KEY 随意 MOD 461168601842738784711
10 unsigned int hash[MAXN], p[MAXN];
11
12 inline unsigned int get_hash(int l, int r) {
13     return (hash[r] + MOD - 1ULL * hash[l - 1] * p[r - l + 1] % MOD) % MOD;
14 }
15
16 void init(char *s, int n) {
17     p[0] = 1;
18     for (int i = 1; i <= n; ++i) {
19         p[i] = p[i - 1] * KEY % MOD;

```

```

20     hash[i] = (1LL * hash[i - 1] * KEY + s[i]) % MOD;
21 }
22 }

```

4.8 哈希例题 (2020 秦皇岛 J)

```

1  // 两次哈希
2  #include <bits/stdc++.h>
3  using namespace std;
4
5  typedef long long ll;
6
7  const int MAXN = 3e5 + 3;
8  const int MAX_PRIME = 8960453 + 3;
9  const int MOD = 998244353;
10 const ll BASE = 709;
11 const ll HASH_MOD = 461168601842738784711;
12
13 char s[MAXN];
14 int fac[MAXN], inv[MAXN], fac_inv[MAXN], prime[MAXN * 2];
15 ll ha[MAXN], p[MAXN], pref[MAXN], suff[MAXN], value[MAXN * 2];
16 pair<ll, int> bin[MAXN];
17
18 int cnt[MAXN], pidx[MAXN], sidx[MAXN];
19 bitset<MAX_PRIME> mark;
20
21 ll fmul(ll a, ll b) {
22     ll k = (ll)((1.1 * a * b) / (1.1 * HASH_MOD)), t = a * b - k * HASH_MOD;
23     for (t -= HASH_MOD; t < 0; t += HASH_MOD) {}
24     return t;
25 }
26 ll getRange(int l, int r) {
27     return (ha[r] - fmul(ha[l - 1], p[r - l + 1]) + HASH_MOD) % HASH_MOD;
28 }
29
30 int gao(int n, int d) {
31     int tot = 0;
32     for (int l = 1, r = d; r <= n; l += d, r += d) value[tot++] = getRange(l, r);
33     int bunch = n / d, rest = n % d;
34     if (rest) {
35         for (int r = n, l = n - d + 1; l >= 1; l -= d, r -= d)
36             value[tot++] = getRange(l, r);
37         sort(value, value + tot);
38         tot = unique(value, value + tot) - value;
39         pref[0] = pref[1] = suff[n] = suff[n + 1] = 1;
40         for (int i = d; i <= n; i += d) {
41             int idx = lower_bound(value, value + tot, getRange(i - d + 1, i)) - value;
42             pidx[i] = idx;
43             pref[i] = fmul(pref[i - d], prime[idx]);
44         }
45         for (int i = n - d + 1; i >= 1; i -= d) {
46             int idx = lower_bound(value, value + tot, getRange(i, i + d - 1)) - value;
47             sidx[i] = idx;
48             suff[i] = fmul(suff[i + d], prime[idx]);
49         }
50         int sc = 0, cur = fac[bunch];
51         memset(cnt, 0, tot * sizeof(int));
52         for (int l = 1, r = rest; r <= n; l += d, r += d) {

```

```

53     if (r + d <= n) {
54         ++cnt[sidx[r + 1]];
55         cur = 1ll * cur * inv[cnt[sidx[r + 1]]] % MOD;
56     }
57     bin[sc++] = {fmul(pref[l - 1], suff[r + 1]), 1};
58 }
59 sort(bin, bin + sc);
60 mark[bin[0].second] = 1;
61 for (int i = 1; i < sc; ++i)
62     mark[bin[i].second] = bin[i].first != bin[i - 1].first;
63
64 int res = 0;
65 for (int l = 1, r = rest; r <= n; l += d, r += d) {
66     if (l - 1 >= 1) {
67         ++cnt[pidx[l - 1]];
68         cur = 1ll * cur * inv[cnt[pidx[l - 1]]] % MOD;
69     }
70     if (mark[l]) {
71         res += cur;
72         if (res >= MOD) res -= MOD;
73     }
74     if (r + 1 <= n) {
75         cur = 1ll * cur * cnt[sidx[r + 1]] % MOD;
76         --cnt[sidx[r + 1]];
77     }
78 }
79 return res;
80 } else {
81     sort(value, value + tot);
82     ll pre = value[0];
83     int res = fac[bunch], cnt = 1;
84     for (int i = 1; i < tot; ++i) {
85         if (value[i] != pre) {
86             if (cnt > 1) res = 1ll * res * fac_inv[cnt] % MOD;
87             cnt = 1, pre = value[i];
88         } else {
89             ++cnt;
90         }
91     }
92     if (cnt > 1) res = 1ll * res * fac_inv[cnt] % MOD;
93     return res;
94 }
95 }
96
97 void solve() {
98     cin >> (s + 1);
99     int n = strlen(s + 1);
100    for (int i = 1; i <= n; ++i)
101        ha[i] = (fmul(ha[i - 1], BASE) + s[i]) % HASH_MOD;
102
103    int ans = 0;
104    for (int d = 1; d <= n; ++d) {
105        ans += gao(n, d);
106        if (ans >= MOD) ans -= MOD;
107        // cerr << "# " << ans << endl;
108    }
109    cout << ans << "\n";
110 }
111

```

```

112 void prework() {
113     p[0] = 1;
114     for (int i = 1; i < MAXN; ++i) p[i] = fmul(p[i - 1], BASE);
115     fac[0] = fac[1] = 1;
116     fac_inv[0] = fac_inv[1] = inv[1] = 1;
117     for (int i = 2; i < MAXN; ++i) {
118         fac[i] = 1ll * fac[i - 1] * i % MOD;
119         inv[i] = 1ll * (MOD - MOD / i) * inv[MOD % i] % MOD;
120         fac_inv[i] = 1ll * fac_inv[i - 1] * inv[i] % MOD;
121     }
122
123     int pc = 0;
124     for (int i = 2; i < MAX_PRIME; ++i) {
125         if (!mark[i]) prime[pc++] = i;
126         for (int j = 0; j < pc; ++j) {
127             int t = i * prime[j];
128             if (t >= MAX_PRIME) break;
129             mark[t] = 1;
130             if (i % prime[j] == 0) break;
131         }
132     }
133 }
134
135 int main(int argc, char *argv[]) {
136     ios::sync_with_stdio(false);
137     cin.tie(nullptr), cout.tie(nullptr);
138
139     prework();
140
141     int T;
142     cin >> T;
143     for (int step = 1; step <= T; ++step) {
144         cout << "Case #" << step << ": ";
145         solve();
146     }
147
148     return 0;
149 }

```

4.9 回文树

```

1 //最长双回文串
2 struct PT {
3     char s[MAXL];
4     int fail[MAXL], ch[26][MAXL], l[MAXL], dep[MAXL], lst, nc, n;
5     void init() {
6         l[0] = 0;
7         l[1] = -1;
8         fail[0] = fail[1] = 1;
9         for (int i = 0; i < 26; ++i) {
10             for (int j = 0; j < nc; ++j) { ch[i][j] = 0; }
11         }
12         for (int i = 2; i < nc; ++i) {
13             l[i] = 0;
14             fail[i] = 0;
15         }
16
17         lst = 0;

```

```

18     nc = 2;
19     n = 0;
20     s[0] = '#';
21 }
22
23 int insert(char c) {
24     int id = c - 'a';
25     s[++n] = c;
26     while (s[n - 1[lst] - 1] != s[n]) { lst = fail[lst]; }
27     if (ch[id][lst] == 0) {
28         l[nc] = l[lst] + 2;
29         int f = fail[lst];
30         while (s[n - 1[f] - 1] != s[n]) { f = fail[f]; }
31         fail[nc] = ch[id][f];
32         dep[nc] = dep[fail[nc]] + 1;
33         ch[id][lst] = nc;
34         ++nc;
35     }
36     lst = ch[id][lst];
37     return lst;
38 }
39 } pt;
40
41 char S[MAXL];
42 int len[MAXL];
43 int main() {
44     ios::sync_with_stdio(false);
45     cin.tie(0);
46     cout.tie(0);
47
48     cin >> S;
49     int n = strlen(S);
50     pt.init();
51     for (int i = 0; i < n; ++i) { len[i] = pt.l[pt.insert(S[i])]; }
52     pt.init();
53     int ans = 0;
54     for (int i = n - 1; i; --i) {
55         ans = max(ans, len[i - 1] + pt.l[pt.insert(S[i])]);
56     }
57     cout << ans << "\n";
58
59     return 0;
60 }

```

4.10 扩展 KMP

```

1 // next[i]:x[i...m-1] 与 x[0...m-1] 的最长公共前缀
2 // extend[i]:y[i...n-1] 与 x[0...m-1] 的最长公共前缀
3 void prework(char x[], int m, int next[]) {
4     next[0] = m;
5     int j = 0;
6     while (j + 1 < m && x[j] == x[j + 1]) ++j;
7     next[1] = j;
8     int k = 1;
9     for (int i = 2; i < m; ++i) {
10         int p = next[k] + k - 1;
11         int L = next[i - k];
12         if (i + L < p + 1)

```

```

13     next[i] = L;
14     else {
15         j = max(0, p - i + 1);
16         while (i + j < m && x[i + j] == x[j]) j++;
17         next[i] = j;
18         k = i;
19     }
20 }
21 }
22 void exkmp(char x[], int m, char y[], int n, int next[], int extend[]) {
23     prework(x, m, next);
24     int j = 0;
25     while (j < n && j < m && x[j] == y[j]) ++j;
26     extend[0] = j;
27     int k = 0;
28     for (int i = 1; i < n; ++i) {
29         int p = extend[k] + k - 1;
30         int L = next[i - k];
31         if (i + L < p + 1)
32             extend[i] = L;
33         else {
34             j = max(0, p - i + 1);
35             while (i + j < n && j < m && y[i + j] == x[j]) j++;
36             extend[i] = j;
37             k = i;
38         }
39     }
40 }

```

5 Graph Theory

5.1 KM

```

1  #include <bits/stdc++.h>
2  using namespace std;
3
4  typedef long long ll;
5
6  const int MAXN = 400 + 3;
7  const int ALPHA = 1e9 + 10;
8  const ll NOT = 0;
9  const ll INF = 311 * MAXN * ALPHA;
10 // 最大费用流时 NOT = 0, 最大费用流最大流时 NOT = -111 * MAXN * ALPHA
11 // 点为 1 .. n (左为 1 .. nl, 右为 1 .. nr)
12 struct KM {
13     int n, nl, nr, lk[MAXN], pre[MAXN];
14     ll lx[MAXN], ly[MAXN], w[MAXN][MAXN], slack[MAXN];
15     bitset<MAXN> vy;
16
17     void init(int n) {
18         this->n = n;
19         memset(lk, 0, sizeof(int) * (n + 1));
20         memset(pre, 0, sizeof(int) * (n + 1));
21         memset(lx, 0, sizeof(ll) * (n + 1));
22         memset(ly, 0, sizeof(ll) * (n + 1));
23         memset(slack, 0, sizeof(ll) * (n + 1));
24         for (int i = 0; i <= n; ++i) fill(w[i], w[i] + n + 1, NOT);

```

```

25 }
26
27 void add_edge(int x, int y, ll z) {
28     if (w[y][x] < z) w[y][x] = z;
29 }
30
31 ll match() {
32     for (int i = 1; i <= n; ++i)
33         for (int j = 1; j <= n; ++j) lx[i] = max(lx[i], w[i][j]);
34     for (int i = 1, py, p, x; i <= n; ++i) {
35         for (int j = 1; j <= n; ++j) slack[j] = INF, vy[j] = 0;
36         for (lk[py = 0] = i; lk[py]; py = p) {
37             ll delta = INF;
38             vy[py] = 1, x = lk[py];
39             for (int y = 1; y <= n; ++y) {
40                 if (vy[y]) continue;
41                 if (lx[x] + ly[y] - w[x][y] < slack[y])
42                     slack[y] = lx[x] + ly[y] - w[x][y], pre[y] = py;
43                 if (slack[y] < delta) delta = slack[y], p = y;
44             }
45             for (int y = 0; y <= n; ++y)
46                 if (vy[y]) {
47                     lx[lk[y]] -= delta, ly[y] += delta;
48                 } else {
49                     slack[y] -= delta;
50                 }
51             }
52         for (; py; py = pre[py]) lk[py] = lk[pre[py]];
53     }
54
55     ll ans = 0;
56     for (int i = 1; i <= n; ++i) {
57         ans += lx[i] + ly[i];
58         if (w[lk[i]][i] == NOT) ans -= NOT;
59     }
60     return ans;
61 }
62 } km;
63
64 int main(int argc, char *argv[]) {
65     ios::sync_with_stdio(false);
66     cin.tie(nullptr), cout.tie(nullptr);
67     cout << fixed << setprecision(10);
68
69     int nl, nr, m;
70     cin >> nl >> nr >> m;
71     km.init(max(nl, nr));
72     for (int x, y, z; m; --m) {
73         cin >> x >> y >> z;
74         km.add_edge(x, y, z);
75     }
76     cout << km.match() << "\n";
77     for (int i = 1; i <= nl; ++i)
78         cout << (km.w[km.lk[i]][i] == NOT ? 0 : km.lk[i]) << " \n"[i == nl];
79
80     return 0;
81 }

```

5.2 SAP

```

1 struct MaxFlow {
2     struct Edge {
3         int to, rest;
4     } edges[MAXM * 4];
5
6     vector<int> adj[MAXN];
7     int n, edges_c, dep[MAXN], depc[MAXN], s, t, last[MAXN];
8
9     void init(int _n) {
10         n = _n, edges_c = 0;
11         for (int i = 1; i <= n; ++i) adj[i].clear();
12     }
13
14     void add_edge(int u, int v, int cap) {
15         edges[edges_c] = {v, cap, 0};
16         adj[u].push_back(edges_c++);
17         edges[edges_c] = {u, 0, 0};
18         adj[v].push_back(edges_c++);
19     }
20
21     int dfs(int u, int flow) {
22         if (u == t || !flow) return flow;
23         int v, e, temp, res = 0;
24         for (int &i = last[u]; i < (int)adj[u].size(); ++i) {
25             e = adj[u][i], v = edges[e].to;
26             if (!edges[e].res || dep[v] != dep[u] - 1) continue;
27             temp = dfs(v, min(flow, edges[e].cap - edges[e].flow));
28             res += temp, flow -= temp;
29             edges[e].rest -= temp, edges[e ^ 1].rest += temp;
30             if (!flow || !dep[s]) return res;
31         }
32         last[u] = 0;
33         if (!(--depc[dep[u]])) dep[s] = n + 1;
34         ++depc[++dep[u]];
35         return res;
36     }
37
38     int max_flow(int s, int t) {
39         this->s = s, this->t = t;
40
41         static queue<int> que;
42         memset(dep + 1, 0, sizeof(int) * n);
43         memset(depc + 1, 0, sizeof(int) * n);
44         memset(last + 1, 0, sizeof(int) * n);
45         while (!que.empty()) que.pop();
46         dep[t] = 1, que.push(t);
47
48         while (!que.empty()) {
49             int u = que.front();
50             que.pop();
51             ++depc[dep[u]];
52             for (int i = 0, v; i < (int)adj[u].size(); ++i) {
53                 v = edges[adj[u][i]].to;
54                 if (dep[v]) continue;
55                 dep[v] = dep[u] + 1;
56                 que.push(v);
57             }
58         }
59     }
60 }

```



```

58
59     int res = 0;
60     while (dep[s] <= n) res += dfs(s, INT_MAX);
61     return res;
62 }
63 };

```

5.3 dinic

```

1  struct MaxFlow {
2      struct Edge {
3          int to, rest;
4      } edges[MAXM * 4];
5
6      vector<int> adj[MAXN];
7      int n, edges_c, dep[MAXN], s, t, last[MAXN];
8
9      void init(int _n) {
10         n = _n, edges_c = 0;
11         for (int i = 1; i <= n; ++i) adj[i].clear();
12     }
13
14     void add_edge(int u, int v, int cap) {
15         edges[edges_c] = {v, cap, 0};
16         adj[u].push_back(edges_c++);
17         edges[edges_c] = {u, 0, 0};
18         adj[v].push_back(edges_c++);
19     }
20
21     bool bfs() {
22         memset(dep + 1, -1, sizeof(int) * n);
23         static queue<int> q;
24         q.push(s);
25         dep[s] = 0;
26         while (!q.empty()) {
27             int u = q.front();
28             q.pop();
29             for (int i = 0; i < adj[u].size(); ++i) {
30                 Edge &e = edges[adj[u][i]];
31                 if ((~dep[e.to]) || !e.rest) continue;
32                 dep[e.to] = dep[u] + 1;
33                 q.push(e.to);
34             }
35         }
36         return ~dep[t];
37     }
38
39     int dfs(int u, int flow) {
40         if (u == t || flow == 0) return flow;
41         int res = 0, temp, e, v;
42         for (int &i = last[u]; i < adj[u].size(); ++i) {
43             e = adj[u][i], v = edges[e].to;
44             if (dep[v] == dep[u] + 1 && edges[e].rest) {
45                 temp = dfs(v, min(edges[e].rest, flow));
46                 res += temp, flow -= temp;
47                 edges[e].rest -= temp, edges[e ^ 1].rest += temp;
48                 if (!flow) break;
49             }

```

```

50     }
51     return flow;
52 }
53
54 int max_flow(int s, int t) {
55     this->s = s, this->t = t;
56     int res = 0;
57     while (bfs()) {
58         memset(last + 1, 0, sizeof(int) * n);
59         res += dfs(s, INF);
60     }
61     return res;
62 }
63 };

```

5.4 tarjan

```

1  vector<int> adj[MAXN];
2  int dfn[MAXN], low[MAXN], dfs_c;
3  int bel[MAXN], size[MAXN], scc, stk[MAXN], top, in_stack[MAXN];
4
5  void tarjan(int u) {
6      dfn[u] = low[u] = ++dfs_c;
7      stk[top++] = u;
8      in_stack[u] = 1;
9      for (size_t i = 0; i < adj[u].size(); ++i) {
10         int v = adj[u][i];
11         if (!dfn[v]) {
12             tarjan(v);
13             (low[v] < low[u]) && (low[u] = low[v]);
14         } else if (in_stack[v] && dfn[v] < low[u]) {
15             low[u] = dfn[v];
16         }
17     }
18     if (low[u] == dfn[u]) {
19         int v;
20         size[++scc] = 0;
21         do {
22             v = stk[--top];
23             in_stack[v] = 0;
24             bel[v] = scc;
25             ++size[scc];
26         } while (u != v);
27     }
28 }

```

5.5 一般图最大匹配

```

1  class GeneralMatch {
2  public:
3      int n;
4      vector<vector<int>>> g;
5      vector<int> match, aux, label, orig, parent;
6      queue<int> q;
7      int aux_time;
8

```

```

9   GeneralMatch(int n)
10       : match(n, -1), aux(n, -1), label(n), orig(n), parent(n, -1),
11         aux_time(-1) {
12       this->n = n;
13       g.resize(n);
14   }
15
16   void add_edge(int u, int v) {
17       g[u].push_back(v);
18       g[v].push_back(u);
19   }
20
21   int find(int x) { return x == orig[x] ? x : orig[x] = find(orig[x]); }
22
23   int lca(int u, int v) {
24       ++aux_time;
25       u = find(u), v = find(v);
26       for (;;) swap(u, v) {
27           if (~u) {
28               if (aux[u] == aux_time) return u;
29               aux[u] = aux_time;
30               if (match[u] == -1) {
31                   u = -1;
32               } else {
33                   u = find(parent[match[u]]);
34               }
35           }
36       }
37   }
38
39   void blossom(int u, int v, int o) {
40       while (find(u) != o) {
41           parent[u] = v;
42           v = match[u];
43           q.push(v);
44           label[v] = 0;
45           orig[u] = orig[v] = o;
46           u = parent[v];
47       }
48   }
49
50   int bfs(int x) {
51       iota(orig.begin(), orig.end(), 0);
52       fill(label.begin(), label.end(), -1);
53       while (!q.empty()) q.pop();
54       q.push(x);
55       label[x] = 0;
56       while (!q.empty()) {
57           int u = q.front();
58           q.pop();
59           for (int v : g[u]) {
60               if (label[v] == -1) {
61                   parent[v] = u;
62                   label[v] = 1;
63                   if (match[v] == -1) {
64                       while (v != -1) {
65                           int pv = parent[v];
66                           int next_v = match[pv];
67                           match[v] = pv;

```

```

68         match[pv] = v;
69         v = next_v;
70     }
71     return 1;
72 }
73 q.push(match[v]);
74 label[match[v]] = 0;
75 } else if (label[v] == 0 && find(u) != find(v)) {
76     int o = lca(u, v);
77     blossom(u, v, o);
78     blossom(v, u, o);
79 }
80 }
81 }
82 return 0;
83 }
84
85 int find_max_match() {
86     int res = 0;
87     for (int i = 0; i < n; ++i) {
88         if (!match[i]) continue;
89         res += bfs(i);
90     }
91     return res;
92 }
93 };

```

5.6 上下界费用流

```

1  #include <bits/stdc++.h>
2  using namespace std;
3
4  const int MAXN = 53;
5  const int MAX_NODE = 113;
6  const int MAX_EDGE = 1e5 + 5;
7  const int INF = 0x3f3f3f3f;
8
9  int n, s, t, ss, tt, tote;
10 int R[MAXN], C[MAXN], board[MAXN][MAXN];
11
12 struct Edge {
13     int to, cap, flow, cost;
14 } edges[MAX_EDGE];
15 vector<int> adj[MAX_NODE];
16
17 int from[MAX_NODE], in[MAX_NODE];
18 void add_edge(int from, int to, int l, int r, int cost) {
19     in[to] += l, in[from] -= l;
20     edges[tote] = (Edge){to, r - l, 0, cost};
21     adj[from].push_back(tote++);
22     edges[tote] = (Edge){from, 0, 0, -cost};
23     adj[to].push_back(tote++);
24 }
25
26 bool spfa(int s, int t) {
27     static queue<int> q;
28     static bool inq[MAX_NODE];
29     static int dist[MAX_NODE];

```

```

30  memset(inq + 1, 0, sizeof(bool) * tt);
31  memset(dist + 1, 0x3f, sizeof(int) * tt);
32  memset(from + 1, -1, sizeof(int) * tt);
33  dist[0] = 0, from[0] = -1;
34  q.push(0);
35  while (!q.empty()) {
36      int u = q.front();
37      q.pop();
38      inq[u] = false;
39      for (int e : adj[u]) {
40          if (edges[e].cap == edges[e].flow) continue;
41          int v = edges[e].to, d = dist[u] + edges[e].cost;
42          if (d >= dist[v]) continue;
43          dist[v] = d;
44          from[v] = e;
45          if (!inq[v]) {
46              q.push(v);
47              inq[v] = true;
48          }
49      }
50  }
51  return dist[t] < INF;
52 }
53
54 pair<int, int> min_cost_max_flow(int s, int t) {
55     int flow = 0, cost = 0;
56     while (spfa(s, t)) {
57         int mi = INF;
58         for (int it = from[t]; ~it; it = from[edges[it ^ 1].to])
59             mi = min(mi, edges[it].cap - edges[it].flow);
60         flow += mi;
61         for (int it = from[t]; ~it; it = from[edges[it ^ 1].to]) {
62             edges[it].flow += mi, edges[it ^ 1].flow -= mi;
63             cost += mi * edges[it].cost;
64         }
65     }
66     return make_pair(flow, cost);
67 }
68
69 void solve() {
70     tote = 0;
71     s = 2 * n + 1, t = 2 * n + 2, ss = 0, tt = 2 * n + 3;
72     for (int i = 0; i <= tt; ++i) adj[i].clear(), in[i] = 0;
73
74     memset(R + 1, 0, sizeof(int) * n);
75     memset(C + 1, 0, sizeof(int) * n);
76
77     for (int i = 1; i <= n; ++i)
78         for (int j = 1; j <= n; ++j) {
79             cin >> board[i][j];
80             R[i] += board[i][j];
81             C[j] += board[i][j];
82         }
83
84     for (int i = 1; i <= n; ++i) {
85         add_edge(s, i, R[i], R[i], 0);
86         add_edge(s, i + n, C[i], C[i], 0);
87     }
88 }

```

```

89     for (int i = 1, l, r; i <= n; ++i) {
90         cin >> l >> r;
91         add_edge(i, t, l, r, 0);
92     }
93     for (int i = 1, l, r; i <= n; ++i) {
94         cin >> l >> r;
95         add_edge(i + n, t, l, r, 0);
96     }
97
98     for (int step = n * n / 2, x1, y1, x2, y2; step; --step) {
99         cin >> x1 >> y1 >> x2 >> y2;
100         if (board[x1][y1] == board[x2][y2]) continue;
101         if (board[x2][y2]) swap(x1, x2), swap(y1, y2);
102         if (x1 == x2)
103             add_edge(y1 + n, y2 + n, 0, 1, 1);
104         else
105             add_edge(x1, x2, 0, 1, 1);
106     }
107     add_edge(t, s, 0, INF, 0);
108     int sum = 0;
109     for (int i = 1; i < tt; ++i) {
110         if (in[i] > 0) {
111             sum += in[i];
112             add_edge(ss, i, 0, in[i], 0);
113         } else if (in[i] < 0) {
114             add_edge(i, tt, 0, -in[i], 0);
115         }
116     }
117
118     pair<int, int> ans = min_cost_max_flow(ss, tt);
119     if (sum != ans.first) {
120         cout << "-1\n";
121     } else {
122         cout << ans.second << '\n';
123     }
124 }
125
126 int main() {
127     ios::sync_with_stdio(false);
128     cin.tie(nullptr);
129
130     while (cin >> n) solve();
131     return 0;
132 }

```

5.7 最小费用流

```

1  class MinCostFlow {
2  public:
3      struct Result {
4          int flow, cost;
5      };
6      struct Edge {
7          int to, next, rest, cost;
8      };
9
10     vector<bool> inq;
11     vector<int> head, dist, from, flow;

```

```

12  vector<Edge> edges;
13
14  MinCostFlow(int n, int m) : inq(n), head(n, -1), dist(n), from(n), flow(n) {
15      edges.reserve(2 * m);
16  }
17
18  void add_edge(int u, int v, int capacity, int cost) {
19      internal_add_edge(u, v, capacity, cost);
20      internal_add_edge(v, u, 0, -cost);
21  }
22
23  void internal_add_edge(int u, int v, int capacity, int cost) {
24      edges.push_back((Edge){v, head[u], capacity, cost});
25      head[u] = edges.size() - 1;
26  }
27
28  Result augment(int source, int sink) {
29      fill(dist.begin(), dist.end(), INT_MAX);
30      dist[source] = 0;
31      flow[source] = INT_MAX;
32      queue<int> q;
33      q.push(source);
34      while (!q.empty()) {
35          int u = q.front();
36          q.pop();
37          inq[u] = false;
38          for (int it = head[u]; ~it; it = edges[it].next) {
39              auto &e = edges[it];
40              int v = e.to;
41              if (e.rest > 0 && dist[u] + e.cost < dist[v]) {
42                  from[v] = it;
43                  dist[v] = dist[u] + e.cost;
44                  flow[v] = min(e.rest, flow[u]);
45                  if (!inq[v]) {
46                      q.push(v);
47                      inq[v] = true;
48                  }
49              }
50          }
51      }
52
53      if (dist[sink] == INT_MAX) return {0, 0};
54      int min_flow = flow[sink];
55      for (int u = sink; u != source; u = edges[from[u] ^ 1].to) {
56          edges[from[u]].rest -= min_flow;
57          edges[from[u] ^ 1].rest += min_flow;
58      }
59      return {min_flow, dist[sink]};
60  }
61
62  Result min_cost_flow(int source, int sink) {
63      int flow = 0, cost = 0;
64      for (;;) {
65          auto result = augment(source, sink);
66          if (!result.flow) break;
67          flow += result.flow, cost += result.cost;
68      }
69      return {flow, cost};
70  }

```

```
71 };
```

5.8 高标预流推进

```
1  #include <cstdio>
2  #include <cstring>
3  #include <queue>
4  using namespace std;
5  const int N = 1e4 + 4, M = 2e5 + 5, INF = 0x3f3f3f3f;
6  int n, m, s, t;
7
8  struct qxx {
9      int nex, t, v;
10 };
11 qxx e[M * 2];
12 int h[N], cnt = 1;
13 void add_path(int f, int t, int v) { e[++cnt] = (qxx){h[f], t, v}, h[f] = cnt; }
14 void add_flow(int f, int t, int v) {
15     add_path(f, t, v);
16     add_path(t, f, 0);
17 }
18
19 int ht[N], ex[N], gap[N]; // 高度;超额流;gap 优化
20 bool bfs_init() {
21     memset(ht, 0x3f, sizeof(ht));
22     queue<int> q;
23     q.push(t), ht[t] = 0;
24     while (q.size()) { // 反向 BFS, 遇到没有访问过的结点就入队
25         int u = q.front();
26         q.pop();
27         for (int i = h[u]; i; i = e[i].nex) {
28             const int &v = e[i].t;
29             if (e[i ^ 1].v && ht[v] > ht[u] + 1) ht[v] = ht[u] + 1, q.push(v);
30         }
31     }
32     return ht[s] != INF; // 如果图不连通, 返回 0
33 }
34 struct cmp {
35     bool operator()(int a, int b) const { return ht[a] < ht[b]; }
36 }; // 伪装排序函数
37 priority_queue<int, vector<int>, cmp> pq; // 将需要推送的结点以高度高的优先
38 bool vis[N]; // 是否在优先队列中
39 int push(int u) { // 尽可能通过能够推送的边推送超额流
40     for (int i = h[u]; i; i = e[i].nex) {
41         const int &v = e[i].t, &w = e[i].v;
42         if (!w || ht[u] != ht[v] + 1) continue;
43         int k = min(w, ex[u]); // 取到剩余容量和超额流的最小值
44         ex[u] -= k, ex[v] += k, e[i].v -= k, e[i ^ 1].v += k; // push
45         if (v != s && v != t && !vis[v])
46             pq.push(v), vis[v] = 1; // 推送之后, v 必然溢出, 则入堆, 等待被推送
47         if (!ex[u]) return 0; // 如果已经推送完就返回
48     }
49     return 1;
50 }
51 void relabel(int u) { // 重贴标签(高度)
52     ht[u] = INF;
53     for (int i = h[u]; i; i = e[i].nex)
54         if (e[i].v) ht[u] = min(ht[u], ht[e[i].t]);
```



```

55     ++ht[u];
56 }
57 int hlpp() { // 返回最大流
58     if (!bfs_init()) return 0; // 图不连通
59     ht[s] = n;
60     memset(gap, 0, sizeof(gap));
61     for (int i = 1; i <= n; i++)
62         if (ht[i] != INF) gap[ht[i]]++; // 初始化 gap
63     for (int i = h[s]; i; i = e[i].nex) {
64         const int v = e[i].t, w = e[i].v; // 队列初始化
65         if (!w) continue;
66         ex[s] -= w, ex[v] += w, e[i].v -= w, e[i ^ 1].v += w; // 注意取消 w 的引用
67         if (v != s && v != t && !vis[v]) pq.push(v), vis[v] = 1; // 入队
68     }
69     while (pq.size()) {
70         int u = pq.top();
71         pq.pop(), vis[u] = 0;
72         while (push(u)) { // 仍然溢出
73             // 如果 u 结点原来所在的高度没有结点了, 相当于出现断层
74             if (!--gap[ht[u]])
75                 for (int i = 1; i <= n; i++)
76                     if (i != s && i != t && ht[i] > ht[u] && ht[i] < n + 1) ht[i] = n + 1;
77             relabel(u);
78             ++gap[ht[u]]; // 新的高度, 更新 gap
79         }
80     }
81     return ex[t];
82 }
83 int main() {
84     scanf("%d%d%d", &n, &m, &s, &t);
85     for (int i = 1, u, v, w; i <= m; i++) {
86         scanf("%d%d%d", &u, &v, &w);
87         add_flow(u, v, w);
88     }
89     printf("%d", hlpp());
90     return 0;
91 }

```

6 Java

6.1 进制转换

```

1 import java.io.*;
2 import java.util.*;
3 import java.math.*;
4
5 /**
6  * Built using CHelper plug-in
7  * Actual solution is at the top
8  */
9 public class Main {
10     public static void main(String[] args) {
11         InputStream inputStream = System.in;
12         OutputStream outputStream = System.out;
13         Scanner in = new Scanner(inputStream);
14         PrintWriter out = new PrintWriter(outputStream);
15         Solver solver = new Solver();

```

```

16     int testCount = Integer.parseInt(in.next());
17     for (int i = 1; i <= testCount; i++)
18         solver.solve(i, in, out);
19     out.close();
20 }
21
22 static class Solver {
23     public void solve(int testNumber, Scanner in, PrintWriter out) {
24         int a = in.nextInt();
25         int b = in.nextInt();
26         String num = in.next();
27
28         BigInteger value = BigInteger.ZERO;
29         for (int i = 0; i < num.length(); ++i) {
30             value = value.multiply(BigInteger.valueOf(a));
31             value = BigInteger.valueOf(getValue(num.charAt(i))).add(value);
32         }
33         out.println(a + " " + num);
34
35         if (value.equals(BigInteger.ZERO)) {
36             out.println(b + " 0");
37             out.println();
38             return;
39         }
40
41         out.print(b + " ");
42
43         char[] ans = new char[1000];
44         int length = 0;
45         while (!value.equals(BigInteger.ZERO)) {
46             int digit = value.mod(BigInteger.valueOf(b)).intValue();
47             value = value.divide(BigInteger.valueOf(b));
48             ans[length] = getChar(digit);
49             ++length;
50         }
51
52         for (int i = length - 1; i >= 0; --i) {
53             out.print(ans[i]);
54         }
55         out.println("\n");
56     }
57
58     private int getValue(char ch) {
59         if (ch >= 'A' && ch <= 'Z') {
60             return ch - 'A' + 10;
61         }
62         if (ch >= 'a' && ch <= 'z') {
63             return ch - 'a' + 36;
64         }
65         return ch - '0';
66     }
67
68     private char getChar(int x) {
69         if (x < 10) {
70             return (char) ('0' + x);
71         } else if (x < 36) {
72             return (char) ('A' + x - 10);
73         } else {
74             return (char) ('a' + x - 36);
75         }
76     }
77 }

```

```

75         }
76     }
77
78 }
79 }

```

7 Others

7.1 FastIO

```

1  namespace FastIO {
2  struct Control {
3      int ct, val;
4      Control(int Ct, int Val = -1) : ct(Ct), val(Val) {}
5      inline Control operator()(int Val) { return Control(ct, Val); }
6  } _endl(0), _prs(1), _setprecision(2);
7
8  const int IO_SIZE = 1 << 16 | 127;
9
10 struct FastIO {
11     char in[IO_SIZE], *p, *pp, out[IO_SIZE], *q, *qq, ch[20], *t, b, K, prs;
12     FastIO() : p(in), pp(in), q(out), qq(out + IO_SIZE), t(ch), b(1), K(6) {}
13     ~FastIO() { fwrite(out, 1, q - out, stdout); }
14     inline char getc() {
15         return p == pp && (pp = (p = in) + fread(in, 1, IO_SIZE, stdin), p == pp)
16             ? (b = 0, EOF)
17             : *p++;
18     }
19     inline void putc(char x) {
20         q == qq && (fwrite(out, 1, q - out, stdout), q = out), *q++ = x;
21     }
22     inline void puts(const char str[]) {
23         fwrite(out, 1, q - out, stdout), fwrite(str, 1, strlen(str), stdout),
24         q = out;
25     }
26     inline void getline(string &s) {
27         s = "";
28         for (char ch; (ch = getc()) != '\n' && b;) s += ch;
29     }
30 #define indef(T) \
31     inline FastIO &operator>>(T &x) { \
32         x = 0; \
33         char f = 0, ch; \
34         while (!isdigit(ch = getc()) && b) f |= ch == '-'; \
35         while (isdigit(ch)) x = (x << 1) + (x << 3) + (ch ^ 48), ch = getc(); \
36         return x = f ? -x : x, *this; \
37     }
38 indef(int);
39 indef(long long);
40
41 inline FastIO &operator>>(string &s) {
42     s = "";
43     char ch;
44     while (isspace(ch = getc()) && b) {}
45     while (!isspace(ch) && b) s += ch, ch = getc();
46     return *this;
47 }

```

```

48 inline FastIO &operator>>(double &x) {
49     x = 0;
50     char f = 0, ch;
51     double d = 0.1;
52     while (!isdigit(ch = getc()) && b) f |= (ch == '-');
53     while (isdigit(ch)) x = x * 10 + (ch ^ 48), ch = getc();
54     if (ch == '.')
55         while (isdigit(ch = getc())) x += d * (ch ^ 48), d *= 0.1;
56     return x = f ? -x : x, *this;
57 }
58 #define outdef(_T) \
59 inline FastIO &operator<<(_T x) { \
60     !x && (putc('0'), 0), x < 0 && (putc('-'), x = -x); \
61     while (x) *t++ = x % 10 + 48, x /= 10; \
62     while (t != ch) *q++ = *--t; \
63     return *this; \
64 }
65 outdef(int);
66 outdef(long long);
67 inline FastIO &operator<<(char ch) { return putc(ch), *this; }
68 inline FastIO &operator<<(const char str[]) { return puts(str), *this; }
69 inline FastIO &operator<<(const string &s) { return puts(s.c_str()), *this; }
70 inline FastIO &operator<<(double x) {
71     int k = 0;
72     this->operator<<(int(x));
73     putc('.');
74     x -= int(x);
75     prs && (x += 5 * pow(10, -K - 1));
76     while (k < K) putc(int(x *= 10) ^ 48), x -= int(x), ++k;
77     return *this;
78 }
79 inline FastIO &operator<<(const Control &cl) {
80     switch (cl.ct) {
81     case 0: putc('\n'); break;
82     case 1: prs = cl.val; break;
83     case 2: K = cl.val; break;
84     }
85     return *this;
86 }
87 inline operator bool() { return b; }
88 };
89 } // namespace FastIO

```

7.2 duipai

```

1  #/usr/bin/bash
2
3  while true; do
4      python gen.py > in.txt
5      time ./my < in.txt > out.txt
6      time ./std < in.txt > ans.txt
7      if diff out.txt ans.txt; then
8          echo AC
9      else
10         echo WA
11         exit 0
12     fi
13 done

```

7.3 emacs

```

1 (defun myc++ ()
2   (c-set-style "stroustrup")
3   (setq tab-width 2)
4   (setq indent-tabs-mode nil)
5   (setq c-basic-offset 2)
6   (c-toggle-hungry-state)
7   (defun compile-and-run()
8     (interactive)
9     (setq file-name (file-name-sans-extension (file-name-nondirectory buffer-file-name)))
10    (compile
11      (format "g++ %s.cpp -o %s -Wall -Wextra -Wshadow -O2 && ./%s < in.txt"
12              file-name file-name file-name)))
13    (local-set-key (kbd "C-c C-c") 'compile-and-run)
14    (local-set-key (kbd "C-c C-k") 'kill-compilation))
15  (add-hook 'c++-mode-hook 'myc++))
16
17 (global-set-key [(meta ?o)] 'other-window)
18 (global-set-key [(meta ?/)] 'hippie-expand)
19 (global-set-key [(control tab)] 'senator-completion-menu-popup)
20 (setq hippie-expand-try-functions-list
21   '(try-expand-dabbrev
22     try-expand-dabbrev-visible
23     try-expand-dabbrev-all-buffers
24     try-expand-dabbrev-from-kill
25     try-complete-file-name-partially
26     try-complete-file-name
27     try-expand-all-abbrevs
28     try-expand-list
29     try-expand-line))
30
31 (setq auto-save-mode nil)
32 (setq make-backup-files nil)
33
34 (ido-mode t)
35 (show-paren-mode 1)
36 (delete-selection-mode t)
37 (global-linum-mode t)
38 (global-auto-revert-mode t)

```

7.4 myalloc

```

1 // useage: vector<int, myalloc<int>> L;
2 static char space[10000000], *sp = space;
3 template <typename T> struct myalloc : allocator<T> {
4   myalloc() {}
5   template <typename T2> myalloc(const myalloc<T2> &a) {}
6   template <typename T2> myalloc<T> &operator=(const myalloc<T2> &a) {
7     return *this;
8   }
9   template <typename T2> struct rebind { typedef myalloc<T2> other; };
10  inline T *allocate(size_t n) {
11    T *result = (T *)sp;
12    sp += n * sizeof(T);
13    return result;
14  }
15  inline void deallocate(T *p, size_t n) {}

```

```
16 };
```

7.5 vimrc

```
1 syntax enable
2 set syntax=on
3 set nobackup
4 set noswapfile
5 set noundofile
6 set nu
7 set smartindent
8 set cindent
9 set noeb
10 set tabstop=2
11 set softtabstop=2
12 set shiftwidth=2
13 set expandtab
14
15 :imap jk <Esc>
16
17 map <F5> : call Complie() <CR>
18 func Complie()
19     exec "w"
20     exec "!g++ % -o %< -g -Wall -std=gnu++14 -static"
21 endfunc
22
23 map <F6> : call Run() <CR>
24 func Run()
25     exec "!./%<"
26 endfunc
27
28 map <F9> : call DeBug() <CR>
29 func DeBug()
30     exec "!gdb %<"
31 endfunc
```