*CPC Template Manaual

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cycleke

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1 Math

1.1 BGSG

```
// Finds the primitive root modulo p
   int generator(int p) {
     vector<int> fact;
3
     int phi = p - 1, n = phi;
4
      for (int i = 2; i * i <= n; ++i) {
5
        if (n \% i == 0) {
6
7
          fact.push_back(i);
8
          while (n \% i == 0) n /= i;
9
        }
     }
10
11
     if (n > 1) fact.push_back(n);
12
      for (int res = 2; res <= p; ++res) {</pre>
        bool ok = true;
13
        for (int factor : fact)
15
          if (mod_pow(res, phi / factor, p) == 1) {
            ok = false;
16
            break;
17
          }
18
19
20
        if (ok) return res;
21
22
     return -1;
23
   }
24
   // This program finds all numbers x such that x^k=a (mod n)
   vector<int> BSGS(int n, int k, int a) {
26
     if (a == 0) return vector<int>({0});
27
28
     int g = generator(n);
      // Baby-step giant-step discrete logarithm algorithm
29
     int sq = (int) sqrt(n + .0) + 1;
30
     vector<pair<int, int>> dec(sq);
31
      for (int i = 1; i <= sq; ++i)
32
        dec[i-1] = \{mod\_pow(g, i * sq * k % (n-1), n), i\};
33
34
      sort(dec.begin(), dec.end());
35
      int any_ans = -1;
36
37
      for (int i = 0; i < sq; ++i) {
38
        int my = mod_pow(g, i * k % (n - 1), n) * a % n;
39
        auto it = lower_bound(dec.begin(), dec.end(), make_pair(my, 0));
40
        if (it != dec.end() && it->first == my) {
41
          any_ans = it->second * sq - i;
          break;
42
        }
43
44
     if (any_ans == -1) return vector<int>();
45
      // Print all possible answers
46
     int delta = (n - 1) / \underline{gcd(k, n - 1)};
47
48
     vector<int> ans;
      for (int cur = any_ans % delta; cur < n - 1; cur += delta)</pre>
49
50
        ans.push_back(mod_pow(g, cur, n));
51
      sort(ans.begin(), ans.end());
52
     return ans;
53 }
```

1.2 lucas

```
// C(n, m) = C(n / p, m / p) * C(n % p, m % p) (mod p)
   ll lucas(ll n, ll k, int p) {
3
     ll ret = 1:
      while (n && k) {
4
        ll nn = n \% p, kk = k \% p;
5
        if (nn < kk) return 0;</pre>
6
        ret = ret * f[nn] * mod_pow(f[kk]) * f[nn - kk] % p, p - 2, p) % p;
7
        n \neq p, k \neq p;
8
9
10
     return res;
   }
11
```

1.3 LinearProgramming

```
1 // CCPC Final 2017 F
   // sum(P(s)) = 1, P(s) >= 0
3 // \max \text{ and equal } (sum(P(s)) | i in s)
4 #include <bits/stdc++.h>
5 using namespace std;
6
7 const int MAXN = int(3e3);
  const int MAXM = int(3e3);
   const double INF = 1e20, EPS = 1e-9;
10
11 int n, m;
12 double a[MAXM][MAXN], v;
13
  void pivot(int l, int e) {
14
15
     int i, j;
16
     a[l][e] = 1 / a[l][e];
17
      for (j = 0; j \le n; ++j)
18
       if (j != e) a[l][j] *= a[l][e];
19
     for (i = 1; i \le m; ++i)
20
       if (i != l && fabs(a[i][e]) > EPS) {
21
          for (j = 0; j \le n; ++j)
22
            if (j != e) a[i][j] -= a[i][e] * a[l][j];
23
          a[i][e] = -a[i][e] * a[l][e];
24
       }
25
     v += a[0][e] * a[1][0];
     for (j = 1; j \le n; ++j)
26
       if (j != e) a[0][j] -= a[0][e] * a[l][j];
27
28
      a[0][e] = -a[0][e] * a[1][e];
29
   }
30
   double simplex() {
31
     int e, l, i;
32
     double mn;
33
     v = 0;
34
     while (true) {
35
       for (e = 1; e <= n; ++e)
36
37
         if (a[0][e] > EPS) break;
38
       if (e > n) return v;
       for (i = 1, mn = INF; i \le m; ++i)
39
          if (a[i][e] > EPS && mn > a[i][0] / a[i][e])
40
           mn = a[i][0] / a[i][e], l = i;
41
42
       if (mn == INF) return INF;
```

```
pivot(l, e);
43
44
    }
45
46
    void solve() {
47
48
      static int n, m, g[10];
       static vector<int> con[10], able;
49
50
       scanf("%d %d", &n, &m);
51
       for (int i = 0; i < n; ++i) {
52
53
        scanf("%d", g + i);
54
        con[i].clear();
55
56
      if (n == 1) {
57
        printf("%.10f\n", m >= g[0] ? 1. : 0.);
58
59
        return;
60
61
62
      able.clear();
       for (int s = 0, S = 1 << n; s < S; ++s) {
63
        int sum = 0;
64
        for (int i = 0; i < n; ++i)
65
66
           if (s >> i \& 1) sum += g[i];
67
        if (sum > m) continue;
        able.push_back(s);
68
69
        for (int i = 0; i < n; ++i)
           if (s >> i & 1) con[i].push_back(able.size());
70
71
       ::n = able.size();
72
 73
       ::m = 0;
74
      static random_device rd;
      mt19937 gen(rd());
75
       shuffle(able.begin(), able.end(), gen);
76
       for (int step = 0; step < n; ++step) {</pre>
77
        int f = ++::m;
78
79
        for (int i = 0; i \le ::n; ++i) a[f][i] = 0;
80
        for (int x : con[step]) ++a[f][x];
81
        if (step + 1 < n) {
82
           for (int x : con[step + 1]) --a[f][x];
83
        } else {
           for (int x : con[0]) --a[f][x];
84
85
        }
86
      }
87
88
      ++::m;
89
      a[::m][0] = 1;
       for (int i = 1; i <= ::n; ++i) a[::m][i] = 1;
90
91
92
      ++::m;
93
      a[::m][0] = -1;
94
       for (int i = 1; i \le ::n; ++i) a[::m][i] = -1;
95
96
      for (int i = 0; i \le ::n; ++i) a[0][i] = 0;
97
      for (int x : con[0]) ++a[0][x];
      printf("%.10f\n", simplex());
98
99
100
101 int main() {
```

```
int o_o, case_number = 1;
102
       for (scanf("%d", &o_o); case_number <= o_o; ++case_number) {</pre>
103
        printf("Case #%d: ", case_number);
104
105
        solve();
106
107
      return 0;
108
    }
109
110 // 备份
111 #include <bits/stdc++.h>
112 using namespace std;
113
114 typedef long double db;
115 const int MAXN = 3000;
116 const int MAXM = 3000;
117 const db EPS = 1e-9;
118 const db INF = 1e200;
119
120 namespace LP {
121 db a[MAXM][MAXN];
122 int idA[MAXN], idB[MAXN];
123 int m, n;
124
125
    void put_out(int x) {
126
       if (x == 0)
        printf("Infeasible\n");
127
128
        printf("Unbounded\n");
129
130
      exit(0);
131
    void pivot(int xA, int xB) {
132
       swap(idA[xA], idB[xB]);
133
       static int next[MAXN];
134
       int i, j, last = MAXN - 1;
135
       db tmp = -a[xB][xA];
136
       a[xB][xA] = -1.0;
137
138
       for (j = 0; j \le n; j++)
139
        if (fabs(a[xB][j]) > EPS) a[xB][last = next[last] = j] /= tmp;
140
      next[last] = -1;
141
142
      for (i = 0; i <= m; i++)</pre>
        if (i != xB \&\& fabs(tmp = a[i][xA]) > EPS)
143
           for (a[i][xA] = 0.0, j = next[MAXN - 1]; ~j; j = next[j])
144
145
             a[i][j] += tmp * a[xB][j];
146
    }
147
    db calc() {
148
      int xA, xB;
       db Max, tmp;
149
      while (1) {
150
151
        xA = n + 1, idA[xA] = n + m + 1;
152
        for (int i = 1; i <= n; i++)</pre>
153
           if (a[0][i] > EPS \&\& idA[i] < idA[xA]) xA = i;
154
155
        if (xA == n + 1) return a[0][0];
        xB = m + 1, idB[xB] = n + m + 1, Max = -INF;
156
        for (int i = 1; i <= m; i++)</pre>
157
158
           if (a[i][xA] < -EPS && ((tmp = a[i][0] / a[i][xA]) > Max + EPS ||
159
                                    (tmp > Max - EPS \&\& idB[i] < idB[xB])))
160
             Max = tmp, xB = i;
```

```
161
162
         if (xB == m + 1) put_out(1);
163
164
         pivot(xA, xB);
165
166
      return a[0][0];
167
    }
168 db solve() {
       for (int i = 1; i <= n; i++) idA[i] = i;</pre>
169
       for (int i = 1; i \le m; i++) idB[i] = n + i;
170
171
       static db tmp[MAXN];
172
       db Min = 0.0;
       int l:
173
       for (int i = 1; i <= m; i++)
174
         if (a[i][0] < Min) Min = a[i][0], l = i;
175
       if (Min > -EPS) return calc();
176
177
       idA[++n] = 0;
178
       for (int i = 1; i <= m; i++) a[i][n] = 1.0;
179
180
       for (int i = 0; i \le n; i++) tmp[i] = a[0][i], a[0][i] = 0.0;
       a[0][n] = -1.0;
181
182
      pivot(n, l);
183
184
185
       if (calc() < -EPS) put_out(0);</pre>
186
       for (int i = 1; i <= m; i++)
187
         if (!idB[i]) {
           for (int j = 1; j \le n; j++)
188
             if (fabs(a[0][j]) > EPS) {
189
190
               pivot(j, i);
191
               break;
192
193
           break;
194
195
       int xA;
196
197
       for (xA = 1; xA \le n; xA++)
198
         if (!idA[xA]) break;
       for (int i = 0; i <= m; i++) a[i][xA] = a[i][n];</pre>
199
200
       idA[xA] = idA[n], n--;
201
       for (int i = 0; i \le n; i++) a[0][i] = 0.0;
202
       for (int i = 1; i <= m; i++)
203
204
         if (idB[i] <= n) {</pre>
205
           for (int j = 0; j \le n; j++) a[0][j] += a[i][j] * tmp[idB[i]];
206
         }
207
208
       for (int i = 1; i <= n; i++)</pre>
209
         if (idA[i] <= n) a[0][i] += tmp[idA[i]];</pre>
210
      return calc();
211 }
212 db ans[MAXN];
213
    void findAns() {
214
       for (int i = 1; i \le n; i++) ans[i] = 0.0;
215
       for (int i = 1; i <= m; i++)</pre>
216
         if (idB[i] <= n) ans[idB[i]] = a[i][0];
217
    void work() {
218
219
       for (int i = 1; i <= m; ++i)
```

```
220
         for (int j = 1; j \le n; ++j) a[i][j] *= -1;
      printf("%.10f\n", -double(solve()));
221
222
    } // namespace LP
223
224
225 void solve() {
      static int n, m, g[10];
226
227
       static vector<int> con[10], able;
228
       scanf("%d %d", &n, &m);
229
230
       for (int i = 0; i < n; ++i) {
         scanf("%d", g + i);
231
         con[i].clear();
232
233
       }
234
      if (n == 1) {
235
         printf("%.10f\n", m >= g[0] ? 1.0 : 0.0);
236
237
      }
238
239
240
      able.clear();
       for (int s = 0; s < (1 << n); ++s) {
241
         int sum = 0;
242
243
         for (int i = 0; i < n; ++i)
244
           if (s >> i \& 1) sum += g[i];
         if (sum > m) continue;
245
246
         able.push_back(s);
247
248
         for (int i = 0; i < n; ++i)
           if (s >> i & 1) con[i].push_back(able.size());
249
250
251
252
      LP::n = able.size();
      LP::m = 0;
253
254
255
      for (int step = 0; step < n; ++step) {</pre>
256
         int &f = ++LP::m;
257
         for (int i = 0; i <= LP::n; ++i) LP::a[f][i] = 0;</pre>
         for (int x : con[step]) ++LP::a[f][x];
258
259
         if (step + 1 < n) {
260
           for (int x : con[step + 1]) --LP::a[f][x];
261
         } else {
           for (int x : con[0]) --LP::a[f][x];
262
263
         }
264
      }
265
266
      ++LP::m;
      LP::a[LP::m][0] = 1;
267
       for (int i = 1; i <= LP::n; ++i) LP::a[LP::m][i] = 1;</pre>
268
269
270
      ++LP::m;
271
      LP::a[LP::m][0] = -1;
       for (int i = 1; i <= LP::n; ++i) LP::a[LP::m][i] = -1;
272
273
274
       for (int i = 0; i <= LP::n; ++i) LP::a[0][i] = 0;
275
       for (int x : con[0]) ++LP::a[0][x];
276
277
       static db a2[MAXM][MAXN];
278
       for (int i = 1; i <= LP::m; ++i)</pre>
```

```
279
         for (int j = 1; j <= LP::n; ++j) a2[i][j] = LP::a[i][j];</pre>
280
       for (int i = 1; i <= LP::m; ++i)</pre>
         for (int j = 1; j <= LP::n; ++j) LP::a[j][i] = a2[i][j];</pre>
281
       swap(LP::n, LP::m);
282
       for (int i = 1; i \le \max(LP::n, LP::m); ++i) \sup(LP::a[0][i], LP::a[i][0]);
283
       LP::a[0][0] = 0;
284
285
       for (int i = 1; i <= LP::m; ++i)</pre>
         for (int j = 1; j <= LP::n; ++j) LP::a[i][j] *= -1;
286
287
       for (int i = 1; i <= LP::m; ++i) LP::a[i][0] *= -1;
       for (int i = 1; i <= LP::n; ++i) LP::a[0][i] *= -1;
288
289
290
      LP::work();
291 }
292
293 int main() {
      int o_o;
294
       scanf("%d", &o_o);
for (int i = 1; i <= o_o; ++i) {
295
296
         printf("Case #%d: ", i);
297
298
         solve();
299
       }
300
       return 0;
301 }
    1.4 exctr
    int exctr(int n, int *a, int *m) {
       int M = m[0], res = a[0];
 3
       for (int i = 1; i < n; ++i) {</pre>
         int a = M, b = m[i], c = (a[i] - res \% b + b) \% b, x, y;
 4
         int g = exgcd(a, b, x, y), bg = b / g;
 5
 6
         if (c % g != 0) return -1;
         x = 1LL * x * (c / g) % bg;
 7
         res += x * M;
 8
 9
         M \stackrel{*}{=} bq:
         res = (res \% M + M) \% M;
 10
11
12
      return res;
13 }
         杜教筛
    1.5
 1 // e = mu \times 1
 2 // d = 1 \times 1
 3 // sigma = d x 1
 4 // phi = mu x id
 5 // id = phi x 1
 6 // id^2 = (id * phi) x id
 8 // S = sum(f)
 9 // sum(fxg) = sum(g(i)S(n/i))
10 map<int, int> mp_mu;
11
12 int S_mu(int n) {
      if (n < MAXN) return sum_mu[n];</pre>
13
14
       if (mp_mu[n]) return mp_mu[n];
15
       int ret = 1;
```

```
16
     for (int i = 2, j; i \le n; i = j + 1) {
17
       j = n / (n / i);
18
       ret -= S_mu(n / i) * (j - i + 1);
19
20
     return mp_mu[n] = ret;
21
   }
22
23
  ll S_phi(int n) {
24
     ll res = 0;
25
     for (int i = 1, j; i \le n; i = j + 1) {
26
       j = n / (n / i);
27
       res += 1LL * (S_mu(j) - S_mu(i - 1)) * (n / i) * (n / i);
28
     return (res - 1) / 2 + 1;
29
30 }
   1.6 Miller Rabin
   inline ll mod_mul(const ll &a, const ll &b, const ll &mod) {
     ll k = (ll)((1.0L * a * b) / (1.0L * mod)), t = a * b - k * mod;
2
3
     t -= mod;
4
     while (t < 0) t += mod;
5
     return t;
6
   }
   inline ll mod_pow(ll a, ll b, const ll &mod) {
7
     ll res = 1;
8
9
     for (; b; b >>= 1, a = mod_mul(a, a, mod))
        (b & 1) && (res = mod_mul(res, a, mod));
10
11
     return res;
   }
12
13
   inline bool check(const ll &x, const ll &p) {
14
     if (!(x \% p) \mid | mod_pow(p \% x, x - 1, x) \land 1) return false;
15
     ll k = x - 1, t;
16
     while (~k & 1) {
17
       if (((t = mod_pow(p \% x, k >>= 1, x)) ^ 1) \&\& (t ^ (x - 1))) return false;
18
19
       if (!(t \wedge (x - 1))) return true;
20
21
     return true;
22 }
23
24 inline bool Miller_Rabin(const ll &x) {
     if (x < 2) return false;
     static const int p[12] = \{2, 3, 5, 7, 11, 13, 17, 19, 61, 2333, 4567, 24251\};
27
     for (int i = 0; i < 12; ++i) {
       if (!(x ^ p[i])) return true;
28
29
       if (!check(x, p[i])) return false;
     }
30
31
     return true;
  }
32
   1.7 burnside
1 // |X/G| = \{1 | G|\}  \setminus \{g | G\} |X^g|
2 // Gym - 101873B
3 // m边形,每边是n*n的矩形,用c种颜色染色,可进行水平旋转,问不同多边形个数。
4 #include <bits/stdc++.h>
```

```
using namespace std;
   const int MOD = 1e9 + 7;
7
8
   int mod_pow(int a, int b) {
9
     int r = 1;
10
     for (; b; b >>= 1, a = 1LL * a * a % MOD)
11
       if (b & 1) r = 1LL * a * r % MOD;
12
13
     return r;
14
  }
15
16 int main() {
17
     ios::sync_with_stdio(false);
     cin.tie(nullptr);
18
19
20
     int n, m, c;
21
     cin >> n >> m >> c;
22
23
     int ans = 0;
     for (int i = 1; i <= m; ++i)</pre>
24
       ans = (ans + mod_pow(c, n * n * __gcd(i, m))) % MOD;
25
     ans = 1LL * ans * mod_pow(m, MOD - 2) % MOD;
26
27
     cout << ans << '\n';
     return 0;
29 }
   1.8 类欧几里德算法
1 // \# f = sum((a*i+b)/c), g = sum((a*i+b)/c*i), h = sum(((a*i+b)/c)^2), for i in [0..n],
2 //整除向下
3 #include <bits/stdc++.h>
4 #define int long long
5 using namespace std;
6 const int P = 998244353;
7 int i2 = 499122177, i6 = 166374059;
8 struct data {
9
     data() \{ f = g = h = 0; \}
10
     int f, g, h;
11 }; // 三个函数打包
   data calc(int n, int a, int b, int c) {
12
13
     int ac = a / c, bc = b / c, m = (a * n + b) / c, n1 = n + 1, n21 = n * 2 + 1;
14
     data d;
     if (a == 0) { // 迭代到最底层
15
       d.f = bc * n1 \% P;
16
17
       d.g = bc * n \% P * n1 \% P * i2 \% P;
       d.h = bc * bc % P * n1 % P;
18
       return d;
19
20
21
     if (a >= c || b >= c) { // 取模
       d.f = n * n1 \% P * i2 \% P * ac \% P + bc * n1 \% P;
22
23
       d.q = ac * n \% P * n1 \% P * n21 \% P * i6 \% P + bc * n \% P * n1 \% P * i2 % P;
       d.h = ac * ac % P * n % P * n1 % P * n21 % P * i6 % P +
24
25
              bc * bc % P * n1 % P + ac * bc % P * n % P * n1 % P;
       d.f %= P, d.g %= P, d.h %= P;
26
27
28
       data e = calc(n, a % c, b % c, c); // 迭代
29
       d.h += e.h + 2 * bc % P * e.f % P + 2 * ac % P * e.g % P;
30
```

```
d.g += e.g, d.f += e.f;
31
        d.f %= P, d.g %= P, d.h %= P;
32
33
        return d;
34
35
     data e = calc(m - 1, c, c - b - 1, a);
     d.f = n * m % P - e.f, d.f = (d.f % P + P) % P;
36
     d.g = m * n % P * n1 % P - e.h - e.f, d.g = (d.g * i2 % P + P) % P;
37
     d.h = n * m \% P * (m + 1) \% P - 2 * e.g - 2 * e.f - d.f;
38
     d.h = (d.h \% P + P) \% P;
39
40
     return d;
41
42
43 int T, n, a, b, c;
   signed main() {
44
     scanf("%lld", &T);
45
     while (T--) {
46
        scanf("%lld%lld%lld", &n, &a, &b, &c);
47
        data ans = calc(n, a, b, c);
48
        printf("%lld %lld %lld\n", ans.f, ans.h, ans.g);
49
50
51
     return 0;
52 }
   1.9 Pollard rho
   inline ll rand64(ll x) {
     return 1ll * ((rand() << 15 ^ rand()) << 30 ^ (rand() << 15 ^ rand())) % x;
2
3
4
   inline ll Pollard_rho(const ll &x, const int &y) {
5
6
     ll\ v0 = rand64(x - 1) + 1, \ v = v0, \ d, \ s = 1;
7
     for (register int t = 0, k = 1;;) {
8
        if (v = (mod_mul(v, v, x) + y) \% x, s = mod_mul(s, abs(v - v0), x),
9
            !(v ^ v0) || !s)
10
         return x;
        if (++t == k) {
11
          if ((d = \underline{gcd}(s, x)) \land 1) return d;
12
          v0 = v, k \iff 1;
13
14
15
   }
16
17
18 ll ans;
19
   vector<ll> factor;
   void findfac(ll n) {
20
     if (Miller_Rabin(n)) {
21
22
        factor.push_back(n);
23
        return;
24
25
     while (p \ge n) \{ p = Pollard_rho(p, rand64(n - 1) + 1); \}
26
27
     findfac(p);
     findfac(n / p);
28
29 }
```

1.10 FFT

```
1 const int MAXN = 4 * 1e5 + 3;
   const double PI = acos(-1);
   complex<double> a[MAXN], b[MAXN];
3
5
   int n, bit;
6 int rev[MAXN];
7
   void fft(complex<double> *a, int sign) {
8
     for (int i = 0; i < n; ++i)
9
        if (i < rev[i]) swap(a[i], a[rev[i]]);</pre>
10
11
12
      for (int j = 1; j < n; j <<= 1) {
        complex<double> wn(cos(2 * PI / (j << 1)), sign * sin(2 * PI / (j << 1)));
13
        for (int i = 0; i < n; i += (j << 1)) {
14
          complex<double> w(1, 0), t0, t1;
15
          FOR(k, 0, j) {
16
            t0 = a[i + k];
17
            t1 = w * a[i + j + k];
18
            a[i + k] = t0 + t1;
19
20
            a[i + j + k] = t0 - t1;
21
            w *= wn;
22
         }
23
        }
24
     }
25
     if (sign == -1)
        for (int i = 0; i < n; ++i) a[i] /= n;
26
27
   }
28
   int main() {
29
     ios::sync_with_stdio(false);
30
31
     cin.tie(0);
32
     cout.tie(0);
33
34
     int n, m, x;
35
     cin >> n >> m;
     for (int i = 0; i \le n; ++i) {
36
37
        cin >> x;
38
        a[i].real(x);
39
40
     for (int i = 0; i <= m; ++i) {</pre>
        cin >> x;
41
42
        b[i].real(x);
43
44
     ::n = 1;
45
46
     bit = 0;
47
     while (::n <= n + m) {
48
        ::n <<= 1;
        ++bit;
49
50
     }
51
     rev[0] = 0;
52
     FOR(i, 1, ::n) rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (bit - 1));
53
      fft(a, 1);
     fft(b, 1);
54
     FOR(i, 0, ::n) a[i] *= b[i];
55
      fft(a, -1);
56
57
     FOR(i, 0, n + m + 1) cout << int(a[i].real() + .5) << " ";
     cout << "\n";
58
59
     return 0;
```

```
60 }
   1.11 gauss
1
   const double EPS = 1e-9;
2
   const int MAXN = MAX_NODE;
   double a[MAXN][MAXN], x[MAXN];
5
  int equ, var;
6
   int gauss() {
7
     int i, j, k, col, max_r;
8
      for (k = 0, col = 0; k < equ && col < var; k++, col++) {
9
10
        \max_{r} = k;
        for (i = k + 1; i < equ; i++)
11
          if (fabs(a[i][col]) > fabs(a[max_r][col])) max_r = i;
12
        if (fabs(a[max_r][col]) < EPS) return 0;</pre>
13
14
        if (k != max_r) {
15
          for (j = col; j < var; j++) swap(a[k][j], a[max_r][j]);
16
          swap(x[k], x[max_r]);
17
18
19
        x[k] /= a[k][col];
20
21
        for (j = col + 1; j < var; j++) a[k][j] /= a[k][col];</pre>
22
        a[k][col] = 1;
23
        for (i = k + 1; i < equ; i++)
24
25
          if (i != k) {
            x[i] = x[k] * a[i][col];
26
            for (j = col + 1; j < var; j++) a[i][j] -= a[k][j] * a[i][col];</pre>
27
            a[i][col] = 0;
28
29
          }
      }
30
31
      for (col = equ - 1, k = var - 1; ~col; --col, --k) {
32
        if (fabs(a[col][k]) > 0) {
33
          for (i = 0; i < k; ++i) {
34
            x[i] = x[k] * a[i][col];
35
            for (j = col + 1; j < var; j++) a[i][j] -= a[k][j] * a[i][col];</pre>
36
            a[i][col] = 0;
37
38
          }
39
        }
      }
40
41
42
     return 1;
43 }
   1.12 exgcd
   int exgcd(int a, int b, int &x, int &y) {
     if (b == 0) return x = 1, y = 0, a;
     int g = exgcd(b, a \% b, y, x);
     y = a / b * x;
5
     return g;
6 }
```

1.13 china

```
int china(int n, int *a, int *m) {
     int lcm = 1, res = 0;
     for (int i = 0; i < n; ++i) lcm *= m[i];</pre>
3
4
     for (int i = 0; i < n; ++i) {
5
       int t = lcm / m[i], x, y;
6
       exgcd(t, m[i], x, y);
       x = (x \% m[i] + m[i]) \% m[i];
7
       res = (res + 1LL * t * x) % lcm;
8
9
10
     return res;
  }
11
   1.14 LinearSieve
   const int MAXN = 1e7 + 5;
2
   bool vis[MAXN];
3
   int prime[MAXN / 10], prime_cnt;
   int fac[MAXN], e[MAXN], d[MAXN], mu[MAXN], phi[MAXN];
   // e 质因子最高次数, d 因数个数
   void sieve() {
7
     fac[1] = 1, e[1] = 0, d[1] = 1, mu[1] = 1, phi[1] = 1;
8
9
     for (int i = 2; i < MAXN; ++i) {</pre>
       if (!vis[i]) {
10
         prime[prime_cnt++] = i;
11
          fac[i] = i, e[i] = 1, d[i] = 2, mu[i] = -1, phi[i] = i - 1;
12
13
       for (int j = 0; j < prime_cnt; ++j) {</pre>
14
         int t = prime[j] * i;
15
         if (t >= MAXN) { break; }
16
         vis[t] = true;
17
          fac[t] = prime[j];
18
         if (i % prime[j] == 0) {
19
20
           e[t] = e[i] + 1;
21
           d[t] = d[i] / (e[i] + 1) * (e[t] + 1);
           mu[t] = 0;
22
           phi[t] = phi[i] * prime[j];
23
24
           break:
          } else {
25
26
            e[t] = 1:
           d[t] = d[i] * 2;
27
           mu[t] = -mu[i];
28
29
           phi[t] = phi[i] * (prime[j] - 1);
30
       }
31
32
33
   1.15 LinearRecurrence
1 struct LinearRecurrence {
2
     using int64 = long long;
3
     using vec = std::vector<int64>;
     static void extand(vec &a, size_t d, int64 value = 0) {
```

```
if (d <= a.size()) return;</pre>
6
7
        a.resize(d, value);
8
9
      static vec BerlekampMassey(const vec &s, int64 mod) {
10
        std::function<int64(int64)> inverse = [&](int64 a) {
11
          return a == 1 ? 1 : (int64)(mod - mod / a) * inverse(mod % a) % mod;
12
13
        };
        vec A = \{1\}, B = \{1\};
14
        int64 b = s[0];
15
        for (size_t i = 1, m = 1; i < s.size(); ++i, m++) {</pre>
16
17
          int64 d = 0;
          for (size_t j = 0; j < A.size(); ++j) \{ d += A[j] * s[i - j] % mod; \}
18
          if (!(d %= mod)) continue;
19
          if (2 * (A.size() - 1) <= i) {</pre>
20
            auto temp = A;
21
            extand(A, B.size() + m);
22
23
            int64 coef = d * inverse(b) % mod;
24
            for (size_t j = 0; j < B.size(); ++j) {</pre>
25
              A[j + m] = coef * B[j] % mod;
26
              if (A[j + m] < 0) A[j + m] += mod;
27
            B = temp, b = d, m = 0;
28
29
          } else {
30
            extand(A, B.size() + m);
            int64 coef = d * inverse(b) % mod;
31
            for (size_t j = 0; j < B.size(); ++j) {</pre>
32
              A[j + m] -= coef * B[j] % mod;
33
              if (A[j + m] < 0) A[j + m] += mod;
34
35
36
          }
37
38
        return A;
39
40
      static void exgcd(int64 a, int64 b, int64 &g, int64 &x, int64 &y) {
41
42
43
          x = 1, y = 0, g = a;
44
        else {
          exgcd(b, a % b, g, y, x);
45
          y = x * (a / b);
46
        }
47
      }
48
49
      static int64 crt(const vec &c, const vec &m) {
50
        int n = c.size();
51
52
        int64 M = 1, ans = 0;
        for (int i = 0; i < n; ++i) M *= m[i];
53
        for (int i = 0; i < n; ++i) {
54
          int64 x, y, g, tm = M / m[i];
55
          exgcd(tm, m[i], g, x, y);
56
57
          ans = (ans + tm * x * c[i] % M) % M;
58
        }
        return (ans + M) % M;
59
60
61
62
      static vec ReedsSloane(const vec &s, int64 mod) {
63
        auto inverse = [](int64 a, int64 m) {
          int64 d, x, y;
64
```

```
65
           exgcd(a, m, d, x, y);
           return d == 1 ? (x % m + m) % m : -1;
66
67
         auto L = [](const vec &a, const vec &b) {
68
           int da = (a.size() > 1 || (a.size() == 1 && a[0])) ? a.size() - 1 : -1000;
69
           int db = (b.size() > 1 || (b.size() == 1 && b[0])) ? b.size() - 1 : -1000;
70
           return std::max(da, db + 1);
71
72
         };
         auto prime_power = [&](const vec &s, int64 mod, int64 p, int64 e) {
73
           // linear feedback shift register mod p^e, p is prime
74
           std::vector<vec> a(e), b(e), an(e), bn(e), ao(e), bo(e);
75
76
           vec t(e), u(e), r(e), to(e, 1), uo(e), pw(e + 1);
77
           pw[0] = 1;
78
           for (int i = pw[0] = 1; i \le e; ++i) pw[i] = pw[i - 1] * p;
79
           for (int64 i = 0; i < e; ++i) {
80
             a[i] = \{pw[i]\}, an[i] = \{pw[i]\};
81
             b[i] = \{0\}, bn[i] = \{s[0] * pw[i] % mod\};
82
             t[i] = s[0] * pw[i] % mod;
83
             if (t[i] == 0) {
84
               t[i] = 1, u[i] = e;
85
             } else {
86
               for (u[i] = 0; t[i] \% p == 0; t[i] /= p, ++u[i])
87
88
89
             }
90
           for (size_t k = 1; k < s.size(); ++k) {</pre>
91
             for (int g = 0; g < e; ++g) {
92
               if (L(an[g], bn[g]) > L(a[g], b[g])) {
93
                 ao[g] = a[e - 1 - u[g]];

bo[g] = b[e - 1 - u[g]];
94
95
                 to[g] = t[e - 1 - u[g]];
96
                 uo[g] = u[e - 1 - u[g]];
97
                 r[g] = k - 1;
98
99
               }
             }
100
             a = an, b = bn;
101
102
             for (int o = 0; o < e; ++o) {
               int64 d = 0;
103
               for (size_t i = 0; i < a[o].size() && i <= k; ++i) {</pre>
104
                 d = (d + a[o][i] * s[k - i]) % mod;
105
106
               if (d == 0) {
107
                 t[o] = 1, u[o] = e;
108
109
               } else {
                 for (u[o] = 0, t[o] = d; t[o] % p == 0; t[o] /= p, ++u[o])
110
111
                 int g = e - 1 - u[o];
112
                 if (L(a[g], b[g]) == 0) {
113
                   extand(bn[o], k + 1);
114
115
                   bn[o][k] = (bn[o][k] + d) \% mod;
                 } else {
116
117
                   int64 coef =
                        t[o] * inverse(to[g], mod) % mod * pw[u[o] - uo[g]] % mod;
118
                   int m = k - r[g];
119
                   extand(an[o], ao[g].size() + m);
120
121
                   extand(bn[o], bo[g].size() + m);
122
                   for (size_t i = 0; i < ao[g].size(); ++i) {</pre>
123
                      an[o][i + m] -= coef * ao[g][i] % mod;
```

```
if (an[o][i + m] < 0) an[o][i + m] += mod;
124
125
                   while (an[o].size() && an[o].back() == 0) an[o].pop_back();
126
                   for (size_t i = 0; i < bo[g].size(); ++i) {</pre>
127
128
                     bn[o][i + m] = coef * bo[g][i] % mod;
129
                     if (bn[o][i + m] < 0) bn[o][i + m] -= mod;
130
                   while (bn[o].size() && bn[o].back() == 0) bn[o].pop_back();
131
132
                 }
133
               }
134
            }
135
           }
136
          return std::make_pair(an[0], bn[0]);
137
138
        std::vector<std::tuple<int64, int64, int>> fac;
139
        for (int64 i = 2; i * i <= mod; ++i)</pre>
140
           if \pmod{\%} i == 0 {
141
             int64 cnt = 0, pw = 1;
142
             while (mod \% i == 0) mod /= i, ++cnt, pw *= i;
143
             fac.emplace_back(pw, i, cnt);
144
145
        if (mod > 1) fac.emplace_back(mod, mod, 1);
146
147
        std::vector<vec> as;
148
        size_t n = 0:
        for (auto &&x : fac) {
149
           int64 mod, p, e;
150
151
           vec a, b;
           std::tie(mod, p, e) = x;
152
153
           auto ss = s;
154
           for (auto &&x : ss) x %= mod;
           std::tie(a, b) = prime_power(ss, mod, p, e);
155
           as.emplace_back(a);
156
           n = std::max(n, a.size());
157
158
        }
        vec a(n), c(as.size()), m(as.size());
159
160
         for (size_t i = 0; i < n; ++i) {</pre>
161
           for (size_t j = 0; j < as.size(); ++j) {</pre>
             m[j] = std::get<0>(fac[j]);
162
163
             c[j] = i < as[j].size() ? as[j][i] : 0;
164
165
           a[i] = crt(c, m);
        }
166
167
        return a;
168
169
170
      LinearRecurrence(const vec &s, const vec &c, int64 mod)
           : init(s), trans(c), mod(mod), m(s.size()) {}
171
172
173
      LinearRecurrence(const vec &s, int64 mod, bool is_prime = true) : mod(mod) {
174
        vec A = is_prime ? BerlekampMassey(s, mod) : ReedsSloane(s, mod);
175
        if (A.empty()) A = \{0\};
176
        m = A.size() - 1;
177
        trans.resize(m);
        for (int i = 0; i < m; ++i) { trans[i] = (mod - A[i + 1]) % mod; }
178
179
        std::reverse(trans.begin(), trans.end());
180
         init = {s.begin(), s.begin() + m};
181
182
```

```
int64 calc(int64 n) {
183
         if (mod == 1) return 0;
184
         if (n < m) return init[n];</pre>
185
         vec v(m), u(m \ll 1);
186
         int msk = !!n;
187
         for (int64 m = n; m > 1; m >>= 1) msk <<= 1;</pre>
188
         v[0] = 1 \% mod;
189
         for (int x = 0; msk; msk >>= 1, x <<= 1) {
190
           std::fill_n(u.begin(), m * 2, 0);
191
           x = !!(n \& msk);
192
           if(x < m)
193
194
             u[x] = 1 \% mod;
           else { // can be optimized by fft/ntt
195
             for (int i = 0; i < m; ++i) {
196
               for (int j = 0, t = i + (x \& 1); j < m; ++j, ++t) {
197
                 u[t] = (u[t] + v[i] * v[j]) % mod;
198
               }
199
             }
200
             for (int i = m * 2 - 1; i >= m; --i) {
201
               for (int j = 0, t = i - m; j < m; ++j, ++t) {
202
                 u[t] = (u[t] + trans[j] * u[i]) % mod;
203
               }
204
             }
205
206
207
           v = \{u.begin(), u.begin() + m\};
         }
208
         int64 ret = 0;
209
         for (int i = 0; i < m; ++i) { ret = (ret + v[i] * init[i]) % mod; }</pre>
210
211
         return ret;
212
213
214
      vec init, trans;
215
       int64 mod;
       int m;
216
217 };
```

2 Dynamic Programming

2.1 斜率优化

```
1 // 树上斜率优化
   // 定义dpi 表示i节点传递到根节点的最短耗时,规定dproot=-P。
   // 有如下转移方程dpu=dpv+dist(u,v)^2+P,v is an ancestor of u.
5
   #include <bits/stdc++.h>
   using namespace std;
6
7
8
   typedef long long ll;
9 typedef pair<int, int> pii;
10 const int MAXN = 1e5 + 5;
12 vector<pii> adj[MAXN];
13 ll dp[MAXN], d[MAXN];
int n, p, q[MAXN], head, tail;
16 inline ll S(int a, int b) { return (d[b] - d[a]) << 1; }
17 inline ll G(int a, int b) { return dp[b] - dp[a] + d[b] * d[b] - d[a] * d[a]; }</pre>
18
```

```
void dfs(int u, int from) {
     vector<int> dhead, dtail;
20
21
      if (u ^ 1) {
        while (head + 2 <= tail &&
22
               S(q[head + 1], q[head]) * d[u] \leftarrow G(q[head + 1], q[head]))
23
          dhead.push_back(q[head++]);
24
25
        int v = q[head];
        dp[u] = dp[v] + p + (d[u] - d[v]) * (d[u] - d[v]);
26
27
     while (head + 2 <= tail &&</pre>
28
29
             G(u, q[tail - 1]) * S(q[tail - 1], q[tail - 2]) <=
30
                 G(q[tail - 1], q[tail - 2]) * S(u, q[tail - 1]))
        dtail.push_back(q[--tail]);
31
     q[tail++] = u;
32
      for (pii &e : adj[u]) {
33
        if (e.first == from) continue;
34
        d[e.first] = d[u] + e.second;
35
36
        dfs(e.first, u);
37
     }
38
     --tail;
     for (int i = dtail.size() - 1; ~i; --i) q[tail++] = dtail[i];
39
      for (int i = dhead.size() - 1; ~i; --i) q[--head] = dhead[i];
40
41 }
42
43
   void solve() {
44
     cin >> n >> p;
      for (int i = 1; i <= n; ++i) adj[i].clear();</pre>
45
      for (int i = 1, u, v, w; i < n; ++i) {
46
        cin >> u >> v >> w;
47
        adj[u].emplace_back(v, w);
48
49
        adj[v].emplace_back(u, w);
50
     dp[1] = -p;
51
     head = tail = 0;
52
     dfs(1, 1);
53
54
55
     Il ans = 0;
56
      for (int i = 1; i \le n; ++i)
        if (dp[i] > ans) ans = dp[i];
57
     cout << ans << '\n';
58
   }
59
60
   int main() {
61
     // freopen("in.txt", "r", stdin);
62
     ios::sync_with_stdio(false);
63
     cin.tie(0);
64
65
66
     int o_o;
     for (cin >> o_o; o_o; --o_o) solve();
67
68
69
     return 0;
70 }
```

3 Data Structure

3.1 splay

1 #include <algorithm>

```
2 #include <cstdio>
3 #include <cstring>
    #include <iostream>
    using namespace std;
    const int MAXN = 2e5 + 10;
7
8
   struct Node {
9
       long long sum;
10
       int id, val, lazy, size;
11
       Node *fa, *ch[2];
13 } node_pool[MAXN], *pool_it, *root, *nil;
14
15 Node *newnode(int id, int val) {
       pool_it->id = id;
16
       pool_it->lazy = 0;
17
       pool_it->size = 1;
18
19
       pool_it->sum = pool_it->val = val;
       pool_it\rightarrow fa = pool_it\rightarrow ch[0] = pool_it\rightarrow ch[1] = nil;
20
21
       return pool_it++;
22 }
23
24 void maintain(Node *u) {
       if (u == nil) { return; }
26
       u \rightarrow size = u \rightarrow ch[0] \rightarrow size + u \rightarrow ch[1] \rightarrow size + 1;
       u -> sum = u -> ch[0] -> sum + u -> ch[1] -> sum + u -> val;
27
28 }
29
    void push_down(Node *u) {
30
       if (u->lazy) {
31
          if (u->ch[0] != nil) {
32
33
            u \rightarrow ch[0] \rightarrow val += u \rightarrow lazy;
            u\rightarrow ch[0]\rightarrow sum += 1LL * u\rightarrow ch[0]\rightarrow size * u\rightarrow lazy;
34
            u\rightarrow ch[0]\rightarrow lazy += u\rightarrow lazy;
35
36
          }
          if (u->ch[1] != nil) {
37
38
            u\rightarrow ch[1]\rightarrow val += u\rightarrow lazy;
39
            u \rightarrow ch[1] \rightarrow sum += 1LL * u \rightarrow ch[1] \rightarrow size * u \rightarrow lazy;
40
            u\rightarrow ch[1]\rightarrow lazy += u\rightarrow lazy;
          }
41
          u \rightarrow lazy = 0;
42
43
44
45
    inline void rot(Node *u) {
46
       Node *f = u \rightarrow fa, *ff = f \rightarrow fa;
47
       int d = u == f -> ch[1];
48
       push_down(f);
49
       push_down(u);
50
       if ((f->ch[d] = u->ch[d \land 1]) != nil) f->ch[d]->fa = f;
52
       if ((u-)fa = ff) != nil) ff->ch[f == ff->ch[1]] = u;
53
       f\rightarrow fa = u;
       u\rightarrow ch[d \land 1] = f;
54
       maintain(f);
55
       maintain(u);
56
57
   }
58
    void splay(Node *u, Node *target) {
59
       for (Node *f; u->fa != target; rot(u))
60
```

```
if ((f = u \rightarrow fa) \rightarrow fa != target) {
61
62
            ((u == f->ch[1]) \land (f == f->fa->ch[1])) ? rot(u) : rot(f);
63
       if (target == nil) root = u;
 64
65
66
     inline void insert(int id, int val) {
67
       if (root == nil) {
68
          root = newnode(id, val);
69
 70
          return;
 71
 72
       Node *u = root;
       while (u != nil) {
 73
          int d = id >= u -> id;
 74
          ++u->size;
 75
          push_down(u);
 76
          u->sum += val;
 77
          if (u->ch[d] != nil) {
 78
            u = u \rightarrow ch[d];
 79
 80
          } else {
            u->ch[d] = newnode(id, val);
 81
            u\rightarrow ch[d]\rightarrow fa = u;
 82
            u = u \rightarrow ch[d];
 83
 84
            break;
 85
          }
       }
 86
 87
       splay(u, nil);
     }
 88
 89
     inline Node *find_pred(int id) {
 90
 91
       Node *u = root, *ret = nil;
92
       while (u != nil) {
          push_down(u);
93
          if (u->id < id) {</pre>
94
95
            ret = u;
            u = u \rightarrow ch[1];
96
 97
          } else {
98
            u = u \rightarrow ch[0];
99
100
       }
101
       return ret;
102
103
    inline Node *find_succ(int id) {
105
       Node *u = root, *ret = nil;
106
       while (u != nil) {
107
          push_down(u);
          if (u->id > id) {
108
            ret = u;
109
110
            u = u \rightarrow ch[0];
111
          } else {
112
            u = u \rightarrow ch[1];
113
          }
       }
114
115
       return ret;
116
117
118
     Node *find_kth(int k) {
119
       Node *u = root;
```

```
while (u != nil) {
120
121
         push_down(u);
         if (u->ch[0]->size + 1 == k) {
122
123
           splay(u, nil);
124
           return u;
125
         if (u->ch[0]->size >= k) {
126
           u = u \rightarrow ch[0];
127
         } else {
128
           k = u - ch[0] - size + 1;
129
130
           u = u \rightarrow ch[1];
131
         }
       }
132
133
      return nil;
134
135
    Node *range(int l, int r) {
136
      Node *pred = find_pred(l);
137
      Node *succ = find_succ(r);
138
139
       splay(pred, nil);
140
       splay(succ, root);
141
       push_down(pred);
142
143
      push_down(succ);
144
      return root->ch[1]->ch[0];
145 }
146
    int main() {
147
148
       // freopen("input.txt", "r", stdin);
149
150
151
       ios::sync_with_stdio(false);
       cin.tie(0);
152
       cout.tie(0);
153
154
       int n;
155
156
      cin >> n;
157
       pool_it = node_pool;
158
159
      nil = pool_it++;
      nil->ch[0] = nil->ch[1] = nil->fa = nil;
160
      nil->id = -1;
161
      nil->val = 0;
162
163
       root = nil;
164
       insert(-0x3fffffff, 0);
165
166
       insert(0x3fffffff, 0);
167
168
       return 0;
169
   }
    3.2 lct
    struct LCT {
 1
       struct node {
 2
 3
         int val, add;
         node *fa, *ch[2];
 4
         void modify(const int &x) {
```

```
6
           val += x;
7
           add += x;
8
      } node_mset[MaxS], *cnode, *null;
9
10
      LCT() {
         cnode = node_mset;
11
12
         null = cnode++;
         *null = (node){0, 0, null, {null, null}};
13
      }
14
      inline node *newnode() {
15
         *cnode = (node){0, 0, null, {null, null}};
16
17
         return cnode++;
18
      inline bool isrt(node *u) const {
19
         return (u-fa-ch[0] != u) \&\& (u-fa-ch[1] != u);
20
21
      inline bool which(node *u) const { return u->fa->ch[1] == u; }
22
      void push_down(node *u) {
23
         if (!isrt(u)) push_down(u->fa);
24
         if (u->add) {
25
           u \rightarrow ch[0] \rightarrow modify(u \rightarrow add);
26
27
           u \rightarrow ch[1] \rightarrow modify(u \rightarrow add);
           u->add = 0;
28
29
         }
30
      }
      inline void rotate(node *u) {
31
         node *f = u - > fa;
32
         int d = which(u);
33
         f->ch[d] = u->ch[d ^ 1];
34
         f \rightarrow ch[d] \rightarrow fa = f;
35
36
         u - ch[d \land 1] = f;
37
         u\rightarrow fa = f\rightarrow fa;
         if (!isrt(f)) f->fa->ch[which(f)] = u;
38
         f\rightarrow fa = u;
39
40
      inline void splay(node *u) {
41
42
         push_down(u);
43
         for (node *f; !isrt(u); rotate(u))
           if (!isrt(f = u->fa)) rotate(which(u) == which(f) ? f : u);
44
45
      inline void access(node *x) {
46
         for (node *y = null; x = null; x = x \rightarrow fa) {
47
48
           splay(x);
49
           x->ch[1] = y;
50
           y = x;
         }
51
52
      inline void cut(node *u) {
53
         access(u);
54
55
         splay(u);
56
         u\rightarrow ch[0]\rightarrow fa = null:
57
         u \rightarrow ch[0] = null;
58
      inline void link(node *u, node *v) {
59
         cut(u);
60
61
         u\rightarrow fa = v;
62
63
    } tree;
```

3.3 kdtree

```
1 // 寻找近点
  #include <bits/stdc++.h>
   using namespace std;
5 const int MAXN = 2e5 + 5;
   typedef long long ll;
6
7
  namespace KD_Tree {
8
9
10 const int DIM = 2;
11
12 inline ll sqr(int x) { return 1LL * x * x; }
13
   struct Point {
14
     int x[DIM], id, c;
15
16
     ll dist2(const Point &b) const {
17
        return sqr(x[0] - b.x[0]) + sqr(x[1] - b.x[1]);
18
19
20
   };
   struct QNode {
21
22
     Point p;
     ll dis2;
23
24
25
     QNode() {}
26
     QNode(Point _p, ll _dis2) : p(_p), dis2(_dis2) {}
27
28
     bool operator<(const QNode &b) const {</pre>
       return dis2 < b.dis2 || (dis2 == b.dis2 && p.id < b.p.id);</pre>
29
30
     }
31 } ans;
32 struct cmpx {
33
     int div;
     cmpx(int _div) : div(_div) {}
34
35
     bool operator()(const Point &a, const Point &b) {
36
        for (int i = 0; i < DIM; ++i)
          if (a.x[(i + div) \% DIM] != b.x[(i + div) \% DIM])
37
            return a.x[(i + div) \% DIM] < b.x[(i + div) \% DIM];
39
        return true;
40
     }
41
   };
42
   bool cmp(const Point &a, const Point &b, int div) {
43
44
     cmpx cp = cmpx(div);
     return cp(a, b);
45
   }
46
47
48 struct Node {
49
     Point e;
     Node *lc, *rc;
50
     int div;
51
52 } node_pool[MAXN], *tail, *root;
   void init() { tail = node_pool; }
  Node *build(Point *a, int l, int r, int div) {
     if (l >= r) return nullptr;
55
     Node *p = tail++;
56
     p\rightarrow div = div;
```

```
int mid = (l + r) \gg 1;
 58
        nth_element(a + l, a + mid, a + r, cmpx(div));
 59
        p\rightarrow e = a[mid];
 60
        p->lc = build(a, l, mid, div ^ 1);
 61
 62
        p\rightarrow rc = build(a, mid + 1, r, div \wedge 1);
 63
        return p;
 64 }
     void search(Point p, Node *x, int div) {
 65
        if (!x) return;
 66
        if (cmp(p, x->e, div)) {
 67
 68
          search(p, x \rightarrow lc, div ^ 1);
 69
          if (ans.dis2 == -1) {
             if (x\rightarrow e.c \le p.c) ans = QNode(x\rightarrow e, p.dist2(x\rightarrow e));
 70
             search(p, x \rightarrow rc, div ^ 1);
 71
          } else {
 72
             QNode temp(x\rightarrow e, p.dist2(x\rightarrow e));
 73
             if (x->e.c \le p.c \&\& temp < ans) ans = temp;
 74
 75
             if (\operatorname{sqr}(x->e.x[\operatorname{div}] - p.x[\operatorname{div}]) \le \operatorname{ans.dis2}) search(p, x->rc, div ^ 1);
 76
          }
 77
        } else {
          search(p, x->rc, div ^ 1);
 78
 79
          if (ans.dis2 == -1) {
             if (x\rightarrow e.c \le p.c) ans = QNode(x\rightarrow e, p.dist2(x\rightarrow e));
 80
 81
             search(p, x->lc, div ^ 1);
 82
          } else {
             QNode temp(x\rightarrow e, p.dist2(x\rightarrow e));
 83
 84
             if (x\rightarrow e.c \le p.c \&\& temp < ans) ans = temp;
             if (\operatorname{sqr}(x\rightarrow e.x[\operatorname{div}] - p.x[\operatorname{div}]) \leftarrow \operatorname{ans.dis2}) \operatorname{search}(p, x\rightarrow lc, \operatorname{div} 1);
 85
 86
        }
 87
 88
     }
     void search(Point p) {
 89
 90
        ans.dis2 = -1;
        search(p, root, 0);
 91
 92
 93 } // namespace KD_Tree
 94
 95
     void solve() {
        static KD_Tree::Point p[MAXN];
 96
        int n, m;
 97
        cin >> n >> m;
 98
        for (int i = 0; i < n; ++i) {
99
100
          p[i].id = i;
101
          cin >> p[i].x[0] >> p[i].x[1] >> p[i].c;
102
103
        KD_Tree::init();
        KD_Tree::root = KD_Tree::build(p, 0, n, 0);
104
105
        for (KD_Tree::Point q; m; --m) {
106
107
          cin \gg q.x[0] \gg q.x[1] \gg q.c;
108
          KD_Tree::search(q);
109
          cout << KD_Tree::ans.p.x[0] << ' ' << KD_Tree::ans.p.x[1] << ' '</pre>
110
                 << KD_Tree::ans.p.c << '\n';
111
        }
112
     }
     int main() {
113
114
        ios::sync_with_stdio(false);
115
        cin.tie(nullptr);
116
```

```
117
       int o_o;
118
       for (cin >> o_o; o_o; --o_o) solve();
119
120
      return 0;
121 }
122
123
    // 寻找远点
124 inline void cmin(int &a, int b) { b < a ? a = b : 1; }
125 inline void cmax(int &a, int b) { a < b ? a = b : 1; }</pre>
126 inline int ibs(int a) { return a < 0 ? -a : a; }
    struct D {
128
       int d[2], mx0, mx1, mi0, mi1;
      D *l, *r;
129
130 } t[N], *rt;
    int cpd, ans;
131
    inline bool cmp(const D &a, const D &b) {
      return (a.d[cpd] ^ b.d[cpd]) ? a.d[cpd] < b.d[cpd]</pre>
133
134
                                       : a.d[cpd ^ 1] < b.d[cpd ^ 1];
135
    }
    inline void kd_upd(D *u) {
136
       if (u->1) {
137
         cmax(u->mx0, u->l->mx0);
138
         cmax(u->mx1, u->l->mx1);
139
140
         cmin(u->mi0, u->l->mi0);
141
         cmin(u->mi1, u->l->mi1);
142
       if (u->r) {
143
         cmax(u->mx0, u->r->mx0);
144
         cmax(u->mx1, u->r->mx1);
145
         cmin(u->mi0, u->r->mi0);
146
         cmin(u->mi1, u->r->mi1);
147
148
       }
149
    }
    D *kd_bld(int l, int r, int d) {
150
       int m = l + r \gg 1;
151
       cpd = d;
152
153
       std::nth_element(t + l + 1, t + m + 1, t + r + 1, cmp);
154
       t[m].mx0 = t[m].mi0 = t[m].d[0];
       t[m].mx1 = t[m].mi1 = t[m].d[1];
155
       if (l ^ m) t[m].l = kd_bld(l, m - 1, d ^ 1);
156
       if (r ^ m) t[m].r = kd_bld(m + 1, r, d ^ 1);
157
      kd_upd(t + m);
158
       return t + m;
159
160 }
    inline void kd_ins(D *ne) {
161
      int cd = 0;
162
163
      D *u = rt;
       while (true) {
164
         cmax(u->mx0, ne->mx0), cmin(u->mi0, ne->mi0);
165
166
         cmax(u\rightarrow mx1, ne\rightarrow mx1), cmin(u\rightarrow mi1, ne\rightarrow mi1);
167
         if (ne->d[cd] < u->d[cd]) {
168
           if (u->l)
169
             u = u \rightarrow l;
170
           else {
171
             u \rightarrow l = ne;
172
             return;
173
174
         } else {
175
           if (u->r)
```

```
176
             u = u \rightarrow r;
177
           else {
178
             u\rightarrow r = ne;
179
             return;
180
181
         cd ^= 1;
182
183
184
    }
    inline int dist(int x, int y, D *u) {
185
       int r = 0;
186
187
       if (x < u->mi0)
188
         r = u - mi0 - x;
       else if (x > u->mx0)
189
190
        r = x - u - mx0;
       if (y < u->mi1)
191
         r += u->mi1 - y;
192
193
       else if (y > u-mx1)
194
         r += y - u -> mx1;
195
       return r;
196 }
    inline void kd_quy(D *u, const int &x, const int &y) {
197
198
       int dl, dr, d0;
       d0 = ibs(u->d[0] - x) + ibs(u->d[1] - y);
199
200
       if (d0 < ans) ans = d0;
       dl = u -> l ? dist(x, y, u -> l) : inf;
201
       dr = u \rightarrow r ? dist(x, y, u \rightarrow r) : inf;
202
       if (dl < dr) {
203
         if (dl < ans) kd_quy(u->l, x, y);
204
205
         if (dr < ans) kd_quy(u->r, x, y);
206
       } else {
         if (dr < ans) kd_quy(u->r, x, y);
207
208
         if (dl < ans) kd_quy(u->l, x, y);
209
210 }
    3.4 zkw
    int tree[MAXN * 2], pre;
 2
 3
    void init(int n, int *a) {
 4
      memset(tree, 0, sizeof(tree));
 5
       for (pre = 1; pre <= n; pre <<= 1) {}</pre>
       for (int i = 1; i <= n; ++i) tree[i + pre] = a[i];</pre>
 6
 7
       for (int i = pre; i; --i) tree[i] = max(tree[i << 1], tree[i << 1 | 1]);
    }
 8
 9
    void update(int pos, const int &val) {
10
11
       tree[pos += pre] = val;
12
       for (pos >>= 1; pos; pos >>= 1)
13
         tree[pos] = max(tree[pos << 1], tree[pos << 1 | 1]);
14
    }
15
16
    int query(int s, int t) {
17
       int res = 0;
       for (s += pre - 1, t += pre + 1; s ^ t ^ 1; s >>= 1, t >>= 1) {
18
19
         if (\sims & 1) res = max(res, tree[s \wedge 1]);
         if (t & 1) res = max(res, tree[t ^ 1]);
20
```

```
21
      }
22
      return res;
23 }
        String
   4.1 mancher
   void mancher(char *s, int n) {
      str[0] = '~';
      str[1] = '!';
3
      for (int i = 1; i <= n; ++i) {</pre>
4
        str[i * 2] = s[i];
5
        str[i * 2 + 1] = '!';
6
7
8
      for (int i = 1, j = 0; i \le n; ++i) {
9
        if (p[j] + j > i) {
          p[i] = min(p[2 * j - i], p[j] + j - i);
10
        } else {
11
          p[i] = 1;
12
13
        while (str[i + p[i]] == str[i - p[i]]) { ++p[i]; }
14
15
        if (i + p[i] > j + p[j]) { j = i; }
16
   }
17
   4.2 SAM
   struct Node {
      int len;
3
      Node *link, *ch[ALPHABET_SIZE];
4
   } node_pool[MAXS], *node_it, *root, *last;
5
6
   Node *new_node(int len) {
7
     node_it->len = len;
8
      return node_it++;
9 }
10 void sam_init() {
      node_it = node_pool;
11
12
      last = root = new_node(0);
13 }
   void sam_extend(int c, int val) {
      Node *p = last, *np = new_node(p->len + 1);
15
16
      for (last = np; p && !p->ch[c]; p = p->link) p->ch[c] = np;
      if (!p) {
17
18
        np->link = root;
      } else {
19
        Node *q = p->ch[c];
20
        if (q->len == p->len + 1) {
21
22
          np \rightarrow link = q;
        } else {
23
24
          Node *nq = new_node(p->len + 1);
25
          memcpy(nq->ch, q->ch, sizeof(q->ch));
26
          nq - link = q - link;
27
          q->link = np->link = nq;
28
          for (; p \&\& p \rightarrow ch[c] == q; p = p \rightarrow link) p \rightarrow ch[c] = nq;
29
```

```
30
31
   }
   4.3 ACam
   int ch[MAX_NODE][26], fail[MAX_NODE], dep[MAX_NODE], node_c;
3
   int add_char(int u, int id) {
     if (ch[u][id] < 0) ch[u][id] = node\_c++;
5
     return ch[u][id];
6
   void build_acam() {
7
     queue<int> que;
8
      for (int i = 0; i < 26; ++i)
9
        if (~ch[0][i]) {
10
          que.push(ch[0][i]);
          fail[ch[0][i]] = 0;
12
          dep[ch[0][i]] = 1;
13
        } else {
14
15
          ch[0][i] = 0;
        }
16
17
     while (!que.empty()) {
18
        int u = que.front();
        que.pop();
19
        for (int i = 0; i < 26; ++i)
20
21
          if (~ch[u][i]) {
            que.push(ch[u][i]);
22
            fail[ch[u][i]] = ch[fail[u]][i];
23
24
            dep[ch[u][i]] = dep[u] + 1;
25
          } else {
            ch[u][i] = ch[fail[u]][i];
26
27
28
     for (int i = 1; i < node_c; ++i) adj[fail[i]].push_back(i);</pre>
29
   }
30
   4.4 后缀数组(倍增)
   char s[MAXN];
   int sa[MAXN], x[MAXN], y[MAXN], c[MAXN];
   int rk[MAXN], height[MAXN], st[17][MAXN], lg[MAXN];
3
 4
   bool cmp(int *r, int i, int j, int l) {
 5
6
     return r[i] == r[j] \&\& r[i + l] == r[j + l];
   }
7
   void da(char *s, int n, int m) {
8
     int i, j, p;
9
10
      for (i = 0; i < m; ++i) c[i] = 0;
      for (i = 0; i < n; ++i) ++c[x[i] = s[i]];
11
      for (i = 1; i < m; ++i) c[i] += c[i - 1];
      for (i = n - 1; \sim i; --i) sa[--c[x[i]]] = i;
13
      for (p = j = 1; p < n; j <<= 1, m = p) {
14
        for (p = 0, i = n - j; i < n; ++i) y[p++] = i;
15
        for (i = 0; i < n; ++i)
16
17
         if (sa[i] >= j) y[p++] = sa[i] - j;
        for (i = 0; i < m; ++i) c[i] = 0;
18
        for (i = 0; i < n; ++i) ++c[x[y[i]]];
19
```

```
for (i = 1; i < m; ++i) c[i] += c[i - 1];
20
       for (i = n - 1; \sim i; --i) sa[--c[x[y[i]]]] = y[i];
21
       for (swap(x, y), p = 1, x[sa[0]] = 0, i = 1; i < n; ++i)
22
23
         x[sa[i]] = cmp(y, sa[i], sa[i-1], j) ? p - 1 : p++;
24
   }
25
26
   void get_height(char *s, int n) {
27
28
     int i, j, k;
29
     for (i = 0; i < n; ++i) rk[sa[i]] = i;</pre>
     for (i = k = height[rk[0]] = 0; i < n; height[rk[i++]] = k)</pre>
31
       if (rk[i])
          for (k > 0 ? --k : 0, j = sa[rk[i] - 1]; s[i + k] == s[j + k]; ++k) {}
32
   }
33
34
35 void init_st_table(int n) {
     int lgn = lg[n];
36
37
     for (int i = 0; i < n; ++i) st[0][i] = height[i];</pre>
     for (int i = 1; i <= lgn; ++i)</pre>
38
       for (int j = 0; j + (1 << i - 1) < n; ++j)
39
          st[i][j] = min(st[i-1][j], st[i-1][j+(1 << i-1)]);
40
41 }
42
   int lcp(int i, int j) {
44
     if (i > j) swap(i, j);
45
     ++i;
     int lgl = lg[j - i + 1];
46
47
     return min(st[lgl][i], st[lgl][j - (1 << lgl) + 1]);</pre>
48 }
   4.5 kmp
void get_next(char *S, int *nxt, int n) {
     nxt[0] = -1;
2
3
     int j = -1;
     for (int i = 1; i < n; ++i) {
4
       while ((\sim j) \&\& S[j + 1] != S[i]) j = nxt[j];
5
       nxt[i] = (S[j + 1] == S[i]) ? (++j) : j;
6
7
     }
   }
8
9
int pattern(char *S, char *T, int *nxt, int n, int m) {
     int j = -1;
     for (int i = 0; i < m; ++i) {
13
       while ((\sim j) \&\& S[j + 1] != T[i]) j = nxt[j];
14
       j += S[j + 1] == T[i];
       if (j == n - 1) return i - n + 1;
15
     }
16
17
     return -1;
18
   }
   4.6 exkmp
1 // next[i]:x[i...m-1] 与 x[0...m-1] 的最长公共前缀
2 // extend[i]:y[i...n-1] 与 x[0...m-1] 的最长公共前缀
3 void prework(char x[], int m, int next[]) {
     next[0] = m;
```

```
int j = 0;
5
     while (j + 1 < m \&\& x[j] == x[j + 1]) ++j;
6
7
     next[1] = j;
8
     int k = 1;
9
     for (int i = 2; i < m; ++i) {
       int p = next[k] + k - 1;
10
       int L = next[i - k];
11
       if (i + L 
12
         next[i] = L;
13
14
       else {
          j = max(0, p - i + 1);
15
16
         while (i + j < m \&\& x[i + j] == x[j]) j++;
17
         next[i] = j;
         k = i;
18
       }
19
     }
20
21
   void exkmp(char x[], int m, char y[], int n, int next[], int extend[]) {
22
23
     prework(x, m, next);
     int j = 0;
24
25
     while (j < n \&\& j < m \&\& x[j] == y[j]) ++j;
26
     extend[0] = j;
27
     int k = 0;
28
     for (int i = 1; i < n; ++i) {
       int p = extend[k] + k - 1;
29
30
       int L = next[i - k];
       if (i + L 
31
          extend[i] = L;
32
       else {
33
          j = max(0, p - i + 1);
34
35
         while (i + j < n \&\& j < m \&\& y[i + j] == x[j]) j++;
36
         extend[i] = j;
37
         k = i;
38
       }
39
     }
40
   }
   4.7 hash
1
   const unsigned int KEY = 6151;
   const unsigned int MOD = 1610612741;
4
  unsigned int hash[MAXN], p[MAXN];
5
   inline unsigned int get_hash(int l, int r) {
7
     return (hash[r] + MOD - 1ULL * hash[l - 1] * p[r - l + 1] % MOD) % MOD;
8
9
   }
10
11 void init(char *s, int n) {
12
     p[0] = 1;
     for (int i = 1; i <= n; ++i) {
13
       p[i] = p[i - 1] * KEY \% MOD;
14
       hash[i] = (1LL * hash[i - 1] * KEY + s[i]) % MOD;
15
16
     }
  }
17
```

4.8 后缀数组 (SAIS)

```
#include <bits/stdc++.h>
1
2
   const int BUFFER_SIZE = 1u << 23 | 1;</pre>
3
   char buffer[BUFFER_SIZE], *buffer_ptr = buffer;
4
   #define alloc(x, type, len)
5
     type *x = (type *)buffer_ptr;
                                                                                       \
6
     buffer_ptr += (len) * sizeof(type);
7
   #define clear_buffer()
8
     memset(buffer, 0, buffer_ptr - buffer), buffer_ptr = buffer;
9
10
11 template <int MAX_LENGTH> class SuffixArray {
12 #define L_TYPE true
13 #define S_TYPE false
14
   public:
     int sa[MAX_LENGTH], rank[MAX_LENGTH], height[MAX_LENGTH];
15
      void compute(int n, int m, int *s) {
16
17
        sais(n, m, s, sa);
       for (int i = 0; i < n; ++i) rank[sa[i]] = i;</pre>
18
19
       for (int i = 0, h = 0; i < n; ++i) {
          if (rank[i]) {
20
            int j = sa[rank[i] - 1];
21
22
            while (s[i + h] == s[j + h]) ++h;
            height[rank[i]] = h;
23
          } else {
24
25
           h = 0;
26
27
          if (h) --h;
28
     }
29
30
31
   private:
32
     int l_bucket[MAX_LENGTH], s_bucket[MAX_LENGTH];
33
34
     void induce(int n, int m, int *s, bool *type, int *sa, int *bucket,
                  int *l_bucket, int *s_bucket) {
35
36
       memcpy(l_bucket + 1, bucket, m * sizeof(int));
       memcpy(s_bucket + 1, bucket + 1, m * sizeof(int));
37
38
       sa[l_bucket[s[n - 1]] ++] = n - 1;
39
       for (int i = 0; i < n; ++i) {
          int t = sa[i] - 1;
40
41
          if (t \ge 0 \& type[t] == L_TYPE) sa[l_bucket[s[t]]++] = t;
42
43
        for (int i = n - 1; i >= 0; --i) {
44
          int t = sa[i] - 1;
          if (t \ge 0 \& type[t] == S_TYPE) sa[--s_bucket[s[t]]] = t;
45
46
47
     }
      void sais(int n, int m, int *s, int *sa) {
48
       alloc(type, bool, n + 1);
49
50
       alloc(bucket, int, m + 1);
       type[n] = false;
51
52
       for (int i = n - 1; i >= 0; --i) {
53
          ++bucket[s[i]];
          type[i] = s[i] > s[i + 1] \mid | (s[i] == s[i + 1] && type[i + 1] == L_TYPE);
54
55
       for (int i = 1; i <= m; ++i) {
56
          bucket[i] += bucket[i - 1];
57
```

```
58
          s_bucket[i] = bucket[i];
59
        memset(rank, -1, n * sizeof(int));
60
61
62
        alloc(lms, int, n + 1);
        int n1 = 0;
63
        for (int i = 0; i < n; ++i) {
64
           if (!type[i] && (i == 0 \mid | type[i - 1])) lms[rank[i] = n1++] = i;
65
66
        lms[n1] = n;
67
        memset(sa, -1, n * sizeof(int));
68
69
        for (int i = 0; i < n1; ++i) sa[--s_bucket[s[lms[i]]]] = lms[i];</pre>
        induce(n, m, s, type, sa, bucket, l_bucket, s_bucket);
70
        int m1 = 0;
71
        alloc(s1, int, n + 1);
72
        for (int i = 0, t = -1; i < n; ++i) {
73
          int r = rank[sa[i]];
74
          if (r != -1) {
75
             int len = lms[r + 1] - sa[i] + 1;
76
             m1 += t == -1 \mid \mid len != lms[rank[t] + 1] - t + 1 \mid \mid
77
                   memcmp(s + t, s + sa[i], len * sizeof(int)) != 0;
78
79
             s1[r] = m1;
             t = sa[i];
80
81
82
        }
83
        alloc(sa1, int, n + 1);
84
        if (n1 == m1) {
           for (int i = 0; i < n1; ++i) sa1[s1[i] - 1] = i;
85
        } else {
86
87
           sais(n1, m1, s1, sa1);
88
        memset(sa, -1, n * sizeof(int));
89
90
        memcpy(s_bucket + 1, bucket + 1, m * sizeof(int));
        for (int i = n1 - 1; i >= 0; --i) {
91
           int t = lms[sa1[i]];
92
           sa[--s\_bucket[s[t]]] = t;
93
94
95
        induce(n, m, s, type, sa, bucket, l_bucket, s_bucket);
96
      }
    #undef S_TYPE
97
    #undef L_TYPE
98
99
    };
100
101 const int MAXN = 1e5 + 5;
102 SuffixArray<MAXN> sa;
103 char str[MAXN];
104 int s[MAXN];
105
   int main() {
106
107
      int n = fread(str, 1, MAXN, stdin);
108
      while (str[n - 1] - 97u > 25) --n;
109
      for (int i = 0; i < n; ++i) s[i] = str[i] - 'a' + 1;
110
      sa.compute(n, 26, s);
      for (int i = 0; i < n; ++i) printf("%d%c", sa.sa[i] + 1, " \n"[i == n - 1]);
111
      for (int i = 1; i < n; ++i) printf("%d%c", sa.height[i], " \n"[i == n - 1]);
112
113
      return 0;
114 }
```

4.9 回文树

```
//最长双回文串
1
   struct PT {
2
3
     char s[MAXL];
      int fail[MAXL], ch[26][MAXL], l[MAXL], dep[MAXL], lst, nc, n;
4
      void init() {
5
        l[0] = 0;
6
7
        l[1] = -1;
        fail[0] = fail[1] = 1;
8
        for (int i = 0; i < 26; ++i) {
9
10
          for (int j = 0; j < nc; ++j) { ch[i][j] = 0; }
11
12
        for (int i = 2; i < nc; ++i) {</pre>
13
          l[i] = 0;
          fail[i] = 0;
14
15
16
        lst = 0;
17
18
        nc = 2;
        n = 0;
19
        s[0] = '#';
20
21
22
      int insert(char c) {
23
24
        int id = c - 'a';
25
        s[++n] = c;
26
        while (s[n - l[lst] - 1] != s[n]) \{ lst = fail[lst]; \}
        if (ch[id][lst] == 0) {
27
          l[nc] = l[lst] + 2;
28
          int f = fail[lst];
29
          while (s[n - l[f] - 1] != s[n]) { f = fail[f]; }
30
31
          fail[nc] = ch[id][f];
32
          dep[nc] = dep[fail[nc]] + 1;
33
          ch[id][lst] = nc;
34
          ++nc;
35
        }
36
        lst = ch[id][lst];
37
        return lst;
38
      }
39 } pt;
40
   char S[MAXL];
41
   int len[MAXL];
43
   int main() {
44
     ios::sync_with_stdio(false);
      cin.tie(0);
45
     cout.tie(0);
46
47
     cin >> S;
48
      int n = strlen(S);
49
50
      pt.init();
      for (int i = 0; i < n; ++i) { len[i] = pt.l[pt.insert(S[i])]; }</pre>
51
52
      pt.init();
53
      int ans = 0;
      for (int i = n - 1; i; --i) {
54
        ans = \max(ans, len[i - 1] + pt.l[pt.insert(S[i])]);
55
56
57
     cout << ans << "\n";
```

```
58
59 return 0;
60 }
```

5 Graph Theory

5.1 上下界费用流

```
#include <bits/stdc++.h>
   using namespace std;
3
   const int MAXN = 53;
4
   const int MAX_NODE = 113;
   const int MAX_EDGE = 1e5 + 5;
   const int INF = 0x3f3f3f3f;
7
8
9
   int n, s, t, ss, tt, tote;
   int R[MAXN], C[MAXN], board[MAXN][MAXN];
11
12 struct Edge {
     int to, cap, flow, cost;
13
  } edges[MAX_EDGE];
  vector<int> adj[MAX_NODE];
16
   int from[MAX_NODE], in[MAX_NODE];
17
   void add_edge(int from, int to, int l, int r, int cost) {
18
19
     in[to] += l, in[from] -= l;
     edges[tote] = (Edge)\{to, r - l, 0, cost\};
20
21
     adj[from].push_back(tote++);
     edges[tote] = (Edge){from, 0, 0, -cost};
22
     adj[to].push_back(tote++);
23
   }
24
25
26
   bool spfa(int s, int t) {
27
     static queue<int> q;
      static bool inq[MAX_NODE];
28
29
      static int dist[MAX_NODE];
30
     memset(inq + 1, 0, sizeof(bool) * tt);
31
     memset(dist + 1, 0x3f, sizeof(int) * tt);
     memset(from + 1, -1, sizeof(int) * tt);
32
     dist[0] = 0, from[0] = -1;
33
     q.push(0);
34
35
     while (!q.empty()) {
       int u = q.front();
36
37
       q.pop();
       inq[u] = false;
38
39
       for (int e : adj[u]) {
          if (edges[e].cap == edges[e].flow) continue;
40
          int v = edges[e].to, d = dist[u] + edges[e].cost;
41
         if (d >= dist[v]) continue;
42
         dist[v] = d;
43
         from[v] = e;
44
45
         if (!inq[v]) {
46
            q.push(v);
            inq[v] = true;
47
48
49
       }
     }
50
```

```
51
      return dist[t] < INF;</pre>
    }
52
53
    pair<int, int> min_cost_max_flow(int s, int t) {
54
      int flow = 0, cost = 0;
55
56
      while (spfa(s, t)) {
         int mi = INF;
57
         for (int it = from[t]; ~it; it = from[edges[it ^ 1].to])
58
           mi = min(mi, edges[it].cap - edges[it].flow);
59
60
         flow += mi;
         for (int it = from[t]; ~it; it = from[edges[it ^ 1].to]) {
61
62
           edges[it].flow += mi, edges[it ^ 1].flow -= mi;
           cost += mi * edges[it].cost;
63
         }
64
      }
65
      return make_pair(flow, cost);
66
67
68
    void solve() {
69
70
      tote = 0;
       s = 2 * n + 1, t = 2 * n + 2, ss = 0, tt = 2 * n + 3;
71
       for (int i = 0; i <= tt; ++i) adj[i].clear(), in[i] = 0;</pre>
72
73
74
      memset(R + 1, 0, sizeof(int) * n);
75
      memset(C + 1, 0, sizeof(int) * n);
76
77
       for (int i = 1; i <= n; ++i)</pre>
         for (int j = 1; j \le n; ++j) {
78
           cin >> board[i][j];
79
80
           R[i] += board[i][j];
81
           C[j] += board[i][j];
82
83
84
       for (int i = 1; i \le n; ++i) {
         add_edge(s, i, R[i], R[i], 0);
85
         add_edge(s, i + n, C[i], C[i], \emptyset);
86
87
88
       for (int i = 1, l, r; i <= n; ++i) {
89
         cin >> l >> r;
90
         add_edge(i, t, l, r, 0);
91
92
       for (int i = 1, l, r; i <= n; ++i) {
93
94
         cin >> l >> r;
         add_edge(i + n, t, l, r, 0);
95
96
       }
97
       for (int step = n * n / 2, x1, y1, x2, y2; step; --step) {
98
         cin >> x1 >> y1 >> x2 >> y2;
99
100
         if (board[x1][y1] == board[x2][y2]) continue;
101
         if (board[x2][y2]) swap(x1, x2), swap(y1, y2);
         if (x1 == x2)
102
103
           add_edge(y1 + n, y2 + n, 0, 1, 1);
104
         else
           add_edge(x1, x2, 0, 1, 1);
105
106
107
       add_edge(t, s, 0, INF, 0);
108
      int sum = 0;
109
       for (int i = 1; i < tt; ++i) {
```

```
if (in[i] > 0) {
110
           sum += in[i];
111
           add_edge(ss, i, 0, in[i], 0);
112
113
         } else if (in[i] < 0) {</pre>
114
           add_edge(i, tt, 0, -in[i], 0);
115
         }
      }
116
117
      pair<int, int> ans = min_cost_max_flow(ss, tt);
118
119
       if (sum != ans.first) {
120
         cout << "-1\n";
121
      } else {
         cout << ans.second << '\n';</pre>
122
123
124
    }
125
126
    int main() {
      ios::sync_with_stdio(false);
127
      cin.tie(nullptr);
128
129
      while (cin >> n) solve();
130
131
      return 0;
132 }
    5.2 tarjan
   vector<int> adj[MAXN];
    int dfn[MAXN], low[MAXN], dfs_c;
 3
    int bel[MAXN], size[MAXN], scc, stk[MAXN], top, in_stack[MAXN];
 5
    void tarjan(int u) {
      dfn[u] = low[u] = ++dfs_c;
 6
      stk[top++] = u;
 7
 8
      in_stack[u] = 1;
      for (size_t i = 0; i < adj[u].size(); ++i) {</pre>
 9
         int v = adj[u][i];
10
11
         if (!dfn[v]) {
12
           tarjan(v);
13
           (low[v] < low[u]) && (low[u] = low[v]);
14
         } else if (in_stack[v] && dfn[v] < low[u]) {</pre>
15
           low[u] = dfn[v];
         }
16
17
      if (low[u] == dfn[u]) {
18
19
         int v;
         size[++scc] = 0;
20
         do {
21
22
           v = stk[--top];
           in\_stack[v] = 0;
23
           bel[v] = scc;
24
           ++size[scc];
25
         } while (u != v);
26
27
      }
28
    }
```

5.3 一般图最大匹配

```
1 class GeneralMatch {
   public:
 2
3
      int n;
 4
      vector<vector<int>> g;
      vector<int> match, aux, label, orig, parent;
5
6
      queue<int> q;
 7
      int aux_time;
8
9
      GeneralMatch(int n)
          : match(n, -1), aux(n, -1), label(n), orig(n), parent(n, -1),
10
            aux_time(-1) {
11
12
        this->n = n;
        g.resize(n);
13
      }
14
15
      void add_edge(int u, int v) {
16
17
        g[u].push_back(v);
18
        g[v].push_back(u);
19
20
21
      int find(int x) { return x == orig[x] ? x : orig[x] = find(orig[x]); }
22
23
      int lca(int u, int v) {
24
        ++aux_time;
25
        u = find(u), v = find(v);
        for (;; swap(u, v)) {
26
27
          if (~u) {
            if (aux[u] == aux_time) return u;
28
29
            aux[u] = aux_time;
            if (match[u] == -1) {
30
31
              u = -1;
32
            } else {
33
              u = find(parent[match[u]]);
34
35
          }
        }
36
37
      }
38
      void blossom(int u, int v, int o) {
39
        while (find(u) != o) {
40
          parent[u] = v;
41
          v = match[u];
42
43
          q.push(v);
44
          label[v] = 0;
          orig[u] = orig[v] = o;
45
46
          u = parent[v];
47
        }
      }
48
49
50
      int bfs(int x) {
51
        iota(orig.begin(), orig.end(), 0);
52
        fill(label.begin(), label.end(), -1);
53
        while (!q.empty()) q.pop();
54
        q.push(x);
        label[x] = 0;
55
56
        while (!q.empty()) {
57
          int u = q.front();
58
          q.pop();
59
          for (int v : g[u]) {
```

```
if (label[v] == -1) {
60
               parent[v] = u;
61
               label[v] = 1;
62
              if (match[v] == -1) {
63
                 while (v != -1) {
64
                   int pv = parent[v];
65
                   int next_v = match[pv];
66
                   match[v] = pv;
67
                   match[pv] = v;
68
69
                   v = next_v;
70
                 }
71
                 return 1;
              }
72
73
              q.push(match[v]);
              label[match[v]] = 0;
74
            } else if (label[v] == 0 && find(u) != find(v)) {
75
               int o = lca(u, v);
76
77
               blossom(u, v, o);
              blossom(v, u, o);
78
79
            }
80
          }
        }
81
82
        return 0;
83
84
      int find_max_match() {
85
86
        int res = 0;
        for (int i = 0; i < n; ++i) {
87
          if (~match[i]) continue;
88
          res += bfs(i);
89
90
91
        return res;
92
93
   };
   5.4 sap
   struct MF {
2
      struct Edge {
3
        int to, cap, flow;
      } edges[MAXM * 4];
4
5
6
      vector<int> adj[MAXN];
      int n, edges_c, dep[MAXN], depc[MAXN], s, t, last[MAXN];
7
8
9
      void init(int _n) {
10
        n = _n;
        for (int i = 1; i <= n; ++i) adj[i].clear();</pre>
11
12
        edges_c = 0;
      }
13
14
      void add_edge(int v, int u, int cap) {
15
16
        edges[edges_c] = \{v, cap, \emptyset\};
        adj[u].push_back(edges_c++);
17
        edges[edges_c] = \{u, 0, 0\};
18
        adj[v].push_back(edges_c++);
19
20
21
```

```
int dfs(int u, int flow) {
22
        if (u == t || !flow) return flow;
23
        int v, e, temp, res = 0;
24
        for (int &i = last[u]; i < (int)adj[u].size(); ++i) {</pre>
25
26
          e = adj[u][i];
27
          v = edges[e].to;
          if (edges[e].cap == edges[e].flow) continue;
28
29
          if (dep[v] != dep[u] - 1) continue;
          temp = dfs(v, min(flow, edges[e].cap - edges[e].flow));
30
          edges[e].flow += temp, edges[e ^ 1].flow -= temp;
31
32
          res += temp, flow -= temp;
33
          if (!flow) return res;
          if (!dep[s]) return res;
34
35
        }
        last[u] = 0;
36
        if (!(--depc[dep[u]])) dep[s] = n + 1;
37
        ++depc[++dep[u]];
38
39
        return res;
40
      int max_flow(int s, int t) {
41
        this \rightarrow s = s, this \rightarrow t = t;
42
43
        static queue<int> que;
44
45
        memset(dep + 1, 0, sizeof(int) * n);
46
        memset(depc + 1, 0, sizeof(int) * n);
        memset(last + 1, 0, sizeof(int) * n);
47
48
        while (!que.empty()) que.pop();
        dep[t] = 1, que.push(t);
49
50
        while (!que.empty()) {
51
52
          int u = que.front();
53
          que.pop();
          ++depc[dep[u]];
54
          for (int i = 0, v; i < (int)adj[u].size(); ++i) {</pre>
55
            v = edges[adj[u][i]].to;
56
            if (dep[v]) continue;
57
58
            dep[v] = dep[u] + 1;
59
            que.push(v);
          }
60
        }
61
62
        int res = 0;
63
        while (dep[s] <= n) res += dfs(s, INT_MAX);</pre>
64
65
        return res;
66
      }
67
   };
         最小费用流
   class MinCostFlow {
   public:
      struct Result {
3
        int flow, cost;
4
5
      };
6
      struct Edge {
7
        int to, next, rest, cost;
8
9
```

```
10
     vector<bool> inq;
      vector<int> head, dist, from, flow;
11
      vector<Edge> edges;
12
13
      MinCostFlow(int n, int m): inq(n), head(n, -1), dist(n), from(n), flow(n) {
14
        edges.reserve(2 * m);
15
16
17
      void add_edge(int u, int v, int capacity, int cost) {
18
        internal_add_edge(u, v, capacity, cost);
19
20
        internal_add_edge(v, u, 0, -cost);
21
      }
22
      void internal_add_edge(int u, int v, int capacity, int cost) {
23
        edges.push_back((Edge){v, head[u], capacity, cost});
24
        head[u] = edges.size() - 1;
25
      }
26
27
      Result augment(int source, int sink) {
28
        fill(dist.begin(), dist.end(), INT_MAX);
29
        dist[source] = 0;
30
        flow[source] = INT_MAX;
31
        queue<int> q;
32
33
        q.push(source);
34
        while (!q.empty()) {
          int u = q.front();
35
36
          q.pop();
          inq[u] = false;
37
          for (int it = head[u]; ~it; it = edges[it].next) {
38
            auto &e = edges[it];
39
            int v = e.to;
40
            if (e.rest > 0 && dist[u] + e.cost < dist[v]) {</pre>
41
42
              from[v] = it;
              dist[v] = dist[u] + e.cost;
43
              flow[v] = min(e.rest, flow[u]);
44
              if (!inq[v]) {
45
46
                q.push(v);
47
                inq[v] = true;
48
              }
49
            }
50
          }
        }
51
52
53
        if (dist[sink] == INT_MAX) return {0, 0};
        int min_flow = flow[sink];
54
55
        for (int u = sink; u != source; u = edges[from[u] ^ 1].to) {
56
          edges[from[u]].rest -= min_flow;
          edges[from[u] ^ 1].rest += min_flow;
57
        }
58
59
        return {min_flow, dist[sink]};
60
61
62
      Result min_cost_flow(int source, int sink) {
        int flow = 0, cost = 0;
63
        for (;;) {
64
          auto result = augment(source, sink);
65
66
          if (!result.flow) break;
67
          flow += result.flow, cost += result.cost;
68
        }
```

```
return {flow, cost};
70
   };
71
   6
        Java
   6.1 进制转换
   import java.io.*;
   import java.util.*;
3 import java.math.*;
4
5
  /**
6
   * Built using CHelper plug-in
    * Actual solution is at the top
7
    */
8
   public class Main {
9
       public static void main(String[] args) {
10
            InputStream inputStream = System.in;
11
12
            OutputStream outputStream = System.out;
            Scanner in = new Scanner(inputStream);
13
            PrintWriter out = new PrintWriter(outputStream);
14
            Solver solver = new Solver();
15
            int testCount = Integer.parseInt(in.next());
16
            for (int i = 1; i <= testCount; i++)</pre>
17
18
                solver.solve(i, in, out);
19
            out.close();
20
       }
21
       static class Solver {
22
23
            public void solve(int testNumber, Scanner in, PrintWriter out) {
24
                int a = in.nextInt();
25
                int b = in.nextInt();
26
                String num = in.next();
27
                BigInteger value = BigInteger.ZERO;
28
                for (int i = 0; i < num.length(); ++i) {</pre>
29
30
                    value = value.multiply(BigInteger.valueOf(a));
31
                    value = BigInteger.valueOf(getValue(num.charAt(i))).add(value);
32
                out.println(a + " " + num);
33
34
                if (value.equals(BigInteger.ZERO)) {
35
                    out.println(b + " 0");
36
37
                    out.println();
38
                    return;
39
                }
40
                out.print(b + " ");
41
42
                char[] ans = new char[1000];
43
                int length = 0:
44
                while (!value.equals(BigInteger.ZERO)) {
45
                    int digit = value.mod(BigInteger.valueOf(b)).intValue();
46
                    value = value.divide(BigInteger.valueOf(b));
47
                    ans[length] = getChar(digit);
48
49
                    ++length;
                }
50
```

```
51
                for (int i = length - 1; i \ge 0; --i) {
52
53
                    out.print(ans[i]);
54
55
                out.println("\n");
            }
56
57
            private int getValue(char ch) {
58
                if (ch >= 'A' && ch <= 'Z') {
59
                    return ch - 'A' + 10;
60
61
62
                if (ch >= 'a' && ch <= 'z') {
                    return ch - 'a' + 36;
63
64
                return ch - '0';
65
            }
66
67
            private char getChar(int x) {
68
                if (x < 10) {
69
70
                    return (char) ('0' + x);
                else\ if\ (x < 36) {
71
                    return (char) ('A' + x - 10);
72
73
74
                    return (char) ('a' + x - 36);
75
                }
            }
76
77
        }
78
79 }
        Others
   7.1 myalloc
 1 // useage: vector<int, myalloc<int>> L;
   static char space[10000000], *sp = space;
   template <typename T> struct myalloc : allocator<T> {
     myalloc() {}
4
     template <typename T2> myalloc(const myalloc<T2> &a) {}
5
     template <typename T2> myalloc<T> &operator=(const myalloc<T2> &a) {
6
7
        return *this;
8
9
     template <typename T2> struct rebind { typedef myalloc<T2> other; };
10
     inline T *allocate(size_t n) {
        T * result = (T *) sp;
11
12
        sp += n * sizeof(T);
13
        return result;
14
15
     inline void deallocate(T *p, size_t n) {}
16 };
   7.2 duipai
1 #/usr/bin/bash
2
3 while true; do
     python gen.py > in.txt
```

```
time ./my < in.txt > out.txt
5
     time ./std < in.txt > ans.txt
6
     if diff out.txt ans.txt; then
7
       echo AC
8
9
     else
       echo WA
10
       exit 0
11
12
     fi
13
   done
   7.3 vimrc
1 syntax enable
2 set syntax=on
3 set nobackup
4 set noswapfile
5 set noundofile
6 set nu
7 set smartindent
8 set cindent
9 set noeb
10 set tabstop=2
   set softtabstop=2
   set shiftwidth=2
   set expandtab
13
14
   :imap jk <Esc>
15
16
   map <F5> : call Complie() <CR>
17
   func Complie()
18
     exec "w"
19
     exec "!g++ % -o %< -g -Wall -std=gnu++17 -static"
20
  endfunc
21
22
   map <F6> : call Run() <CR>
23
   func Run()
24
     exec "!./%<"
25
26
   endfunc
27
28 map <F9> : call DeBug() <CR>
29 func DeBug()
     exec "!gdb %<"
30
  endfunc
31
   7.4 emacs
   (defun comp ()
1
     (interactive)
2
     (save-some-buffers t)
3
     (setq filename (file-name-nondirectory buffer-file-name))
4
     (setq progname (file-name-sans-extension filename))
5
6
     (setq suffix (file-name-extension filename))
     (compile (concat "g++ " filename " -o " progname " -02 -Wall -Werror")))
7
   (add-hook 'c++-mode
8
              '(lambda ()
9
                 (c-set-style "K&R")
10
                 (setq tab-width 2)
11
```

```
(setq indent-tabs-mode nil)
12
                 (setq c-basic-offset 2)))
13
   (global-set-key [f5] 'comp)
14
15
   (ido-mode t)
16
   (delete-selection-mode t)
17
  (global-auto-revert-mode t)
   7.5 FastIO
1 namespace FastIO {
   struct Control {
3
     int ct, val;
     Control(int Ct, int Val = -1) : ct(Ct), val(Val) {}
4
     inline Control operator()(int Val) { return Control(ct, Val); }
5
   } _endl(0), _prs(1), _setprecision(2);
   const int IO_SIZE = 1 << 16 | 127;</pre>
8
9
10 struct FastIO {
     char in[IO_SIZE], *p, *pp, out[IO_SIZE], *q, *qq, ch[20], *t, b, K, prs;
11
     FastIO() : p(in), pp(in), q(out), qq(out + IO_SIZE), t(ch), b(1), K(6) {}
12
     ~FastIO() { fwrite(out, 1, q - out, stdout); }
13
14
     inline char getc() {
       return p == pp && (pp = (p = in) + fread(in, 1, IO_SIZE, stdin), p == pp)
15
16
                   ? (b = 0, EOF)
17
                   : *p++;
18
     }
     inline void putc(char x) {
19
       q == qq \&\& (fwrite(out, 1, q - out, stdout), q = out), *q++ = x;
20
21
     inline void puts(const char str[]) {
22
23
       fwrite(out, 1, q - out, stdout), fwrite(str, 1, strlen(str), stdout),
24
           q = out;
25
     inline void getline(string &s) {
26
       s = "";
27
28
       for (char ch; (ch = getc()) != '\n' && b;) s += ch;
29
30
   #define indef(T)
31
     inline FastIO &operator>>(T &x) {
32
       x = 0;
33
       char f = 0, ch;
       while (!isdigit(ch = getc()) && b) f |= ch == '-';
34
35
       while (isdigit(ch)) x = (x << 1) + (x << 3) + (ch ^ 48), ch = getc();
       return x = f ? -x : x, *this;
36
37
     indef(int);
38
39
     indef(long long);
40
41
     inline FastIO &operator>>(string &s) {
       s = "":
42
43
       char ch:
44
       while (isspace(ch = getc()) && b) {}
       while (!isspace(ch) && b) s += ch, ch = getc();
45
46
       return *this;
47
     inline FastIO &operator>>(double &x) {
48
```

```
x = 0;
49
        char f = 0, ch;
50
        double d = 0.1;
51
        while (!isdigit(ch = getc()) && b) f |= (ch == '-');
52
53
        while (isdigit(ch)) x = x * 10 + (ch ^ 48), ch = getc();
        if (ch == '.')
54
55
          while (isdigit(ch = getc())) x += d * (ch ^ 48), d *= 0.1;
        return x = f ? -x : x, *this;
56
57
   #define outdef(_T)
58
59
      inline FastIO &operator<<(_T x) {</pre>
60
        !x && (putc('0'), 0), x < 0 && (putc('-'), x = -x);
        while (x) *t++ = x % 10 + 48, x /= 10;
61
        while (t != ch) *q++ = *--t;
62
        return *this;
63
64
      outdef(int);
65
66
      outdef(long long);
      inline FastIO &operator<<(char ch) { return putc(ch), *this; }</pre>
67
      inline FastIO &operator<<(const char str[]) { return puts(str), *this; }</pre>
68
      inline FastIO &operator<<(const string &s) { return puts(s.c_str()), *this; }</pre>
69
      inline FastIO &operator<<(double x) {</pre>
70
71
        int k = 0;
72
        this->operator<<(int(x));
73
        putc('.');
74
        x = int(x);
        prs && (x += 5 * pow(10, -K - 1));
75
        while (k < K) putc(int(x *= 10) ^ 48), x -= int(x), ++k;
76
77
        return *this:
78
      inline FastIO &operator<<(const Control &cl) {</pre>
79
80
        switch (cl.ct) {
        case 0: putc('\n'); break;
81
        case 1: prs = cl.val; break;
82
        case 2: K = cl.val; break;
83
        }
84
85
        return *this:
86
     inline operator bool() { return b; }
87
88
   } // namespace FastIO
89
```