Introduction to fintech hw7

系級: 資工碩一 姓名:胡嘉祐 學號: r07922162

1. Evaluate 4G.

(10338857399563508035974916425421659830878883530402360147780309523428649499368 3 ,
787349480920740724105556683778235783031297677369394103695842975796530058616 45)

2. Evaluate 5G.

(21505829891763648114329055987619236494102133314575206970830385799158076338148 ,
17788380558553574189887744505607047724243097342766425233927699087598871091545)

3. Evaluate Q = dG

d = 922162

(27981534255525559262250955547714639507910381496217459733007401513762805455 25 ,
37390993050425453923041113037110202001157990738649604804893325562897915842592)

4. With standard Double-and Add algorithm for scalar multiplications, how many doubles and additions respectively are required to evaluate dG?

d = 922162;

	Operation	value		Operation	value
First	Initial setting	1	10	Double and add	1801
1	Double and add	3	11	Double	3602
2	Double and add	7	12	Double	7204
3	Double	14	13	Double	14408
4	Double	28	14	Double and add	28817
5	Double	56	15	Double and add	57635
6	Double	112	16	Double	115270
7	Double and add	225	17	Double	230540
8	Double	450	18	Double and add	461081

9	Double	900	19	Double	922162

double operation : 12 ,
double and add operation : 7

5. Note that it is effortless to find P from any P on a curve. If the addition of an inverse point is allowed, try your best to evaluate dG as fast as possible.

轉換成 : binary 形式 111000010100011001
(0 的數量) 10- (1 的數量) 8 = 2 < 3 直接計算
double operation : 12 ,
double and add operation : 7

6. Take a Bitcoin transaction as you wish. Sign the transaction with a random number k and your private key d.

k=
5448938843001574545926730489648080918810671948430864753445166350805545157010 3
sign =
1092438271312808592805924216168307088480976819228009352774879006152875547840 30

7. Verify the digital signature with your public key Q.

digital signature=
6248973374962041255442590543375430023757073747935487241253508729562257701395 8