

# Problem Set 8

Parvesh Adi Lachman

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## 1 Problem 1

**Claim:** Let  $G = (V, E)$  be any undirected graph, and let  $f : V \rightarrow \{1, 2, \dots, k\}$  be a  $k$ -colouring of  $G$ , where  $k = \chi(G)$ . The binary relation  $\equiv_f$  on  $V$  defined by

$$u \equiv_f v \text{ if and only if } f(u) = f(v)$$

## 2 Problem 2

Claim:

### 3 Problem 3

Claim: