

Econometric Methods Homework 9

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1 Problem 1

1.1 Table 12.2

| | Dependent variable: | | | | |
|-------------|----------------------|----------------------|----------------------|----------------------|----------------------|
| | log_wage (1) | education (2) | experience (3) | experience2 (4) | experience2 (5) |
| experience | 0.053*** (0.007) | -0.410*** (0.034) | | | -0.413*** (0.034) |
| experience2 | -0.219*** (0.034) | 0.073 (0.165) | | | 0.093 (0.165) |
| black | -0.264*** (0.018) | -1.006*** (0.090) | -1.468*** (0.115) | 1.468*** (0.115) | 0.282*** (0.024) |
| south | -0.143*** (0.016) | -0.291*** (0.079) | -0.460*** (0.102) | 0.460*** (0.102) | 0.112*** (0.022) |
| urban | 0.185*** (0.018) | 0.404*** (0.085) | 0.835*** (0.109) | -0.835*** (0.109) | -0.176*** (0.023) |
| college | 0.045*** (0.017) | 0.337*** (0.083) | 0.347*** (0.107) | -0.347*** (0.107) | -0.073*** (0.022) |
| age | | 1.061*** (0.301) | -0.061 (0.301) | -0.555*** (0.063) | 0.430*** (0.087) |
| age2 | | -1.876*** (0.523) | 1.876*** (0.523) | 1.313*** (0.110) | 0.123 (0.106) |

Because the length is exceed in my theme, I paste two figure together.

1.2 Table 12.1

| | Dependent variable: | | | | |
|---------------------------------|---------------------------|----------------------|-----------------------|----------------------|----------------------|
| | log_wage | | instrumental variable | | |
| | OLS (1) | (2) | (3) | (4) | (5) |
| education | 0.074*** (0.004) | 0.132*** (0.049) | 0.133*** (0.051) | 0.161*** (0.041) | 0.160*** (0.041) |
| experience | 0.084*** (0.007) | 0.107*** (0.021) | 0.056** (0.026) | 0.119*** (0.018) | 0.047* (0.025) |
| experience2 | -0.224*** (0.032) | -0.228*** (0.033) | -0.080 (0.134) | -0.231*** (0.035) | -0.032 (0.128) |
| black | -0.190*** (0.018) | -0.131** (0.053) | -0.103 (0.077) | -0.102** (0.045) | -0.064 (0.063) |
| south | -0.125*** (0.015) | -0.105*** (0.023) | -0.098*** (0.029) | -0.095*** (0.022) | -0.086*** (0.026) |
| urban | 0.161*** (0.016) | 0.131*** (0.030) | 0.108** (0.050) | 0.116*** (0.027) | 0.083** (0.041) |
| Constant | 4.734*** (0.068) | 3.753*** (0.829) | 4.066*** (0.608) | 3.268*** (0.687) | 3.748*** (0.483) |
| Observations | 3,010 | 3,010 | 3,010 | 3,010 | 3,010 |
| R2 | 0.291 | 0.225 | 0.176 | 0.145 | 0.051 |
| Adjusted R2 | 0.289 | 0.224 | 0.175 | 0.143 | 0.049 |
| Residual Std. Error (df = 3003) | 0.374 | 0.391 | 0.403 | 0.411 | 0.433 |
| F Statistic | 204.932*** (df = 6; 3003) | | | | |

Note: *p<0.1; **p<0.05; ***p<0.01

2 Problem 2

$I_k - Q(Q'Q)^{-1}Q'$ is annihilator matrix (M) of Q
 $\therefore M$ is idempotent and symmetric
 $S \stackrel{d}{\rightarrow} Z'MZ = Z'M'MZ = \|MZ\|^2$ & $Z \sim N(0, I_k)$
 $\text{rank}(I_k - Q(Q'Q)^{-1}Q') = k - k$
 $\therefore S \stackrel{d}{\rightarrow} \chi^2(k-k)$ under H_0 &

GitHub Link

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