

Monitors

Systemes Concurrents

TD 1

Simone Gasparini

simone.gasparini@toulouse-inp.fr

Outline

- The Monitors - reminder
- The sleeping barber problem
 - Methodology
 - Variant
- The Readers-Writers problem
 - Priority policies

The Monitors

Moniteur de Hoare, Brinch-Hansen (1973)

Idée de base

La synchronisation résulte du besoin de partager convenablement un objet entre plusieurs activités concurrentes

- un moniteur est une construction qui permet de définir et de contrôler le bon usage d'un objet partagé par un ensemble d'activités

Définition

Un moniteur = un **module** exportant des **opérations** (et éventuellement des constantes et des types).

- Contrainte :
exécution des opérations du moniteur en **exclusion mutuelle**
- La **synchronisation** des opérations du moniteur est réalisée par des **opérateurs internes au moniteur**.

Un moniteur est **passif** : ce sont les activités utilisant le moniteur qui l'activent, en invoquant ses opérations.



The Monitors

Synchronisation : type *condition*

La **synchronisation** est définie **au sein du moniteur**, en utilisant des variables de type *condition*, internes au moniteur

Définition

Variables de type **condition** définies dans le moniteur.

Opérations possibles sur une variable de type condition *C* :

- **C.wait()** (*C.attendre()*) : bloque l'activité appelante en libérant l'accès exclusif au moniteur.
- **C.signal()** (*C.signaler()*) : si des activités sont bloquées sur *C*, en réveille une ; sinon, nop.
- Une **file d'attente** est associée à **chaque** variable condition
- **condition \approx événement**
 - condition \neq prédicat logique
- Autre opération sur les conditions :
 - C.empty()** : vrai si aucune activité n'est bloquée sur *C*.



The Monitors

Transfert du contrôle exclusif

Les opérations du moniteur s'exécutent en exclusion mutuelle.

→ Lors d'un **réveil** par `signal()`, **qui** obtient/garde l'accès exclusif ?

Priorité au signalé

Signal-and-wait

Lors du réveil par `signal()`,

- l'accès exclusif est **transféré** à l'activité réveillée (signalée) ;
- l'activité signaleuse est mise en attente de pouvoir ré-acquérir l'accès exclusif

Priorité au signaleur

Signal-and-continue

Lors du réveil par `signal()`,

- l'accès exclusif est **conservé** par l'activité réveilleuse ;
- l'activité réveillée (signalée) est mise en attente de pouvoir acquérir l'accès exclusif
 - soit dans une file globale spécifique
 - soit avec les activités entrantes



The Sleeping Barber problem

Configuration

- 1 Barber
- 1 Barber Chair
- A barber shop with N available chairs in the waiting room



Rules

- A client waits in the waiting room if there are chairs available, otherwise it waits outside.
- When the barber is done shaving, it signals the client
 - the client exits the barbershop
 - another client is allowed in the barbershop
- If there are no clients the barber sleep.
- If a client finds the barber sleeping he wakes him up and get on the barber chair.



Methodology

Etapes

- ① Déterminer l'**interface** du moniteur
- ② Énoncer informellement les **prédicats d'acceptation** de chaque opération
- ③ Dédire les **variables d'état** qui permettent d'écrire ces prédicats d'acceptation
- ④ Formuler l'**invariant** du moniteur et les prédicats d'acceptation
- ⑤ Associer à chaque prédicat d'acceptation une **variable condition** qui permettra d'attendre/signaler la validité du prédicat
- ⑥ **Programmer** les opérations, en suivant le schéma précédent
- ⑦ **Vérifier** que
 - l'invariant est vrai à chaque transfert du contrôle du moniteur
 - le prédicat d'acceptation est vrai quand un réveil a lieu



(1) Interface definition

```
Client()  
{  
    loop  
        EnterBarbershop()  
        // wait in the waiting room  
        SitOnBarberChair()  
        // wait end of shaving  
        GetUpAndGetOut()  
    endloop  
}
```

```
Barber()  
{  
    loop  
        StartShaving()  
        // shave client  
        ...  
        EndShaving()  
    endloop  
}
```

(2) Acceptance conditions

EnterBarbershop()	There must be a seat available in the waiting room
SitOnBarberChair()	The barber chair must be free
GetUpAndGetOut()	The client is shaved (no more beard)
StartShaving()	There is a bearded client on the barber chair
EndShaving()	nothing

(3) State variables

They allow to write the acceptance predicates

<code>AvailableSeats : int := N</code>	Number of available seats in the waiting room
<code>BarberChairFree : bool := true</code>	Whether there is a client on the barber chair or not
<code>HasBeard : bool := false</code>	Whether the client currently on the chair still has his beard

(4) Invariants and acceptance predicates

Invariants:

$(0 \leq \text{AvailableSeats} \leq N) \wedge (\text{HasBeard} \Rightarrow \neg \text{BarberChairFree})$

Operation	Condition variable
EnterBarbershop()	<i>There must be a seat available in the waiting room</i> AvailableSeats > 0
SitOnBarberChair()	<i>The barber chair must be free</i> BarberChairFree
GetUpAndGetOut()	<i>The client is shaved (no more beard)</i> ¬HasBeard
StartShaving()	<i>There is a bearded client on the barber chair</i> HasBeard
EndShaving()	<i>nothing</i>

(5) Condition variables

- Associate a **condition variable** with each **acceptance predicate**
- They will be used to wait for/signal the validity of the predicate.

Acceptance predicate	Condition variable
AvailableSeats > 0	WaitingRoom
BarberChairFree	BarberChair
¬HasBeard	ShavedClient
HasBeard	BeardedClient

Recap

Operation	Acceptance predicate	Condition Variable
EnterBarbershop()	<i>There must be a seat available in the waiting room</i> AvailableSeats > 0	WaitingRoom
SitOnBarberChair()	<i>The barber chair must be free</i> BarberChairFree	BarberChair
GetUpAndGetOut()	<i>The client is shaved (no more beard)</i> ¬HasBeard	ShavedClient
StartShaving()	<i>There is a bearded client on the barber chair</i> HasBeard	BeardedClient
EndShaving()	<i>nothing</i>	

(6) Programming

Client

EnterBarbershop()

```
// There must be a seat available in the waiting room
if ¬(AvailableSeats > 0) then
    WaitingRoom.wait()
endif
{AvailableSeats > 0}
AvailableSeats--
{0 ≤ AvailableSeats < N}
```

(6) Programming

Client

SitOnBarberChair()

```
// The barber chair must be free
if ¬(BarberChairFree) then
    BarberChair.wait()
endif
{BarberChairFree == true}
AvailableSeats++
{0 < AvailableSeats ≤ N}
BarberChairFree := false
HasBeard := true
BeardedClient.signal()
WaitingRoom.signal()
```


(6) Programming

Client

```
GetUpAndGetOut()
```

```
  // The client is shaved (no more beard)
```

```
  if  $\neg(\neg\text{HasBeard})$  then // or simply: if (HasBeard)
```

```
    ShavedClient.wait()
```

```
  endif
```

```
  { $\neg\text{HasBeard}$ }
```

```
  BarberChairFree := true
```

```
  BarberChair.signal()
```

(6) Programming

Barber

StartShaving()

```
// There is a bearded client on the barber chair
```

```
if  $\neg$ (HasBeard) then
```

```
    BeardedClient.wait()
```

```
endif
```

```
{HasBeard}
```

(6) Programming

Barber

```
EndShaving()
```

```
  HasBeard := false
```

```
  ShavedClient.signal()
```

(7) Checking

- For each condition variable, check that **each signal precondition** (state at the moment when the signal is called) implies **each wait postcondition** (in this case, the acceptance predicate).

(7) Checking- signal-and-wait

EnterBarbershop()

```
// There must be a seat available
in the waiting room
if ¬(AvailableSeats > 0) then
    WaitingRoom.wait()
endif
{AvailableSeats > 0}
AvailableSeats--
{0 ≤ AvailableSeats < N}
```

GetUpAndGetOut()

```
// The client is shaved (no more beard)
if (HasBeard) then
    ShavedClient.wait()
endif
{¬HasBeard}
BarberChairFree := true
BarberChair.signal()
```

SitOnBarberChair()

```
// The barber chair must be free
if ¬(BarberChairFree) then
    BarberChair.wait()
endif
{BarberChairFree == true}
AvailableSeats++
{0 < AvailableSeats ≤ N}
BarberChairFree := false
HasBeard := true
BeardedClient.signal()
WaitingRoom.signal()
```

StartShaving()

```
// There is a bearded client on the barber chair
if ¬(HasBeard) then
    BeardedClient.wait()
endif
{HasBeard}
```

EndShaving()

```
HasBeard := false
ShavedClient.signal()
```

(7) Checking- signal-and-wait

EnterBarbershop()

```
// There must be a seat available
in the waiting room
if ¬(AvailableSeats > 0) then
    WaitingRoom.wait()
endif
{AvailableSeats > 0}
AvailableSeats--
{0 ≤ AvailableSeats < N}
```

SitOnBarberChair()

```
// The barber chair must be free
if ¬(BarberChairFree) then
    BarberChair.wait()
endif
{BarberChairFree == true}
AvailableSeats++
{0 < AvailableSeats ≤ N}
BarberChairFree := false
HasBeard := true
BeardedClient.signal()
WaitingRoom.signal()
```

GetUpAndGetOut()

```
// The client is shaved (no more beard)
if (HasBeard) then
    ShavedClient.wait()
endif
{¬HasBeard}
BarberChairFree := true
BarberChair.signal()
```

StartShaving()

```
// There is a bearded client on the barber chair
if ¬(HasBeard) then
    BeardedClient.wait()
endif
{HasBeard}
```

EndShaving()

```
HasBeard := false
ShavedClient.signal()
```

(7) Checking- signal-and-wait

EnterBarbershop()

```
// There must be a seat available
in the waiting room
if ¬(AvailableSeats > 0) then
    WaitingRoom.wait()
endif
{AvailableSeats > 0}
AvailableSeats--
{0 ≤ AvailableSeats < N}
```

SitOnBarberChair()

```
// The barber chair must be free
if ¬(BarberChairFree) then
    BarberChair.wait()
endif
{BarberChairFree == true}
AvailableSeats++
{0 < AvailableSeats ≤ N}
BarberChairFree := false
HasBeard := true
BeardedClient.signal()
WaitingRoom.signal()
```

GetUpAndGetOut()

```
// The client is shaved (no more beard)
if (HasBeard) then
    ShavedClient.wait()
endif
{¬HasBeard}
BarberChairFree := true
BarberChair.signal()
```

StartShaving()

```
// There is a bearded client on the barber chair
if ¬(HasBeard) then
    BeardedClient.wait()
endif
{HasBeard} ←
```

EndShaving()

```
HasBeard := false
ShavedClient.signal()
```

(7) Checking- signal-and-wait

EnterBarbershop()

```
// There must be a seat available
in the waiting room
if ¬(AvailableSeats > 0) then
    WaitingRoom.wait()
endif
{AvailableSeats > 0}
AvailableSeats--
{0 ≤ AvailableSeats < N}
```

SitOnBarberChair()

```
// The barber chair must be free
if ¬(BarberChairFree) then
    BarberChair.wait()
endif
{BarberChairFree == true}
AvailableSeats++
{0 < AvailableSeats ≤ N}
BarberChairFree := false
HasBeard := true
BeardedClient.signal()
WaitingRoom.signal()
```

GetUpAndGetOut()

```
// The client is shaved (no more beard)
if (HasBeard) then
    ShavedClient.wait()
endif
{¬HasBeard} ←
BarberChairFree := true
BarberChair.signal()
```

StartShaving()

```
// There is a bearded client on the barber chair
if ¬(HasBeard) then
    BeardedClient.wait()
endif
{HasBeard}
```

EndShaving()

```
HasBeard := false
ShavedClient.signal()
```


(7) Checking- signal-and-wait

EnterBarbershop()

```
// There must be a seat available
in the waiting room
if ¬(AvailableSeats > 0) then
    WaitingRoom.wait()
endif
{AvailableSeats > 0} ←
AvailableSeats--
{0 ≤ AvailableSeats < N}
```

SitOnBarberChair()

```
// The barber chair must be free
if ¬(BarberChairFree) then
    BarberChair.wait()
endif
{BarberChairFree == true}
AvailableSeats++
{0 < AvailableSeats ≤ N} ←
BarberChairFree := false
HasBeard := true
BeardedClient.signal()
WaitingRoom.signal()
```

GetUpAndGetOut()

```
// The client is shaved (no more beard)
if (HasBeard) then
    ShavedClient.wait()
endif
{¬HasBeard}
BarberChairFree := true
BarberChair.signal()
```

StartShaving()

```
// There is a bearded client on the barber chair
if ¬(HasBeard) then
    BeardedClient.wait()
endif
{HasBeard}
```

EndShaving()

```
HasBeard := false
ShavedClient.signal()
```

(7) Checking - signal-and-continue

Configuration

- Client A is on the barber chair
- Client B is waiting for the chair (`BarberChair.wait()`)
- Client C is in the waiting room doing nothing

Scenario

- Barber calls `EndShaving()`
- Client A gets the exclusive access
- Client C tries to call `SitOnBarberChair()` and waits for exclusive access
- Client A signals `BarberChair.signal()`
 - Client B is now unblocked, i.e. he can ask for exclusive access
- Client A is done and give up exclusive access. Who gets it?
 - Client B? --> OK
 - Client C?
 - it gets to the barber chair and signals the barber (`BeardedClient.signal()`)
 - B can then get the access and continue with its `SitOnBarberChair()` but the barber chair is no longer free!

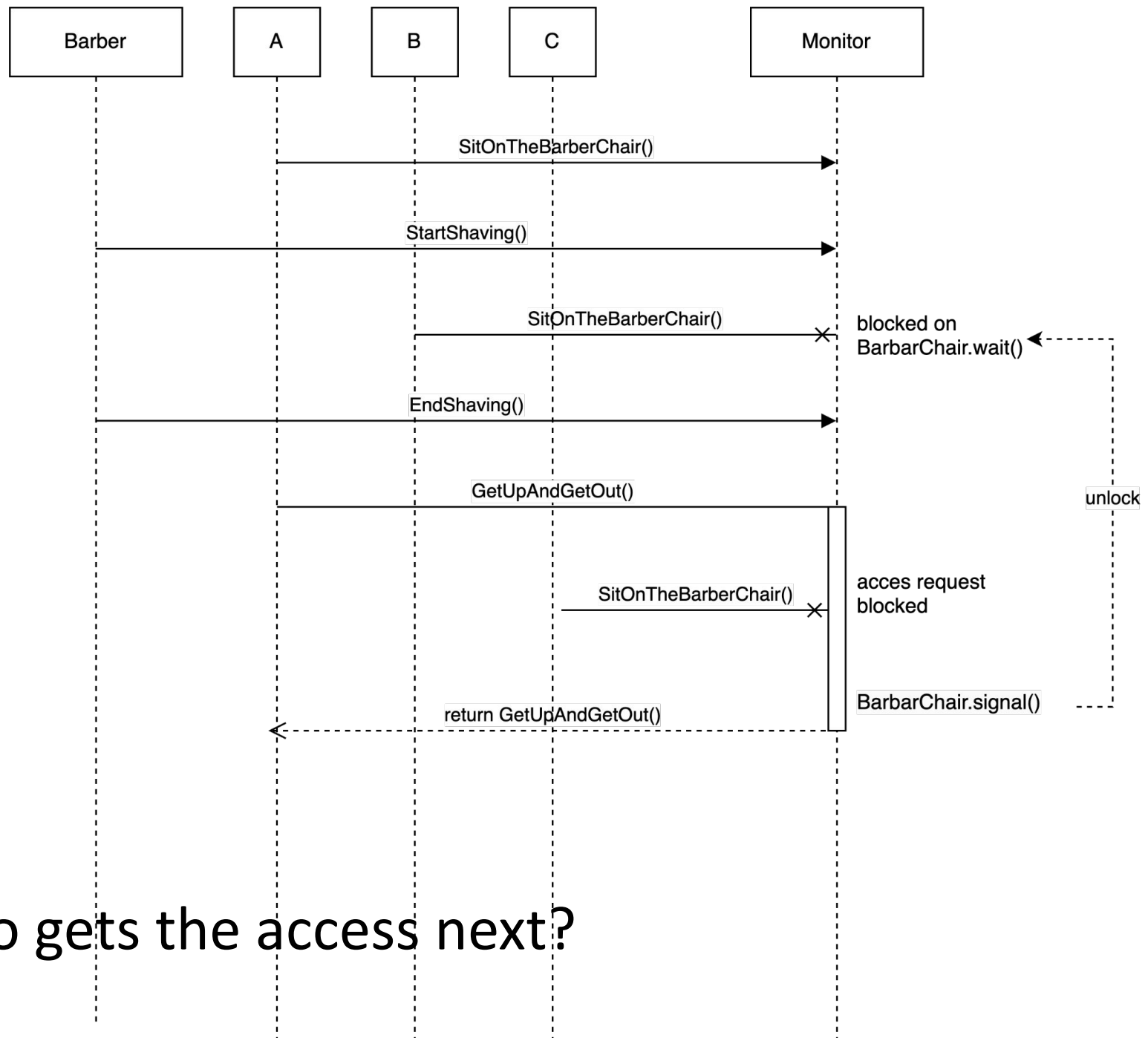
(7) Checking - signal-and-continue

Scenario

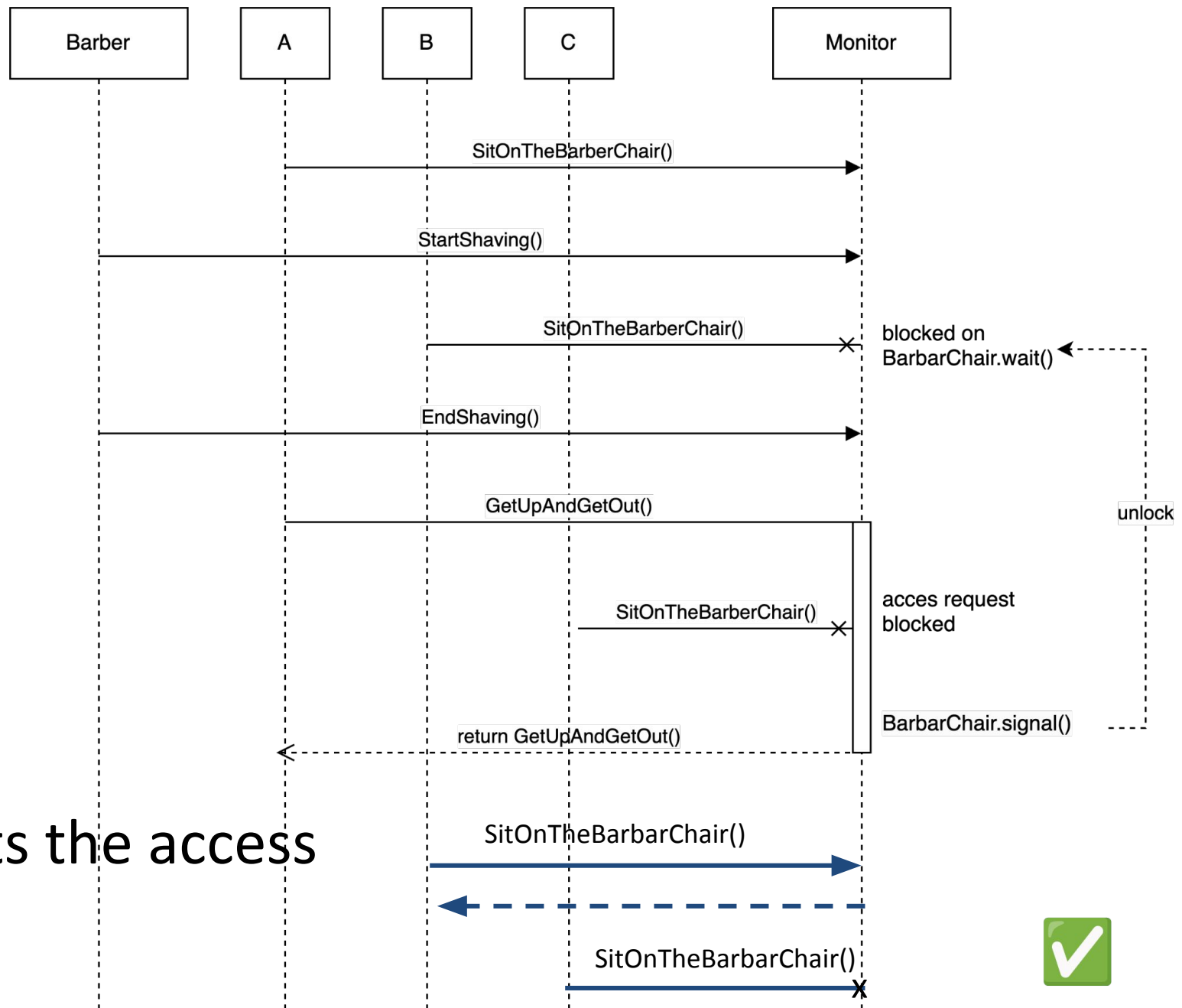
- Barber calls `EndShaving()`
- Client A gets the exclusive access
- Client C tries to call `SitOnBarberChair()` and waits for exclusive access
- Client A signals `BarberChair.signal()`
 - Client B is now unblocked, i.e. he can ask for exclusive access
- Client A is done and give up exclusive access. Who gets it?
 - Client B? --> OK
 - Client C?
 - it gets to the barber chair and signals the barber (`BeardedClient.signal()`)
 - B can then get the access and continue with its `SitOnBarberChair()` but the barber chair is no longer free!

Client needs to recheck the condition once he get the access

```
SitOnBarberChair()
    // The barber chair must be free
    while ¬(BarberChairFree)
        BarberChair.wait()
    endwhile
    {BarberChairFree == true}
    AvailableSeats++
    ....
```



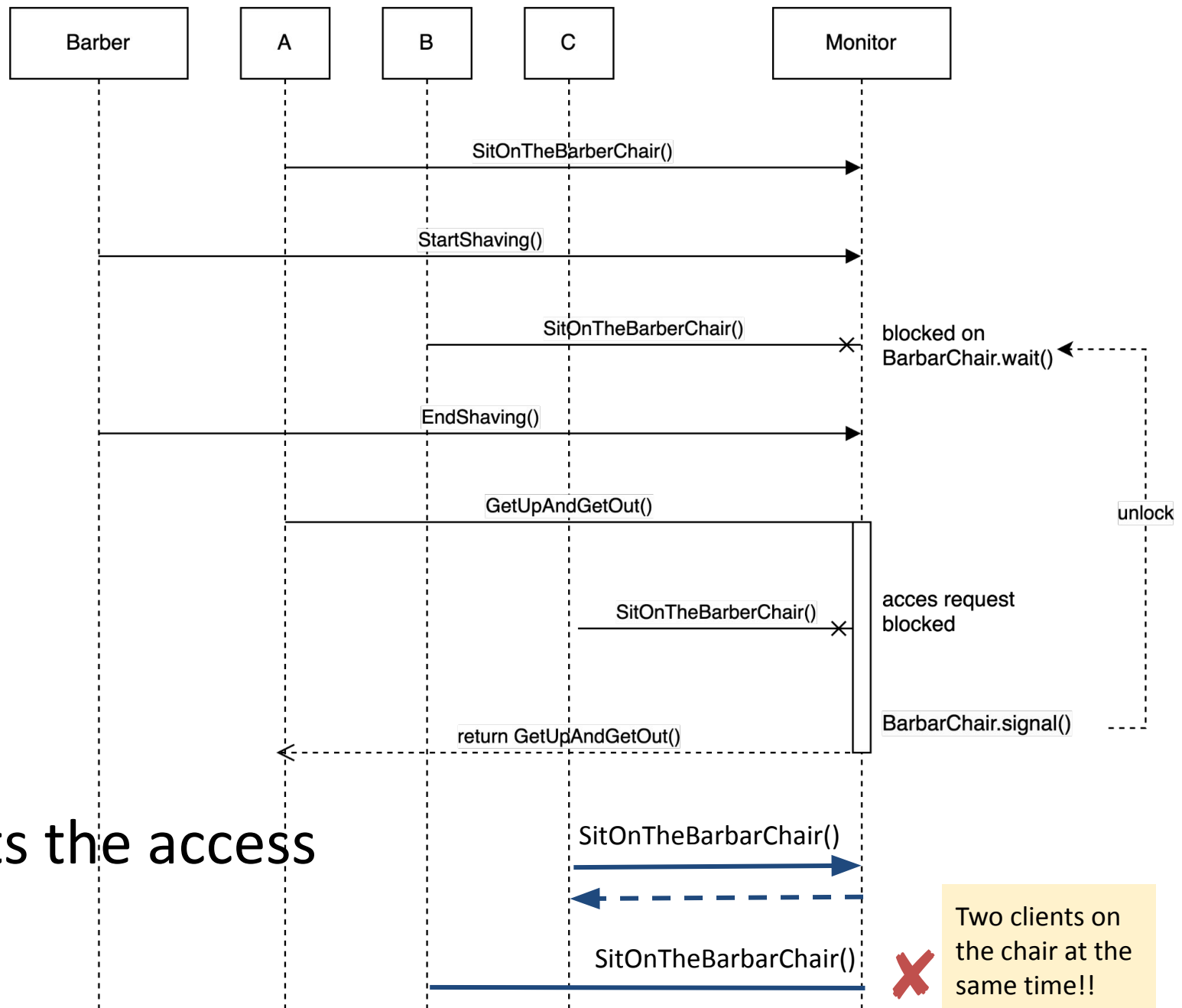
Who gets the access next?



B gets the access



when C gets the exclusive access, it gets blocked on `BarberChair.wait()`



C gets the access

return from BarberChair.wait() and the postcondition is false!

Variant

Configuration

- 1 Barber
- 1 Barber Chair
- A barber shop with N available chairs in the waiting room



Rules

- A client wait in the waiting room if there are chairs available, otherwise he waits outside.
- When the barber is done shaving, he signals the client
 - the client exit the barbershop
 - another client is allowed in the barbershop
- If there are no clients the barber sleep.
- If a client finds the barber sleeping he wakes him up and get on the barber chair.
- If the waiting room is full the client gives up and leave

Variant

- EnterBarbershop() need to return a boolean

```
bool EnterBarbershop()  
    // There must be a seat available in the waiting room  
    if ¬(AvailableSeats > 0) then  
        return false  
    endif  
    {AvailableSeats > 0}  
    AvailableSeats--  
    {0 ≤ AvailableSeats < N}  
    return true
```


Variant

- EnterBarbershop() need to return a boolean

```
Client()
{
    loop
        if EnterBarbershop()
            // wait in the waiting room
            SitOnBarberChair()
            // wait end of shaving
            GetUpAndGetOut()
        endif
    endloop
}
```

Readers–Writers problem

Configuration

- R readers
- W writers
- A shared file they can read or write.

Rules

- Multiple readers can read the file at the same time
- Only one writer can write at a given time
- If readers are reading no writer can write and vice versa

Policies

- Readers priority
 - no reader should wait if a reader has access to the object, while a writer waits till the last reader is done.
- Writers priority
 - No new readers allowed once a writer has asked for access, when a reader finishes it signals another writer in any, otherwise a reader

Readers–Writers problem - Writers priority

Configuration

- R readers
- W writers
- A shared file they can read or write.

Rules

- Multiple readers can read the file at the same time
- Only one writer can write at a given time
- If readers are reading no writer can write and vice versa

Policy

- Writers priority
 - No new readers allowed once a writer has asked for access, when a reader finishes it signals another writer in any, otherwise a reader

(1) Interface definition

```
Writer()  
{  
    loop  
        AskToWrite()  
        // write on the file  
        ...  
        EndWrite()  
    endloop  
}
```

```
Reader()  
{  
    loop  
        AskToRead()  
        // read file  
        ...  
        EndRead()  
    endloop  
}
```

(2) Acceptance conditions

AskToWrite()	No writer and no readers
EndWrite()	nothing
AskToRead()	No writer and no writer(s) waiting
EndRead()	nothing

(3) State variables

They allow to write the acceptance predicates

<code>NumWriters : int := 0</code>	Number of writers on the file
<code>NumWritersWaiting : int := 0</code>	Number of writers waiting to write
<code>NumReaders : int := 0</code>	Number of readers on the file

(4) Invariants and acceptance predicates

Invariants:

$(\text{NumReaders} = 0 \vee \text{NumWriters} = 0) \wedge (\text{NumWriters} \leq 1)$

AskToWrite()	<i>No writer and no readers</i> $(\text{NumReaders} = 0 \wedge \text{NumWriters} = 0)$
AskToRead()	<i>No writer and no writer(s) waiting</i> $(\text{NumWriters} = 0 \wedge \text{NumWritersWaiting} = 0)$

(5) Condition variables

- Associate a **condition variable** with each **acceptance predicate**
- They will be used to wait for/signal the validity of the predicate.

Operation	Acceptance predicate	Condition variable
AskToWrite()	$(\text{NumReaders} == 0 \wedge \text{NumWriters} == 0)$	CanWrite
AskToRead()	$\begin{aligned} &(\text{NumWriters} == 0 \\ &\quad \wedge \\ &\text{NumWritersWaiting} == 0) \end{aligned}$	CanRead

(6) Programming

Writer

AskToWrite()

```
// No writer and no readers
if ¬(NumReaders = 0 ∧ NumWriters = 0) then
    NumWritersWaiting++
    CanWrite.wait()
    NumWritersWaiting--
endif
{NumReaders = 0 ∧ NumWriters = 0}
NumWriters++
{NumWriters = 1}
```

(6) Programming

Writer

EndWrite()

```
{NumReaders = 0  $\wedge$  NumWriters = 1}
NumWriters--
{NumReaders = 0  $\wedge$  NumWriters = 0}
// priority to the writers
if (NumWritersWaiting > 0) then
    CanWrite.signal()
else
    CanRead.signal()
endif
```

(6) Programming

Reader

AskToRead()

```
// No writer and no writer(s) waiting
if ¬(NumWriters = 0 ∧ NumWritersWaiting = 0) then
    CanRead.wait()
endif
{NumWriters = 0 ∧ NumWritersWaiting = 0}
NumReaders++
{NumWriters = 0 ∧ NumReaders > 0 ∧ NumWritersWaiting = 0}
CanRead.signal()
```

(6) Programming

Reader

EndRead()

```
{NumReaders > 0  $\wedge$  NumWriters = 0}
```

```
NumReaders--
```

```
if (NumReaders = 0) then
```

```
    {NumReaders = 0  $\wedge$  NumWriters = 0}
```

```
    CanWrite.signal()
```

```
endif
```

(7) Checking

- For each condition variable, check that **each signal precondition** (state at the moment when the signal is called) implies **each wait postcondition** (in this case, the acceptance predicate).

(7) Checking - signal-and-wait

AskToWrite()

```
// No writer and no readers
if ¬(NumReaders = 0 ∧ NumWriters = 0) then
    NumWritersWaiting++
    CanWrite.wait()
    NumWritersWaiting--
endif
{NumReaders = 0 ∧ NumWriters = 0}
NumWriters++
{NumWriters = 1}
```

EndWrite()

```
{NumReaders = 0 ∧ NumWriters = 1}
NumWriters--
{NumReaders = 0 ∧ NumWriters = 0}
// priority to the writers
if (NumWritersWaiting > 0) then
    CanWrite.signal()
else
    CanRead.signal()
endif
```

AskToRead()

```
// No writer and no writer(s) waiting
if ¬(NumWriters = 0 ∧ NumWritersWaiting = 0) then
    CanRead.wait()
endif
{NumWriters = 0 ∧ NumWritersWaiting = 0}
NumReaders++
{NumWriters = 0 ∧ NumReaders > 0} ∧
NumWritersWaiting = 0
CanRead.signal()
```

EndRead()

```
{NumReaders > 0 ∧ NumWriters = 0}
NumReaders--
if (NumReaders = 0) then
    {NumReaders = 0 ∧ NumWriters = 0}
    CanWrite.signal()
endif
```

(7) Checking - signal-and-wait

AskToWrite()

```
// No writer and no readers
if ¬(NumReaders = 0 ∧ NumWriters = 0) then
    NumWritersWaiting++
    CanWrite.wait()
    NumWritersWaiting--
endif
{NumReaders = 0 ∧ NumWriters = 0} ←
NumWriters++
{NumWriters = 1}
```

AskToRead()

```
// No writer and no writer(s) waiting
if ¬(NumWriters = 0 ∧ NumWritersWaiting = 0) then
    CanRead.wait()
endif
{NumWriters = 0 ∧ NumWritersWaiting = 0}
NumReaders++
{NumWriters = 0 ∧ NumReaders > 0 ∧
NumWritersWaiting = 0}
CanRead.signal()
```

EndWrite()

```
{NumReaders = 0 ∧ NumWriters = 1}
NumWriters--
{NumReaders = 0 ∧ NumWriters = 0} ←
// priority to the writers
if (NumWritersWaiting > 0) then
    CanWrite.signal()
else
    CanRead.signal()
endif
```

EndRead()

```
{NumReaders > 0 ∧ NumWriters = 0}
NumReaders--
if (NumReaders == 0) then
    {NumReaders == 0 ∧ NumWriters = 0} ←
    CanWrite.signal()
endif
```

(7) Checking - signal-and-wait

AskToWrite()

```
// No writer and no readers
if ¬(NumReaders = 0 ∧ NumWriters = 0) then
    NumWritersWaiting++
    CanWrite.wait()
    NumWritersWaiting--
endif
{NumReaders = 0 ∧ NumWriters = 0}
NumWriters++
{NumWriters = 1}
```

AskToRead()

```
// No writer and no writer(s) waiting
if ¬(NumWriters = 0 ∧ NumWritersWaiting = 0) then
    CanRead.wait()
endif
{NumWriters = 0 ∧ NumWritersWaiting = 0} ←
NumReaders++
{NumWriters = 0 ∧ NumReaders > 0 ∧
NumWritersWaiting = 0}
CanRead.signal()
```

EndWrite()

```
{NumReaders = 0 ∧ NumWriters = 1}
NumWriters--
{NumReaders = 0 ∧ NumWriters = 0} ←
// priority to the writers
if (NumWritersWaiting > 0) then
    CanWrite.signal()
else
    CanRead.signal()
endif
```

EndRead()

```
{NumReaders > 0 ∧ NumWriters = 0}
NumReaders--
if (NumReaders == 0) then
    {NumReaders == 0 ∧ NumWriters = 0}
    CanWrite.signal()
endif
```


(7) Checking - signal-and-continue



Configuration

- There is a writer writing, no writers waiting and
- At least one reader waiting (`CanRead.wait()`)

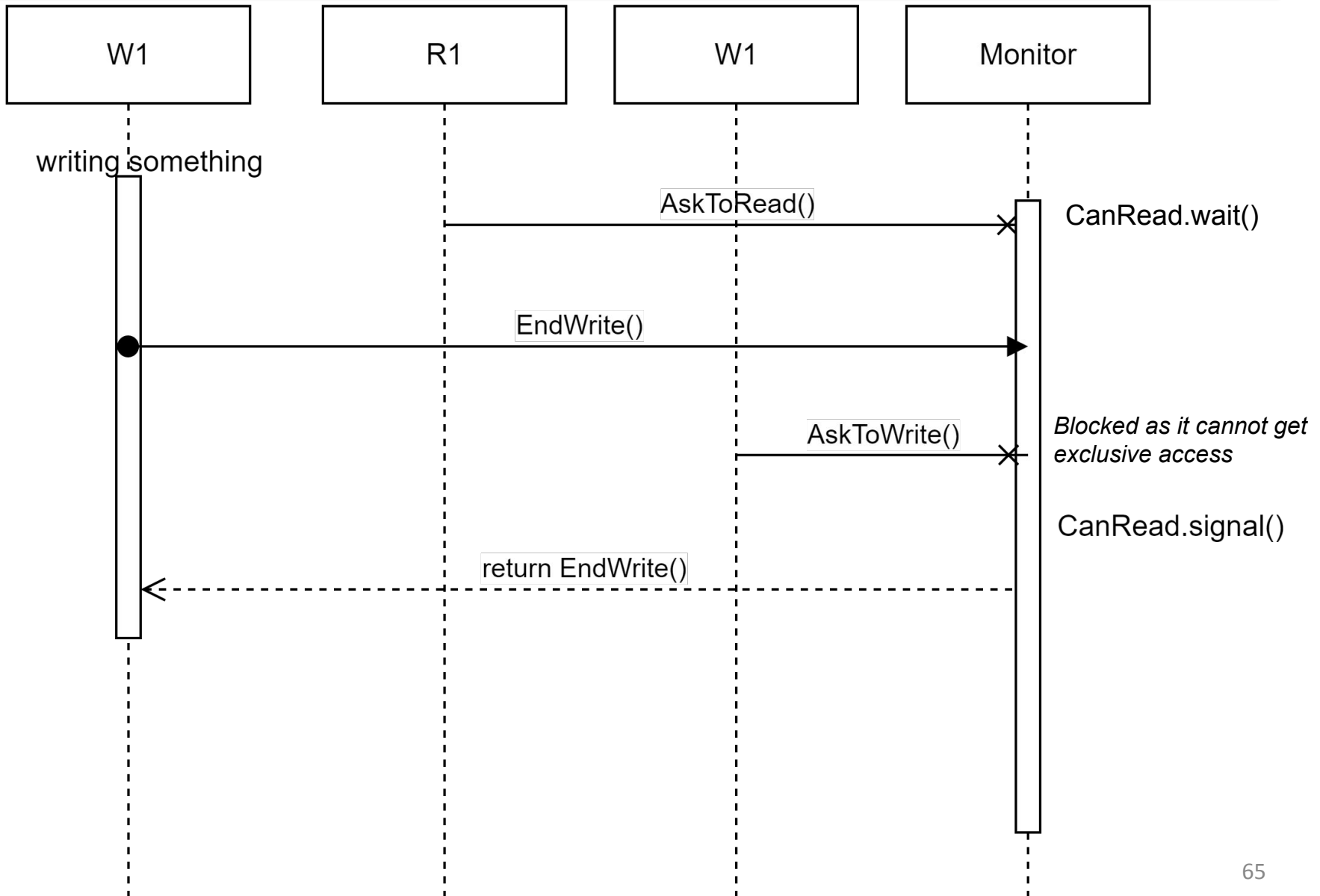
Scenario

- The writer is about to end (`EndWriting()`)
- The writer signals `CanRead.signal()`
 - Waiting reader(s) are now unblocked, i.e. they can ask for exclusive access
- Before the writer finishes a new writer arrives and asks for exclusive access for `AskToWrite()`.

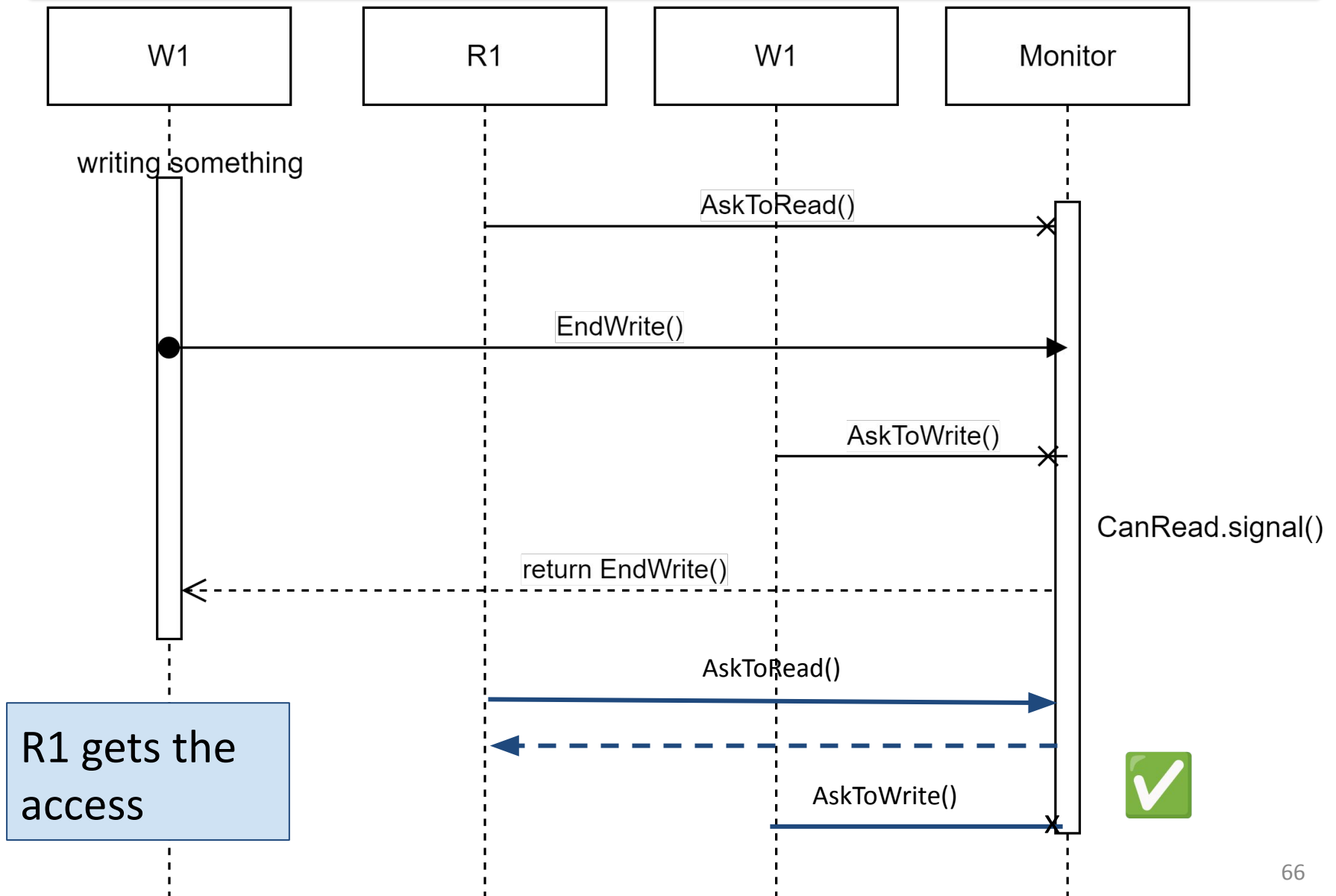
Who gets the access next?

- Reader? -->  OK he will wake all the others and the writer will eventually wait
- New Writer? 
 - the acceptance condition for `AskToWrite()` is satisfied and starts writing.
 - One of the readers will get access and start reading!

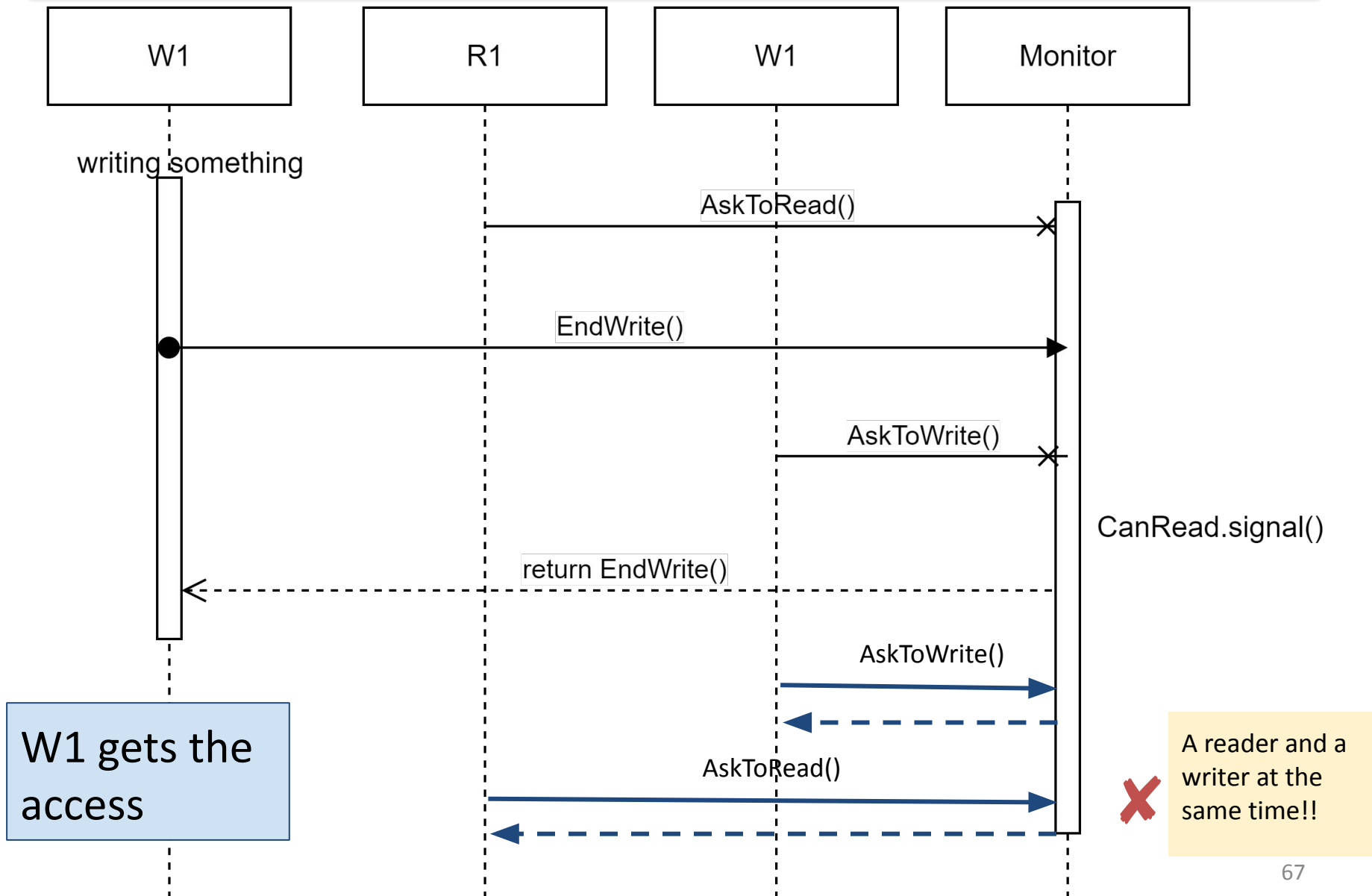
(7) Checking - signal-and-continue



(7) Checking - signal-and-continue



(7) Checking - signal-and-continue





(7) Checking - signal-and-continue

Scenario

- The writer is about to end (`EndWriting()`)
- The writer signals `CanRead.signal()`
 - Waiting reader(s) are now unblocked, i.e. they can ask for exclusive access
- Before the writer finishes a new writer arrives and asks for exclusive access for `AskToWrite()`.

Who gets the access next?

- Reader? -->  OK he will wake all the others and the writer will eventually wait
- New Writer? 
 - the acceptance condition for `AskToWrite()` is satisfied and starts writing.
 - One of the readers will get access and start reading!

It needs to check the condition again

```
AskToRead()  
    // No writer and no writer(s) waiting  
    while ¬(NumWriters = 0 ∧ NumWritersWaiting = 0)  
        CanRead.wait()  
    endwhile  
    {NumWriters = 0 ∧ NumWritersWaiting = 0}  
    NumReaders++  
    {NumWriters = 0 ∧ NumReaders > 0}  
    CanRead.signal()
```

(7) Checking - signal-and-continue

Scenario

- The same for the **writers**, there might be **2 writers at the same time!**
- A writer W1 is writing
- Another W2 is waiting
- As the W1 ends it signals the waiting writer W2
 - W2 is now unblocked and can ask for exclusive access
- Meanwhile a new writer W3 calls AskToWrite()
- Who gets the access after W1 finishes?
 - W2? **OK**, it will start writing and W3 will eventually wait on CanWrite
 - W3? **W3 starts writing and at some point W2 will too when he gets the access**

```
AskToWrite()
    // No writer and no readers
    while ¬(NumReaders = 0 ∧ NumWriters = 0)
        NumWritersWaiting++
        CanWrite.wait()
        NumWritersWaiting--
    endwhile
    {NumReaders = 0 ∧ NumWriters = 0}
    NumWriters++
    {NumWriters = 1}
```