

Supporting information 2: Estimating abundance with interruption in data collection. Simulations and case studies using open population spatial capture-recapture

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5 November 2019

This script performs a data set simulation and OPSCR modelling in the presence of sampling interruption with NIMBLE (NIMBLE Development Team 2019; Valpine et al. 2017). All details about the procedure are provided in Milleret et al. Estimating abundance with interruption in data collection: Simulations and case studies using open population spatial capture-recapture models.

I. Load Libraries

```
library(rgdal)
library(raster)
library(rgeos)
library(sp)
library(nimble)
library(abind)
library(boot)
library(coda)
```

Download the .R data file Containing the R functions [here](#), the Nimble functions [here](#), [here](#) and [here](#) is the R script.

Set working directory where the *SourceRFunctions.R*, *SourceNimblePointProcess.R* and *SourceNimbleObservationModel.R* are located and source the files.

```
setwd("YourWorkingdirectory")
source("SourceRFunctions.R")
source("SourceNimblePointProcess.R")
source("SourceNimbleObservationModel.R")
```

```
## Registering the following user-provided distributions: dbinomPP dbinomPPSingle dbinomMNormSourcePP d
## Registering the following user-provided distributions: dbin_LESS .
## Registering the following user-provided distributions: dbin_LESSCachedAllSparse .
## Warning: random generation function for dbin_LESSCachedAllSparse is not available. NIMBLE is generat
```

II.SET SIMULATION PARAMETERS

```
# HABITAT EXTENT
buffer <- 5
grid.size <- 30
# DETECTOR SPACING
```

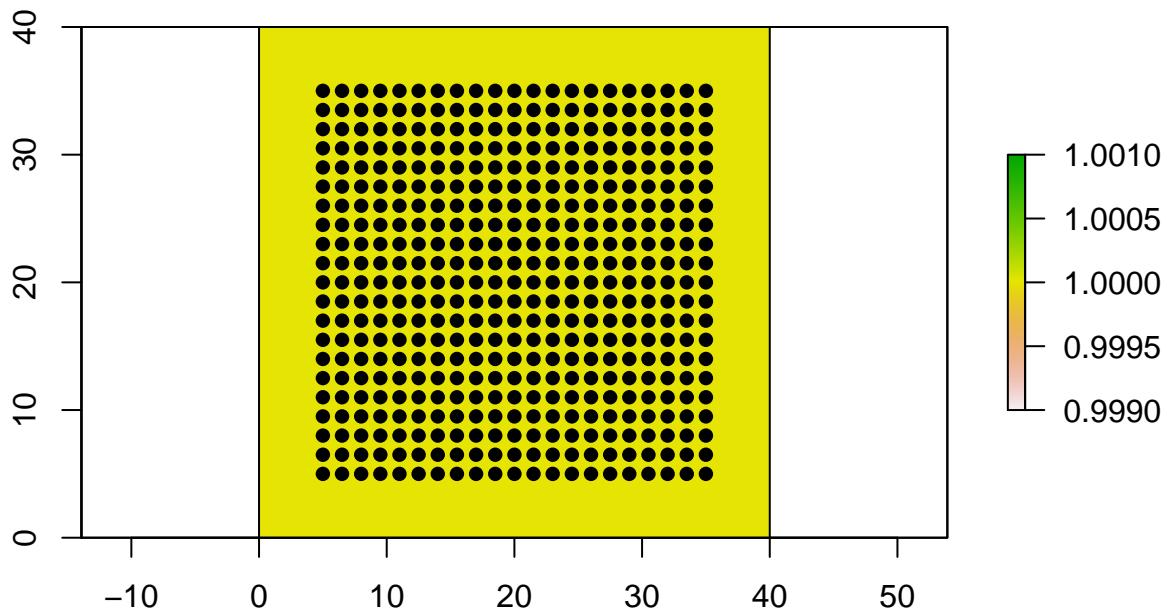


```

x <- rep(co, length(co))
y <- sort(rep(co, length(co)), decreasing = T)
detectors.xy <- cbind(x, y)
detectors.sp <- SpatialPoints(detectors.xy,
                              proj4string = CRS(proj4string(myStudyArea)))

# PLOT CHECK
plot(r)
plot(myStudyArea, add=T)
points(detectors.sp, col="black", pch=16)

```



```

### ===== 3.SIMULATE INDIVIDUAL STATE MATRIX =====
### ===== 3.1 DEFINE PHI AND RHO ARRAYS =====
# CREATE ARRAYS SO PHI AND RHO CAN VARY OVER TIME AND STOCHASTICITY IN VITAL RATES CAN BE ADDED (t)
PHI.arr <- array(NA, c(2,2, n.occasions))
REPRO.arr <- array(NA, c(2,2, n.occasions))
FEC.mat <- matrix(NA, nrow=2, ncol=n.occasions)
phit <- 0
fect <- 0

for(t in 1:n.occasions){
  # DEFINE THE PHI MATRIX
  # two states: ALIVE/DEAD
  # DRAW PHI FROM NORMAL DISTRIB AND APPLY LOGIT
  phit[t] <- inv.logit(rnorm(1, mean=logit(phi), sd=sd.phi))
  PHI.arr[, ,t] <- matrix(c(phit[t], 0,
                            1-phit[t], 1), ncol=2, nrow=2, byrow = TRUE)
}

```

```

# DEFINE REPRO MATRIX (p of reproducing)
# THIS DEFINES THE PROBABILITY OF INDIVIDUALS TO REPRODUCE (ASSUME ALL INDIVIDUALS REPRODUCE HERE)
REPRO.arr[,t] = matrix(c( p.repro, 0,
                          0 , 0 ), ncol=2, nrow=2, byrow = TRUE)

# DEFINE PER CAPITA RECRUITMENT. GIVEN THAT INDIVIDUAL REPRODUCES, HOW MANY ARE RECRUITED
fect[t] <- inv.logit(rnorm(1, mean=logit(rho), sd=sd.rho))
FEC.mat[,t] = c(fect[t], 0)
}

### ===== 3.2 SIMULATE Z =====
z.mx <- SimulateZ( NO = N1,
                  n.occasions = n.occasions-1,
                  PHI = PHI.arr,
                  REPRO = REPRO.arr,
                  FEC = FEC.mat,
                  init.state = 1)

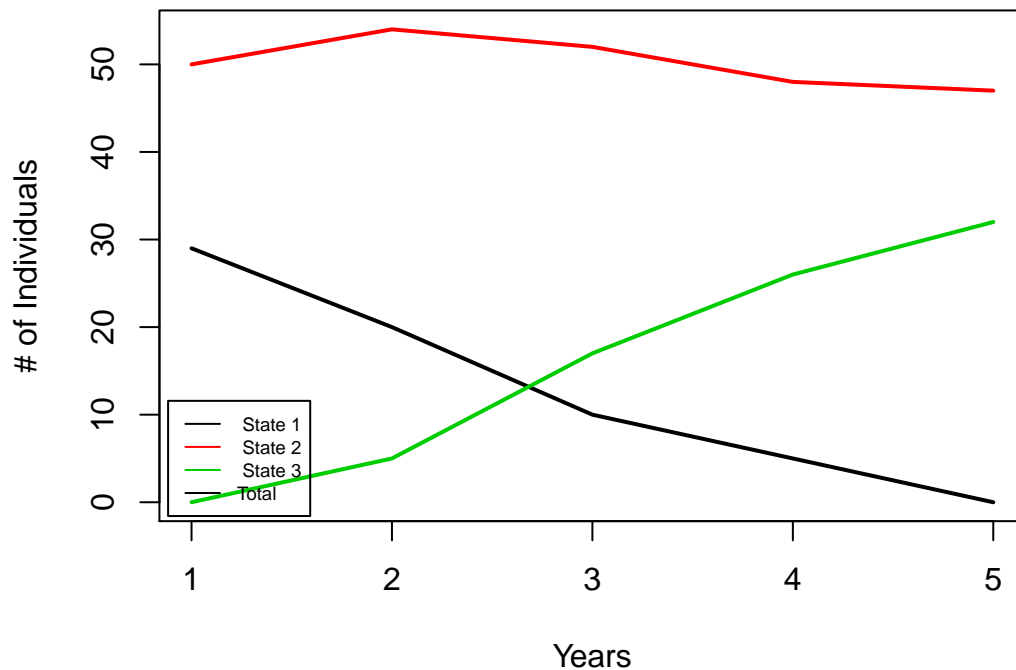
myZ <- z.mx$z
# ADD THE NOT ENTERED STATE
# 1: NOT ENTERED
# 2: ALIVE
# 3: DEAD
myZ <- myZ+1
myZ[is.na(myZ)] <- 1

# GET POP COMPOSITION AND PLOT IT
z.levels <- unique(na.omit(unlist(apply(myZ, 1, unique))))
z.levels <- z.levels[order(z.levels)]
Pop.Compo <- list()
for(l in 1:length(z.levels)){
  Pop.Compo[[l]] <- apply(myZ, 2, function(x){length(which(x == z.levels[l]))})
}#l

# PLOT CHECK
plot(1:dim(myZ)[2], Pop.Compo[[1]], type="l", col=1, lwd=2,
     ylim=c(0, max(unlist(Pop.Compo))),
     xlab = "Years", ylab = "# of Individuals")

for(l in 2:length(Pop.Compo)){
  points(1:dim(myZ)[2], Pop.Compo[[l]], type="l", col=1, lwd=2)
}#l
legend("bottomleft"
      , legend = c(unlist(lapply(z.levels, function(x){paste(" State", x)})), "Total")
      , col = 1:length(Pop.Compo)
      , lwd = 1
      , cex = 0.6
      , inset = 0.01)

```



```

### ===== 4. SIMULATE INDIVIDUAL AC LOCATIONS =====
### ===== 4.1 FIRST OCCASION =====
# CREATE EMPTY OBJECTS
mySimulatedACs <- list()
tempCoords <- matrix(NA, nrow=dim(myZ)[1], ncol=2)

# SIMULATE UNIFORM LOCATION OF ACS
for(i in 1:dim(myZ)[1]){
  tempCoords[i,] <- rbinomPPSingle( n = 1
    , lowerCoords = lowerCoords
    , upperCoords = upperCoords
    , intensityWeights = habitatQuality
    , areAreas = 1
    , numWindows = nrow(lowerCoords))
}#i

# STORE ACS IN A SP OBJECT
mySimulatedACs[[1]] <- SpatialPointsDataFrame( tempCoords
  , data.frame( x = tempCoords[, 1]
    , y = tempCoords[, 2]
    , Id = 1:nrow(tempCoords))
  , proj4string = CRS(proj4string(r)))

### ===== 4.2 FOLLOWING YEARS =====
# DRAW SUBSEQUENT INDIVIDUAL ACS FROM A NORMAL DISTRIBUTION CENTERED AROUND THE SOURCE COORDINATE
# WITH A SD EQUAL TO "tau"
# THERE IS THE POSSIBILITY TO DEFINE A HABITAT QUALITY SURFACE

```

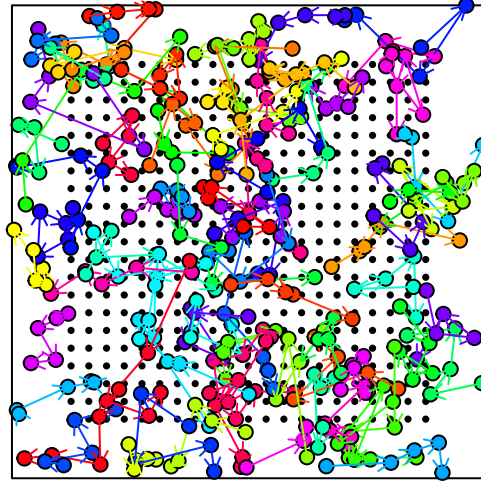
```

# FOR THE PUPORSE OF THE STUDY, HABITAT QUALITY WAS UNIFORM (SET TO 1 EVERYWHERE)
for(t in 2:dim(myZ)[2]){
  for(i in 1:nrow(tempCoords)){
    tempCoords[i,] <- rbinomMNormSourcePPSSingle( n = 1
                                                    , lowerCoords = lowerCoords
                                                    , upperCoords = upperCoords
                                                    , sourceCoords = tempCoords[i,]
                                                    , normSD = tau
                                                    , intensityWeights = habitatQuality
                                                    , areAreas = 1
                                                    , numWindows = nrow(lowerCoords))
  }
  # STORE ACS IN A SP OBJECT
  mySimulatedACs[[t]] <- SpatialPointsDataFrame( tempCoords
                                                    , data.frame( x = tempCoords[, 1]
                                                                , y = tempCoords[, 2]
                                                                , Id = 1:nrow(tempCoords))
                                                    , proj4string = CRS(proj4string(mySimulatedACs[[t-1]]))
)##t

# PLOT CHECK
plot(aggregate(rasterToPolygons(r,fun = function(x){x>0})))
points(detectors.sp, pch=16, cex=0.5)
col <- rainbow(length(mySimulatedACs[[1]]))
points(mySimulatedACs[[1]], pch=21, bg=col)

for(t in 2:length(mySimulatedACs)){
  points(mySimulatedACs[[t]], pch=21, bg=col)
  arrows( x0 = coordinates(mySimulatedACs[[t]])[,1]
          , x1 = coordinates(mySimulatedACs[[t-1]])[,1]
          , y0 = coordinates(mySimulatedACs[[t]])[,2]
          , y1 = coordinates(mySimulatedACs[[t-1]])[,2], col = col, length = 0.08)
}##t

```



```

### ===== 5.SIMULATE DETECTION =====
### ===== 5.1 DETECTION ARRAY =====
z.not.alive <- apply(myZ, 2, function(x){which(x %in% c(1,3))})
Y <- array(NA, c(dim(myZ)[1], length(detectors.sp), dim(myZ)[2]))

for(t in 1:dim(myZ)[2]){
  D <- gDistance(detectors.sp, mySimulatedACs[[t]], byid=TRUE)
  # OBTAIN Y DETECTION MATRIX USING HALF NORMAL DETECTION FUNCTION (EQN 7 IN MAIN TEXT)
  fixed.effects <- rep(log(p0), length(detectors.sp))
  pzero <- exp(fixed.effects)
  p <- pzero * exp(-D*D/(2*sigma*sigma))
  Y[,t] <- apply(p, c(1,2), function(x) rbinom(1, 1, x))
  # individuals not alive can't be detected
  Y[z.not.alive[[t]],t] <- 0
}

}#t
### ===== 5.1 PLOT CHECK =====
par(mfrow=c(2,3), mar=c(0,0,3,0))
for(t in 1:dim(myZ)[2]){
  plot(myStudyArea)
  title(t)
  points(detectors.sp, pch=16, cex=0.6)
  detections <- apply(Y[,t], 1, function(x) which(x>0))
  col <- rainbow(dim(Y)[1])[sample(dim(Y)[1])]
  for(i in 1:length(detections)){
    if(!i %in% z.not.alive[[t]]){

```

```

        if(length(detectors.sp[detections[[i]],]) == 0){
          points(mySimulatedACs[[t]][i,], bg=col[i], pch=21, cex=0.5)
          points(mySimulatedACs[[t]][i,], col=col[i], pch=4)

        }else{
          points(detectors.sp[detections[[i]],], col=col[i], pch=16, cex=0.7)
          ac <- coordinates(mySimulatedACs[[t]][i,])
          dets <- coordinates(detectors.sp[detections[[i]],])
          segments(x0=ac[1,1], x1=dets[1,1], y0=ac[1,2], y1=dets[2,2], col=col[i])
          points(mySimulatedACs[[t]][i,], bg=col[i], pch=21)

        }#else
      }#if
    }#i
  }#t

  ### ===== 6.AUGMENT DATA SET =====
  # REMOVE UNDETECTED IDS
  detected.time <- apply(Y, c(1,3), function(x) any(x >= 1))
  detected <- apply(detected.time, c(1), function(x) sum(x==1)>0)
  Y <- Y[detected,,]

  #AUGMENTATION= "augmentation" x N OF THE SUPER POPULATION
  y.aug <- array(0, c( nrow(myZ)*augmentation - dim(Y)[1], dim(Y)[2:3]))
  y <- abind(Y, y.aug, along = 1)
  dim(y)

  ## [1] 94 441 5

  ### ===== 7.ADD INTERRUPTION =====
  interruptions <- which(toggle.interruption==0)
  if(length(interruptions)>0){
    # ZERO DETECTIONS DURING INTERRUPTIONS
    y[,interruptions] <- 0
  }

  ### ===== 8.RECONSTRUCT z VALUES =====
  z <- apply(y, c(1,3), function(x) any(x>0))
  z <- ifelse(z, 2, NA)

  z <- t(apply(z, 1, function(zz){
    if(any(!is.na(zz))){
      range.det <- range(which(!is.na(zz)))
      zz[range.det[1]:range.det[2]] <- 2
    }
    return(zz)
  })))

  ### ===== 9.GENERATE z INITIAL values=====
  z.init <- t(apply(z, 1, function(zz){
    out <- zz
    out[] <- 1
    if(any(!is.na(zz))){
      range.det <- range(which(!is.na(zz)))

```

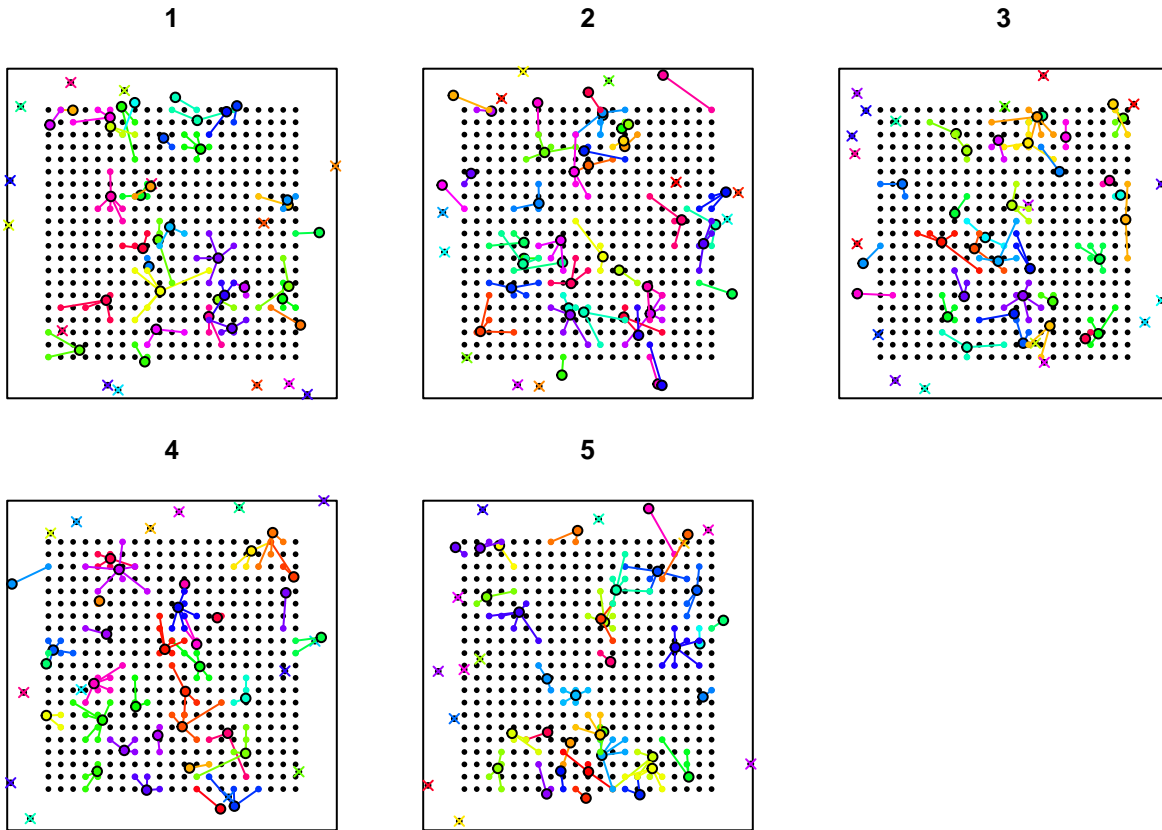


```

    if(range.det[1]>1)zz[1:(range.det[1]-1)] <- 1
    if(range.det[2]<length(zz))zz[(range.det[2]+1):length(zz)] <- 3
    out[] <- zz
  }
  return(out)
}))

z.init <- ifelse(!is.na(z), NA, z.init)

```



III.NIMBLE

```

### ===== 1.MODEL CODE =====
modelCode <- nimbleCode({
  ##-----
  ##-----##
  ##----- SPATIAL PROCESS -----##
  ##-----##
  tau ~ dgamma(0.001, 0.001)

  for(i in 1:n.individuals){
    sxy[i, 1:2, 1] ~ dbinomPPSingle(lowerHabCoords[1:n.cells, 1:2], upperHabCoords[1:n.cells, 1:2], mu[
    for(t in 2:n.years){
      sxy[i, 1:2, t] ~ dbinomMNormSourcePPSingle(lowerHabCoords[1:n.cells, 1:2]
        , upperHabCoords[1:n.cells, 1:2]

```

```

, sxy[i, 1:2, t - 1]
, tau
, mu[1:n.cells]
, 1
, n.cells,-1)

} #t
} #i

##-----##
##-----##
##----- DEMOGRAPHIC PROCESS -----##
##-----##

psi ~ dunif(0, 1)
phi ~ dunif(0, 1)
rho ~ dunif(0, 5)
for (t in 2:n.years) {
  gamma[t - 1] <- (N[t - 1] * rho)/n.available[t - 1]
} #t
omeg1[1] <- 1 - psi
omeg1[2] <- psi
omeg1[3] <- 0
for (t in 1:(n.years1)) {
  # NOT ENTERED
  omega[1, 1, t] <- 1 - gamma[t]
  omega[1, 2, t] <- gamma[t]
  omega[1, 3, t] <- 0
  # ALIVE
  omega[2, 1, t] <- 0
  omega[2, 2, t] <- phi
  omega[2, 3, t] <- 1 - phi
  # DEAD
  omega[3, 1, t] <- 0
  omega[3, 2, t] <- 0
  omega[3, 3, t] <- 1
} #t
for (i in 1:n.individuals) {
  z[i, 1] ~ dcat(omeg1[1:3])
  for (t in 1:(n.years1)) {
    z[i, t + 1] ~ dcat(omega[z[i, t], 1:3, t])
  } #t
}

##-----##
##-----##
##----- DETECTION PROCESS -----##
##-----##

sigma ~ dunif(0,5)
p0 ~ dunif(0,1)
for(i in 1: n.individuals){
  for(t in 1:n.years){
    y[i,1:nMaxDetectors,t] ~ dbin_LESSCachedAllSparse ( pZero = p0 * toggle[t]

```

```

, sxy = sxy[i,1:2,t]
, sigma = sigma
, nbDetections[i,t]
, yDets = yDets[i,1:nMaxDetectors,t]
, detector.xy = detector.xy[1:n.detectors
, trials = trials[1:n.detectors]
, detectorIndex = detectorIndex[1:n.cellsSp
, nDetectorsLESS = nDetectorsLESS[1:n.cells
, ResizeFactor = ResizeFactor
, maxNBDets = maxNBDets
, habitatID = habitatIDDet[1:y.maxDet,1:x.m
, maxDist = maxDist
, indicator = z[i,t]==2)

}#t
}#i

##-----
##-----##
##----- DERIVED PARAMETERS -----##
##-----##
for(t in 1:n.years){
  N[t] <- sum(z[1:n.individuals, t]==2)
  n.available[t] <- sum(z[1:n.individuals, t]==1)
}#t
})

### ==== 2.NIMBLE DATA ====
nimDims <- list( "omeg1" = 3
, "omega" = c(3,3,4)
, "z" = c(dim(y)[1], dim(y)[3]))

params <- c("N", "tau"
, "p0", "phi", "sigma", "rho", "z", "sxy")

nimConstants <- list( n.individuals = dim(y)[1]
, n.detectors = dim(y)[2]
, n.years = dim(y)[3]
, nyears1 = dim(y)[3]-1
, n.cells = nrow(lowerCoords))

myScaledDetectors <- UTMToGrid(grid.sp = SpatialPoints(coordinates(r)),
data.sp = detectors.sp,
plot.check = F)

nimData <- list( z = z
, y = y
, toggle = toggle.interruption
, detector.xy = myScaledDetectors$data.scaled.xy

```

```

, lowerHabCoords = myScaledDetectors$grid.scaled.xy - 0.5
, upperHabCoords = myScaledDetectors$grid.scaled.xy + 0.5
, mu = habitatQuality)

sxy <- MakeInitsXY( y= y
, detector.xy = detectors.xy
, habitat.r = r
, dist.move = 3)

for( t in 1:dim(sxy)[3]){
  sxy[, ,t] <- UTMToGrid(grid.sp = SpatialPoints(coordinates(r)),
    data.sp = SpatialPoints(sxy[, ,t]),
    plot.check = F
  )$data.scaled.xy
}

nimInits <- list(z = z.init, rho = rho, phi = phi, sigma = sigma,
  psi = 0.1, p0 = p0, sxy = sxy, tau = tau)

```

III.NIMBLE TRICKS

Here we need to create a few objects that are necessary to make the computation of OPSCR models more efficient. The first step consists in performing a local evaluation of the state space (LESS) (Milleret et al. 2019). This means that detectors that are further away than a certain distance from a given individual activity center are not evaluated. If the distance threshold is large enough, it should not cause any bias (see Milleret et al. (2019) for further details).

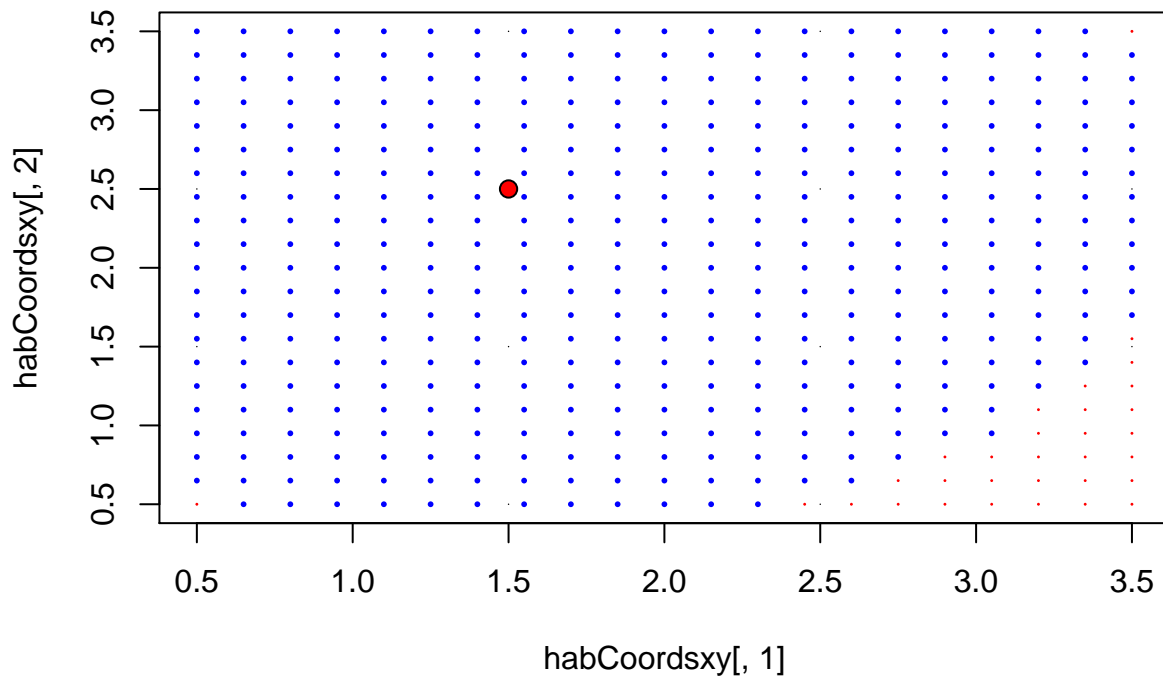
The function GetDetectorIndex identifies the set of detectors that are within a certain distance from each habitat cell center. The distance value should be large enough so that for any particular individual, the sxy values of the initial activity center restrict the calculation of p0 to all detectors with positive detections. Here, we use maxDist=2.2.

When the dimensions of the habitat matrix is large, we can resize it to lower dimensions. This may help reducing the number of habitat cells for which we have to identify the set of detectors that are within a certain distance from the cell center. The ResizeFactor argument which corresponds to the the fact argument used internally in raster::disaggregate. The goal is to create the object DetectorIndex\$detectorIndex of the smallest dimension possible.

```

### ==== 1. CREATE CACHED DETECTORS OBJECTS ====
DetectorIndexLESS <- GetDetectorIndexLESS(habitat.mx = as.matrix(r),
  detectors.xy = myScaledDetectors$data.scaled.xy,
  maxDist = 2.2,
  ResizeFactor = 1,
  plot.check = TRUE)

```



```
nimConstants$maxNBdets <- DetectorIndexLESS$maxNBdets
nimConstants$y.maxDet <- dim(DetectorIndexLESS$habitatID)[1]
nimConstants$x.maxDet <- dim(DetectorIndexLESS$habitatID)[2]
nimData$detectorIndex<- DetectorIndexLESS$detectorIndex
nimData$habitatIDDet<- DetectorIndexLESS$habitatID

nimData$nDetectorsLESS <- DetectorIndexLESS$nDetectorsLESS
nimConstants$n.cellsSparse <- dim(DetectorIndexLESS$detectorIndex)[1]
nimConstants$ResizeFactor <- DetectorIndexLESS$ResizeFactor
nimConstants$maxDist <- 2.2
```

Last, we re-express the detection matrix *y* to reduce its size. We use a new representation, where each row (corresponding to one individual) contains the detector identification numbers (values of *j*) which detected that individual.

A second matrix of identical dimension was also created, containing the number of detections occurring at each detector. The second matrix would be necessary for modelling non-binary detections.

```
### ===== 2. CREATE SPARSE MATRICES =====

SparseY <- GetSparseY(nimData$y)

# ADD TO NIMDATA
nimData$y = SparseY$y ## Detection array
nimData$yDets = SparseY$yDets
nimData$nbDetections = SparseY$nbDetections
```

```
nimData$trials = rep(1, nimConstants$n.detectors)
```

```
nimConstants$nMaxDetectors = SparseY$nMaxDetectors
```

```
## IV.NIMBLE RUN
```

```
model <- nimbleModel(code = modelCode, constants = nimConstants,  
                    data = nimData, inits = nimInits, check = FALSE, calculate = FALSE)
```

```
## defining model...
```

```
## building model...
```

```
## setting data and initial values...
```

```
## checking model sizes and dimensions...
```

```
## Warning in model$checkBasics(): Possible size/dimension mismatch  
## amongst vectors and matrices in BUGS expression: sxy[i, 1:2, 1] ~  
## dbinomPPSingle(lowerCoords = lowerHabCoords[1:16, 1:2], upperCoords =  
## upperHabCoords[1:16, 1:2], intensityWeights = mu[1:16], areAreas = 1,  
## numWindows = 16, lower_ = -Inf, upper_ = Inf). Ignore this warning if the  
## user-provided distribution has multivariate parameters with distinct sizes  
## or if size of variable differs from sizes of parameters.
```

```
## Warning in model$checkBasics(): Possible size/dimension mismatch  
## amongst vectors and matrices in BUGS expression: sxy[i, 1:2, t] ~  
## dbinomMNormSourcePPSingle(lowerCoords = lowerHabCoords[1:16, 1:2],  
## upperCoords = upperHabCoords[1:16, 1:2], sourceCoords = sxy[i, 1:2, t - 1],  
## normSD = tau, intensityWeights = mu[1:16], areAreas = 1, numWindows = 16,  
## localEvalParam = -1, lower_ = -Inf, upper_ = Inf). Ignore this warning if  
## the user-provided distribution has multivariate parameters with distinct  
## sizes or if size of variable differs from sizes of parameters.
```

```
## Warning in model$checkBasics(): Possible size/dimension mismatch  
## amongst vectors and matrices in BUGS expression: y[i, 1:7, t] ~  
## dbin_LESSCachedAllSparse(pZero = lifted_p0_times_toggle_oBt_cB_L32[t],  
## sxy = sxy[i, 1:2, t], sigma = sigma, nbDetections = nbDetections[i,  
## t], yDets = yDets[i, 1:7, t], detector.xy = detector.xy[1:441, 1:2],  
## trials = trials[1:441], detectorIndex = detectorIndex[1:16, 1:410],  
## nDetectorsLESS = nDetectorsLESS[1:16], ResizeFactor = 1, maxNBDets =  
## 410, habitatID = habitatIDDet[1:4, 1:4], maxDist = 2.2, indicator =  
## lifted_z_oBi_comma_t_cB_eq_eq_2_L32[i, t], lower_ = -Inf, upper_ = Inf).  
## Ignore this warning if the user-provided distribution has multivariate  
## parameters with distinct sizes or if size of variable differs from sizes of  
## parameters.
```

```
## This model is not fully initialized. This is not an error. To see which variables are not initialized  
## model building finished.
```

```
cmodel <- compileNimble(model)
```

```
## compiling... this may take a minute. Use 'showCompilerOutput = TRUE' to see C++ compilation details.  
## compilation finished.
```

```
cmodel$calculate()
```

```
## [1] -15711.83
```

```
MCMCconf <- configureMCMC(model = model, monitors = c(params),  
                          control = list(reflective = TRUE, adaptScaleOnly = TRUE),
```

```

                                useConjugacy = FALSE)
MCMC <- buildMCMC(MCMCconf)
cMCMC <- compileNimble(MCMC, project = model, resetFunctions = TRUE)

## compiling... this may take a minute. Use 'showCompilerOutput = TRUE' to see C++ compilation details
## compilation finished.

set.seed(0)
myNimbleOutput <- runMCMC(mcmc = cMCMC,
                          nburnin = nburnin, niter = niter, nchains = nchains, samplesAsCodaMCMC = TRUE)

## running chain 1...
## |-----|-----|-----|-----|
## |-----|
##
## running chain 2...
## |-----|-----|-----|-----|
## |-----|
##
## running chain 3...
## |-----|-----|-----|-----|
## |-----|

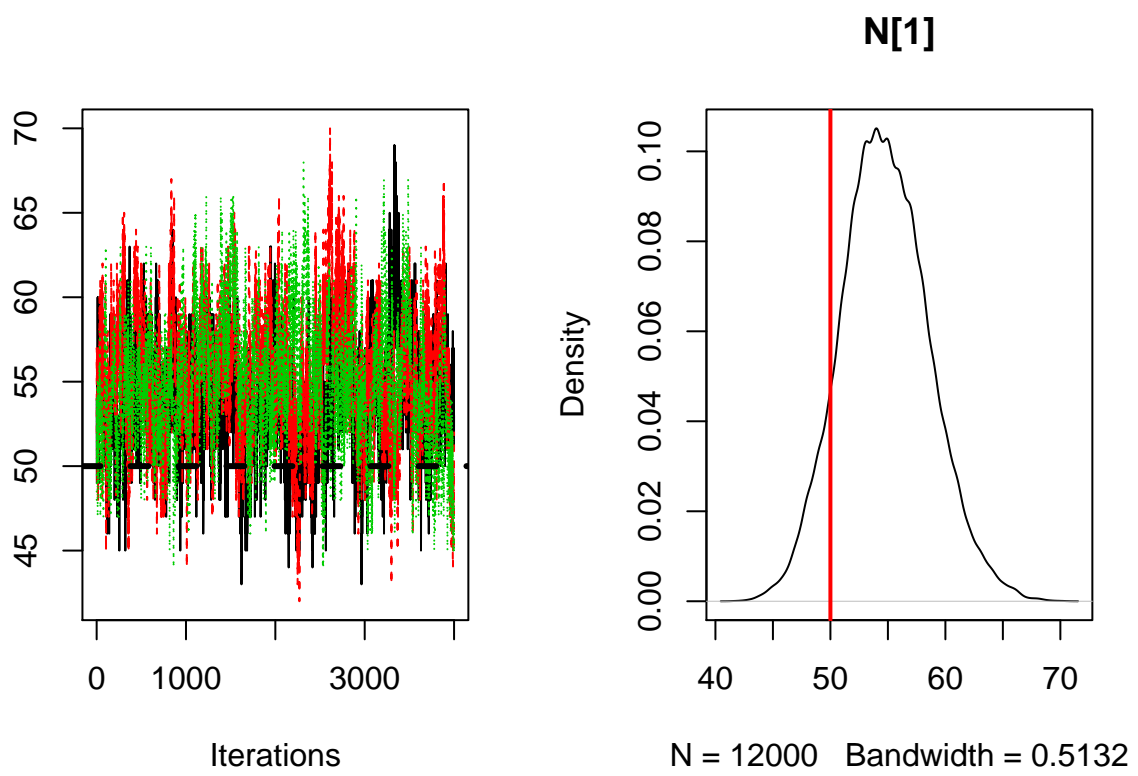
```

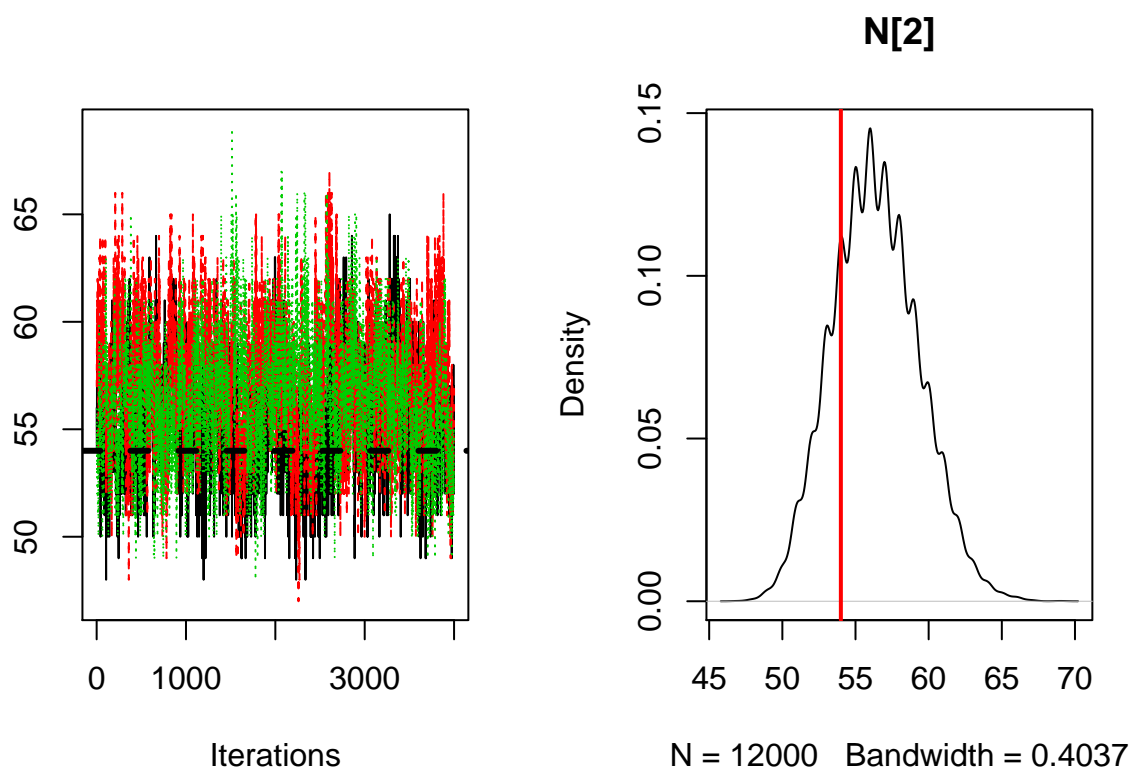
V.PLOT OUTPUT

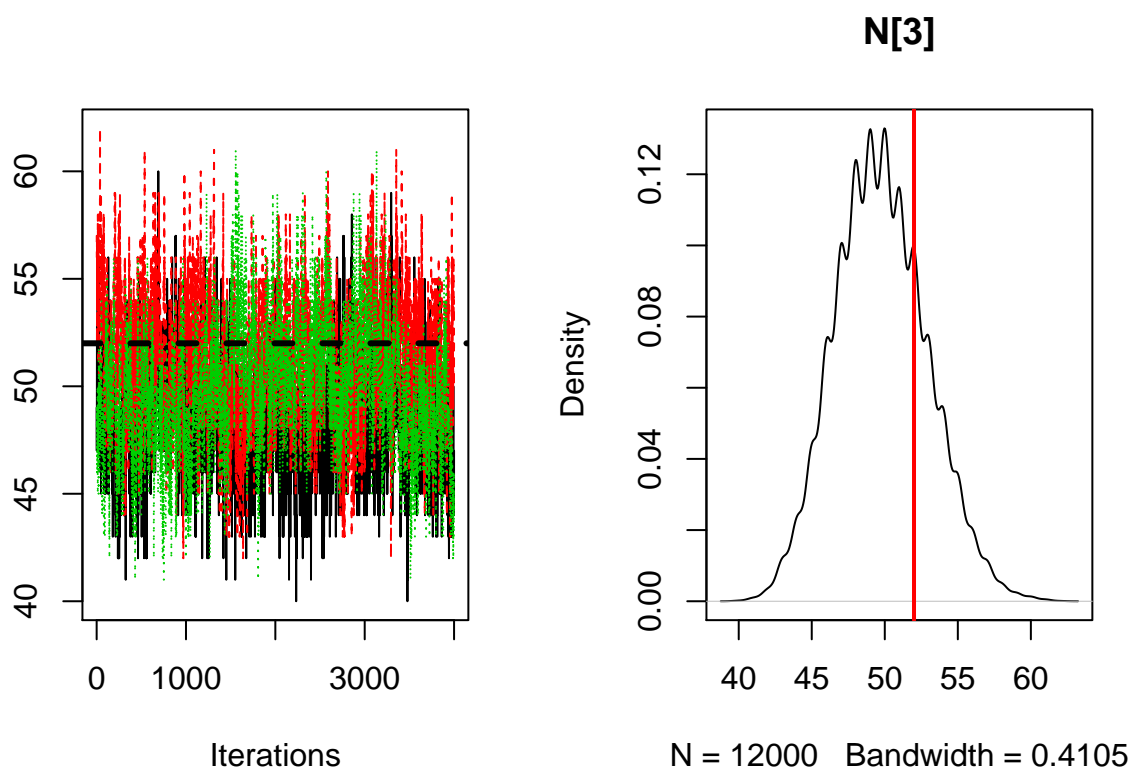
```

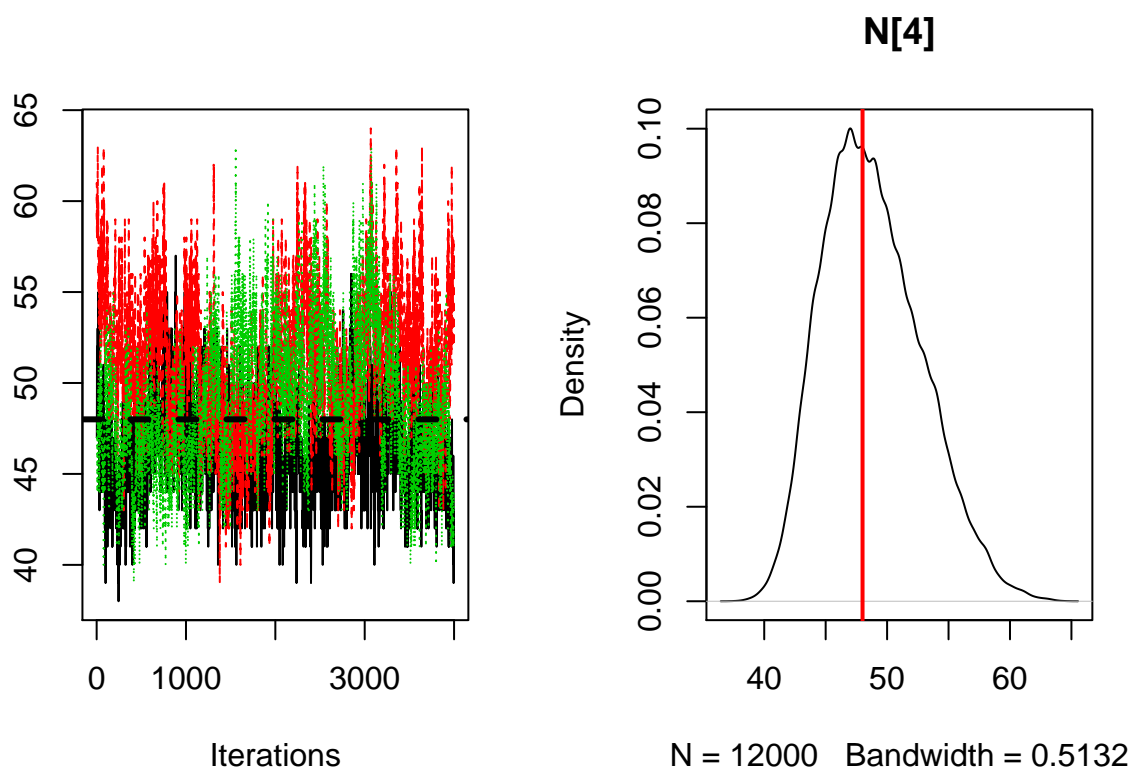
# N
for(t in 1:n.occasions){
  PlotJagsParams(myNimbleOutput, params= paste("N[,t,]", sep=""), sim.values=Pop.Compo[[2]][t])
}

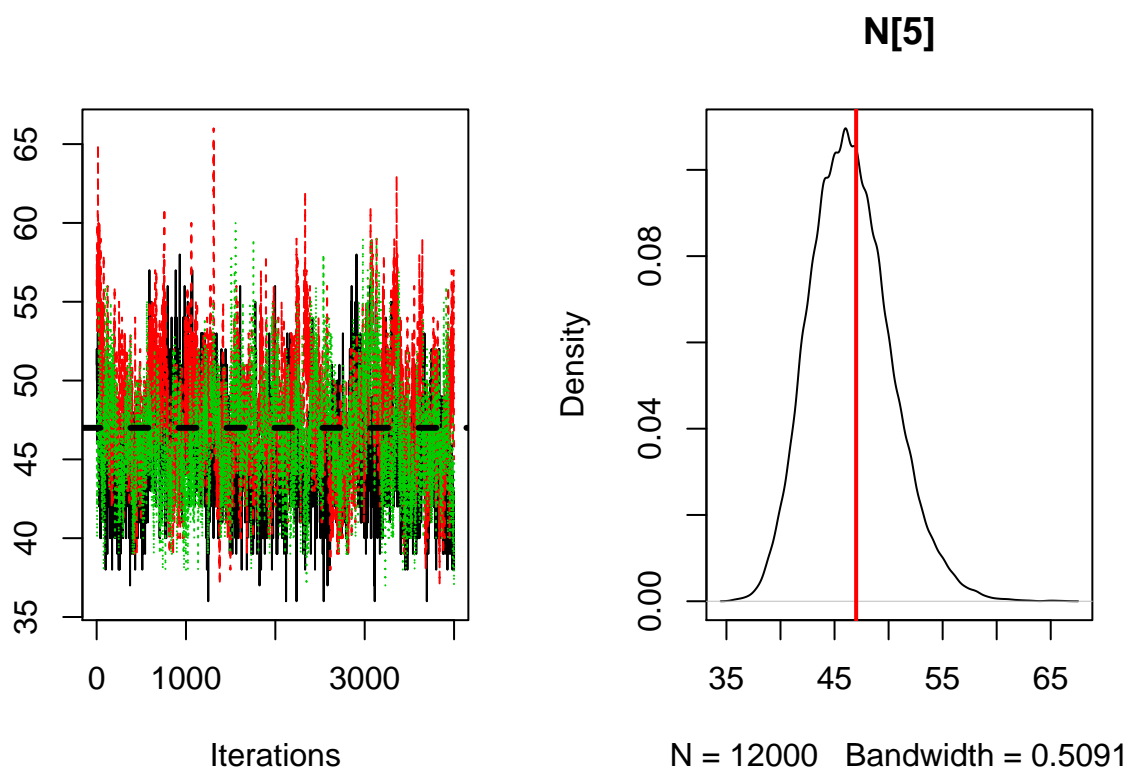
```



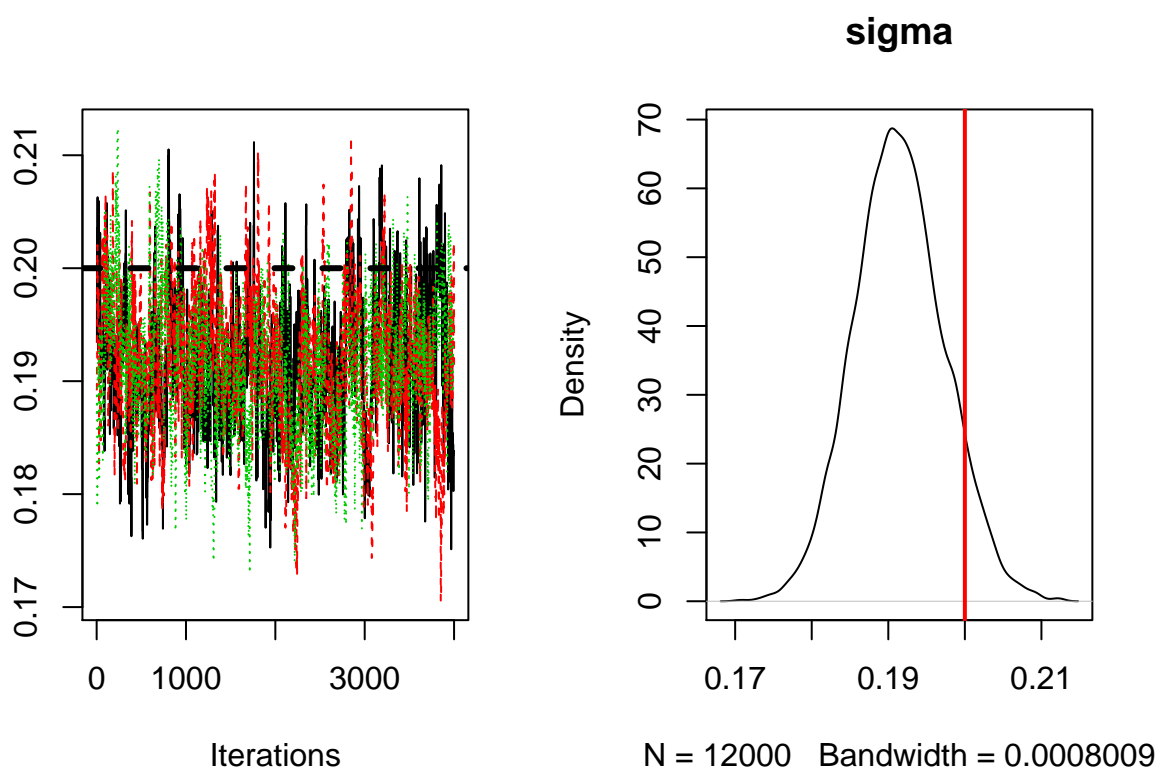




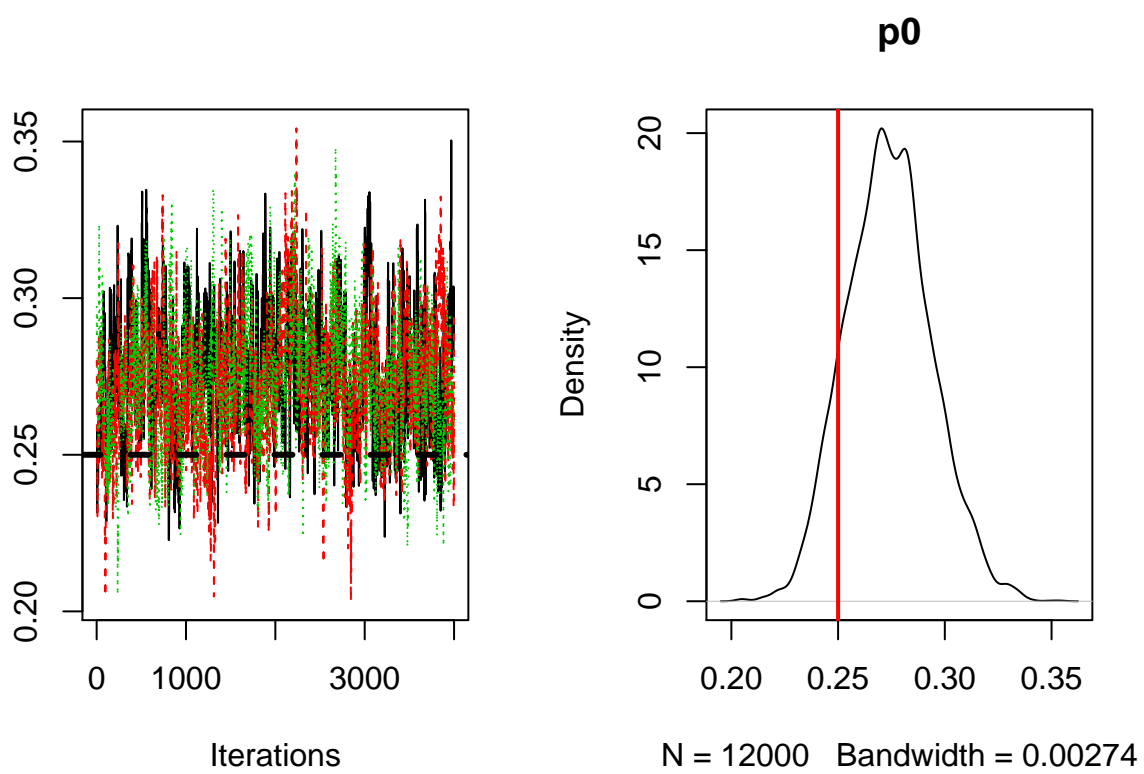




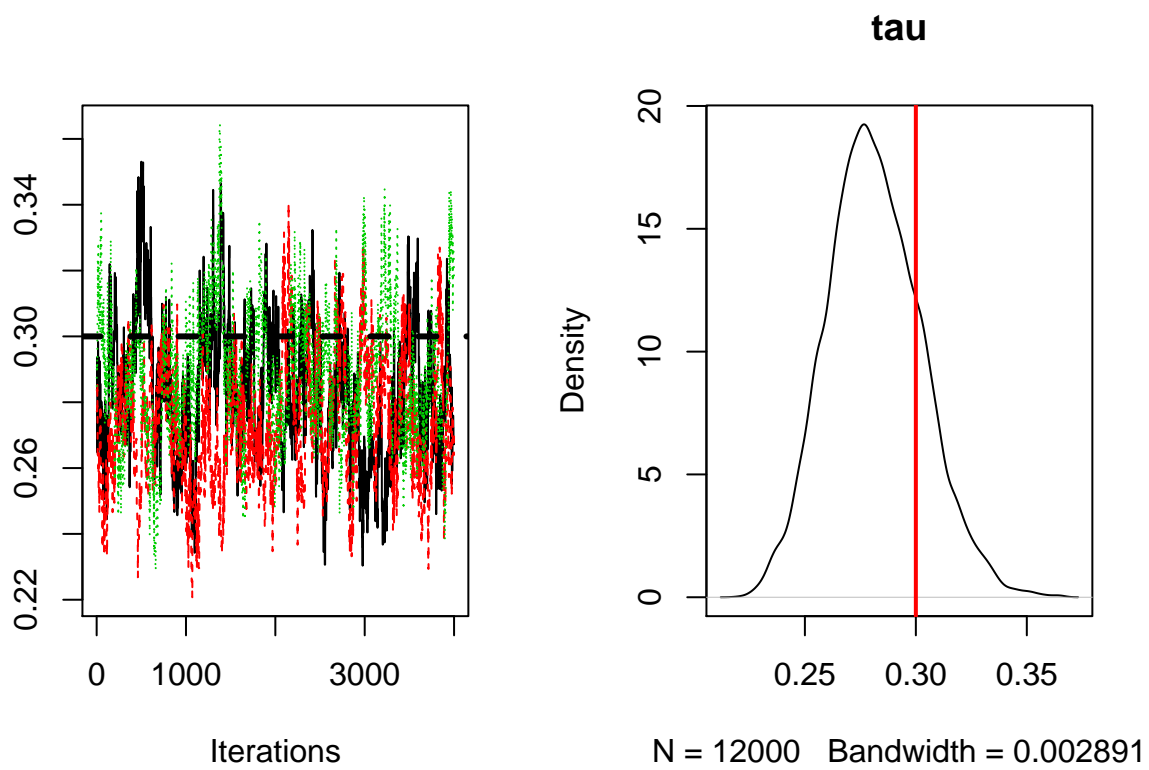
```
# SIGMA
PlotJagsParams(myNimbleOutput, params= "sigma", sim.values=sigma/res(r))
```



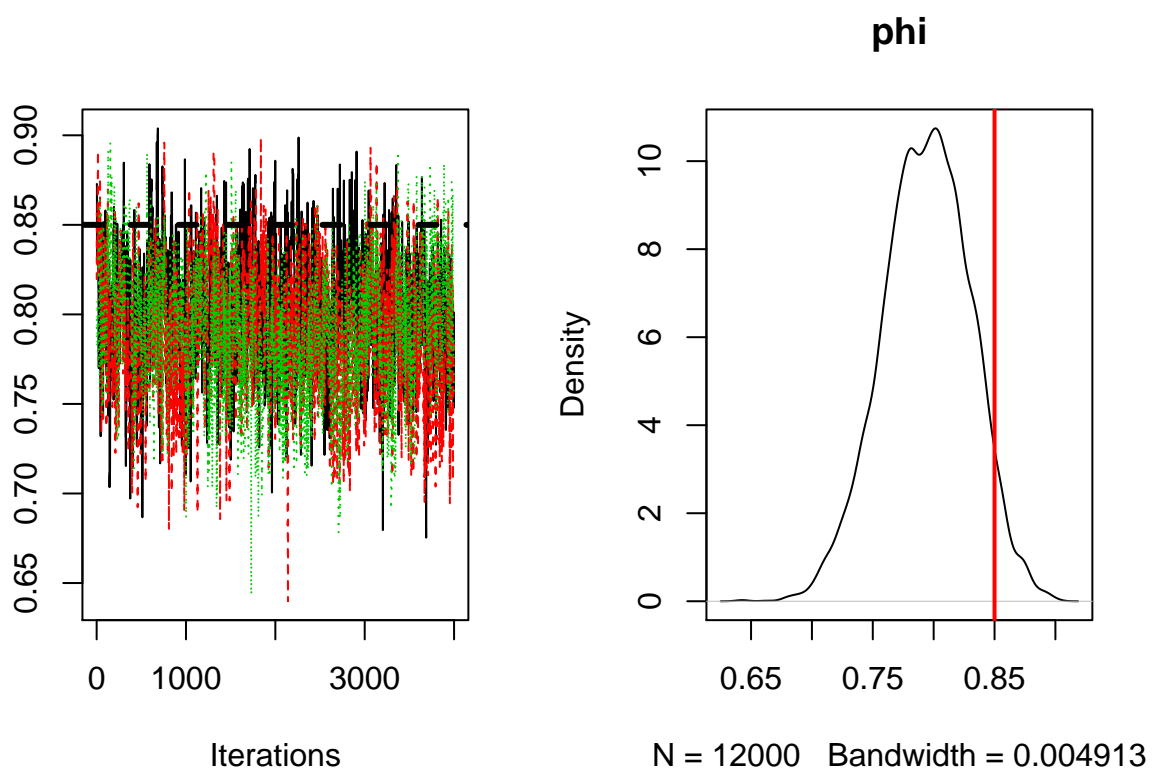
```
# p0
PlotJagsParams(myNimbleOutput, params= "p0", sim.values=p0)
```



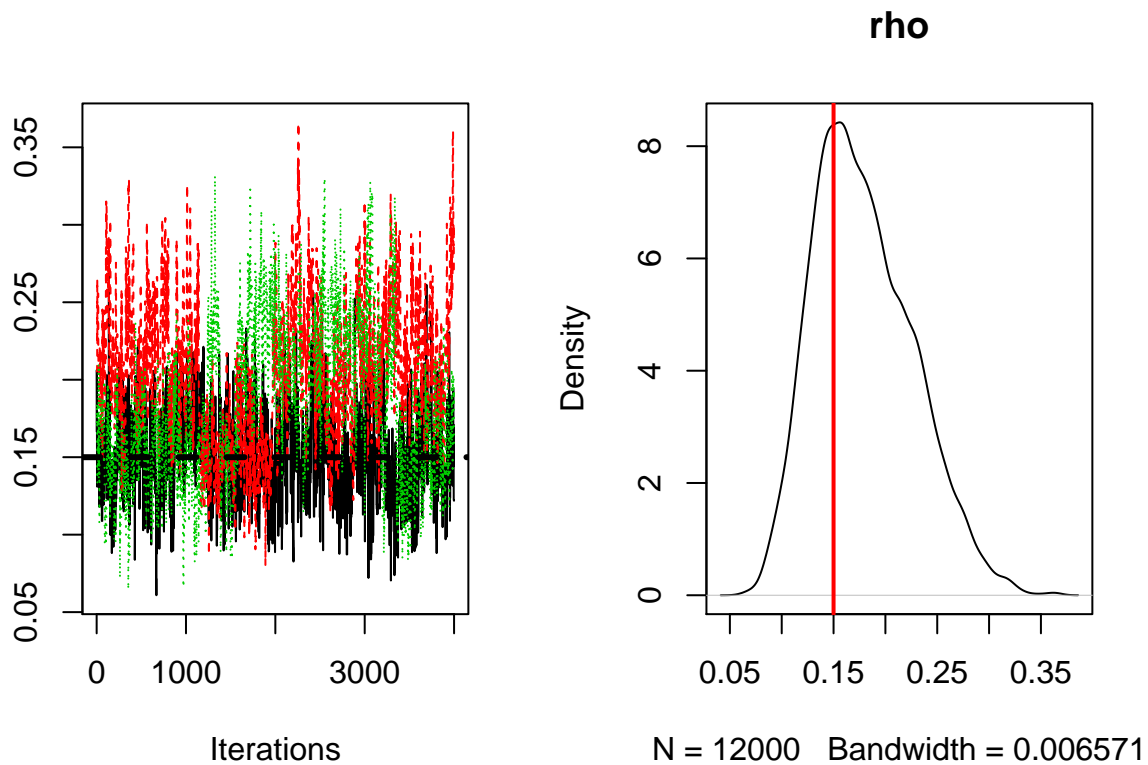
```
# tau
PlotJagsParams(myNimbleOutput, params= "tau", sim.values=tau/res(r))
```



```
# phi
PlotJagsParams(myNimbleOutput, params= "phi", sim.values=phi)
```



```
# rho  
PlotJagsParams(myNimbleOutput, params= "rho", sim.values=rho)
```

REFERENCES

- Milleret, C., P. Dupont, C. Bonenfant, H. Broseth, O. Flagstad, C. Sutherland, and R. Bischof. 2019. “A Local Evaluation of the Individual State Space to Scale up Bayesian Spatial Capture Recapture.” *Ecology and Evolution* 9 (1): 352–63. <https://doi.org/10.1002/ece3.4751>.
- NIMBLE Development Team. 2019. *NIMBLE: MCMC, Particle Filtering, and Programmable Hierarchical Modeling*. <https://cran.r-project.org/package=nimble>; <https://cran.r-project.org/package=nimble>. <https://doi.org/http://doi.org/10.5281/zenodo.1211190>.
- Valpine, P. de, D. Turek, C.J. Paciorek, C. Anderson-Bergman, D.T. Lang, and R. Bodik. 2017. “Programming with Models: Writing Statistical Algorithms for General Model Structures with Nimble.” *Journal of Computational and Graphical Statistics* 26 (2): 403–13.