

Aufgabe 1: Reaktor

a) aus der Energiebilanz.

$$\frac{dE}{dt} = \sum_i \dot{m}_i (h_i) [h_i (A) + h_{ei} (A) + p_{ei} (A)] + \sum_j \dot{Q}_j (A) - \sum_n \dot{W}_n (A) = 0$$

$$\dot{m} (h_{\text{ein}} - h_{\text{aus}}) + \dot{Q}_R + \dot{Q}_{\text{aus}} = 0$$

$$\dot{Q}_{\text{aus}} = -(-\dot{Q}_R + \dot{m} (h_{\text{aus}} - h_{\text{ein}}))$$

aus der TAB A-3.

$$h_{\text{ein}} = 1267 \text{ kJ/kg} = h_f(70^\circ\text{C})$$

$$h_{\text{aus}} = h_f(100^\circ\text{C}) = 1407.6 \text{ kJ/kg}$$

$$\begin{aligned}\dot{Q}_{\text{aus}} &= -(-100 \text{ kW}) + 0.3 \text{ kg/s} \cdot (1267 \text{ kJ/kg} - 1407.6 \text{ kJ/kg}) \\ &= 57.82 \text{ kW}\end{aligned}$$

b) aus der Entropiebilanz.

$$0 = \dot{m} (s_e - s_a) + \sum_j \frac{\dot{Q}_j}{T_j} + \dot{S}_{\text{erz}}$$

aus der Exergiebilanz.

$$0 = \dot{m} [h_e - h_a] + \left(2 - \frac{T_0}{T_f}\right) = 0$$

$$\begin{aligned}\bar{T} &= \frac{\dot{m} (h_e - h_a)}{\dot{m} (s_e - s_a)} = \frac{c_p (T_{\text{ein}} - T_{\text{aus}})}{c_p \ln\left(\frac{T_{\text{ein}}}{T_{\text{aus}}}\right)} \\ &= \frac{(288.15 - 298.15) \text{ K}}{\ln\left(\frac{288.15 \text{ K}}{298.15 \text{ K}}\right)} = 293.12 \text{ K}\end{aligned}$$

c) $\dot{Q}_{\text{ans}} = 65 \text{ kW}$, $\bar{T}_{\text{KF}} = 295 \text{ K}$

aus der Entropiebilanz.

$$0 = \dot{m} [s_e - s_a] + \sum_j \frac{\dot{Q}_j}{T_j} + \dot{S}_{\text{erz}}.$$

$$\dot{S}_{\text{erz}} = \dot{m} [s_e - s_a] - \frac{\dot{Q}_j}{295 \text{ K}}.$$

aus der TAB A-2.

$$s_e = s_f(15^\circ\text{C}) = 62.99 \text{ kJ/kg}.$$

$$s_a = s_f(25^\circ\text{C}) = 104.88 \text{ kJ/kg}.$$

$$\begin{aligned} \dot{S}_{\text{erz}} &= 0.3 \text{ kg/s} \cdot (62.99 - 104.88) \text{ kJ/kg} - \frac{65 \text{ kW}}{295 \text{ K}} \\ &= -12.79 \text{ kW/kg} \end{aligned}$$

d) aus der Energiebilanz

$$\Delta m_{22} (h_{\text{ein}} - h_{\text{aus}}) + \dot{Q} - \dot{W} = 0.$$

$$\Delta m_{22} = \frac{\dot{Q}_{\text{ans}, 22}}{h_a - h_e} = \frac{\dot{Q}_{\text{ans}}}{c_p (T_2 - T_1)}.$$

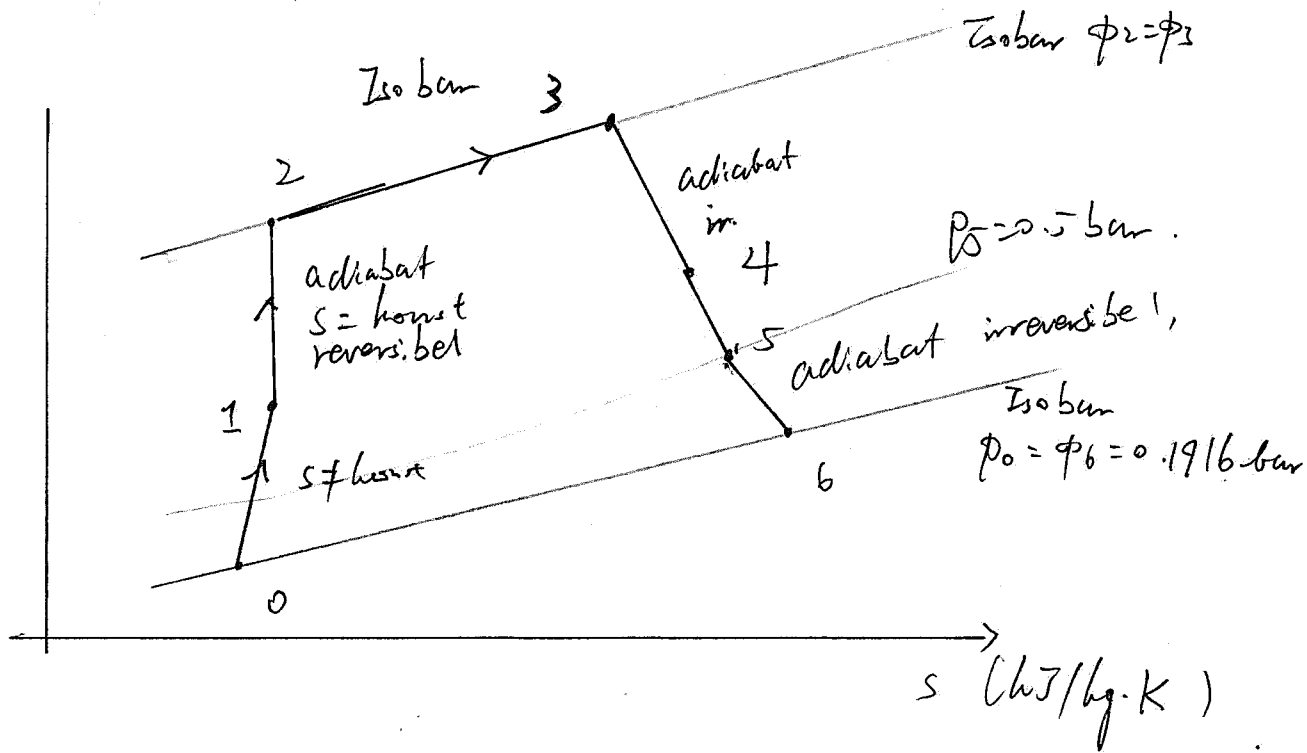
$$c_p =$$

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c) $\Delta m_{12} = 3600 \text{ kg}$.

Aufgabe 2: Energie am Triebwerk

a) T_k



b) aus der Energiebilanz

$$0 = \dot{m} [h_e - h_a + \frac{(w_e^2 - w_a^2)}{2}] + \sum_j \dot{Q}_j - \sum_n \dot{W}_{en} = 0.$$

$$\dot{Q}_j = \dot{W}_{en} = 0.$$

$$\dot{W}_t = 0 \quad \dot{Q} = 1195 \frac{kJ}{kg} \quad w_e = w_{luft} = 200 \text{ m/s}.$$

$$\begin{aligned} \frac{(w_e^2 - w_a^2)}{2} &= h_a - h_e = \dot{Q} \\ &= c_p (T_a - T_e) \end{aligned}$$

$$\begin{aligned} 5 \rightarrow 6 \text{ Isentrop} &\rightarrow \frac{T_6}{T_5} = \left(\frac{p_6}{p_5} \right)^{\frac{\gamma-1}{\gamma}} = \left(\frac{p_a}{p_5} \right)^{\frac{0.4}{1.4}} = \left(\frac{0.191}{0.5} \right)^{\frac{0.4}{1.4}} \\ &= 0.76 \end{aligned}$$

$$T_6 = T_5 \cdot 0.76 = 0.76 \cdot 431.9 \text{ K} = 328.07 \text{ K}$$

$$\left(\frac{W_5^2 - W_6^2}{2}\right) = C_p (T_6 - T_5)$$

$$= 1.006 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} (328.07 - 431.9) \text{K}$$

$$= -104.45 \text{ kJ/kg}$$

$$W_6 = \sqrt{2 \cdot (-104.45 \text{ kJ/kg}) + W_5^2}$$

$$= 510 \text{ m/s}$$

c) $T_0 = 340 \text{ K}, W_6 = 510 \text{ m/s}$

~~$$Ex_{str,6} = h_6 - h_5 - T_6 (s_6 - s_5) + \frac{W_5^2 - W_6^2}{2}$$

$$= C_p (T_6 - T_5)$$~~

$$\Delta Ex_{str} = h_6 - h_0 - T_0 (s_6 - s_0) + \frac{W_5^2 - W_6^2}{2}$$

$$= C_p (T_6 - T_0) - T_0 C_p \ln\left(\frac{T_6}{T_0}\right) - R \ln\left(\frac{P_6}{P_0}\right) + \frac{W_5^2 - W_6^2}{2}$$

$$R = C_p - C_v = C_p - \frac{C_p}{\gamma} = 1.006 - \frac{1.006}{1.4} = 0.287$$

$$T_0 = 273.15 - 30 = 243.15 \text{ K}$$

$$\Delta Ex_{str} = 1.006 \cdot (340 - 243.15) + 243.15 \cdot 1.006 \ln\left(\frac{340}{243.15}\right)$$

$$- 0.287 \cdot \ln(1) + \frac{200^2 - 510^2}{2}$$

$$= -1.78 \text{ kJ/kg}$$

$$\Delta Ex_{str} = 10.0 \text{ kJ/kg}$$

d) $Ex_{rev} = T_0 S_{rev} = T_0 \left(\ln\left(\frac{s_2 - s_1}{T_0}\right) - \frac{Q_{12}}{T_0} \right)$

$$m = \frac{Ex_{rev}}{T_0 (s_2 - s_1)} = \frac{Ex_{rev}}{T_0 \cdot C_p \ln\left(\frac{T_2}{T_0}\right)} = \frac{110 \text{ kJ/kg}}{243.15 \cdot \ln\left(\frac{340}{243.15}\right) \cdot 1.006} = 1.27 \text{ kg}$$

Aufgabe 3: Schmelzen von Eis durch perfektes Gas

a) $pV = nRT$.

$$R = \frac{\bar{R}}{M_g} = \frac{8.314 \text{ kJ/kmol} \cdot \text{K}}{50 \text{ kg/kmol}}$$

$$= 0.16628 \text{ kJ/K}.$$

$$p_g = 1 \text{ bar} + \left(\frac{F}{A} \right) = 1 \text{ bar} + \frac{32 \text{ kg} \cdot 9.81 \text{ m/s}^2}{\cancel{\text{kg}} \cdot \left(\frac{\text{m}}{2} \right)^2 \text{ m}^2}$$

$$= 1 + 0.396$$

$$= 1.4 \text{ bar}.$$

~~$$p_{g,1} = 1.5 \text{ bar}.$$~~

$$m_g = \frac{pRT}{pV} = \frac{0.16628 \text{ kJ/K} \cdot 500^\circ\text{C}}{1.4 \text{ bar} \cdot 3.142}$$

$$= 2.92 \text{ g}.$$

b)

c) Aus dem 1. HS $T_{g,2} = 0.003$.

$$\begin{aligned} Q_{12} &= \cancel{m(h_2 - h_1)} m u = m (c_v (s_2 - s_1)) \\ &= m \cdot c_v (T_2 - T_1) \\ &= 3.6 \text{ g} \cdot 0.663 \frac{\text{J}}{\text{g} \cdot \text{K}} \cdot (0.003^\circ \text{C} - 500^\circ \text{C}) \\ &= -1193 \text{ J} \end{aligned}$$

d) $u_2 = u(T_2 - T_1) = -331.49 \text{ kJ/kg}$.

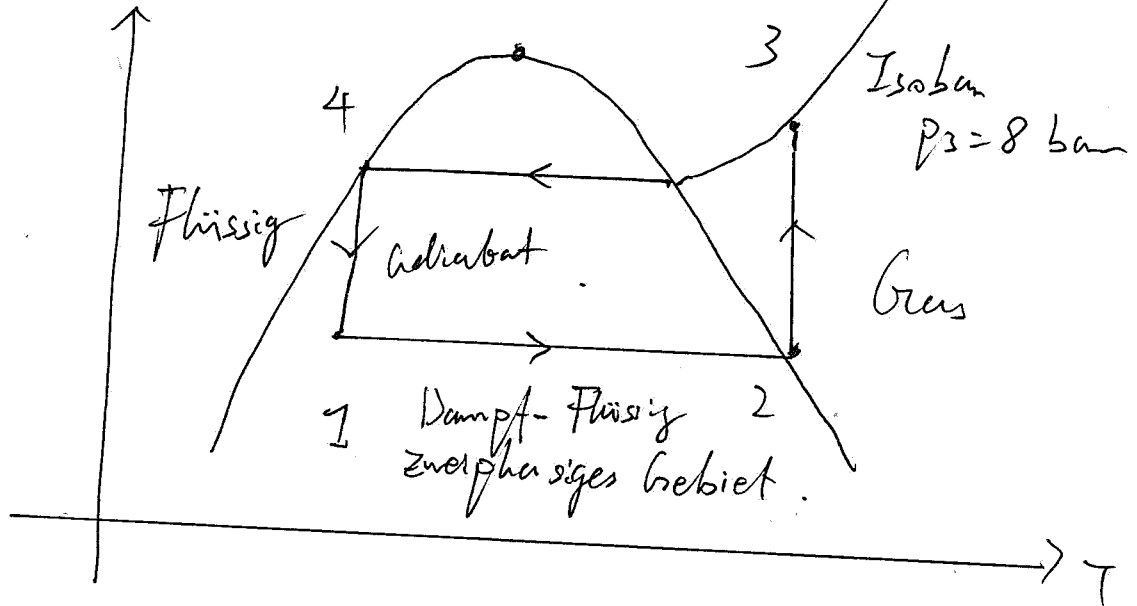
$$X_{\text{Eis}, 2} = \frac{\cancel{-u_g}}{\cancel{u_f - u_g}} \frac{u_2 - u_f}{\cancel{u_g - u_f}}$$

$$= \frac{-331.49 \text{ kJ/kg} + 0.033}{-333.442 \text{ kJ/kg} + 0.033}$$

$$= 0.994$$

Aufgabe 4: Grefrierbohrung mit einem R134a Kältekreislauf.

a)



b) aus der TAB A-15 interpoliert

$$\dot{m}_{\text{R134a}} (h_2 - h_3) \neq \dot{W}_k = \cancel{28 \text{ W}} = 20$$

$$\dot{m}_R = \frac{28 \text{ W}}{h_3 - h_4} = \frac{\cancel{h_4}}{\cancel{h_3}} = \frac{28 \text{ W}}{\cancel{h_3}}$$

$$= 4 \text{ kg/h}$$

c) $x_{1,2} = \frac{u_2 - u_f}{u_g - u_f}$

$$u_1 = u_4$$

$$\begin{aligned}
 d) \quad \epsilon_k &= \frac{|\dot{Q}_{zu}|}{|\dot{W}_e|} \\
 &= \frac{\dot{Q}_{zu}}{|\dot{Q}_{ab} - \dot{Q}_{zu}|} \\
 &= \frac{\quad}{28 \text{ W}}
 \end{aligned}$$

e) Wärmestrom \dot{Q}_k garantiert