

1) a)

$$\Delta E = Q - \dot{W} = \Delta U = m_{\text{in}}(u_{\text{in}}) - m_{\text{aus}} u_{\text{aus}}$$

$$\hookrightarrow \dot{Q}_2 + \dot{Q}_{\text{aus}} = \dot{m}(u_{\text{in}} - u_{\text{aus}})$$

$$u_{\text{in}} = u_f(70^\circ\text{C}) = 292.95 \frac{\text{kJ}}{\text{kg}} \quad \underline{\text{A2}}$$

$$u_{\text{aus}} = u_f(100^\circ\text{C}) = 418.94 \frac{\text{kJ}}{\text{kg}} \quad \underline{\text{A2}}$$

$$\hookrightarrow |\dot{Q}_{\text{aus}}| = 0.3 \frac{\text{kg}}{\text{s}} (292.95 - 418.94) \frac{\text{kJ}}{\text{kg}} + 100 \text{ kW}$$

$$= 62.203 \text{ kW} \rightarrow \underline{\dot{Q}_{\text{aus}} = -62.203 \text{ kW}}$$

$$\text{b)} \quad \overline{T} = \frac{\int_e^a T ds}{s_a - s_e} = \frac{h_a - h_e}{s_a - s_e} = \frac{c_f(T_a - T_e) + v_f \left(\frac{P_a - P_e}{P_a - P_e} \right)^{\alpha} = 0}{c_f \ln \left(\frac{T_a}{T_e} \right)} =$$

$$\overline{T} = \frac{T_a - T_e}{\ln \left(\frac{T_a}{T_e} \right)} = \frac{298.15 \text{ K} - 288.15 \text{ K}}{\ln \left(\frac{298.15 \text{ K}}{288.15 \text{ K}} \right)} = \underline{\underline{293.12 \text{ K}}}$$

c)

$$\dot{Q}_{\text{aus}} = \dot{m}_{\text{TRF}} \dot{t}$$

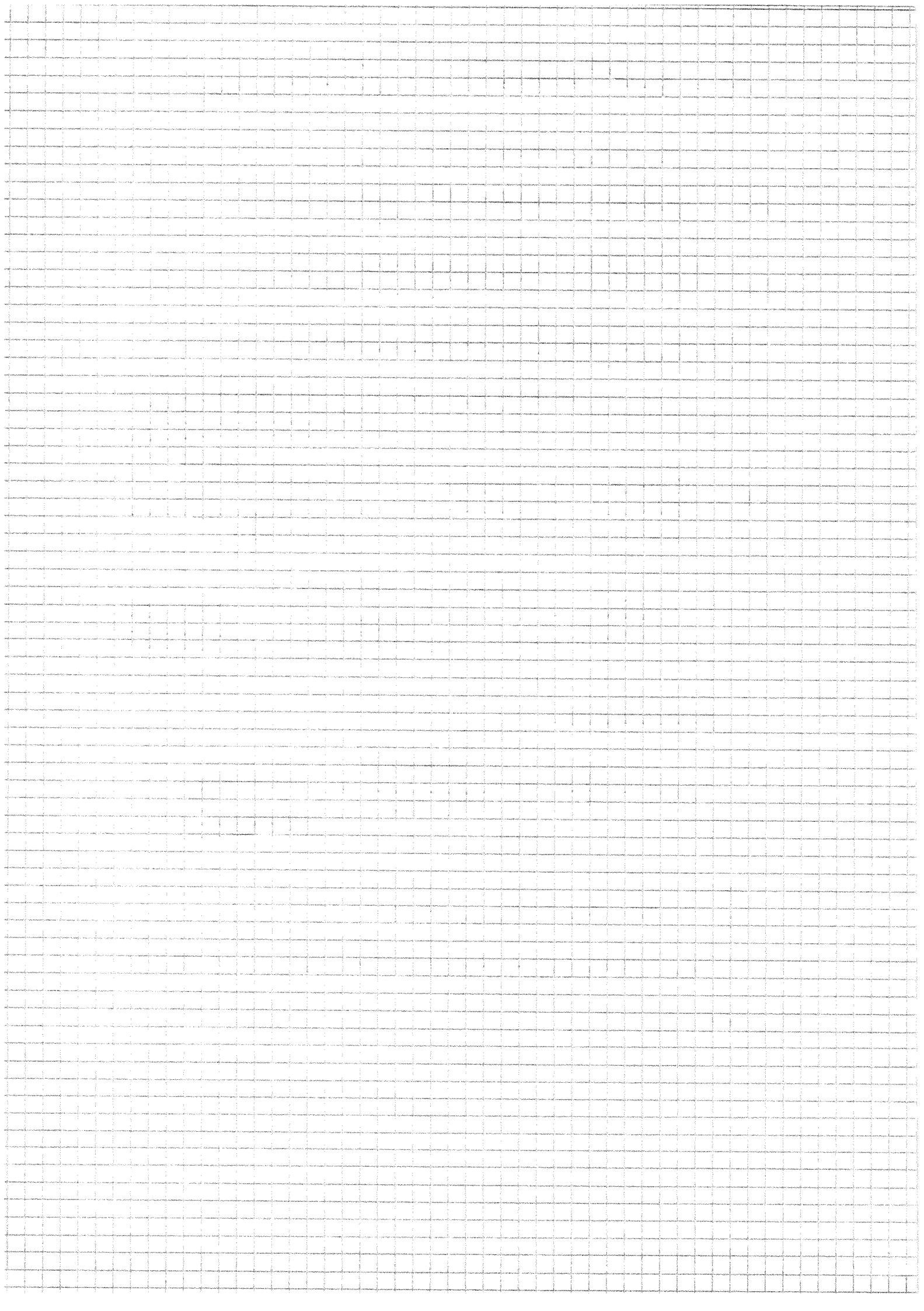
$$\dot{S}_{\text{TRF}} = - \frac{\dot{Q}_{\text{aus}}}{\overline{T}_{\text{RF}}} = - \frac{62.203 \text{ kW}}{293.12 \text{ K}} = \underline{\underline{0.2122 \frac{\text{kW}}{\text{K}}}}$$

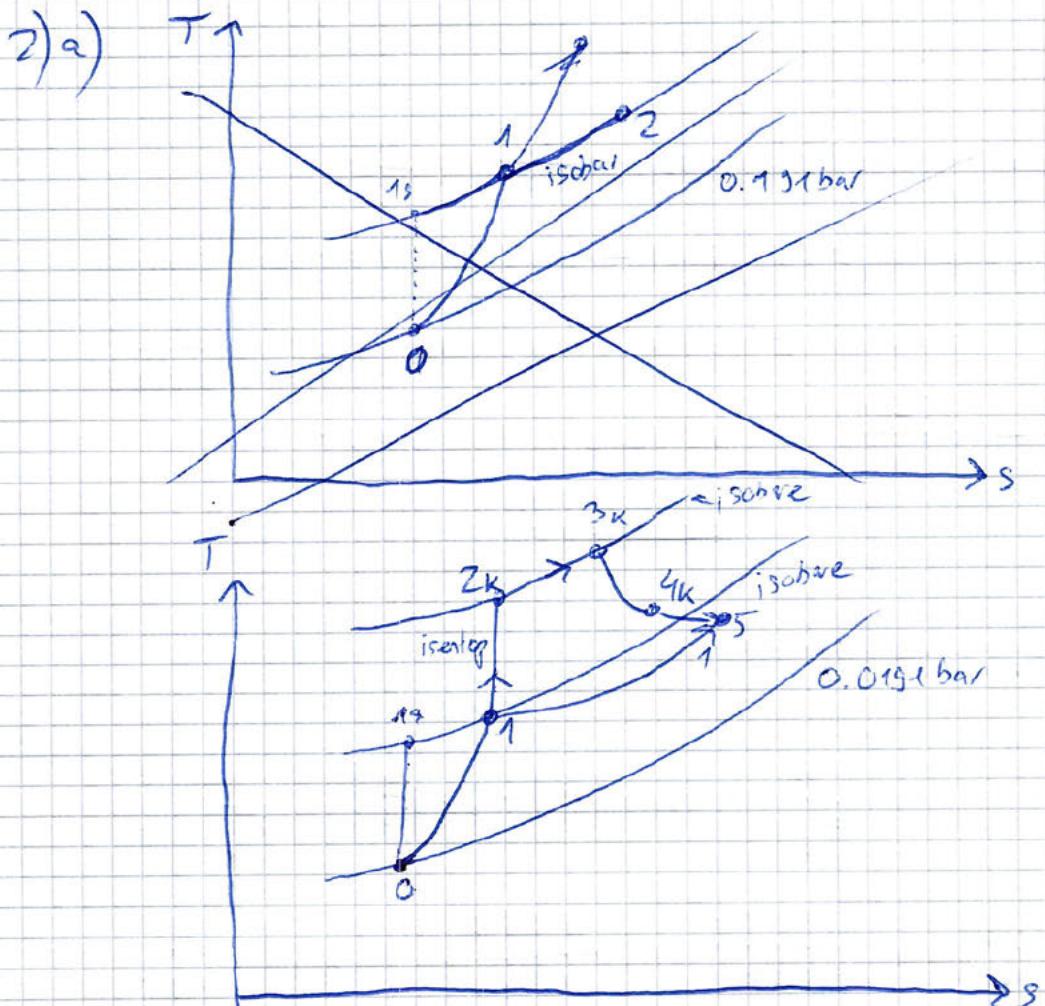
d)

$$\frac{dE}{dt} = \Delta m_{12} h_{12} + Q_{\text{aus12}} = \Delta U$$

$$\hookrightarrow (m_{\text{ges}} + \Delta m_{12}) u_2 - m_{\text{ges}}(u_1) + -\Delta m_{12} u_{12} = Q_{\text{aus12}}$$

$$\cancel{u_1} = u_f \quad ($$





$$\hookrightarrow h_5 + \frac{w_5^2}{2} = h_6 + \frac{w_6^2}{2}$$

Düse ist isentrop $\rightarrow s_5 = s_6 \rightarrow n = k = 1.4$

$$T_6 = T_5 \cdot \left(\frac{p_6}{p_5} \right)^{\frac{k-1}{k}} = 431.9 \text{ K} \cdot \left(\frac{0.191}{0.5} \right)^{\frac{0.4}{1.4}} = \underline{\underline{328.07 \text{ K}}}$$

$$\begin{aligned} \hookrightarrow \frac{w_6^2}{2} &= h_5 - h_6 + \frac{w_5^2}{2} \\ &= c_p^{is} (T_5 - T_6) + \frac{w_5^2}{2} = 1.006 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \cdot (431.9 - 328.07) \text{ K} \\ &\quad + \frac{(220 \text{ m/s})^2}{2} \\ &\approx 104.45 \text{ kJ} + 24.2 \text{ kJ} = 128.65 \text{ kJ} \end{aligned}$$

$$\hookrightarrow w_6 = \sqrt{2 \cdot 128.65 \text{ kJ}} = \underline{\underline{507.24 \text{ m/s}}}$$

c)

$$\begin{aligned}
 \Delta_{ex, st} &= h_b - h_0 - T_0(s_b - s_0) + \frac{w_b^2}{2} - \frac{w_0^2}{2} \\
 &= c_p(T_b - T_0) - T_0(c_p \ln\left(\frac{T_0}{T_b}\right) - R \ln\left(\frac{P_0}{P_b}\right)) + \frac{w_b^2}{2} - \frac{w_0^2}{2} \\
 &= 1.006 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} (328.07 \text{K} - 243.15 \text{K}) - 243.15 \text{K} (1.006 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \ln\left(\frac{328.07}{243.15}\right) \\
 &\quad + \frac{(507.24 \text{m/s})^2}{2} + \frac{220 \text{m/s}^2}{2} = 12.16 \text{kJ} + 128.65 \text{kJ} - 74.7 \text{kJ} \\
 &\quad = \underline{\underline{116.61 \text{kJ}}}
 \end{aligned}$$

d)

$$\bar{E}_{ex, st} = \underline{\underline{q_{ex, st}}} + \left(1 - \frac{T_0}{T_b}\right) q_B$$

$$\begin{aligned}
 \bar{s}_{ex, st} &= (s_0 - s_b) + \frac{q_B}{T_B} = c_p \ln\left(\frac{T_0}{T_b}\right) - R \ln\left(\frac{P_0}{P_b}\right) + \frac{q_B}{T_B} \\
 &= 1.006 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \cdot \ln\left(\frac{243.15 \text{K}}{328.07 \text{K}}\right) + \frac{1195 \frac{\text{kJ}}{\text{kg}}}{1283 \text{K}} = 0.6257 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}
 \end{aligned}$$

$$\hookrightarrow \bar{E}_{ex, st} = \bar{s}_{ex, st} \cdot T_0$$

$$\hookrightarrow \bar{E}_{ex, st} = \bar{s}_{ex, st} \cdot T_0 = \underline{\underline{152.14 \frac{\text{kJ}}{\text{kg}}}}$$

3) a)

$$p_{g1} = p_{amb} + p_{kolben}$$

$$p_{kolben} = \frac{32\text{kg} \cdot 9.81 \frac{\text{m}}{\text{s}^2}}{(0.05\text{m})^2 \pi} = \underline{\underline{35.9695 \text{kPa}}}$$

$$\hookrightarrow p_{g1} = 100\text{kPa} + 35.9695\text{kPa} = \underline{\underline{135.97 \text{kPa}}}$$

$$m_{g1} = \frac{V_{g1} \cdot p_{g1}}{\frac{R}{M_g} \cdot T_{g1}} = \frac{0.00314\text{m}^3 \cdot 135.97 \text{kPa}}{\frac{8.314 \frac{\text{kJ}}{\text{kmol K}}}{50\text{kg kmol}}} \approx \underline{\underline{273.15 \text{K}}} = \underline{\underline{3.419 \text{g}}}$$

$$b) p_{g2} = p_{61} = 135.97 \text{kPa}$$

\hookrightarrow bleibt gleich, weil die Masse des Kolbens und der Druck der Atmosphäre gleich bleiben.

c)

$$Q_1 \quad \Delta E_{12} = Q_{12} - W_{12}$$

$$T_{g2} = \underline{\underline{273.15 \text{K}}}$$

$$W_{12} = p_{g1} \cdot (V_{g2} - V_{g1}) =$$

$$V_{g2} = \frac{m_{g1} \cdot \frac{R}{M_g} \cdot T_{g2}}{p_{g2}} = \underline{\underline{0.001109 \text{m}^3}}$$

$$\hookrightarrow W_{12} = 135.97 \text{kPa} \cdot (0.001109 \text{m}^3 - 0.00314 \text{m}^3) = \underline{\underline{-0.2842 \text{kJ}}}$$

$$\hookrightarrow \Delta E_{12} = \Delta U_{12} = m_{ew}(T_{ew2} - T_{ew1})(u_{ew2} - u_{ew1}) + m_g(u_{g2} - u_{g1})$$

$$\Rightarrow = m$$

d)

$$\dot{Q}_{12} = \cancel{x_{Eis2} \cdot m_{EW}(u_2)} - \cancel{x_{Eis1} \cdot m_{EW}(u_{Eis1})} \\ + (1-x_{Eis2}) m_{EW}(u_2) - (1-x_{Eis1}) m_{EW}(u_{Eis1})$$

$$\textcircled{O} \quad Q_{12} = x_{Eis2} m_{EW} u_{Eis2} + (1-x_{Eis2}) m_{EW} u_{w2} + m_g \cdot u_{g2} \\ - x_{Eis1} m_{EW} u_{Eis1} - (1-x_{Eis1}) m_{EW} u_{w1} - m_g u_{g1}$$

$$\sim m_{EW} = 0.1 \text{ kg} \quad u_{Eis2} = u_{\text{Fest}}(0.003^\circ\text{C}) = -333.442 \frac{\text{kJ}}{\text{kg}}$$

$$u_{w2} = u_{\text{flüssig}}(0.003^\circ\text{C}) = -0.033 \frac{\text{kJ}}{\text{kg}}$$

$$\cancel{u_{g2}} = u_{Eis1} = u_{\text{Fest}}(0^\circ\text{C}) = -333.458 \frac{\text{kJ}}{\text{kg}}$$

$$u_{w1} = u_{\text{flüssig}}(0^\circ\text{C}) = -0.045 \frac{\text{kJ}}{\text{kg}}$$

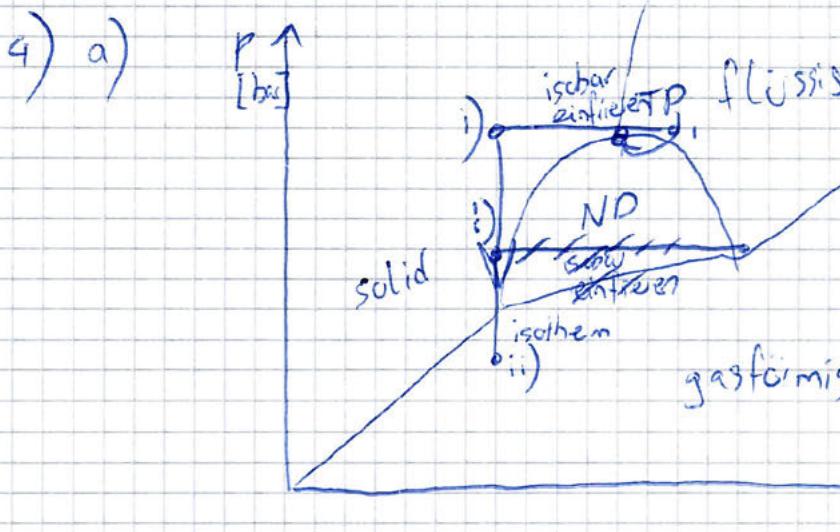
$$\left. \begin{aligned} \hookrightarrow & x_{Eis} m_{EW}(u_{w2} - u_{Eis2}) = m_{EW} u_{w2} - x_{Eis} m_{EW} u_{Eis1} - (1-x_{Eis1}) m_{EW} u_{w1} \\ & + m_g (u_{g2} - u_{g1}) \quad \cancel{\text{Erläuterung}} \\ & = c_v m_g (T_{g2} - T_{g1}) \end{aligned} \right\}$$

$$\hookrightarrow x_{Eis} = \frac{0.1 \text{ kg} \cdot (-0.033 \frac{\text{kJ}}{\text{kg}}) - 0.6 \cdot 0.1 \text{ kg} \cdot (-333.458 \frac{\text{kJ}}{\text{kg}}) - (1-0.6) 0.1 \text{ kg} \cdot (-0.045 \frac{\text{kJ}}{\text{kg}})}{0.1 \text{ kg} \cdot (-0.033 + 333.442) \frac{\text{kJ}}{\text{kg}}} \\ + \frac{0.6 \cdot 0.033 \frac{\text{kJ}}{\text{kg}} \cdot 0.003418 \text{ kg} (273.15 \text{ K} - 773.15 \text{ K})}{0.1 \text{ kg} \cdot (-0.033 + 333.442) \frac{\text{kJ}}{\text{kg}}} \quad \checkmark$$

$$\hookrightarrow Q_{12} = \cancel{x_2 \cdot m_{EW} \cdot u_{Eis2}} - x_1 m_{EW} \cdot u_{Eis1} \\ + (1-x_2) m_{EW} \cdot u_{w2} - (1-x_1) m_{EW} \cdot u_{w1}$$

$$\hookrightarrow m_{EW} \cancel{x_2 (u_{w2} - u_{Eis2})} = \cancel{+ Q_{12}} - x_1 m_{EW} \cdot u_{Eis1} + m_{EW} u_{w2} - (1-x_1) m_{EW} \cdot u_{w1}$$

$$\hookrightarrow x_2 = \frac{1.5 \text{ kJ} - 0.6 \cdot 0.1 \text{ kg} \cdot (-333.458 \frac{\text{kJ}}{\text{kg}}) + 0.1 \text{ kg} \cdot (-0.033 \frac{\text{kJ}}{\text{kg}}) - 0.4 \cdot 0.1 \text{ kg} \cdot (-0.045 \frac{\text{kJ}}{\text{kg}})}{0.1 \text{ kg} \cdot (-0.033 + 333.442) \frac{\text{kJ}}{\text{kg}}} \\ = \underline{\underline{0.52}}$$



b)

$$s_f = \cancel{f} s_f(8\text{ bar}) = 0.3459 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \text{ TAB A.11}$$

$\hookrightarrow = s_1$

$$h_a = h_f(8\text{ bar}) = 93.42 \frac{\text{kJ}}{\text{kg}} \text{ TAB A.11}$$

$$4-1 \text{ isenthalp} \rightarrow h_1 = h_a = 93.42 \frac{\text{kJ}}{\text{kg}}$$

c) $m_{R134} = \frac{4k_2}{h} \quad T_2 = -72^\circ\text{C}$

$$h_a = h_1 \rightarrow h_a = h_f(8\text{ bar}) = 93.42 \frac{\text{kJ}}{\text{kg}} = h_1$$

d)

