

# Aufgabe 1

	in	aus	kein	k <sub>aus</sub>
m	0,3	0,3		
T	70°	100°	284,15 K	298,15 K
x	1	1		

$$m_{ges} = 5 + 55 \text{ kg}$$

$$x_D = \frac{m_P}{m_{gl}} = 0,005$$

$$T_{Rekt} = 100^\circ\text{C}$$

$$Q_R = 100 \text{ kW}$$

$$Q_{aus} =$$

a) ges:  $Q_{aus}$

Energiebilanz

$$\left. \begin{aligned} h(x=1/70^\circ) &= 292,98 \frac{\text{kJ}}{\text{kg}} \\ h(x=1/100^\circ) &= 419,04 \frac{\text{kJ}}{\text{kg}} \end{aligned} \right\} \text{Tab 11z A-2}$$

$$\frac{dE}{dt} = \dot{m} h_i + Q - W_i \rightarrow \underbrace{\dot{m}_{in} h_{in}}_{\text{kein}} - \underbrace{\dot{m}_{aus} h_{aus}}_{\text{kein}} + m$$

$$0 = \dot{m}(h_e - h_a) + Q_R - Q_{aus} \rightarrow Q_{aus} = \dot{m}(h_e - h_a) + Q_R$$

$$Q_{aus} = 0,3 (292,98 - 419,04) + 100 \text{ kW} = 62,18 \text{ kW}$$

b) ges:  $\bar{T}_{KF}$

$$\int T ds = Q_{rev} = h_a - h_e$$

$$\bar{T}_{KF} = \frac{\int_e^a T ds}{s_a - s_e} = \frac{h_a - h_e}{s_a - s_e} = \frac{\int_{T_1}^{T_2} (T_2 - T_1) + \cancel{\int_{T_1}^{T_2} (p_2 - p_1)}^0}{\int_{T_1}^{T_2} \ln\left(\frac{T_2}{T_1}\right)} = \frac{T_2 - T_1}{\ln\left(\frac{T_2}{T_1}\right)} = \frac{298,15 - 288,15}{\ln\left(\frac{298,15}{288,15}\right)} =$$

$$\bar{T}_{KF} = \frac{10}{\ln\left(\frac{298,15}{288,15}\right)} = 293,12$$

c) ges:  $S_{e2}$

$$0 = \dot{m}[s_e - s_a] + \frac{\dot{Q}_j}{\bar{T}_j} + S_{e2} \rightarrow S_{e2} = \dot{m}[s_a - s_e] - \frac{\dot{Q}_{aus}}{\bar{T}_j}$$

$$S_{e2} = 0,3 [7,3549 - 7,7553] - \frac{62,18}{293,12} = -0,12012 - 0,212132 = 0,33 \frac{\text{kJ}}{\text{kg}}$$

$$\left. \begin{aligned} s(1/70^\circ) &= 7,7553 \\ s(1/100^\circ) &= 7,3549 \end{aligned} \right\} \text{Tab A-2}$$

Aufgabe 2

2. Teil:  $\dot{Q}_{12}$

d)  $T_1 = 100^\circ\text{C}$   
 $m_1 = 5,755 \text{ kg}$

$T_2 = 70^\circ\text{C}$   
 $T_{12\text{ein}} = 20^\circ\text{C} \quad (x=1)$

Ges:  $\Delta m_{12}$

$Q_{12} = 35 \text{ MJ}$

$\dot{W} = 0$  Energiebilanz mit  $Q$

$Q_1 - Q_{12\text{ein}} = Q_{12} \rightarrow m_1 \cdot c_v \cdot T_1 - m_{12} \cdot c_v \cdot T_2 = Q_{12}$

$c_v(T_1 - T_2) \rightarrow u_1 - u_2$

$u_1(100^\circ\text{C}/x=0,005) = 429,38 \frac{\text{kJ}}{\text{kg}} \left\{ \begin{array}{l} \text{Tab A2} \\ \text{A2 (x=1/200)} = 2402,9 \frac{\text{kJ}}{\text{kg}} \end{array} \right.$

$m_1 \cdot u_1 - m_{12} \cdot u_2 = Q_{12}$

$m_{12} = \frac{m_1 \cdot u_1 - Q_{12}}{u_2} = \frac{5,755 \cdot 429,38 - 35'000}{2402,9} =$

$u_1 \neq u_f + x(u_g - u_f) = 418,94 + 0,005(2506,4 - 418,94) = 429,377$

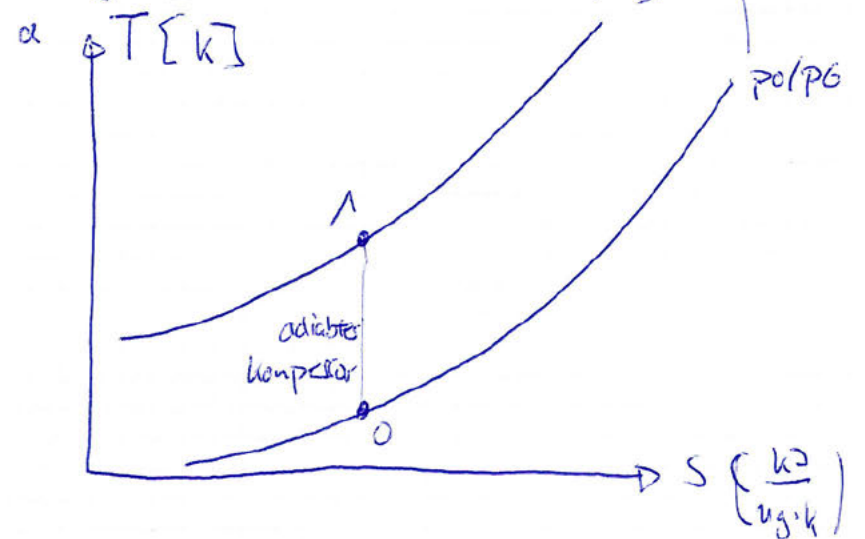
$m_{12} = 10,14 \text{ kg}$

Tabelle A-2

e) Ges:  $\dot{S}_{12}$

$m_2 \cdot s_2 - m_1 \cdot s_1 = m_{12} \cdot s_{12} + \dot{S}_{12}$

## Aufgabe 2



b) Ges:  $w_6 + T_0$

Düse:  $Q=0 \mid W=0 \Rightarrow h_5 = h_6!$

$w_5 = 220 \frac{m}{s}$

$0 = \cancel{h_5} - \cancel{h_6} + \frac{w_5^2 - w_6^2}{2} \rightarrow w_5 = w_6 = 220 \frac{m}{s}$

c)  $\dot{m}_{ext} = \dot{m} [h_6 - h_0 - T_0 (s_6 - s_0) + ke + pe]$

$\dot{m}_{ext} = \dot{m}_{ges} \left[ c_p (T_6 - T_0) - T_0 \left( c_p \ln \left( \frac{T_6}{T_0} \right) - R \ln \left( \frac{p_6}{p_0} \right) \right) + \frac{(200 \frac{m}{s})^2 - (510 \frac{m}{s})^2}{2} \right]$

$\dot{m}_{ext} = \dot{m}_{ges} \left[ 1,006 \left( 340 K - 243,15 \right) - 243,15 \left( 1,006 \left( \frac{340}{243,15} \right) \right) - \right]$

$R = c_p - c_v$

$\eta = \kappa = \frac{c_p}{c_v} \rightarrow \boxed{c_v = \frac{c_p}{\kappa}}$

d)  $ex_{vel} = \frac{T_0 \cdot \dot{s}_{s2}}{\dot{m}_{ges}}$

### Aufgabe 3

→ per Gas

	Zustand 1	Zustand 2
$V_g$	3,14 L	
$T_g$	500°C = 773,15	
$m_{EW}$	0,1 kg	
$T_{EW}$	0°C	
$x_E$	0,6	

$$m_k = 32 \text{ kg} \quad / \quad p_{\text{atm}} = 1 \text{ bar} \quad / \quad D = 0,1 \text{ m} \quad / \quad c_v = 0,633 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \quad / \quad M_g = 50 \frac{\text{kg}}{\text{kmol}}$$

a) Ges:  $p_{g,1}$  /  $m_g$

Wasser inkompressibel daher wie extra gewicht!

↓  $p_0$    ↓  $F_{EK}$    ↓  $F_{E}$   
 ↑  $p_{g,1}$    Membran

$$F = p \cdot A$$

$$A = \frac{d^2 \cdot \pi}{4}$$

$$p_0 \cdot A + m_k \cdot g + m_{EW} \cdot g = p_{g,1} \cdot A$$

$$\rightarrow p_{g,1} = \frac{p_0 \cdot A + m_k \cdot g + m_{EW} \cdot g}{A} = \frac{1 \cdot 10^5 \cdot 0,1^2 \cdot \pi}{4} + 32 \cdot 9,81 + 0,1 \cdot 9,81$$

$$p_{g,1} = \frac{785,398 + 313,92 + 0,981}{\frac{0,1^2 \cdot \pi}{4}} = 140'094 \text{ Pa} = 1,4 \text{ bar}$$

$$p_g \cdot V_g = m_g \cdot R \cdot T \rightarrow m_g = \frac{p_g \cdot V_g}{R \cdot T} = \frac{140'094 \cdot 3,14 \cdot 10^{-3}}{166,28 \cdot 773,15} = 3,422 \cdot 10^{-3} \text{ kg}$$

↳ 3,422 g

$$R = \frac{\overline{R}}{M} = \frac{8,314 \text{ J/mol}}{50 \cdot 10^{-3} \text{ kg/mol}} = 166,28 \frac{\text{J}}{\text{kg} \cdot \text{K}}$$

$$\left[ \frac{\frac{\text{kg}}{\text{mol}} \cdot \frac{\text{J}}{\text{mol} \cdot \text{K}}}{\text{kg} \cdot \text{K}} \right]$$



b) Ges:  $T_{g2} + p_{g2}$

Der Vorgang ist adiabatisch daher ist der Vorgang polytrop  $pV^n = \text{const.}$   
 aus der idealen Gasgleichung  $pV = mRT$  folgt wenn  $pV = \text{const.}$ , muss  
 das ganze auch isotherm sein!

Daher  $T_{g2} = T_{g1} = 500^\circ\text{C}$

$$\left( \begin{array}{l} pV^n = mRT \\ p_2 = \frac{mRT}{V^n} = \frac{3,422 \cdot 10^{-3} \cdot 166,28}{(3,14 \cdot 10^{-3})} \end{array} \right)$$

c) Ges:  $Q_{12}$

~~$U + pV + pV - Q_1 - U_1$~~

$\frac{dE}{dt} = Q - W = 0 \rightarrow$  da geschlossenes System

$Q = W = \int_1^2 p \cdot dV = p_0 (V_{g2} - V_{g1}) = 1500 \text{ J}$

d) Ges:  $x_{\text{Eis2}}$

$m_{\text{Eis1}} = 0,6 \cdot m_E = 0,06 \text{ kg}$

$m_{\text{Wasser}} = 0,04 \text{ kg}$

$V_1 = V_2$

$p_1 = p_2$

$T_1 = 273,15 \text{ K} = 0^\circ$

$\Delta U_{FI} = Q = u(T_2) - u(T_1) = m_{\text{cu}} (T_2 - T_1) = 1500 \text{ J}$

$p_E = p_0 + \frac{m_K \cdot g}{A} = 1 + 0,4 = 1,4 \text{ bar}$

$T_2 - T_1 = \frac{\Delta u \cdot Q}{c_v} \rightarrow T_2 = \frac{\Delta u \cdot Q}{c_v} + T_1 = 0,633 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \cdot 1,5 \text{ KJ} + 273,15$

$U = m(\Delta u) = m \cdot c_v (T_2 - T_1) = Q$

$T_2 - T_1 = \frac{Q}{m \cdot c_v} \rightarrow T_2 = \frac{Q}{m \cdot c_v} + T_1 = \frac{1,5 \text{ kJ} \cdot \text{kg} \cdot \text{K}}{0,1 \text{ kg} \cdot 0,633 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}} + 273,15 = 296,846 \text{ K}$

$\Delta u = \frac{1500 \text{ J}}{0,1 \text{ kg} \cdot 1000} = 15 \frac{\text{kJ}}{\text{kg}}$

$u_{\text{Fest}}(1,4 \text{ bar}) = -333,458 \frac{\text{kJ}}{\text{kg}}$

$u_{\text{Flüssig}}(1,4 \text{ bar}) = -0,045 \frac{\text{kJ}}{\text{kg}}$

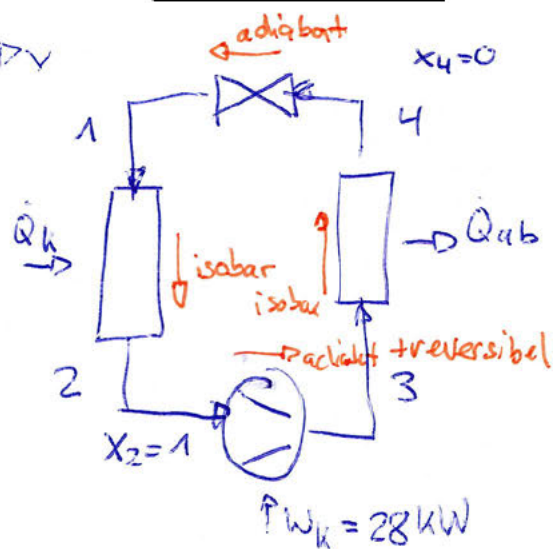
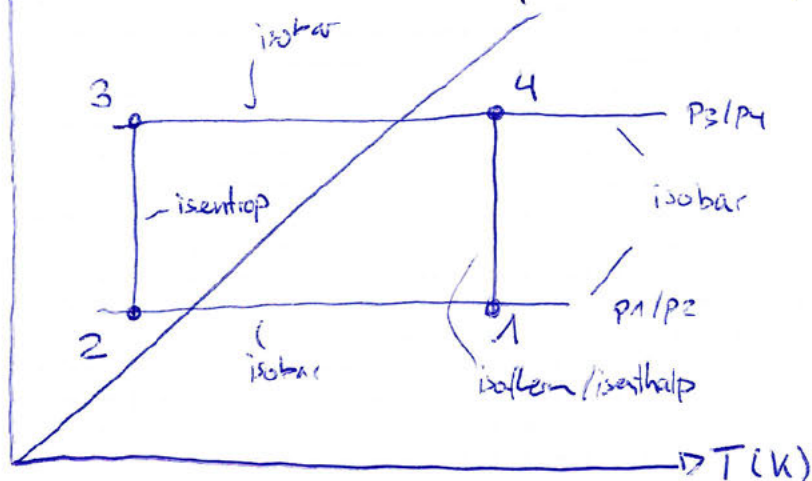
$\Delta u = u_{FI} + x(u_{\text{Fest}} - u_{FI}) \Rightarrow x = \frac{\Delta u - u_{FI}}{u_{\text{Fest}} - u_{FI}} = \frac{15 - 0,045}{-333,458 - 0,045} = 0,045$

# Aufgabe 4

OP (bar)

Flüssig-  
Dampfgebiet

T



b) Gas: mp134a

Stationärer Fließprozess, E-bilanz

$$0 = \dot{m} [h_4 - h_2] + \dot{Q}_k$$

$$\dot{Q}_k = \dot{m} [h_2 - h_1]$$

$$0 = \dot{m} [h_2 - h_3] - W_k$$

$$\dot{m} = \frac{W_k}{h_2 - h_3} = \frac{-28 \text{ kW}}{(234,08 - 571,39) \frac{\text{kJ}}{\text{kg}}} = 0,083 \frac{\text{kg}}{\text{s}}$$

	1	2	3	4
P			$8 \cdot 10^5$	$8 \cdot 10^5$
x		1		0
T		$T_i - 6 = -22^\circ\text{C}$		$T_i - 6$
h	93,42	234,08		93,42

$$p_3 = p_4$$

$$h_1 = h_4$$

$$T_1 = T_4$$

adiabate Prozess

Tab A-10

$$s_2 = s_3 = s_2(-22^\circ\text{C}, x=1) = 0,9351 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$$

$$h_2(-22^\circ\text{C}, x=1) = 234,08 \frac{\text{kJ}}{\text{kg}}$$

$$s_3(8 \text{ bar}) = 0,9351$$

zwischen  $s(8140)$  &  $s(8 \text{ bar}, 50^\circ\text{C})$

interpolieren:

$$h_3 = h(40) + \frac{h(50) - h(40)}{s(50) - s(40)} \cdot s_3$$

$$h_3 = 273,66 + \frac{284,39 - 273,66}{0,5711 - 0,9374} \cdot 0,9351 = 571,39 \frac{\text{kJ}}{\text{kg}}$$

c) Ges:  $x_1$

$$h_1 = h_4$$

$$T_1 = T_4$$

$$x_4 = 0$$

$$h_4 (x=0,8 \text{ bar}) = 93,42 \text{ kJ/kg}$$

Tabelle A-11

$$h_1 = h_4 = 93,42 \frac{\text{kJ}}{\text{kg}}$$

$$\rightarrow 238,08 \text{ kJ/kg}$$

~~Tabelle A-11~~

$$d) \varepsilon_K = \frac{|\dot{Q}_{zu}|}{|\dot{W}_K|} = \frac{|\dot{Q}_K|}{|\dot{W}_K|} = \frac{12 \text{ kW}}{28 \text{ kW}} = 0,429$$

$$\textcircled{*} 0 = \dot{m}_{R134} (h_1 - h_2) + \dot{Q}_K \rightarrow \dot{Q}_K = \dot{m}_{R134} (h_2 - h_1) = 0,083 (238,08 - 93,42) = 12 \text{ kW}$$

e) Wasser geht sofort in Gasphase über.