

1) a) Energiebilanz:

$$0 = \dot{m} [h_{\text{ein}} - h_{\text{aus}}] + \dot{Q}_R - \dot{Q}_{\text{aus}}$$

$$\dot{Q}_{\text{aus}} = \dot{m} [h_{\text{ein}} - h_{\text{aus}}] + \dot{Q}_R$$

$$h_{\text{ein}} = h_f(70^\circ\text{C}) = 292.98 \frac{\text{kJ}}{\text{kg}} \quad (\text{Tab. A-2})$$

$$h_{\text{aus}} = h_g(100^\circ\text{C}) = 419.04 \frac{\text{kJ}}{\text{kg}} \quad (\text{Tab. A-2})$$

$$\dot{Q}_{\text{aus}} = 0.3 \frac{\text{kg}}{\text{s}} \left(292.98 \frac{\text{kJ}}{\text{kg}} - 419.04 \frac{\text{kJ}}{\text{kg}} \right) + 100 \text{ kW}$$

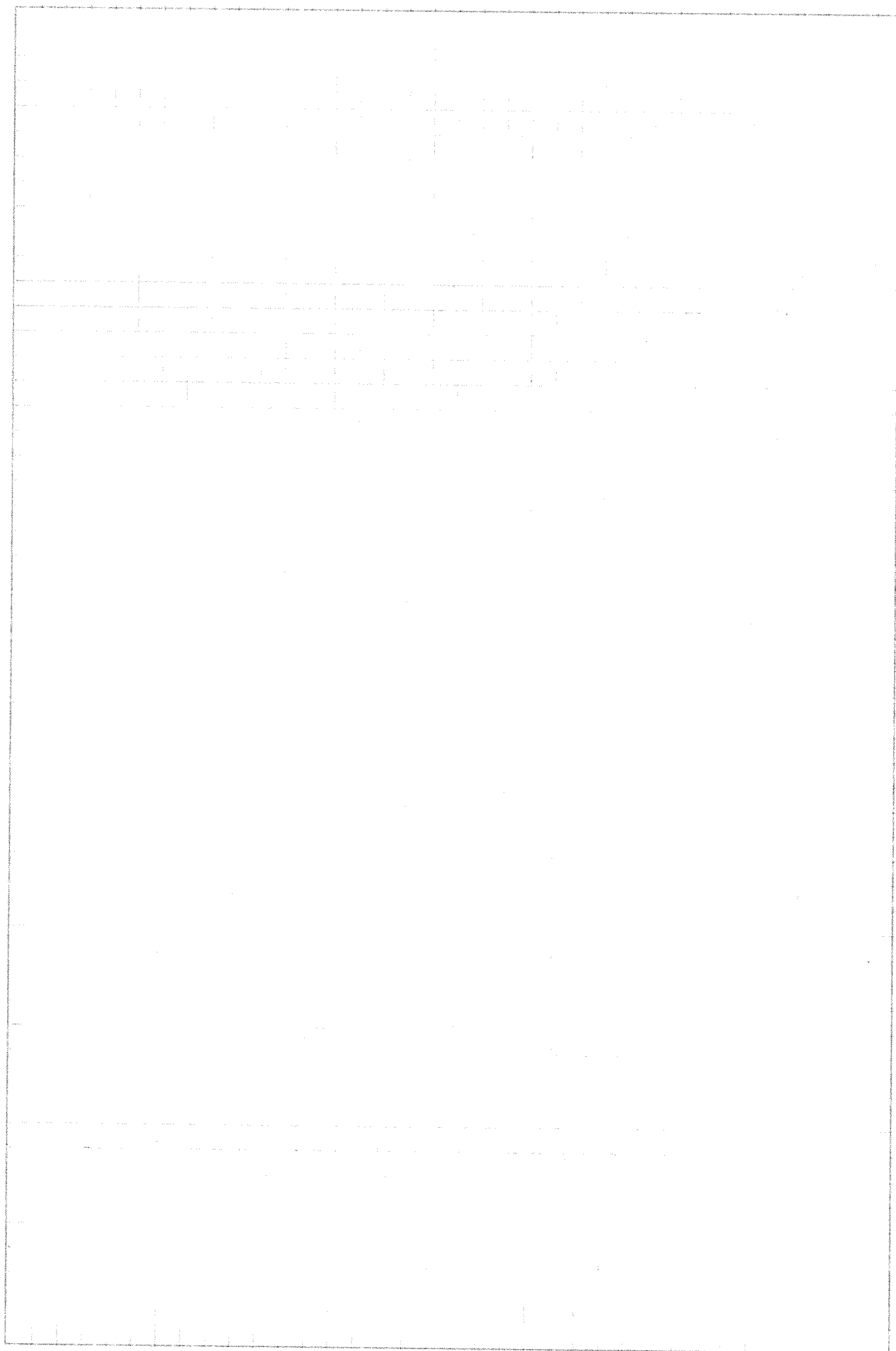
$$= \underline{\underline{62.182 \text{ kW}}}$$

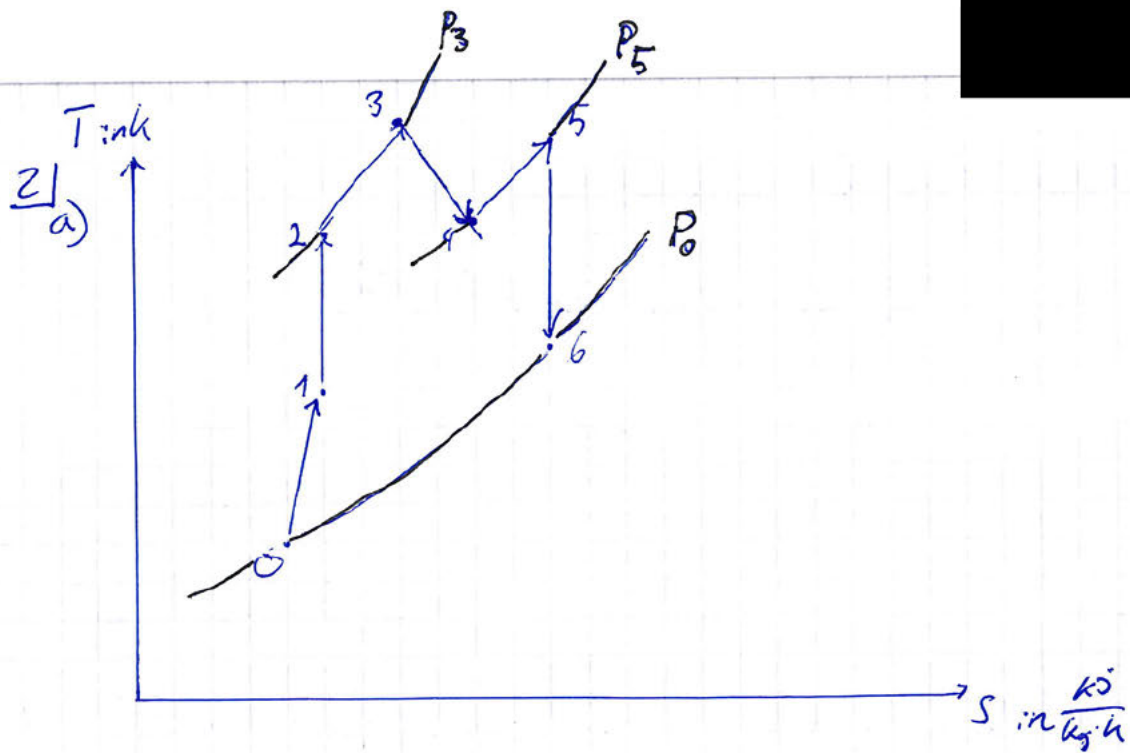
$$b) \quad \bar{T} = \frac{\int_{\text{ein}}^{\text{aus}} T ds}{s_{\text{aus}} - s_{\text{ein}}}$$

$$c) \quad s_{\text{ent}} = \dot{m} (s_{\text{aus}} - s_{\text{ein}}) - \frac{\dot{Q}_R}{T_{\text{Reaktor}}} + \frac{\dot{Q}_{\text{aus}}}{T_{\text{UF}}}$$

$$= 0.3 \left(1.3069 \frac{\text{kJ}}{\text{kg K}} - 0.9589 \frac{\text{kJ}}{\text{kg K}} \right) - \frac{100 \text{ kW}}{372.15 \text{ K}} + \frac{62.182 \text{ kW}}{295 \text{ K}}$$

$$= \underline{\underline{0.0684 \frac{\text{kJ}}{\text{K}}}}$$





b)

$$\frac{T_6}{T_5} = \left(\frac{P_6}{P_5}\right)^{\frac{n-1}{n}}$$

$$T_6 = T_5 \left(\frac{P_0}{P_5}\right)^{\frac{n-1}{n}} = 431.9 \text{ K} \cdot \left(\frac{0.791 \text{ bar}}{0.5 \text{ bar}}\right)^{\frac{0.4}{1.4}} = \underline{\underline{328.1 \text{ K}}}$$

Energiebilanz:

$$0 = \dot{m} \left[h_5 - h_6 + \frac{(w_5^2 - w_6^2)}{2} \right]$$

$$h_5 - h_6 = c_{p, \text{gas}} (T_5 - T_6) = 1.006 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} (431.9 - 328.1) = 104.42 \frac{\text{kJ}}{\text{kg}}$$

$$w_6^2 = (h_5 - h_6) + w_5^2$$

$$w_6^2 = 2(h_5 - h_6) + w_5^2 = 2 \cdot 104.42 \frac{\text{kJ}}{\text{kg}} + (220 \frac{\text{m}}{\text{s}})^2$$

$$= 2 \cdot 104420 \frac{\text{J}}{\text{kg}} + 220^2 \frac{\text{m}^2}{\text{s}^2} = 257240 \frac{\text{m}^2}{\text{s}^2}$$

$$w_6 = \sqrt{257240 \frac{\text{m}^2}{\text{s}^2}} = \underline{\underline{507.19 \frac{\text{m}}{\text{s}}}}$$

$$c) \quad \cancel{e_{x, str, b} = h_b - h_o - T_o(S_b - S_o) + P_o(V - V_o)}$$

$$\Delta e_{x, str} = (h_{aus} - h_{ein} - T_o(S_{aus} - S_{ein}) + \frac{w_{aus}^2 - w_{ein}^2}{2})$$

$$\begin{aligned} h_{aus} - h_{ein} &= h_b - h_o = c_{p, Luft}^{is} (T_b - T_o) = 1.006 \frac{kJ}{kg \cdot K} (328.14 - 243.15 K) \\ &= 85.4597 \frac{kJ}{kg} \end{aligned}$$

$$\begin{aligned} T_o(S_{aus} - S_{ein}) &= T_o(S_b - S_o) = T_o \left(c_{p, Luft}^{is} \cdot \ln\left(\frac{T_b}{T_o}\right) - R \ln\left(\frac{P_b}{P_o}\right) \right) \\ &= 243.15 K \left(1.006 \frac{kJ}{kg \cdot K} \cdot \ln\left(\frac{328.1}{243.15}\right) - \underbrace{R \ln\left(\frac{P_b}{P_o}\right)}_{=0 \text{ (} P_b=P_o)} \right) = 73.2946 \frac{kJ}{kg} \end{aligned}$$

$$\begin{aligned} \frac{w_{aus}^2 - w_{ein}^2}{2} &= \frac{w_b^2 - w_o^2}{2} = \frac{507.19 \frac{m^2}{s^2} - 200 \frac{m^2}{s^2}}{2} = 108620.85 \frac{J}{kg} \\ &= 108.621 \frac{kJ}{kg} \end{aligned}$$

$$\begin{aligned} \Delta e_{x, str} &= 85.4597 \frac{kJ}{kg} - 73.2946 \frac{kJ}{kg} + 108.621 \frac{kJ}{kg} \\ &= 120.786 \frac{kJ}{kg} \end{aligned}$$

d) Energiebilanz, stationär, massenspezifisch

~~oder~~

$$0 = \underbrace{(h_{ein} - h_{aus} - T_o(S_{ein} - S_{aus}) + \Delta h_e)}_{= -\Delta e_{x, str}} + \left(1 - \frac{T_o}{T_B}\right) \dot{q}_B - \underbrace{w_{ein} - e_{x, val}}_{=0}$$

$$\begin{aligned} e_{x, val} &= -\Delta e_{x, str} + \left(1 - \frac{T_o}{T_B}\right) \dot{q}_B \\ &= -120.786 \frac{kJ}{kg} \left(1 - \frac{243.15 K}{1289 K}\right) \cdot 1195 \frac{kJ}{kg} = 898.796 \frac{kJ}{kg} \end{aligned}$$

$$3) a) P_{g,1} = P_{EW} + P_{amb} + P_u$$

$$P_{EW} = \frac{m_{EW} \cdot g \cdot \cancel{\pi \cdot 0.05^2}}{\pi \cdot (0.05 \text{ m})^2} = \cancel{0.1 \text{ kg} \cdot 9.81 \frac{\text{m}}{\text{s}^2} \cdot \pi \cdot 0.0025 \text{ m}^2} = \cancel{7.705 \cdot 10^{-3}}$$

$$= \frac{0.1 \text{ kg} \cdot 9.81 \frac{\text{m}}{\text{s}^2}}{\pi \cdot 0.0025 \text{ m}^2} = 124.905 \text{ Pa}$$

$$P_{amb} = 1 \text{ bar} = 100000 \text{ Pa}$$

$$P_u = \frac{m_u \cdot g}{\pi \cdot (0.05 \text{ m})^2} = 39969.5 \text{ Pa}$$

$$P_{g,1} = 140094 \text{ Pa} = \underline{\underline{1.4 \text{ bar}}}$$

$$P_{g,1} \cdot V_{g,1} = m_{g,1} \cdot R \cdot T_{g,1} \quad T_{g,1} = 500^\circ\text{C} = 773.15 \text{ K}$$

$$R = \frac{\bar{R}}{M_g} = \frac{8.314 \frac{\text{J}}{\text{mol} \cdot \text{K}}}{50 \frac{\text{kg}}{\text{kmol}}} = 166.28 \frac{\text{J}}{\text{kg} \cdot \text{K}}$$

$$m_g = \frac{P_{g,1} \cdot V_{g,1}}{R \cdot T_{g,1}} = \frac{140094 \text{ Pa} \cdot 3.14 \cdot 10^{-3} \text{ m}^3}{166.28 \frac{\text{J}}{\text{kg} \cdot \text{K}} \cdot 773.15 \text{ K}} = 3.4217 \cdot 10^{-3} \text{ kg} = 3.4217 \text{ g}$$

b) $P_{g,2} = P_{g,1}$ da sich das Gewicht des Kolbens und das Gewicht des Eis-Wasser-Gemischs, sowie der Umgebungsdruck nicht verändern

~~Innerer Energie des Systems bleibt unverändert~~

$$T_{gg} = \frac{0.1 \text{ kg} \cdot 773.15 \text{ K} + 3.4217 \cdot 10^{-3} \text{ kg} \cdot 773.15 \text{ K}}{0.1 \text{ kg} + 3.4217 \cdot 10^{-3} \text{ kg}} = 289.69 \text{ K} = 16.54^\circ\text{C}$$

$$c) \quad E_2 - E_1 = Q_{12}$$

$$u_2 - u_1 = Q_{12}$$

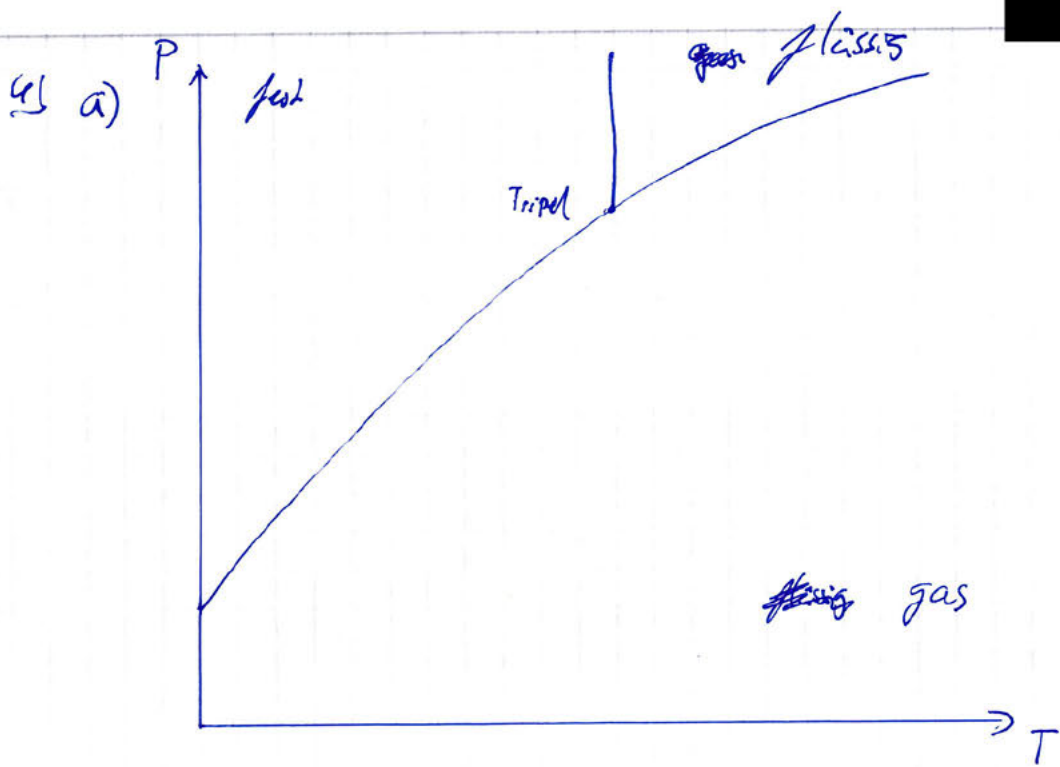
$$m_g(u_2 - u_1) = Q_{12}$$

~~3421 mg~~

$$Q_{12} = m_g c_v^* (T_{2,g} - T_{1,g}) = 3.4217 \cdot 10^{-3} \text{ kg} \cdot 0.683 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \cdot (0.003^\circ\text{C} - 500^\circ\text{C})$$

$$= -1.08296 \text{ kJ} = \underline{\underline{-1082.96 \text{ J}}}$$

d)



b)

$$0 = \dot{m}_{\text{Rück}} (h_2 - h_3) - \dot{W}_k$$

