

Aufgabe 1

a) $\dot{Q}_{\text{aus}}?$

$$\dot{Q}_R = 100 \text{ kW}$$

$$\dot{m}_{\text{gas},1} = 5.755 \text{ kg/s}$$

$$\dot{m}_w = 0.3 \frac{\text{kg}}{\text{s}}$$

$$x_D = 0.005$$

Energiebilanz: (Reaktor)

$$0 = \dot{m}_w(h_e - h_a) + \dot{Q}_R - \dot{Q}_{\text{aus}} - \dot{W}$$

$$h_e = h_f(70^\circ\text{C}) + x_D \cdot (h_g(70^\circ\text{C}) - h_f(70^\circ\text{C}))$$

$$h_e = 304.649 \frac{\text{kJ}}{\text{kg}}$$

$$h_a = h_f(100^\circ\text{C}) + x_D \cdot (h_g(100^\circ\text{C}) - h_f(100^\circ\text{C}))$$

$$h_a = 430.33 \frac{\text{kJ}}{\text{kg}}$$

$$\dot{Q}_{\text{aus}} = \dot{m}_w \cdot (304.649 - 430.33) \frac{\text{kJ}}{\text{kg}} + 100 \text{ kW}$$

$$\dot{Q}_{\text{aus}} = 67.3 \text{ kW}$$

(\dot{Q}_{aus} positiv definiert in Strömungsrichtung K.F.)

$$h_f(70^\circ\text{C}) = 292.98 \frac{\text{kJ}}{\text{kg}} \quad (\text{TAB A-2})$$

$$h_g(70^\circ\text{C}) = 2626.8 \frac{\text{kJ}}{\text{kg}}$$

$$h_f(100^\circ\text{C}) = 419.04 \frac{\text{kJ}}{\text{kg}}$$

$$h_g(100^\circ\text{C}) = 2676.7 \frac{\text{kJ}}{\text{kg}} \quad (\text{TAB A-2})$$

$$b) \quad \bar{T}_{\text{KF}} = \frac{\int_1^2 T ds}{s_2 - s_1} = \frac{q_{\text{rev}}^{12}}{s_2 - s_1} = \frac{h_2 - h_1}{s_2 - s_1} \quad \begin{array}{l} T_1 = 288.15 \\ T_2 = 298.15 \end{array}$$

$$\text{i.f.: } h_2 - h_1 = \int_{T_1}^{T_2} c^{if} dT + v^{if} (p_2 - p_1) = c^{if} (T_2 - T_1)$$

$$s_2 - s_1 = c^{if} \cdot \ln\left(\frac{T_2}{T_1}\right)$$

$$\bar{T}_{\text{KF}} = \frac{T_2 - T_1}{\ln\left(\frac{T_2}{T_1}\right)} = \frac{298.15 - 288.15}{\ln\left(\frac{298.15}{288.15}\right)} = 293.12 \text{ K}$$

c/

Entropiebilanz am Reaktorrand:

$$0 = \frac{\dot{Q}_{\text{sur}}}{\bar{T}_{\text{reak}}} - \frac{\dot{Q}_{\text{abg}}}{\bar{T}_{\text{KF}}} + \dot{S}_{\text{erz}}$$

$$\dot{S}_{\text{erz}} = \dot{Q}_{\text{abg}} \cdot \left(\frac{1}{\bar{T}_{\text{KF}}} - \frac{1}{\bar{T}_{\text{reak}}} \right)$$

$$\bar{T}_{\text{reak}} = 100^\circ\text{C} = 373.15 \text{ K}$$

$$\dot{S}_{\text{erz}} = 62.3 \text{ kW} \cdot \left(\frac{1}{283.12} - \frac{1}{373.15} \right) = \underline{\underline{0.570 \frac{\text{W}}{\text{K}}}}$$

d/

$$T_{\text{Reaktor}} = 70^\circ\text{C}$$

$$\Delta m_{12}, T_1 = 20^\circ\text{C}$$

$$Q_{R,12} = 35 \text{ MJ}$$

Halboffenes System:

$$\Delta E = \Delta U = m_2 u_2 - m_1 u_1 = \Delta m_{12} \cdot (h_{\text{ein}}) + Q_{R,12}$$

Nassdampf:

$$m_2 = m_1 + \Delta m$$

$$u_1 = u_f(100^\circ\text{C}) + x_D \cdot (u_g(100^\circ\text{C}) - u_f(100^\circ\text{C}))$$

$$u_2 = u_f(70^\circ\text{C}) + x_D \cdot (u_g(70^\circ\text{C}) - u_f(70^\circ\text{C}))$$

$$h_{\text{ein}} = u_f(20^\circ\text{C}) + x_D \cdot (u_g(20^\circ\text{C}) - u_f(20^\circ\text{C}))$$

e/

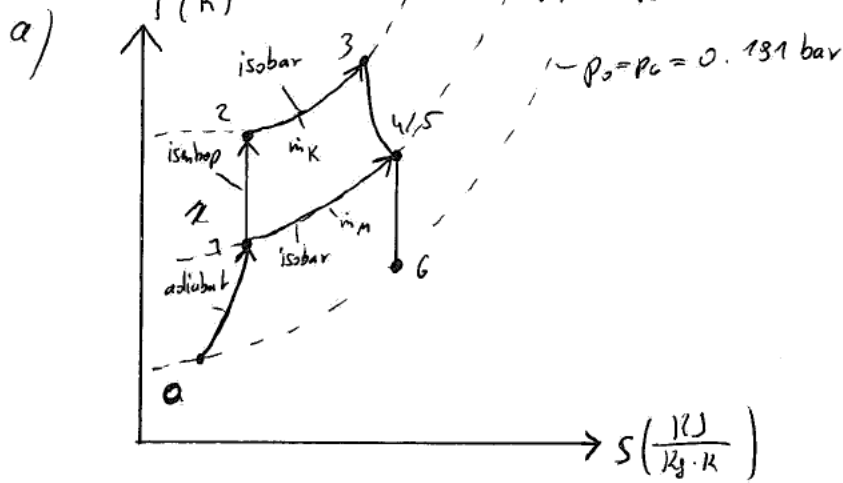
$$\Delta S = m_2 s_2 - m_1 s_1 = \left(\Delta m_{\text{ein}} s_{\text{ein}} - \frac{\dot{Q}_{\text{abg}}}{\bar{T}} + S_{\text{erz}} \right)$$

$$s_2 = s_f(70^\circ\text{C}) + x_D \cdot (s_g(70^\circ\text{C}) - s_f(70^\circ\text{C}))$$

$$s_1 = s_f(100^\circ\text{C}) + x_D \cdot (s_g(100^\circ\text{C}) - s_f(100^\circ\text{C}))$$

$$m_2 = m_1 + \Delta m_{12}$$

Aufgabe 2



b) $w_5 = 220 \frac{m}{s}$

$T_5 = 431.9 \text{ K}$

isentrop: $s_5 = s_6 =$

$p_5 = 0.5 \text{ bar}$

$p_6 = 0.131 \text{ bar}$

$T_5 = 431.9 \text{ K}$

$\kappa = 1.4$

isentrop: $\underline{T_6} = T_5 \cdot \left(\frac{p_6}{p_5} \right)^{\frac{\kappa-1}{\kappa}} = 431.9 \cdot \left(\frac{0.131}{0.5} \right)^{\frac{1.4-1}{1.4}} = \underline{\underline{328.7 \text{ K}}}$

~~$Q = m \cdot (h_5 - h_6) + \frac{w_5^2 - w_6^2}{2}$~~

$0 = m \cdot \left(h_5 - h_6 + \left(\frac{w_5^2 - w_6^2}{2} \right) \right) + \cancel{Q} - \cancel{W}$

$h_5 - h_6 = \frac{w_6^2 - w_5^2}{2}$

$2(h_5 - h_6) + w_5^2 = w_6^2$

$h_5 - h_6 = c_p \cdot (T_5 - T_6)$

$w_6 = \sqrt{2 \cdot (c_p \cdot (T_5 - T_6) + w_5^2)} = \sqrt{2 \cdot 1.006 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \cdot (431.9 - 328.7) \text{ K} + (220)^2 \frac{\text{m}^2}{\text{s}^2}}$

$w_6 =$

$$c) \dot{W}_6 = 570 \frac{\text{m}}{\text{s}}$$

$$T_6 = 340 \text{ K}$$

$$\Delta e_{\text{istr}} = e_{\text{istr},6} - e_{\text{istr},0}$$

$$e_{\text{istr},6} = h_6 - h_u - T_u (s_6 - s_u) + \frac{w_6^2}{2}$$

$$e_{\text{istr},0} = h_0 - h_u - T_u (s_0 - s_u) + \frac{w_0^2}{2}$$

$$\Delta e_{\text{istr}} = h_6 - h_0 - T_u (s_6 - s_0) + \frac{w_6^2 - w_0^2}{2}$$

$$T_u = T_0 = 243.15 \text{ K}$$

$$h_6 - h_0 = c_{p,\text{Luft}} \cdot (T_6 - T_0) \quad (\text{stationary 1g})$$

$$s_6 - s_0 = c_{p,\text{Luft}} \cdot \ln \left(\frac{T_6}{T_0} \right) - R \ln \left(\frac{p_6}{p_0} \right) \rightarrow 0 \quad (p_6 = p_0)$$

$$\Delta e_{\text{istr}} = c_{p,\text{Luft}} \cdot \left((T_6 - T_0) - T_0 \ln \left(\frac{T_6}{T_0} \right) \right) + \frac{w_6^2 - w_0^2}{2}$$

$$\Delta e_{\text{istr}} = 1.006 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \cdot \left((340 - 243.15) - 243.15 \cdot \ln \left(\frac{340}{243.15} \right) \right) + \frac{570^2 - 200^2}{2}$$

$$\Delta e_{\text{istr}} = 125.42 \frac{\text{kJ}}{\text{kg}}$$

$$d) \quad 0 = -\Delta e_{\text{istr}} + \underbrace{q_B \cdot \left(1 - \frac{T_0}{T_B} \right)}_{= L_{\text{ex},Q}} - \dot{W}_v^0 - \dot{e}_{\text{xivel}}$$

$$\dot{e}_{\text{xivel}} = -\Delta e_{\text{istr}} + q_B \cdot \left(1 - \frac{T_0}{T_B} \right)$$

$$\underline{\underline{\dot{e}_{\text{xivel}} = -125.42 \frac{\text{kJ}}{\text{kg}} + 1185 \frac{\text{kJ}}{\text{kg}} \cdot \left(1 - \frac{243.15}{1283} \right) = 844.16 \frac{\text{kJ}}{\text{kg}}}}$$

Aufgabe 3

a)

$$p_{g,1}?$$

$$m_g?$$

$$c_{v, \text{gas}} = 0.633 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$$

$$M_g = 50 \frac{\text{kg}}{\text{kmol}}$$

$$R_g = \frac{8.316}{M_g} = 0.16628 \frac{\text{kJ}}{\text{kg} \cdot \text{K}}$$

$$T_{g,1} = 500^\circ\text{C} = 773.15 \text{ K}$$

$$V_{g,1} = 3.14 \text{ L} = 3.14 \cdot 10^{-3} \text{ m}^3$$

$$A_K = \pi \cdot \left(\frac{0}{2}\right)^2 = \pi \cdot \left(\frac{0.1}{2}\right)^2 = \underline{0.00785 \text{ m}^2}$$

$$p_g = p_{\text{amb}} + m_K \cdot g \cdot \frac{1}{A_K} + m_{EW} \cdot g \cdot \frac{1}{A_K} = p_{\text{amb}} + \frac{g}{A_K} \cdot (m_K + m_{EW})$$

$$\underline{p_{g,1} = 1 \text{ bar} + \frac{9.81}{A_K} \cdot (32 + 0.1) = \underline{1.4 \text{ bar}}}$$

$$p \cdot V = m R T$$

$$\underline{m} = \frac{p_1 V_1}{R_g \cdot T_1} = \frac{1.4 \text{ bar} \cdot 3.14 \cdot 10^{-3} \text{ m}^3}{0.16628 \frac{\text{kJ}}{\text{kg} \cdot \text{K}} \cdot 773.15 \text{ K}} = \underline{3.473 \text{ g}}$$

b)

$$pV = mRT$$

$$m_{1,3} = m_{2,3}$$

$$\underline{p_{1,3} = p_{2,3} = 1.4 \text{ bar}} \quad (\text{Druck durch } p_{\text{amb}} \text{ und Gewicht bleibt unverändert})$$

$$\underline{U_g = U_{EW}}$$

c)

$$T_{g,2} = 0.003^\circ\text{C}$$

$$Q_{12}?$$

E.B. um Gas!

$$\Delta E = E_2 - E_1 = Q_{12} - W_V - W_L$$

$$\Delta E = \Delta U + \Delta KE + \Delta PE$$

$$\Delta U = m_g (u_2 - u_1) = m_g \cdot (C_v \cdot (T_2 - T_1)) = 3.418 \cdot 10^{-3} \text{ kg} \cdot (0.633 \frac{\text{kJ}}{\text{kg K}} \cdot (0.003 - 500))$$

$$\Delta U = -1.082 \text{ kJ}$$

$$W_{12} =$$

$$W_{12} = Q_{12} = -1.082 \text{ kJ}$$

$$p_2 = p_1$$

$$m_2 = m_1$$

$$pV = mRT$$

$$\underline{V_2} = \frac{m_g R_g T_2}{p_1} = \frac{3.418 \cdot 10^{-3} \cdot 0.8 \cdot 273.153 \text{ K}}{1.4 \text{ bar}} = \underline{1.103 \text{ L}}$$

$$W_V = p_1 \cdot (V_2 - V_1) = 1.4 \text{ bar} \cdot (1.103 - 3.14) \cdot 10^{-3} \text{ m}^3$$

$$W_L = -0.284 \text{ kJ}$$

$$\Delta PE = m_{K+EW} \cdot g \cdot \left(\frac{\Delta V}{A_K} \right) = -81.47 \text{ J}$$

$$\Delta U + \Delta PE = Q_{12} - W_V$$

$$\underline{Q_{12}} = \Delta U + \Delta PE + W_V = -1.082 - 81.47 \cdot 10^{-3} - 0.284 = \underline{716.5 \text{ J}}$$

Aufgabe 3

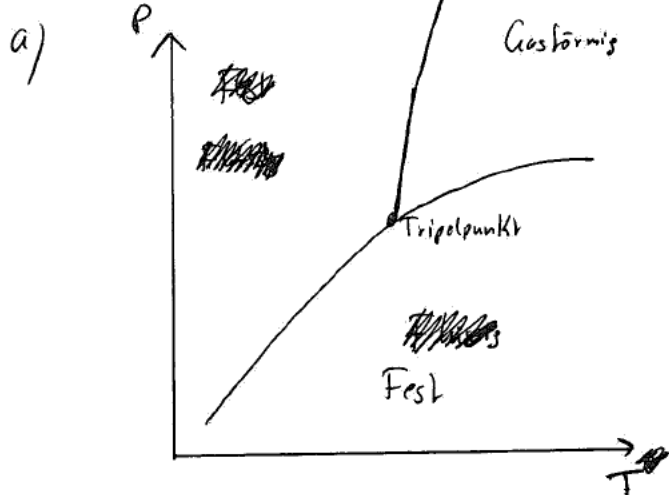
d)

$$x_{Eis,2} = \frac{u_2 - u_{fl}(7.4 \text{ bar})}{\frac{u_{fl}(7.4 \text{ bar})}{F_{shr}} - \frac{u_p(7.4 \text{ bar})}{F_{fl}}}$$

$$u_{fl}(7.4 \text{ bar}) = -0.045 \frac{\text{kJ}}{\text{kg}}$$

$$u_{fl}(7.4 \text{ bar}) = \cancel{333.458} - 333.458 \frac{\text{kJ}}{\text{kg}}$$

Aufgabe 6



b) \dot{m}_{R134a}

$$x_2 = 1$$

2-3 reversibel ($s_2 = s_3$) / isentrop

A	T	P	x
1			x
2			1
3		8	
4			

$$T_2 = \text{~~20~~ } T_1 - 6 \text{ K}$$

$$P_i = 1 \text{ mbar} = 10^{-3} \cdot 10^5 \text{ Pa} = 100 \text{ Pa} = 0.1 \text{ kPa}$$

$T(0.3855 \text{ KPa}) \quad T(0.1035 \text{ KPa})$

— TAB A-6

$$\underline{T_{1a}} = \frac{-22 - (-20)}{0.0853 - 0.1035} \cdot (0.1 - 0.1035) + (-20) = \underline{\underline{-20.385^\circ \text{C}}}$$

$$\underline{T_2} = -20.385 - 6 \text{ K} = \underline{\underline{-26.385^\circ \text{C}}}$$

$$h_2 = h_g(-26.385^\circ \text{C})$$

$$0 = \dot{m}_{R134a} \cdot (h_2 - h_3) + \dot{Q} - \underbrace{28 \text{ W}}_{= \dot{W}_K}$$

$$\dot{m}_{R134a} = \frac{28 \text{ W}}{h_2 - h_3}$$

KZE

$$s_2 = s_3 = s(-26.385^\circ \text{C})$$

$$x_3 = \frac{s_3 - s_f(8 \text{ bar})}{s_g(8 \text{ bar}) - s_f(8 \text{ bar})}$$

$$s_f(8 \text{ bar}) = 0.3459 \frac{\text{kJ}}{\text{kg K}}$$

$$s_g(8 \text{ bar}) = 0.9066 \frac{\text{kJ}}{\text{kg K}}$$

TAB A-11

$$h_3 = h_f(8 \text{ bar}) + x_3 \cdot (h_g(8 \text{ bar}) - h_f(8 \text{ bar}))$$

$$h_f(8 \text{ bar}) = 93.42 \frac{\text{kJ}}{\text{kg}}$$

$$h_g(8 \text{ bar}) = 264.15 \frac{\text{kJ}}{\text{kg}}$$

TAB A-11

c)

$$p_1 = p_2 =$$

$$h_1 = h_4 = h_f(8 \text{ bar}) = 93.42 \frac{\text{kJ}}{\text{kg}} \quad \text{TAB A-11}$$

$$* x_1 = \frac{h_1 - h_f(p_2)}{h_g(p_2) - h_f(p_2)}$$

d)

$$\epsilon_K = \frac{|\dot{Q}_{zu}|}{|\dot{Q}_{ab}| - |\dot{Q}_{zu}|} = \frac{|\dot{Q}_{zu}|}{|\dot{Q}_K|}$$

$$\dot{Q}_{zu} = \dot{Q}_K$$

$$\epsilon_K = \frac{|\dot{Q}_K|}{|\dot{Q}_{ab}| - |\dot{Q}_K|}$$