# **Programmable Semantic Fragments**

Cyrus Omar Jonathan Aldrich

Carnegie Mellon University

{comar, aldrich}@cs.cmu.edu

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#### **Abstract**

This paper introduces typy, a statically typed programming language embedded by reflection into Python. Rather than defining a monolithic semantics, typy has a *fragmentary semantics*, i.e. it delegates semantic control over each term, drawn from Python's fixed syntax, to a contextually relevant user-defined *semantic fragment*. This fragment programmatically 1) typechecks the term, and 2) assigns dynamic meaning to the term by computing its translation to Python.

We argue that this design is *expressive* with examples of fragments that express the semantics of 1) functional record types; 2) a variation on JavaScript's prototypic object system; 3) labeled sum types (with nested pattern matching *a la* ML); and 4) foreign interfaces to Python and OpenCL.

We further argue that this design is *compositionally well-behaved*. It sidesteps the problems of grammar composition and the expression problem by allowing different fragments to deterministically share a fixed concrete and abstract syntax. Moreover, programs are semantically stable under fragment composition (unlike systems where the semantics is a "bag of inference rules.")

#### 1. Introduction

As programming languages proliferate, programmers face the daunting problem of *lateral compatibility*, i.e. of interfacing with libraries written in sibling languages. For example, there are useful libraries written in TypeScript [7], Flow [1] and PureScript [2], but these libraries are not directly accessible across language boundaries because these languages are all syntactically and semantically incompatible with one another (the first two define different object systems, and PureScript is a functional language similar to Haskell and ML.)

One common workaround is to interface indirectly with libraries written in sibling languages through the code generated by a compiler that targets a more established language for which a *foreign interface (FI)* is available. For example, all of the languages above have compilers that target JavaScript and

they are all capable of interfacing with JavaScript. Unfortunately, this approach is unnatural (the syntactic and semantic conveniences of the sibling language are unavailable), unsafe (the type system of the sibling language is not enforced) and anti-modular (if the compiler representations change, client programs can break.) Although the safety problem can be ameliorated by inserting dynamic checks [35], it appears that the language-oriented approach [56] is difficult to reconcile with the best practices of "programming in the large" [16].

In this paper, we propose a more compositional *fragment-oriented* approach to the problem of expressing new semantic structures. In particular, we introduce a single "extensible" language, typy, that allows library providers to package a variety of semantic structures into *semantic fragments* that library clients can import in any combination. For example, rather than building functional record types into typy, a library provider can define a fragment that expresses their static and dynamic semantics. This approach sidesteps the lateral compatibility problem in that the clients of a library that requires record values at its public interface can simply import that fragment themselves. Of course, designing an expressive semantic fragment system equipped with useful composition principles presents several challenges.

First, language designers typically define concrete forms specific to the primitive structures that they introduce, but if we allow fragment providers to define new concrete forms in a decentralized manner (following the approach of Sugar\* [19] and similar systems), then different fragments could define conflicting forms. For example, consider the following family of forms:

{  $label_1$ :  $expr_1$ , ...,  $label_n$ :  $expr_n$  }

One fragment might take these as the introductory forms for functional records, while another fragment might take these as the introductory forms for TypeScript-style objects. These forms might also conflict with those for Python-style dictionaries (which use values, rather than labels, as keys.) Such syntactic conflicts inhibit composition.

We also encounter the classic *expression problem* [44, 55]: if library providers are able to define new term constructors in a decentralized manner, then it becomes difficult to define functions that proceed by exhaustive case analysis over term constructors, like pretty-printers.

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<sup>&</sup>lt;sup>1</sup> We assume throughout that simple naming conflicts are handled by some external coordination mechanism, e.g. a package repository.

At the level of the semantics, we must maintain essential metatheoretic properties, like type safety. Moreover, clients should be able to assume that importing a new fragment for use in one portion of a program will not change the meaning of other portions of the program, nor allow a program to take on ambiguous meaning. This implies that we cannot simply operationalize the semantics as a "bag of rules" that fragments contribute to unconstrained.

The semantic fragment system that we introduce addresses the problems of concrete and abstract syntax quite simply: fragment providers are not given the ability to extend typy's concrete nor abstract syntax. Instead, the semantics allows fragments to "share" syntactic forms by delegating control over each term to a contextually relevant fragment definition. For example, our semantics delegates control over terms of curly-brace delimited form (see above) to the fragment that defines the type that the term is being checked against. As such, these forms can serve as introductory forms for records, objects and dictionaries alike. The delegation protocol is deterministic, so ambiguities cannot arise, and stable under fragment composition, so defining a new fragment cannot change the meaning of an existing program component.

What does it mean for a fragment to be "delegated control" over a term? In our system, the delegated fragment is tasked first with programmatically typechecking the term, following a *bidirectional* protocol, i.e. one that supports local type inference [42]. (Scala is another notable language that has a bidirectional type system, albeit of different design [39].) If the fragment decides that the term is ill-typed, it generates an error message. If typechecking succeeds, the fragment is tasked with assigning dynamic meaning to the term by computing a translation to a fixed *internal language* (IL). The IL is analagous to a first-stage compiler intermediate language (here shifted into the semantics of the language.) Defining the dynamics by translation (following the approach taken in the type theoretic definition of Standard ML [26]) means that we need only be convinced that the IL is type safe.

The general fragment delegation protocol just outlined is the primary conceptual contribution of this paper. To make matters concrete, we must choose a particular syntax and IL for typy. We choose to repurpose Python's syntax and use Python itself as the IL (which explains why we named our language typy.) There are two main reasons for this choice: 1) Python supports both dynamic reflection and code generation, so we can embed our system itself into Python as a library (no standalone compiler is needed); and 2) Python's syntax, cleverly repurposed, is rich enough to express a wide variety of interesting constructs cleanly (so we inherit various tooling "for free".)

Sec. 2 introduces various aspects of typy's fragment system with simple examples. Sec. 3 then describes more sophisticated case studies. Sec. 4 summarizes related work. We conclude after a discussion of present limitations and future work in Sec. 5.

# Listing 1 Types and values in typy.

```
1 from typy import component
2 from typy.std import record, string_in, py
4
  @component
5 def Listing1():
    Account [: type] = record[
                   : string_in[r'.+'],
8
      account_num : string_in[r'\d{2}-\d{8}'],
9
10
    ]
11
12
    test_acct [: Account] = {
13
                     "Harry Q. Bovik",
      name:
14
      account_num:
                    "00-12345678",
15
      memo:
                    { }
16
```

# 2. Fragments in typy

Listing 1 shows an example of a well-typed typy program that first imports several fragments, then defines a top-level component, Listing1, that exports a record type, Account, and a value of that type, test\_acct.

### 2.1 Dynamic Embedding

typy is dynamically embedded into Python, meaning that Listing 1 is simply a standard Python script at the top level. typy supports Python 2.6+, though in later examples, we use syntactic conveniences not introduced until Python 3.0. Appendix A discusses the minor changes necessary to port these examples to Python 2.6+.

**Package Management** On Line 2, we use Python's import mechanism to import three fragments from typy.std, the typy standard library. This library receives no special treatment from typy's semantics – it comes bundled with typy merely for convenience.

**Fragments** typy fragments are Python classes that extend typy. Fragment. These classes are never instantiated – instead, typy interacts with them exclusively through class methods (i.e. methods on the class object.) Listing 2 shows a portion of the record fragment, which is discussed in Sec. 2.2.

**Top-Level Components** On Lines 4-16 of Listing 1, we define a top-level typy component by decorating a Python function value with component, a decorator defined by typy. This decorator discards the decorated function value after extracting its abstract syntax tree (AST) and *static environment*, i.e. its closure and globals dictionary, using the reflection mechanisms exposed by the ast and inspect packages in Python's standard library.<sup>2</sup> It then processes the syntactic forms in the body of the function definition according to an alternative semantics. In particular, component repurposes Python's assignment and array slicing forms to allow for the definition of type members, described in Sec. 2.2, and value members,

 $<sup>^2</sup>$  The reader may need to refer to documentation for the ast package, available at https://docs.python.org/3.6/library/ast.html, to fully understand some examples in the remainder of this paper.

## Listing 2 Record type validation.

```
import ast, typy
2 class record(typy.Fragment):
    @classmethod
    def init_idx(cls, ctx, idx_ast):
      if isinstance(idx_ast, ast.Slice):
         # Python special cases single slices
6
         # we don't want that
        idx_ast = ast.ExtSlice(dims=[idx_ast])
8
9
      if isinstance(idx_ast, ast.ExtSlice):
10
        idx_value = dict()
        for dim in idx_ast.dims:
11
12
           if (isinstance(dim, ast.Slice) and
13
               dim.step is None and
14
               dim.upper is not None and
               isinstance(dim.lower, ast.Name)):
15
16
             lbl = dim.lower.id
17
             if lbl in idx_value:
               raise typy.TypeFormationError(
18
                 "Duplicate label.", dim)
19
             ty = ctx.as_type(dim.upper)
20
21
             idx_value[lbl] = ty
           else: raise typy.TypeFormationError(
22
23
             "Invalid field spec.", dim)
24
        return idx_value
25
      else: raise typy.TypeFormationError(
         "Invalid record spec.", idx_ast)
```

described in Sec. 2.3. The return value of the decorator is an instance of typy. Component that tracks 1) the identities of type members; and 2) the types and evaluated translations of value members.

#### 2.2 Fragmentary Type Validation

The type member definition on Lines 6-10 of Listing 1 is of the following general form:

```
name [: kind] = ty_expr
```

where name is a Python name, kind is a typy *kind* and ty\_expr is a typy *type expression*. Kinds classify type expressions, so when typy encounters a definition like this, it checks that ty\_expr is of kind kind.

typy adopts the system of *dependent singleton kinds* first developed for the ML module system [13, 25], which elegantly handles the details of type synonynms, type members and parameterized types (we will define a parameterized type in Listing 7.) The only major deviation from this established account of type expressions, which we will not repeat here, is that types in canonical form are expressed as follows:

```
fragment[idx]
```

where fragment is a fragment in the static environment and idx is some Python slice form. In other words, every typy type in canonical form is associated with a fragment – there are no "primitive" types defined by typy itself. For convenience, programmers can write fragment by itself when the index is trivial, i.e. when it is of the form ().

For example, the type expression on Lines 6-10 of Listing 1 is a record type in canonical form. The index, which is in Python's *extended slice form*, specifies fields named name, account\_num and memo and corresponding field types as shown.

We discuss the field types in Sec. 2.3 – for now, it suffices to see that these are also canonical.

To establish that a type in canonical form is valid, i.e. of kind type, typy calls the fragment class method init\_idx with the *context* and the AST of the index as arguments. This method must return a Python value called the type's *index value* if the type is valid, or raise typy.TypeValidationError with an error message and a reference to the location of the error within the index otherwise.

For example, the record.init\_idx class method given in Listing 2 validates record types by checking that 1) the index consists of a sequence of field specifications of the form name: ty, where name is a Python name; 2) no names are duplicated; and 3) ty is a valid type as determined by calling a method of the context object, ctx.as\_type (Line 20.) This method turns the given Python AST into a type expression, i.e. an instance of typy.TyExpr, and checks that it is of kind type. The returned index value is a Python dictionary mapping the names to the corresponding instances of typy.TyExpr.\_\_\_\_

show example?

# 2.3 Fragmentary Bidirectional Typing and Translation

The value member definition on Lines 12-16 of Listing 1 is of the following general form:

```
name [: ty_expr] = expr
```

where name is a Python name, ty\_expr is a type expression and expr is an expression. When typy encounters a definition like this, it 1) checks that ty\_expr is of kind type, as described in Sec. 2.2; 2) analyzes expr against ty\_expr; and 3) generates a translation for expr, which is another Python AST.

The type annotation is not necessary:

```
name = expr
```

In this case, typy attempts to *synthesize* a type from expr before generating a translation, rather than analyzing it against a known type.

Type systems that distinguish type analysis (where the type is known) from type synthesis (also known as *local type inference*, where the type must be determined from the expression) are called *bidirectional type systems* [42]. Our system is based on the system developed by Dunfield and Krishnaswami [17]. Again, we will not repeat standard details here – our interest will be only in how typy delegates control to some contextually relevant fragment according to the typy *delegation protocol*. This section describes how the delegation protocol works for different expression forms.

# 2.3.1 Literal Forms

typy delegates control over the typechecking and translation of expressions of literal form to the fragment defining the type that the expression is being analyzed against.

For example, the expression on Lines 12-16 of Listing 1 is of dictionary literal form. The type that this expression is being analyzed against is Account, which is synonymous with a record type. typy first calls the record.ana\_Dict class method, shown in Figure 3. This method receives the context, the index value of the type and the AST of the literal

### **Listing 3** Typing and translation of literal forms.

```
1 # class record(typy.Fragment):
    # ... continued from Listing 2 ...
3
    @classmethod
4
    def ana_Dict(cls, ctx, idx, e):
5
      for lbl, value in zip(e.keys, e.values):
        if isinstance(lbl, ast.Name):
6
           if lbl.id in idx:
8
             ctx.ana(value, idx[lbl.id])
9
           else:
10
            raise typy.TyError("<bad label>", f)
11
        else:
12
           raise typy.TyError("<not a label>", f)
13
      if len(idx) != len(e.keys):
14
        raise typy.TyError("<label missing>", e)
15
16
    @classmethod
    def trans_Dict(self, ctx, idx, e):
17
      ast_dict = dict((k.id, v)
18
19
        for k, v in zip(e.keys, e.values))
20
      return ast.Tuple(
21
         (lbl, ctx.trans(ast_dict[lbl]))
        for lbl in idx.iterkeys())
22
```

expression and must return (trivially) if typechecking is successful or raise typy.TyError with an error message and a reference to the subterm where the error occurred otherwise. In this case, record.ana\_Dict checks that each key expression is a Python name that appears in the type index, and then asks typy to analyze the value against the corresponding type by calling ctx.ana. Finally, it makes sure that all the components specified by the type index have appeared in the literal.

The three subexpressions in Listing 1 that record.ana\_Dict asks typy to analyze are also of literal form – the values of name and account\_num are string literals and the value of memo is another dictionary literal. As such, when ctx.ana is called, typy follows the same protocol just described, delegating to string\_in.ana\_Str to analyze the string literals and to py.ana\_Dict to analyze the dictionary literal. The string\_in fragment implements a regex-based constrained string system, which we described, along with its implementation in typy, in a workshop paper [23].<sup>3</sup> The py fragment allows dynamic Python values to appear inside typy programs, so { } is analyzed as an empty Python dictionary. We omit the details of these methods for concision.

If typechecking is successful, typy delegates to the same fragment to generate a translation. For example, typy calls the record.trans\_Dict method shown in Figure 3, which translates records to Python tuples (the labels do not need to appear in the translation.) This method asks typy to determine translations for the field values by calling ctx.trans.

#### 2.3.2 Function Forms

Listing 4 shows an example of another component, Listing4, that defines a typy function, hello, on Lines 7-11 and then applies it to print a greeting on Line 13. This listing imports

Listing 4 Functions, targeted forms and binary forms.

```
from typy import component
2 from typy.std import fn
3 from listing1 import Listing1
5 @component
6 def Listing4():
    def hello(account : Listing1.Account):
8
9
       """Computes a string greeting."
10
      name = account.name
       "Hello, " + name
11
12
    print(hello(Listing1.test_acct))
13
```

the component Listing 1 defined in Listing 1 (we assume that Listing 1 is in a file called listing1.py.)

typy delegates control over the typechecking and translation of function definitions that appear inside components to the fragment that appears as the top-most decorator.

Here, the fn fragment appears as the top-most decorator, so typy begins by calling the fn.syn\_FunctionDef class method, outlined in Listing 5. This method is passed the context and the AST of the function and must manipulate the context as desired and return the type that is to be synthesized for the function, or raise typy.TyError if this is not possible. We omit some of the details of this method for concision.

Observe on Lines 7-8 of Listing 5 that fn calls ctx.check on each statement in the body of the function definition (other than the docstring, following Python's conventions.) This prompts typy to follow its delegation protocol for each statement, described in Sec. 2.3.3.

We chose to take the value of the final expression in the body of the function as its return value, following the usual convention in functional languages (an alternative function fragment could use Python-style return statements.) The synthesized function type is constructed programmatically on Lines 15-16 by pairing the argument types (elided) with the synthesized return type.

If typechecking is successful, typy calls the class method fn.trans\_FunctionDef to generate the translation of the function definition. This method, elided due to its simplicity, recursively asks typy to generate the translations of the statements in the body of the function definition by calling ctx.trans and inserts the necessary return keyword on the final statement.

#### 2.3.3 Statement Forms

4

Statement forms, unlike expression forms, are not classified by types. Rather, typy simply checks them for validity when the governing fragment calls ctx.check.

For most statement forms, typy simply delegates control over validation back to the fragment delegated control over the function that the statement appears within. For example, when fn.syn\_FunctionDef calls ctx.check on the assignment statement on Line 10 of Listing 4, typy delegates control back to the fn fragment by calling fn.check\_Assign. Similarly, fn.check\_Expr handles expression statements, i.e. statements

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<sup>&</sup>lt;sup>3</sup> Certain details of typy have changed since that paper was published, but the essential idea remains the same.

#### **Listing 5** A portion of the fn fragment.

```
class fn(typy.Fragment):
    @classmethod
3
    def syn_FunctionDef(cls, ctx, tree):
      # (elided) process args + their types
5
      # (elided) process docstring
6
      # check each statement in remaining body
      for stmt in tree.proper_body:
8
        ctx.check(stmt)
9
       # synthesize return type from last stmt
10
      last_stmt = tree.proper_body[-1]
11
      if isinstance(last stmt. ast.Expr):
12
         rty = ctx.syn(last_stmt.value)
13
      else: rty = unit
14
      # generate fn type
      return typy.CanonicalType(
15
16
        fn, (arg_types, rty))
17
    @classmethod
18
    def check_Assign(cls, ctx, stmt):
19
      # (details of _process_assn elided)
20
21
      pat, ann, e = _process_assn(stmt)
22
      if ann is None:
23
         ty = ctx.syn(e)
24
       else:
25
        ty = ctx.as_type(ann)
26
         ctx.ana(e, ty)
27
      bindings = ctx.ana_pat(pat, ty)
28
      ctx.push_bindings(bindings)
29
    @classmethod
30
31
    def check_Expr(cls, ctx, stmt):
      ctx.syn(stmt.value)
32
33
    # trans_FunctionDef, trans_Assign & trans_Expr
34
35
    # are elided
```

that consist of a single expression, like the expression statement on Line 11 of Listing 4. Let us consider these in turn.

**Assignment** The definition of fn.check\_Assign given in Listing 5 begins by extracting a *pattern* and an optional *type annotation* from the left-hand side of the assignment, and an expression from the right-hand side of the assignment.

No type annotation appears on the assignment in Listing 4, so fn.check\_Assign asks typy to synthesize a type from the expression by calling ctx.syn (Line 23 of Listing 5.) We will describe how typy synthesizes a type for the expression account.name in Sec. 2.3.4.

In cases where an annotation is provided, fn.check\_Assign instead asks typy to kind check the ascription to produce a type, then it asks typy to analyze the expression against that type by calling ctx.ana (Lines 25-26 of Listing 5.)

Finally, fn.check\_Assign checks that the pattern matches values of the type that was synthesized or provided as an annotated by calling ctx.ana\_pat. Patterns of variable form, like name in Listing 4, match values of any type. We will see more sophisticated examples of pattern matching in Sec. 2.4. The ctx.push\_bindings method pushes the bindings (here, a single binding) into the typing context.

During translation, typy delegates to fn.trans\_Assign. This method is again omitted because it is straightforward.

### **Listing 6** Typing and translation of targeted forms.

```
1 # class record(typy.Fragment):
    # ... continued from Listing 3 ...
3
    @classmethod
4
    def syn_Attribute(cls, ctx, idx, e):
      if e.attr in idx:
5
6
        return idx[e.attr]
8
        raise typy.TypeError("<bad label>", e)
9
10
    @classmethod
    def trans_Attribute(self, ctx, idx, e):
11
12
      position = position_of(e.attr, idx)
13
      return ast.Subscript(
14
        value=ctx.trans(e.value),
        slice=ast.Index(ast.Num(n=position)))
15
```

The only subtlety has to do with shadowing – fn follows the functional convention where different bindings of the same name are entirely distinct, rather than treating them as imperative assignments to a common stack location. This requires generating fresh identifiers when a name is reused. As with the semantics of return values, a different function fragment could make a different decision in this regard.

**Expression Statements** The fn.check\_Expr method, shown in Listing 5, handles expression statements, e.g. the statement on Line 11 of Listing 4, by simply asking typy to synthesize a type for the expression. In Listing 4, this expression is of binary operator form – we will describe how typy synthesizes a type for expressions of this form in Sec. 2.3.5.

Other Statement Forms typy does not delegate to the fragment governing the enclosing function for statements of function definition form that have their own fragment decorator. Instead, typy delegates to the decorating fragment, just as at the top-level of a component definition. The fragment governing the enclosing function determines only how the translation is integrated into its own translation (through a integrate\_trans\_FunctionDef method, omitted for concision.)

typy also does not delegate to the decorating fragment for statements that 1) assign to an attribute, e.g. e1.x = e2; 2) assign to a subscript, e.g. e1[e2] = e3; or 3) statements with guards, e.g. **if**, **for** and **while**. These operate as *targeted* forms, described next.

#### 2.3.4 Targeted Forms

Targeted forms include 1) the statement forms just mentioned; 2) expression forms having exactly one subexpression, like -e1 or e1.attr; and 3) expression forms where there may be multiple subexpressions but the left-most one is the only one required, like e1(args). When typy encounters terms of targeted form, it first synthesizes a type for the target subexpression e1. It then delegates control over typechecking and translation to the fragment defining the type of e1.

For example, the expression on the right-hand side of the assignment statement on Line 10 of Listing 4 is account.name, so typy first synthesizes a type for account. Due to the type annotation on hello, we have that account synthesizes type

Listing1.Account (following the rule for variables, which are tracked by the context.) This type is synonymous with a record type, so typy first calls the record.syn\_Attribute class method given in Listing 6. This method looks up the attribute, here name, in the type index and returns the corresponding field type, here string\_in[r".+"], or raises a type error if the attribute is not found in the type index.

To generate the translation for account.name, typy calls record.trans\_Attribute, shown in Listing 6. Because record values translate to tuples, this class method translates field projection to tuple projection, using the position of the attribute within the index to determine the slice index.

## 2.3.5 Binary Forms

Python's grammar also defines a number of binary operator forms, e.g. e1 + e2. One approach for handling these forms would be to privilege the leftmost argument, e1, and treat these forms as targeted forms. This approach is unsatisfying because these binary operators are often commutative. For this reason, typy instead uses a more sophisticated protocol to determine which fragment is delegated control over binary forms. First, typy attempts to synthesize a type for both arguments. If neither argument synthesizes a type, a type error is raised.

If only one of the two arguments synthesizes a type, then the fragment defining that type is delegated control. For example, the binary operator on Line 11 of Listing 4 consists of a string literal on the left (which does not synthesize a type, per Sec. 2.3.1) and a variable, name, of type string\_in[r".+"] on the right, so string\_in is delegated control over this form.

If both arguments synthesize a type and both types are defined by the same fragment, then that fragment is delegated control. If each type is defined by a different fragment, then typy refers to the *precedence sets* of each fragment to determine which fragment is delegated control. The precedence sets are Python sets listed in the precedence attribute of the fragment that contain other fragments that the defining fragment claims precedence over (if omitted, the precedence set is assumed empty.) The precedent fragment is delegated control. typy checks that if one fragment claims precedence over another, then the reverse is not the case (i.e. precedence is anti-symmetric.) Precedence is not transitive. If no precedence can be determined, then a type error is raised.

For example, if we would like to be able to add ints and floats and these are defined by separate fragments, then we can put the necessary logic in either fragment and then place the other fragment in its precendence set.

#### 2.4 Fragmentary Pattern Matching

As we saw on Line 27 of Listing 5, fragments can request that typy check that a given *pattern* matches values of a given type by calling ctx.ana\_pat. In the example in Listing 4, the pattern was simply a name – name patterns match values of any type. In this section, we will consider more sophisticated

**Listing 7** Polymorphism, recursion and pattern matching in typy. An analagous OCaml file is shown in Appendix C.

```
from typy import component
2 from typy.std import finsum, tpl, fn
4 @component
  def Listing7():
       # polymorphic recursive finite sum type
       tree(+a) [: type] = finsum[
 8
9
         Node(tree(+a), tree(+a)),
10
         Leaf(+a)
11
12
13
       # polymorphic recursive function over trees
14
15
       def map(f : fn[+a, +b],
16
               t : tree(+a)) -> tree(+b):
17
         [t].match
18
         with Empty: Empty
19
         with Node(left, right):
20
           Node(map(f, left), map(f, right))
21
         with Leaf(x):
           Leaf(f(x))
```

patterns. For example, the assignment statement below uses a tuple pattern:

```
(x, y, z) = e
```

typy also supports a more general match construct, shown on Lines 17-22 of Listing 7. This construct, which spans several syntactic statements, is treated as a single expression statement by typy. The *scrutinee* is t and each *clause* is of the following form:

```
with pat: e
```

where pat is a pattern and e is the corresponding branch expression.

To typecheck a match expression statement, typy first synthesizes a type for the scrutinee. Here, the scrutinee, t, is a variable of type tree(+a). This type is an instance of the parameterized recursive type tree defined on Lines 7-11 (the mechanisms involved in defining recursive and parameterized types are built into typy in the usual manner.) Type variables prefixed by +, like +a and +b, implicitly quantify over types at the function definition site (like 'a in OCaml [32].)

More specifically, tree(+a) is a recursive finite sum type defined by the finsum fragment imported from typy.std [25]. Values of finite sum type are translated into Python tuples, where the first element is a string tag giving one of the names in the type index and the remaining elements are the corresponding values. For example, a value Node(e1, e2) translates to ("Node", tr1, tr2) where tr1 and tr2 are the translations of e1 and e2. Note that names and call expressions beginning with a capitalized letter are treated as literal forms in typy (following Haskell's datatype convention [28].)

For each clause in a match expression statement, typy checks that the pattern matches values of the scrutinee type by delegating to the fragment defining that type. For example, to check the pattern Node(left, right) on Line 18, typy calls

Listing 8 Typing and translation of patterns.

```
import ast. tvpv
 2 class finsum(typy.Fragment):
3
    # ...
    @classmethod
5
    def ana_pat_Call(cls, ctx, idx, pat):
6
       if (isinstance(pat.func, ast.Name) and
8
           pat.func.id in idx and
9
           len(pat.args) == len(idx[pat.func.id])):
10
         bindings, lbl = {}, pat.func.id
11
         for p, ty in zip(pat.args, idx[lbl]):
12
           _combine(bindings, ctx.ana_pat(p, ty))
         return bindings
13
14
       else:
         raise typy.TyError("<bad pattern>", pat)
15
16
17
    @classmethod
    def trans_pat_Call(cls, ctx, idx, pat,
18
19
                         scrutinee_trans):
       conditions = \Gamma
20
21
         ast.Compare( # tag check
22
           left=_project(scrutinee_trans, 0),
23
           ops=[ast.Eq()].
24
           comparators=[ast.Str(s=pat.func.id)])
25
       binding_translations = {}
26
27
       for n, p in enumerate(pat.args):
28
         arg_scrutinee = _project(scrutinee_trans,
29
                                   n+1)
30
         c, b = ctx.trans_pat(p, arg_scrutinee)
31
         conditions.append(c)
         binding_translations[pat.func.id] = b
32
33
       condition = ast.BoolOp(op=ast.And(),
34
         values=conditions)
       return (condition, binding_translations)
35
36
37 def _project(e, n): # helper function
38
    return ast.Subscript(value=e,
39
       slice=ast.Index(ast.Num(n=n)))
```

finsum.ana\_pat\_Call, shown in Listing 8. This method must either return a dictionary of bindings, i.e. a mapping from variables to types, which typy adds to the typing context when typechecking the corresponding branch expression, or raise a type error if the pattern does not match values of the scrutinee type. In this case, finsum.ana\_pat\_Call first checks to make sure that 1) the name that appears in the pattern appears in the type index (for finsum types, this is a mapping from names to sequences of types); and 2) that the correct number of pattern arguments have been provided. If so, it asks typy to check each subpattern against the corresponding type. Here, left and right are both checked against tree(+a). The returned dictionary of bindings is constructed by combining the two dictionaries returned by these calls to ctx.ana\_pat. The \_combine function, not shown, also checks to make sure that the bound variables are distinct.

Match expression statements translate to Python if...elif statements. For each clause, typy needs a boolean *condition expression*, which determines whether that branch is taken, and for each binding introduced by that clause, typy needs a translation. Both the the condition expression and

the binding translations can refer to the scrutinee. To determine the condition and the binding translations, typy again delegates to the fragment defining the scrutinee type, here by calling finsum.trans\_pat\_Call, given in Listing 8. This class method is passed the context, the type index, the pattern AST and an AST representing the scrutinee (bound to a variable, to avoid duplicating effects.) The generated condition expression first checks the tag. Then, for each, subpattern, it recursively generates its conditions and binding translations by calling ctx.trans\_pat(p, arg\_scrutinee), where arg\_scrutinee makes the new "effective scrutinee" for the subpattern be the corresponding projection out of the original scrutinee. The returned condition expression is the conjunction of the tag check and the subpattern conditions.

show example?

# 3. More Examples

The examples in the previous section are all found in existing languages. In this section, we give examples of novel semantic structures.

### 3.1 Prototypic Objects

### 3.2 Foreign Function Interfaces

# 4. Related Work

In our recent work on *type-specific languages (TSLs)* in the Wyvern language, we used a bidirectional protocol to delegate control over the parsing of literal forms to functions associated with type definitions [40, 41]. This inspired our treatment of literal forms in typy. Unlike Wyvern, the literal forms are parsed according to Python's fixed syntax. Unlike typy, Wyvern has a monolithic semantics.

Like typy, Typed Racket is a statically typed language embedded into a dynamic language [52]. However, Typed Racket also has a monolithic semantics – defining new semantic structures requires directly modifying the language.

Language-external mechanisms for creating and combining language dialects, e.g. extensible compilers like Xoc [12], JastAdd [18], Polyglot [38], JaCo [57], Silver [54] and various "language workbenches" [20], suffer from the possibility of ambiguity. In particular, combining different dialects can cause the syntax or semantics to become ambiguous, even if the dialects in isolation are unambiguous. The problem is fundamentally that systems like these allow extension/dialect providers to introduce new concrete and abstract syntactic forms. Our insight is that we can sidestep the difficulties inherent in doing so by instead repurposing a fixed syntax.

Proof assistants, e.g. TinkerType [33], PLT Redex [21], Agda [37] and Coq [36] can be used to inductively specify and mechanize the metatheory of languages. These tools generally require a complete specification (this has been identified as a key challenge [6].) Techniques for composing specifications and proofs exist [14, 15, 46], relying on various algebraic methods to encode "open" term encodings (e.g. Mendler-style *f*-algebras [15]), but these techniques require additional proofs at "combine-time". Several authors, e.g.

Chlipala [11], have suggested proof automation as a heuristic solution to the problem of combine-time proof obligations. The typy fragment system does not operate on inductive semantic specifications – instead, fragment providers directly implement their intended semantics in Python. Python is a complex dynamic language, so it is difficult to formally verify that fragments are correct and do not explicitly interfere with one another (though a formal specification of a substantial subset of Python does exist [43].) In future work, we plan to design a fragment system where the fragment definition language is dependently typed. This would make it possible to prove interesting properties about fragments, e.g. correctness with respect to an inductive specification. A complementary approach would be to automate the generation of fragment definitions and the accompanying proofs from inductive specifications, building on the techniques developed by the Veritas project [24].

Refinement type systems [22], pluggable type systems [5, 8, 9, 34] and gradual type system [47, 48] define additional static checks for programs written against an existing semantics. Some of these systems support fragmentary definitions of new analyses [9, 34]. typy is different in that its semantics (static and dynamic) is itself programmable. In other words, typy is not a gradual type system for Python (like mypy [31]), but rather a distinct language that 1) repurposes Python's syntax; and 2) is defined by typed translation to Python. We have implemented an interface to Python using our fragment system (i.e. the py fragment.) Calling into typy from Python, however, is only possible by defining a typy function. Luckily, typy is itself embedded into Python as a library, rather than a separate compiler, so this is straightforward. Defining a fragmentary refinement system that sits atop our fragmentary semantics is an interesting avenue for future work. This might allow us to use mypy's annotations as refinements of the py type.

Lightweight modular staging (LMS) is a Scala library that supports staged translation of well-typed Scala terms to other targets [45]. In contrast, typy's type system is itself programmable. No specific type structure is built in to typy. As we discussed in Sec. 3, typy can be used to implement and even extend low-level foreign languages in a staged manner. We plan to further explore this approach in future work.

Macros implement local term rewritings [10, 27]. Our fragment system is similar in that translation methods programmatically generate term representations, but the translation target is a different language – Python – from the source language – typy (they happen to share a syntactic representation, but are governed by different semantics.) In fact, macros can be implemented using our fragment system (by defining a singleton type for the macro for which the call operation, which is a targeted form, constructs the rewriting and then asks the context to typecheck and translate it.)

Operator overloading [53] and metaobject dispatch [29] are protocols that rewrite operator invocations into method

calls. The method is typically selected according to either the type or the dynamic tag or value of one or more operands. These protocols share the notion of *inversion of control* with our strategy for targeted expressions, described in Sec. 2.3.4. However, our strategy is a *compile-time* protocol and gives control over typing and translation. An object system with support for operator overloading could be implemented using our fragment system.

#### 5. Discussion

In summary, typy is a bidirectionally typed programming language with no primitive types. Instead, it is organized around a novel semantic fragment system that allows library providers to implement the kinding semantics for new types, the static and dynamic semantics of their associated operations and the pattern matching semantics of their associated patterns programmatically. Library clients can import these fragments in any combination because fragments are contextually delegated control over non-overlapping sets of expressions in a deterministic and stable manner. Unlike other language extension systems, the syntax of the language is fixed, which we take to be a feature of our system because it eliminates a number of difficult problems related to composition. We were able to implement typy itself as a Python library, using Python's standard reflection and code generation facilities.

Our design does have its limitations. As discussed in the previous section, Python is a complex dynamic language, so we cannot rigorously prove interesting metatheorems about our system, nor can fragment providers rigorously prove interesting metatheorems about their fragments. This is comparable to the situation of many programming languages for which "the compiler is the specification", but it is nevertheless ultimately unsatisfactory. In the future, we hope to develop a dialect of typy using a reduced subset of Python (e.g. RPython [4] or some variant thereof) for which a complete formal definition is available. A related line of future work is to allow new fragments to be written using typy itself, rather than Python.

The fragment system that we have developed here could be adapted to use a different surface syntax and internal language without major difficulty. If the internal language itself has non-trivial type structure, e.g. JVM bytecode, then fragments must define a type translation method (to complement the type validation method.) Moreover, term translations must be validated against the corresponding type translations. This form of translation validation has been studied in the design of the TIL compiler for Standard ML [51].

Another aspect of translation validation that we did not consider here is *hygiene*, i.e. that the translations do not make inappropriate assumptions about the surrounding bindings, or inadvertently shadow bindings in an unexpected manner [3, 30]. A proper hygiene mechanism would require that we use an internal language with a more restricted binding

structure than Python. For now, the context simply provides the standard tool to fragment providers: a mechanism for generating unique identifiers.

By repurposing Python's syntax, typy is able to benefit from many well-developed Python tools. Debuggers and other tools that rely not just on Python's syntax but also its semantics do not work directly with typy. It is likely that there is interesting work to be done on enabling fragments to extend the workings of a tool like a debugger.

typy imposes a bidirectional structure on all fragments. This structure is known to be highly flexible [17], and even advanced dependently typed languages like Agda are fundamentally bidirectional [37]. That said, we have not explored the practicality of implementing more advanced type systems, e.g. dependent or linear type systems, using our fragment system. Type systems that require tracking specialized contextual information are possible using our framework, but the corresponding attribute of the context needs to be initialized on first use of a type that needs it. This is somewhat awkward, so we plan to include a mechanism that allows imported fragments to initialize the context ahead of typechecking. It would not be straightforward to implement type systems that are not bidirectional, e.g. those that rely on non-local type inference or flow typing [1].

We have experimented with various extensions of typy that we did not have space to describe here. In particular, we have added a notion of fragmentary implicit coercion to typy (which generalizes subtyping [50].) We have also experimented with a system where literal forms can be annotated with *incomplete types*, i.e. types where the type index contains an ellipsis. For example, rather than stating all of the element types in the tuple below, we simply state that it is a tpl. The tpl fragment synthesizes the complete index:

Finally, it may be wise to acknowledge that not all fragments will be tasteful. Indeed, some language designers worry that offering too much flexibility to users leads to abuse. This concern must be balanced with the possibilities of a vibrant ecosystem of competing fragments that can be developed and deployed as libraries, and thus more easily evaluated in the wild. We plan to curate a substantial standard library of fragments, so that different programmers do not reimplement the same structures. With an appropriate community process, our position is that a fragmentary language like typy will lead to faster adoption of ideas from the research community, and make it easier to abandon mistakes.

# **Implementation**

At the time of submission, we have implemented all of the mechanisms and fragments described in this paper, though many of these fragments were developed against previous versions of typy, which had a slightly different API. We plan to update these and release typy and its standard library as a free open source project before the conference.

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# A. Support for Python 2.x

# B. Type Equivalence

Although not necessary in the examples in this paper, fragments can compare type expressions for equivalence [49]. Two types in canonical form are equivalent if they arise from the same fragment and have equivalent index values (as determined by Python's == operator, which can be overloaded to introduce interesting equivalences.) For example, we can freely reorder the fields in the definition of Account because Python dictionaries are not order-preserving.

refer to this somewhere

# C. OCaml Example

**Listing 9** An OCaml module analagous to the component defined in Listing 7.

```
1 module Listing7 =
2 struct
    type 'a tree =
4
    | Empty
   | Node of 'a tree * 'a tree
    | Leaf of 'a
6
    let map (f : 'a -> b,
8
             tree : 'a tree) : 'b tree =
9
10
      match tree with
11
      | Empty -> Empty
12
      | Node(left, right) ->
          Node(map(f, left), map(f, right))
13
14
      | Leaf(x) -> Leaf(f(x))
15 end
```