Modularly Metaprogrammable Syntax and Type Structure (Thesis Proposal)

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Abstract

Functional programming languages like ML descend conceptually from simple lambda calculi, but to be pragmatic, must expose a syntax and type structure to programmers of a decidedly more elaborate design. The design space at this level is large, as evidenced by the diverse array of dialects that continue to proliferate around all major languages. But language dialects cannot, in general, be modularly composed, limiting the choices available to programmers. We propose a new language, Verse, designed to decrease the need for dialects by giving library providers the ability to safely and modularly express new derived concrete syntax and external type structure of a variety of designs atop a minimal typed lambda calculus called the Verse *internal language*.

1 Motivation

Functional programming languages like Standard ML (SML) and Haskell descend directly from mathematically elegant typed lambda calculi, diverging mainly in that they present a more pragmatic concrete syntax and type structure to programmers. In other words, their design considers important human factors in addition to fundamental metatheoretic issues. For example, they build in record types, generalizing the nullary and binary product types more common in simpler calculi, because labels are cognitively useful. Similarly, they build in derived concrete syntax for the list datatype.

Ideally, transitioning from a minimal calculus to a pragmatic programming language would require introducing only a limited number of primitive "embellishments" like this. The community around the language would then be able to redirect its efforts exclusively toward the development of a wide variety of useful libraries. Alas, a language design that achieves this ideal has proven elusive, as evidenced by the diverse array of dialects that continue to proliferate around all major languages, functional languages included. In fact, tools for constructing new "domain-specific" dialects seem only to be increasingly popular. This calls for an investigation: why is it that well-informed programmers and researchers are so often unsatisfied with expressing the constructs that they need in libraries, as modes of use of the "general-purpose" functional primitives already available today?

Perhaps the most common reason may simply be that the *syntactic cost* of expressing a construct of interest using contemporary general-purpose primitives is not always ideal. For example, we will consider regular expression patterns expressed using abstract data types (in ML, a mode of use of the module system) in Section 4. This will give us precisely the semantics that we seek to express, but syntactically, the usual approach of using strings to introduce patterns actually leaves much to be desired. In response, we may be tempted to construct a *derived syntactic dialect*, i.e. a dialect specified by context-free elaboration to the existing language, that introduces derived syntax specific to our library, just as languages like SML have introduced derived syntax for constructs in the standard library,

like lists. This is not at all an isolated example. For example, Ur/Web is a derived syntactic dialect of Ur (itself descended from ML) that builds in derived syntax for SQL queries, HTML elements and other datatypes common in web programming [6]. Tools like Camlp4 [18] and Sugar* [7, 8] (which we will return to later) are designed to lower the engineering costs of constructing such dialects, contributing to their proliferation.

More advanced dialects introduce new type structure, going beyond what is possible by context-free elaboration to the existing language. For example, as mentioned above, Standard ML goes beyond the nullary and binary product types found in simpler calculi, instead exposing record types. Other dialects have explored "record-like" primitives that support functional update and extension operators, width and depth coercions (sometimes implicit), mutable rows, methods, prototypic dispatch and various other embellishments. Ocaml builds in a sophisticated object system, polymorphic variants and conveniences like logic for typechecking operations that use format strings, e.g. sprintf [18]. ReactiveML builds in primitives for functional reactive programming [20]. ML5 builds in primitives for distributed programming [22]. Manticore builds in parallel arrays [9]. Alice ML builds in futures and promises [28]. MLj builds in essentially the entire Java programming language, to support typesafe interoperation with existing Java programs [3]. Indeed, perusal of the proceedings of any major programming languages conference will typically yield several more examples. Tools like proof assistants and logical frameworks support specifying and reasoning metatheoretically about dialects like these, and tools like compiler generators and language workbenches lower their implementation cost, again contributing to their continued proliferation.

The reason why this proliferation of language dialects should be considered alarming is that it is, in an important sense, anti-modular: a program written in one dialect cannot, in general, safely and idiomatically interface with libraries written in a different dialect. To do so would fundamentally require combining the two dialects into a single language. Left unconstrained, this is an ill-posed problem, i.e. given two dialects that are specified by judgements of arbitrary form, it is not clear what it would even mean to combine them. Even when the dialects are specified using some formalism that does provide a means to naïvely combine two dialects, there is generally no guarantee that the composition will conserve important syntactic and semantic properties. For example, consider two derived syntactic dialects, one building in derived syntax for JSON (a popular data interchange format), the other using a similar syntax for finite mappings of some other type. Though each is known to have an unambiguous concrete syntax in isolation, when their syntax is naïvely combined (e.g. by Camlp4), ambiguities arise. Any putative "combined language" must formally be considered a distinct system for which one must derive all metatheorems of interest anew, guided only informally by those derived for the dialects individually. Due to this paucity of modular reasoning principles, language dialects are not practical artifacts for software development "in the large".

Dialects do have an indirect impact on large-scale software development because the language designers that control comparatively popular languages, like Ocaml and Scala, can be convinced to incorporate ideas from dialects into backwards compatible language revisions. In this this way, these languages have become more general over time. However, this has come at a cost: they have also ballooned in size. And yet, because there appears to be a "long tail" of potentially useful primitives (for derived syntax, our group has gathered initial data speaking to this [23]), primitives that are only situationally useful, or that trigger aesthetic disagreements between different factions of the community, are still often left languishing in "toy" dialects. Recalling the words of Reynolds, which are as relevant today as they were nearly half a century ago [27]:

The recent development of programming languages suggests that the simultaneous achievement of simplicity and generality in language design is a serious unsolved problem.

— John Reynolds (1970)

This leaves the language design community with two possible paths forward if we wish to keep general-purpose languages small and free of ad hoc primitives. One, exemplified (arguably) by SML, is to generally eschew the introduction of new primitives and settle on a set of primitives that sit at a "sweet spot" in the overall language design space, accepting that in some circumstances, this trades away expressive power or leads to high syntactic cost. The other path forward is to continue on in the search for even more general language primitives, i.e. primitives that are so expressive that they permit us to degrade a broad class of existing primitives, including those found in dialects, to modularly composable library constructs, so that they can be evaluated on their individual merits by programmers and used together without the possibility of conflict. Encouragingly, primitives that have this effect on a language do occasionally arise. For example, Ocaml in a recent revision added support for "generalized algebraic data types" (GADTs), based on research on guarded recursive datatype constructors [33]. Using GADTs, Ocaml was able to move some of the machinery for typechecking operations that use format strings, like sprintf, out of the language and into the standard library (unfortunately, some machinery remains built in). Our broad aim is to introduce a new functional programming language called Verse that takes even more dramatic steps down this second path.

2 Proposed Contributions

Verse has a module system taken directly from SML, but its core language is organized in a novel manner around a minimal typed lambda calculus, called the Verse *internal language*, discussed in Section 3. In lieu of typical external (i.e. programmer-facing) derived syntax and type structure, Verse introduces two novel primitive constructs:

- Typed syntax macros (TSMs), which we introduce in Section 4, subsume the need
 for derived syntax specific to library constructs, e.g. list syntax as built in to SML, by
 giving library providers static control over the parsing and elaboration of delimited
 segments of concrete syntax.
- **Metamodules**, which we introduce in Section 5, give library providers static hooks directly into the type-directed translation protocol that governs the Verse external language. For example, library providers will be able to define a metamodule that introduces extensible labeled product types and their associated operators, defining their semantics by type-directed translation to the internal language, which builds in only nullary and binary product types.

Both TSMs and metamodules can be understood as *metaprogramming* primitives, because they involve static code generation.

The key challenge in the design of these primitives will come in ensuring that they are metatheoretically well-behaved, given that they aim to give library providers decentralized control over aspects of the language that have typically been under the monolithic control of the language designer. If we are not careful, many of the problems discussed earlier as inherent to combining distinct language dialects could simply manifest themselves in the semantics of these primitives.² Our main technical contributions will come in showing how to address these problems in a principled manner. In particular, syntactic conflicts will be impossible by construction and we will validate the code statically generated by TSMs and metamodules to maintain a hygienic type discipline and, most uniquely, powerful modular reasoning principles. In other words, library providers will have the ability to

¹We distinguish Verse from Wyvern, which is the language referred to in prior publications about some of the work being proposed here, because Wyvern is a group effort evolving independently in some important ways.

²This is why languages like Verse are often called *extensible languages*, though this is somewhat of a misnomer. The chief characteristic of an extensible language is that it *doesn't* need to be extended in situations where other languages would need to be extended. We will avoid this somewhat confusing terminology.

reason about the constructs that they have defined in isolation, and library clients will be able to use them safely in any combination, without the possibility of conflict.³

2.1 **Thesis Statement**

In summary, we propose a thesis defending the following statement:

A functional programming language can give library providers the ability to metaprogrammatically express new derived syntax and external type structure atop a minimal typed internal language while maintaining a hygienic type discipline and modular reasoning principles.

2.2 **Disclaimers**

Before we continue, it may be useful to explicitly acknowledge that completely eliminating the need for dialects would indeed be asking for too much: certain design decisions are fundamentally incompatible with others or require coordination across a language design. We aim only to decrease the need for dialects.

It may also be useful to explicitly acknowledge that library providers could leverage the primitives we introduce to define constructs that are in rather poor taste. We expect that in practice, Verse will come with a standard library defining a carefully curated collection of standard constructs, as well as guidelines for advanced users regarding when it would be sensible to use the mechanisms we introduce (following the example of languages that support operator overloading or typeclasses, which also have the potential for "abuse").

Finally, we are not interested here in languages that feature full-spectrum dependent types, which blur the phase separation between compile-time and run-time, though we conjecture that the primitives we introduce could be introduced into languages like Gallina (the "external language" of the Coq proof assistant) with some modifications. Verse should be compared to languages that maintain a phase separation, like ML, Haskell and Scala.

Summary of Judgements 3

To situate ourselves within a formal framework, let us begin with a brief summary of how Verse is organized and specified. Verse consists of a module language atop a core language. The module language is based directly on SML's module language, which we assume working familiarity with for the purposes of this proposal [13, 19]. We will give examples of its use in both Section 4 and Section 5, but do not plan to specify it in detail in the thesis.

The core language is organized much like the first stage of a type-directed compiler (e.g. the TIL compiler for Standard ML [31]), consisting of a user-facing typed external language (EL) specified by type-directed translation to a minimal typed internal language (IL).⁴ The main judgements in the specification of the EL take the following form (omitting various contexts for now):

Judgement Form Pronunciation

 $\vdash e \Rightarrow \sigma \leadsto \iota$ Expression *e* synthesizes type σ and has translation ι . $\vdash e \Leftarrow \sigma \leadsto \iota$ Expression e analyzes against type σ and has translation ι . $\vdash \sigma \text{ type} \leadsto \tau$ Static expression σ is a type with translation τ .

Note that the expression typing judgements are bidirectional, i.e. we make a judgemental distinction between type synthesis (the type is an "output") and type analysis (the type is an "input") [26]. This is to allow us to explicitly specify how Verse's local type inference works,

reminder that we are not going to re-specify the module system

³We assume that simple naming conflicts can be avoided extrinsically, e.g. by using a URI-based naming scheme as in the Java ecosystem.

⁴Note that we will use the terms "expression" and "type" without qualification to refer to external expressions and types, respectively.

and in particular, how it interacts with the primitives that we aim to introduce. Like Scala, we intentionally do not attempt to support global type inference, primarily because it is not technically possible to do so (but also because we believe that compilers for languages that support only local type inference generate clearer error messages).

Our design is largely insensitive to the details of the internal language – the only strict requirements are that the IL be type safe and support parametric type abstraction. For our purposes, we will keep things simple by using the strictly evaluated polymorphic lambda calculus with nullary and binary product and sum types and recursive types, which we assume the reader has familiarity with and for which all the necessary metatheorems are well-established (we follow [14]). The main judgements in the static semantics of the IL (again omitting contexts for now) take the following essentially standard form:

Judgement Form Pronunciation

 $\vdash \iota : \tau$ Internal expression ι has internal type τ .

 $\vdash \tau$ itype Internal type τ is valid.

The dynamic semantics can be specified also in the standard manner as a transition system with judgements of the following form:

Judgement Form Pronunciation

 $\iota \mapsto \iota'$ Internal expression ι transitions to ι' . ι val Internal expression ι is a value.

The iterated transition judgement $\iota \mapsto^* \iota'$ is the reflexive, transitive closure of the transition judgement, and the evaluation judgement $\iota \Downarrow \iota'$ is derivable iff $\iota \mapsto^* \iota'$ and ι' val.

Features like state, exceptions, simple concurrency primitives, scalars, arrays and others characteristic of a first-stage compiler intermediate language would also be included in the IL in practice, and in some cases this would affect the shape of the internal semantics, but we omit them for simplicity.

4 Modularly Metaprogrammable Textual Syntax

Verse, like most major contemporary programming languages, specifies a textual concrete syntax. We have chosen to specify a layout-sensitive textual concrete syntax (i.e. newlines and indentation are not ignored). This design choice is not fundamental to our proposed contributions, but it will be useful for cleanly expressing a class of examples that we plan to discuss later. We plan to specify some novel aspects of Verse's concrete syntax with an *Adams grammar* [2] (such a specification for Wyvern, which has a very similar syntax, can be found in [23]), but for the purposes of this proposal, we will simply introduce Verse's concrete syntax by example as we go on.

A programming language's concrete syntax serves as its human-facing user interface, so it is common practice to build in derived forms (colloquially, *syntactic sugar*) that capture common idioms more concisely or naturally. For example, derived list syntax is built in to most dialects of ML, so that instead of having to write Cons(1, Cons(2, Cons(3, Nil))), a programmer can equivalently write [1, 2, 3]. Many languages go further, building in syntax associated with various other types of data, like vectors (SML/NJ), arrays (Ocaml), commands (Haskell), syntax trees (Scala), XML data (Scala, Ur/Web) and SQL queries (F#, Ur/Web).

Rather than privileging particular library constructs with primitive syntactic support, Verse exposes primitives that allow library providers to introduce new derived syntax on their own. To specifically motivate our desire for this level of syntactic control, we begin in Sec. 4.1 with a representative example: regular expression patterns expressed using abstract data types. We show how the usual approach of using strings to introduce patterns is not ideal. We then survey existing alternatives in Sec. 4.2, finding that they involve an unacceptable loss of modularity and other undesirable trade-offs. In Sec. 4.3, we outline

our proposed mechanisms and discuss how they will resolve these issues. We conclude in Sec. 4.4 with a timeline for remaining work.

4.1 Motivating Example: Regular Expression Syntax

Let us begin from the perspective of a regular expression library provider. Recall that regular expressions are a common way to capture patterns in strings [32]. We will assume that the abstract syntax of patterns, p, over strings, s, is specified as below:

```
p := \mathsf{empty} \mid \mathsf{str}(s) \mid \mathsf{seq}(p; p) \mid \mathsf{or}(p; p) \mid \mathsf{star}(p) \mid \mathsf{group}(p)
```

The most direct way to express this abstract syntax is by defining a recursive sum type [14]. Verse supports these as case types, which are analogous to datatypes in ML (we will see how the type structure of case types can in fact be expressed in libraries later):

```
casetype Pattern
  Empty
  Str of string
  Seq of Pattern * Pattern
  Or of Pattern * Pattern
  Star of Pattern
  Group of Pattern
```

However, there are some reasons not to expose this representation of patterns directly to clients. First, such patterns are usually identified up to their reduction to a normal form. For example, $\mathbf{seq}(\mathbf{empty}, p)$ has normal form p. It might be useful for patterns with the same normal form to be indistinguishable from the perspective of client code. Second, it can be useful for performance reasons to maintain additional data alongside patterns (e.g. a corresponding finite automata) without exposing this "implementation detail" to clients. Indeed, there may be many ways to represent regular expression patterns, each with different performance trade-offs. For these reasons, a better approach is to use *abstract data types*, which in Verse, as in ML, are a mode of use of the module system. In particular, we can define the following *module signature*, where the type of patterns, t, is held abstract. The client of any module P: PATTERN can then identify patterns as terms of type P. t.

```
signature PATTERN
```

```
type t
val Empty : t
val Str : string -> t
val Seq : t * t -> t
val Or : t * t -> t
val Group : t -> t
val case : (
    'a ->
    (string -> 'a) ->
    (t * t -> 'a) ->
    (t * t -> 'a) ->
    (t -> 'a) ->
    (a)
```

By holding the representation type of patterns abstract, the burden of proving that the case analysis function above cannot be used to distinguish patterns with the same normal form is localized to each module implementing this signature. The details are standard and not particularly interesting given our purposes, so we omit them.

Concrete Syntax The abstract syntax of patterns is too verbose to be used directly in all but the most trivial examples, so patterns are conventionally written using a more concise concrete syntax. For example, the concrete syntax A|T|G|C corresponds to abstract syntax with the following much more verbose expression:

```
P.Or(P.Str "A", P.Or(P.Str "T", P.Or(P.Str "G", P.Str "C")))
```

To express the concrete syntax of patterns, regular expression library providers usually provide a utility function that transforms strings to patterns. Because, as just mentioned, there may be many implementations of the PATTERN signature, the standard approach is to define a *parameterized module* (a.k.a. *functor* in SML) defining utility functions generically:

```
module PatternUtil(P : PATTERN)
fun parse(s : string) : P.t
    (* ... pattern parser here ... *)
```

This allows the client of any module P: PATTERN to use the following definitions:

```
module PU = PatternUtil(P)
let pattern = PU.parse
to construct patterns like this:
```

```
pattern "A|T|G|C"
```

Unfortunately, this approach is imperfect for several reasons:

1. First, there are syntactic conflicts between string escape sequences and pattern escape sequences. For example, the following is not a well-formed term:

```
let ssn = pattern "\d\d\-\d\d\d\d"
```

When compiling an expression like this, the programmer would see an error message like error: illegal escape character.⁵ In a small lab study, we observed that this sort of error was common, and that solving the problem was nearly always initially challenging to even experienced programmers who hadn't used regular expressions recently [25]. The inelegant workaround is to double backslashes:

```
let ssn = pattern "\d\d\d-\d\d\d'
```

Some languages, anticipating such modes of use, build in alternative string forms that leave escape sequences uninterpretted. For example, Ocaml allows the following, which is perhaps more acceptable:

```
let ssn = pattern \{rx | \frac{d}{d} - \frac{d}{d} \}
```

2. The next problem is that pattern parsing does not occur until the pattern is evaluated at run-time. For example, the following malformed pattern will only trigger an error when this expression is evaluated during the full moon:

```
case moon_phase
Full => pattern "(GC" (* malformedness not statically detected *)
_ => (* ... *)
```

Such issues can sometimes be found via testing, but empirical data gathered from open source projects suggests that there remain many malformed regular expression patterns that are not detected by a project's test suite "in the wild" [30].

We might instead attempt to treat the well-formedness of patterns constructed from strings as a static verification condition. Statically proving that this condition holds throughout a program is wildly difficult to automate in general, because it involves reasoning about arbitrary dynamic behavior. In the example above, we must know that the variable pattern is equivalent to the function PU.pattern. Moreover, if the argument were not written literally, e.g. we had written strconcat "(G" "C", we would need to be able to establish that this is equivalent to the string above. It is simple to come up with arbitrarily more complex examples that thwart any putative decision procedure, particularly for patterns that are dynamically constructed based on input to the program (further discussed below).

⁵This is the error message that javac produces. When compiling an analagous expression using SML of New Jersey (SML/NJ), we encounter the rather bizarre error message Error: unclosed string.

Parsing patterns at run-time also incurs a performance penalty. To avoid incurring it every time the pattern is encountered (e.g. for each item in a very large dataset), one must be careful to stage the computation appropriately, or use an appropriately tuned caching strategy.

3. The final problem is that using strings to construct patterns encourages programmers to use operations over strings, like concatenation, to construct patterns derived from user input that happens also to be of type string. This can lead to subtle but serious bugs. For example, consider the following function:

```
fun example_bad(name : string)
  pattern (name ^ ": \\d\\d\\d-\\d\\d\\d\\d\\d")
```

The (unstated) intent here is to treat name as a sub-pattern matching only itself, but this is not the observed behavior when name contains special characters that have other meanings in patterns. The correct code again resembles abstract syntax:

```
fun example_fixed(name : string)
  P.Seq(P.Str(name), P.Seq(pattern ": ", ssn)) (* ssn as above *)
```

Note that both functions have the same type and behave identically at many inputs, particularly those that would be expected during typical executions of the program (i.e. alphabetic names), so testing can miss the problem. Proving that such problems cannot arise involves reasoning about complex run-time data flows, so it is once again difficult to automate. In applications that query sensitive data, mistakes like this lead to *injection attacks*, which are both common and catastrophic from the perspective of software security [1].

4.2 Existing Approaches

The difficulties above are common whenever one uses strings transiently to construct more richly structured data, merely for the sake of syntactic convenience. This key observation has motivated a substantial quantity of research on reducing the need for run-time string parsing [4]. Existing approaches can be classified in one of two ways: as being based on *syntax extension* or *static term rewriting*.

4.2.1 Syntax Extension

One approach to address the problems above would be to leverage a system that allows us to directly extend the syntax of our language with new derived syntactic forms.

The simplest such systems are those where each new syntactic form is described by a single rewrite rule. For example, Gallina, the external language of the Coq proof assistant, provides such a system [21]. A formal account of systems like these has been developed by Griffin [12]. Unfortunately, these systems are not flexible enough to allow us to express pattern syntax in the conventional manner. For example, sequences of characters can only be parsed as identifiers using these systems, rather than as characters in a pattern. Syntax extension systems based on context-free grammars like Sugar* [8], Camlp4 [18] and many others are more expressive, however, and thus would allow us to directly introduce pattern syntax into our core language's grammar, perhaps like this:

```
let ssn = /\d\d-\d\d\d
```

However, this is a rather perilous approach because none of these systems guarantee freedom from *syntactic conflicts*, i.e. as the Coq manual states: "mixing different symbolic notations in [the] same text may cause serious parsing ambiguity". So if another library provider used similar syntax for a different implementation of regular expressions, or for some other unrelated abstraction, then a client could not simultaneously use both libraries in the same scope. Properly considered, every combination of extensions introduced by one of these mechanisms creates a *de facto* derived syntactic dialect of our language.

In response to this problem, Schwerdfeger and Van Wyk developed a modular analysis that accepts only grammar extensions that specify a universally unique starting token and obey subtle constraints on the follow sets of base language non-terminals [29]. Extensions that satisfy these criteria can be used together in any combination without the possibility of conflict. However, note that the most natural starting tokens like pattern cannot be guaranteed to be universally unique, so we would be forced to use a more verbose token like edu_cmu_verse_rx_pattern. There is no principled way for clients of our extension to define local abbreviations for starting tokens because this mechanism is language-external.

Putting this issue aside, we must now decide how our newly introduced derived forms elaborate to forms in our base grammar. This is tricky because we have defined a modular encoding of patterns – which particular module should the elaboration logic use? Clearly, simply assuming that some module identified as P satisying PATTERN is in scope is a brittle solution. Indeed, we should expect that the extension mechanism actively prevents such capture of specific variable names to ensure that variables (including module variables) can be freely renamed. Such a *hygiene discipline* is well-understood when performing term-to-term rewriting (discussed below) or in simple rewrite systems like those found in Coq. For more flexible mechanisms, the issue is a topic of ongoing research (none of the grammar-based mechanisms described above enforce hygiene).

Putting aside this question of hygiene as well, we can address the problem by requiring that the client explicitly identify the module the elaboration should use:

```
let ssn = edu\_cmu\_verse\_rx\_pattern P /\d\d\d-\d\d-\d\d\d/d
```

For patterns constructed compositionally, we can define *splicing* syntax for both strings and other patterns, e.g. as shown below:

```
fun example_syn(name : string)
  edu_cmu_verse_rx_pattern P /@name: %ssn/
```

Had we mistakenly used the pattern splicing syntax, writing %name, rather than the string splicing syntax, @name, we would get a static type error, rather than the silent injection vulnerability that we discussed earlier.

A general problem with approaches like these (in addition to those already mentioned) is that they suffer from a paucity of direct reasoning principles – given an unfamiliar piece of syntax, there is no simple method for determining what type it will have, or even for identifying which extension determines its elaboration, causing difficulties for both humans (related to code comprehension) and tools.

4.2.2 Static Term Rewriting

An alternative approach is to leave the concrete syntax of the language fixed, but repurpose it for novel ends using a *local term-rewriting system*. Among the earliest examples is the LISP macro system [15], later modified, notably in the Scheme language, to support reasoning hygienically about the rewriting that is performed [17]. In languages with a stronger static type discipline, variations on macros that restrict rewriting to a particular type and perform the rewriting in an explicitly staged manner have also been studied [16, 11] and integrated into languages, e.g. MacroML [11] and Scala [5].

The most immediate problem with using these in our example is that we are not aware of any such statically-typed macro system that integrates cleanly with an ML-style module system. However, let us imagine a macro system that would allow us to repurpose string syntax as follows:

```
let ssn = pattern P \{rx | \frac{d}{d} - \frac{d}{d} \}
```

Here, pattern is a macro parameterized by a module P: PATTERN. It statically parses the provided string literal (which must still be written using an Ocaml-style literal here) to generate an elaboration, specified by the macro to be at type P.t.

For patterns that are constructed compositionally, we need to get more creative. For example, we might repurpose the infix operators that the language normally uses for other purposes to support string and pattern splicing as follows:

```
fun example_macro(name : string)
  pattern P (name ^ ": " + ssn)
```

While this does not leave us with syntax that is quite as clean as would be possible with a naïve syntax extension, it does address many of the problems we discussed above: there cannot be syntactic conflicts (because the syntax is not extended), we can define macro abbreviations because macros are integrated into the language, there is a hygiene discipline that guarantees that the elaboration will not capture variables inadvertently, and by using a typed macro system, there is a typing discipline (i.e. creativewe need not examine the elaboration directly to know what type it must have).

4.3 Contributions

We propose a new primitive, the **typed syntax macro** (TSM), that combines the flexibility of syntax extensions with the reasoning guarantees of statically-typed macros, and show how to integrate it into a language with an ML-style module system, addressing all of the problems described thusfar. We then introduce **type-specific languages** (TSLs), which leverage local type inference to control TSM dispatch, further decreasing syntactic cost (which is, of course, the entire purpose of this exercise). The result is that derived syntax defined by library providers using TSMs and TSLs approaches the cost of derived syntax built in primitively by a language designer (using a naïve tool like Camlp4).

4.3.1 Typed Syntax Macros (TSMs)

Consider the following concrete external expression:

```
pattern P /A|T|G|C/
```

Here, a parameterized TSM, pattern, is applied to a module parameter, P, and a delimited form, /A|T|G|C/. The TSM statically parses the body of the provided delimited form, i.e. the characters between the delimiters (shown here in blue), and computes an elaboration, i.e. another external expression. In this case, it is as if we wrote the following directly:

```
P.Or(P.Str "A", P.Or(P.Str "T", P.Or(P.Str "G", P.Str "C")))
The definition of pattern is shown below:
syntax pattern(P : PATTERN) at P.t
  fn (ps : ParseStream) => (* pattern parser here *)
```

Note that identifying the module parameter as P here is unimportant, i.e. the TSM can be used with *any* module matching signature PATTERN. The module parameter is bound in the scope of the type clause **at** P.t. This clause specifies that all elaborations successfully generated by this TSM will be of type P.t. Elaborations are generated by the static action of the parse function defined in the indented block on the next line. The parse function must be of type ParseStream -> Exp, where the type ParseStream gives the function access to the body of the delimited form (in blue above) and the type Exp is a case type that encodes the abstract syntax of the base language (i.e. the Verse EL). Both types are defined in the Verse *prelude*, which is a set of definitions available ambiently.

For concision in analytic positions, i.e. those where an expected type is known due to, for example, a type ascription, the module parameter P can be inferred:

```
let N : P.t = pattern /A|T|G|C/
```

TSMs can be partially applied and abbreviated using a let-binding style mechanism:

TSMs can identify portions of the body of the delimited form that should be treated as spliced expressions, allowing us to support splicing syntax as described in Sec. 4.2.1:

```
fun example_tsm(name: string)
  pat /@name: %ssn/
```

The hygiene mechanism ensures that only those portions of the elaboration derived from such spliced expressions can refer to variables at the site of use, preventing inadvertent variable capture by the elaboration. Put another way, the generated elaboration must be context-independent.

Formalization To give a flavor of the formal specification underlying TSMs, let us look at the rule for handling TSM invocation in a synthetic position:

$$\begin{split} & (\text{syn-aptsm}) \\ & \Delta \vdash s \circledcirc \sigma \left\{ \iota_{\text{parser}} \right\} \quad \underset{}{\textbf{parsestream}} (body) = \iota_{\text{ps}} \quad \iota_{\text{parser}} (\iota_{\text{ps}}) \Downarrow \iota_{\text{elab}} \quad \iota_{\text{elab}} \uparrow e_{\text{elab}} \\ & \Delta; \Gamma; \emptyset; \emptyset \vdash e_{\text{elab}} \Leftarrow \sigma \leadsto \iota \\ & \Delta_{\text{out}}; \Gamma_{\text{out}}; \Delta; \Gamma \vdash \text{invoketsm}(s; body) \Rightarrow \sigma \leadsto \iota \end{split}$$

Note that the judgement forms are slightly simplified here, e.g. they omit various contexts relevant only to other Verse primitives. We include only *typing contexts*, Γ , which map variables to types, and *type abstraction contexts*, Δ , which track universally quantified type variables (both in the standard way). The premises have the following meanings:

- 1. The first premise can be pronounced "Under Δ , TSM expression s is a TSM at type σ with parser ι_{parser} ". We elide the details of issues like module parameter application here for simplicity.
- 2. The second premise creates a parse stream, ι_{ps} , from the body of the delimited form.
- 3. The third premise applies the parser to the parse stream to generate an encoding of the elaboration, ι_{elab} .
- 4. The fourth premise decodes ι_{elab} , producing the elaboration e_{elab} .
- 5. The fifth premise validates the elaboration by analyzing it against the type σ under empty contexts. The *current* typing and type abstraction contexts are "saved" for use when a spliced term is encountered during this process by setting them as the new *outer contexts*.

Variables in the outer contexts cannot be used directly by the elaboration, e.g. they are ignored by the (syn-var) rule:

$$\frac{\text{(syn-var)}}{\Delta_{\text{out}}; \Gamma_{\text{out}}; \Delta; \Gamma, x : \sigma \vdash x \Rightarrow \sigma \leadsto x}$$

The outer contexts are switched back in only when encountering a spliced expression, which is marked:

$$(\text{syn-spliced}) \\ \underline{\emptyset; \emptyset; \Delta_{\text{out}}; \Gamma_{\text{out}} \vdash e \Rightarrow \sigma \leadsto \iota} \\ \underline{\Delta_{\text{out}}; \Gamma_{\text{out}}; \Delta; \Gamma \vdash \mathbf{spliced}(e) \Rightarrow \sigma \leadsto \iota} \\ \underline{(\text{ana-spliced})} \\ \underline{\emptyset; \emptyset; \Delta_{\text{out}}; \Gamma_{\text{out}} \vdash e \Leftarrow \sigma \leadsto \iota} \\ \underline{\Delta_{\text{out}}; \Gamma_{\text{out}}; \Delta; \Gamma \vdash \mathbf{spliced}(e) \Leftarrow \sigma \leadsto \iota}$$

For example, the elaboration generated in example_tsm above would, if written concretely, be:

```
P.Seq(P.Str(spliced(name)), P.Seq(P.Str ": ", spliced(ssn)))
```

4.3.2 Type-Specific Languages (TSLs)

To further lower the syntactic cost of using TSMs, Verse also supports *type-specific languages* (TSLs), which allow library providers to associate a TSM directly with a declared type. For example, a module P can associate pattern with P.t as follows:

```
module P : PATTERN with syntax pattern at t
type t = (* ... *)
(* ... *)
```

Local type inference then determines which TSM is applied when analyzing a delimited form not prefixed by a TSM name. For example, this is equivalent to example_tsm:

```
fun example_tsl(name : string) : P.t
    /@name: %ssn/
```

As another example, we can use TSLs to express derived list syntax. For example, if we use a case type, we can declare the TSL directly upon declaration as follows:

```
casetype list('a) {
  Nil
  Cons of 'a * list('a)
} with syntax
  fn (body : ParseStream) => (* ... comma-delimited spliced exps ... *)
```

Together, this allows us to write a list of patterns like this:

```
let x : list(P.t) = [/\d/, /\d\d/, /\d\d/]
```

From the client's perspective, it is essentially as if the language had built in derived syntax for lists and regular expression patterns directly.

4.4 Timeline

We have described and given a more detailed formal specification of TSMs in a recently published paper [24], and TSLs in a paper last year [23], both in the context of the Wyvern language. At the time of publication, Wyvern did not specify a module system, so in the context of Verse, there are some changes that need to be made in the formalization to handle module parameters. We plan to complete this in the course of writing the dissertation.

5 Modularly Metaprogrammable Type Structure

Let us now turn our attention to the type structure of the Verse external language (EL). In contrast to other languages, which build in constructs like case types (shown briefly at the beginning of Sec. 4.1), tuples, records, objects and so on primitively, in Verse these can all be expressed as modes of use of *metamodules* (which are distinct from, though conceptually related to, *modules*). In fact, only polymorphic function types are built primitively into the Verse EL.

This section is organized much like Section 4. We begin with examples of type structure that we wish to express in Section 5.1, then discuss how existing approaches are insufficient in Section 5.2. Next, we show how metamodules (together with TSMs and TSLs) serve to address these problems in Section ?? and conclude with a timeline in Section ??.

5.1 Motivating Example: Labeled Tuples and Regular Strings

As a simple introductory example, let us consider a type classifying conference papers:

```
let type Paper = ltuple {
  title : rstring /.+/
  conf : rstring /([A-Z]+) (\d\d\d\d)/
}
```

The **let type** construction defines a synonym, Paper, for a type constructed by applying the *type constructor* (or more concisely, *tycon*) ltuple to an ordered finite mapping from labels to types, delimited here by curly braces. Its first component is labeled title and specifies the regular string type rstring /.*/. Regular string types are constructed by applying the tycon rstring to a regular expression pattern, written literally here. They classify values that behave like strings in the corresponding regular language. So in this case, we have specified that paper titles must be non-empty strings. The second component of our labeled product type is labeled conf and specifies a regular string type with two parenthesized groups, corresponding to the conference abbreviation and year.

We can introduce a value of type Paper in an analytic position in one of two ways. We can omit the labels and provide component values positionally:

```
let exmpl : Paper = {"An Example Paper", "EXMPL 2015"}
```

Alternatively, we can include the component labels explicitly for readability or if we want to give the components in an alternative order:

```
let exmpl : Paper = {conf => "EXMPL 2015", title => "An Example Paper"}
Given a value of type Paper, we can project out a component value by providing a label:
let exmpl_conf = # <conf> exmpl
```

Here, # is an *operator constructor* (or *opcon*) parameterized by a static label, written literally here as <conf>. The resulting *operator*, # <conf>, takes one *argument*, exmpl.

We can also project captured groups out of a regular string using the #group operator constructor, which is parameterized by a natural number referring to the group index:

```
let exmpl_conf_name = #group 0 exmpl_conf
```

Note that the variable exmpl_conf_name has type rstring /[A-Z]+/.

Both labeled tuples and regular strings support a number of other basic operations. For example, labeled tuples can be concatenated (with any common components updated with the value on the right) using the ltuple+ operator:

```
let a : lprodtype {authors : list(rstring /.+/)} = {["Harry Q. Bovik"]}
let exmpl_paper_final = ltuple+ exmpl_paper a
```

We can drop a component using the operator constructor ltuple-, which is parameterized by a static label:

```
let exmpl_paper_anon = ltuple- <authors> exmpl_paper_final
```

5.2 Existing Approaches

5.2.1 Labeled Product Types

Recall that Verse builds in only nullary and binary products into its internal language, so the type structure described above for labeled tuples is not directly expressible using IL primitives. The EL does not build in even these. However, so as to separate concerns, let us assume for the moment that regular string types are available in the EL:

```
(* type synonyms for concision *)
let type title_t = rstring /.+/
let type conf_t = rstring /([A-Z]+) (\d\d\d\d)/
```

Modules One approach we might take is to attempt to express the type structure of any particular labeled tuple type using the module system. For example, we might define the following signature for our example above:

```
signature PAPER
type t
(* introduction without labels *)
val intro : title_t -> conf_t -> t
```

```
(* introduction with explicit labels, in both orders *)
val intro_title_conf : title_t -> conf_t -> t
val intro_conf_title : conf_t -> title_t -> t
(* projection *)
val prj_title : t -> title_t
val prj_conf : t -> conf_t
```

We've simply taken all possible valid introductory and projection operators and expressed them as functions, moving label parameters into identifiers. Even with the minimal EL we are assuming, we could implement this signature using a Church-style encoding. The details are straightforward and omitted. Alternatively, if we only slightly relax slightly our insistence on minimalism and add binary products to the EL, we could use them as well:

```
module Paper : PAPER
type t = title_t * conf_t
fun intro_tpl title conf = (title, conf)
fun intro_title_conf title conf = (title, conf)
fun intro_conf_title conf title = (title, conf)
fun prj_title (title, conf) = title
fun prj_conf (title, conf) = conf

type Paper = Paper.t
```

One problem is that this requires a volume of boilerplate code quadratic in the number of components of our labeled tuple type. It is also not entirely satisfying syntactically from the client's perspective. To avoid these problems and recover the syntax used previously, we could define a TSM for every such signature, though this too involves much boilerplate.

More fundamentally, this encoding is limited to expressing the basic introductory and projection operators. We did not express all possible valid operators that arise from the opcon ltuple- as functions, because to do so, we would need to construct an encoding of every labeled tuple type that might arise from dropping one or more components. This would require an exponential volume of boilerplate code. Finally, there is no way to define ltuple+ as a function or a finite collection of functions, because there are infinitely many extensions of any particular labeled product type.

Records and Tuples If, instead of settling for such a module-based encoding, we further weaken our insistence on minimalism and primitively build in record/tuple types, as SML and many other languages have done, let us consider what might be possible. We note at the outset that records and tuples too are library constructs in Verse, but because they are so commonly built in to other languages, this situation is worth considering.

The simplest approach we might consider taking is to directly map each labeled tuple type to a record type defining the same component mapping:

```
let type Paper_rcd = record {
  title : title_t
  conf : conf_t
}
```

Unlike labeled tuple types, record types are identified only up to component reordering. In other words, this mapping does not preserve certain type disequalities between labeled tuple types. Lacking positional information, it is not possible to omit component labels and rely on positional information when introducing a value of this type.

To work around this limitation if we do not otherwise care about preserving these type disequalities, we would need to define two conversion functions involving tuples:

```
fun Paper_of_tpl (title : title_t, conf : conf_t)
  {title => title, conf => conf}
fun tpl_of_Paper {title => title, conf => conf} = (title, conf)
```

For providers, this has syntactic cost linear in the number of components. For clients, we must explicitly invoke these functions, which incurs both a syntactic and run-time cost.

We could define a TSM for every such type to reduce this cost to clients, though this is an additional cost to providers.

If on the other hand we do care about preserving the type disequality mentioned, the workaround is even less elegant: we first need to define a record type with component labels tagged in some sufficiently unambiguous way by position, e.g.:

```
let type Paper = record {
   __0_title : title_t
   __1_conf : conf_t
}
```

To avoid exposing this directly to clients, we need two auxiliary type definitions:

```
let type Paper_tpl = (title_t * conf_t)
let type Paper_rcd = (* as above *)

and four conversion functions:

fun Paper_of_tpl (title : title_t, conf : conf_t) = {
    __0_title => title,
    __1_conf => conf
}

fun tpl_of_Paper {__0_title => title, __1_conf => conf} = (title, conf)

fun Paper_of_rcd {title => title, conf => conf} = {
    __0_title => title,
    __1_conf => conf
}

fun rcd_of_Paper {__0_title => title, __1_conf => conf} = {
    title => title,
    conf => conf
}
```

Clients again bear the cost of applying these conversion functions ahead of every operation and providers again bear the burden of defining this boilerplate (which is again linear in the number of components, albeit with a constant factor that is again not easy to dismiss).

As with our modular encoding above, neither of these workarounds provides us with any way to uniformly express the more interesting operations, like concatenation, that we discussed earlier.

5.2.2 Regular Strings

Let us now turn to regular string types.

Run-Time Checks The most common alternative to regular strings in existing languages is to instead use standard strings (which themselves may be expressed as lists or vectors of characters together with derived syntax), inserting run-time checks around operations to maintain the regular string invariant dynamically. This clearly does not express the static semantics of regular strings, and incurs syntactic and run-time cost.

Type Refinements We might instead try to express the static semantics of regular strings by using standard strings and moving the logic governing regular string types into an external system of *type refinements* [10]. These systems typically examine refinement specifications supplied in comments:

```
let conf : string (* ~ rstring /([A-Z]+) (\d\d\d\d)/ *) = "EXMPL 2015"
```

One problem with this is that there is no way to express the group projection operator described above. We cannot define a function #group that can be used like this:

```
let conf_venue = #group 0 conf
```

The reason is that this function would need information that is available only in the type refinement of each regular string, i.e. the positions of the captured groups.

A closely related problem is that type refinements do not introduce type disequalities. As a result, compilers cannot use the type refinements to optimize the representation of a value. For example, the fact that some value of type string can be given the refined type rstring /A|B/ cannot be justification to locally alter its representation to, for example, a single bit, both because it could later be passed into a function expecting a standard string and because there are many other possible refinements. For regular strings, there may be limited benefit to controlling representation differentially, but in other situations, this can have significant performance ramifications. For example, it is quite common to justify the omission of a primitive type of "non-negative integers representable in 32 bits" by the fact that this is "merely" a refinement of integers, but in so doing one loses the ability to use a machine representation more suitable to this particular static invariant.

Modules To create type disequalities, we might consider again turning to the module system, defining a signature for each regular string type that we wish to work with. Again, this requires a non-trivial amount of boilerplate code:

```
signature TITLE
  type t
  val intro : string -> t
  val strcase : t -> (unit -> 'a) -> (string * string -> 'a) -> 'a

signature CONF
  type t
  val intro : string -> t
  val strcase : t -> (unit -> 'a) -> (string * string -> 'a) -> 'a
  val prj_group_0 : t -> string
  val prj_group_1 : t -> string
```

To ensure that applications of the introductory operators are correct statically, we would need to couple this with a system of refinement types.

Unfortunately, this again reveals itself to be too limited a solution when we need other operators, e.g. concatenation. Expressing concatenation uniformly using a single function or a finite set of functions is impossible, for the same reason that applied to ltuple+ above, i.e. we would need to define one such function for every pair of possible regular string types (of which there are infinitely many).

5.3 Contributions

Metamodules introduce type and operator constructors parameterized by arbitrary *static* values and metaprogrammatically express the logic governing their typechecking and translation to the IL. Metamodules are classified by *metasignatures*. For example, let us consider the following metasignature:

```
metasignature LTUPLE
     tycon c of LblTyMap
2
     ana opcon intro_unlabeled
3
     ana opcon intro_labeled of LblList
     syn opcon # of Lbl
   syntax ltpl(L ~ LTUPLE, idx : LblTyList) at L.c(idx)
  metamodule LTuple ~ LTUPLE with syntax ltpl for c
8
     tycon c(idx : LblTyList) ~> ...
     ana opcon intro_unlabeled(ty : Ty, args : List(Arg)) ~> ...
10
     ana opcon intro_labeled(lbls : List(Lbl), ty : Ty, args : List(Arg)) ~> ...
11
     syn opcon #(lbl, args) ~> ...
12
  let tycon ltuple = LTuple.c
13
  let opcon # = LTuple.#
```

c is a tycon parameterized by static maps from labels to types. intro unlabeled is a trivially parameterized opcon, i.e. just one operator.

intro labeled is an opcon parameterized by a list of labels. # is an opcon parameterized by a single label. ltpl is a TSM parameterized by a metamodule and a static value LTuple uses ltpl as a TSL

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