# A Type System for String Sanitation Implemented Inside a Python

#### **ABSTRACT**

Security-oriented programming languages do not enjoy wide adoption. Conversely, library and framework-based approaches to security are pervasive. Unfortunately, libraries and frameworks are only effective solutions if they are implemented and used properly. In this paper, we propose that extensible programming languages provide a promising mechanism for increasing the amount of trust that can be place in libraries and frameworks. To demonstrate this approach, we present a conservative extension to the simply-typed lambda calculus for checking the correctness of input sanitation algorithms. We also demonstrate how this language's security guarantees are preserved under translation into an underlying language containing a regular expression library. We believe this approach - complementing existing techniques with light-weight, composable type-based analyses - constitutes a promising compromise between usability, potential for industry adoption, and theoretically grounded safety guarantees.

### 1. INTRODUCTION

Improper input sanitation is a leading cause of security vulnerabilities in web applications [OWASP]. Command injection attacks exploit improper input sanitation by inserting malicious code into an otherwise benign command. Modern web frameworks, libraries, and database abstraction layers attempt to ensure proper sanitation of user input. When these methods are unavailable or insufficient, developers implement custom sanitation techniques. Im both cases, sanitation algorithms are implemented using the language's regular expression capabilities and usually replace potentially unsafe strings with equivalent escaped strings.

In this paper, we present a type system for implementing and statically checking input sanitation techniques. Our solution suggests a more general approach to the integration of security concerns into programming language design. This approach is characterized by *composable* type system extensions which *complement* existing and well-understood

solutions with compile-time checks.

To demonstrate this approach, we present a simply typed lambda calculus with constrained strings; that is, a set of string types parameterized by regular expressions. If s: stringin[r], then s is a string matching the language r. Additionally, we include an operation  $rreplace[r](s_1, s_2)$  which corresponds to the replace mechanism available in most regular expression libraries; that is, any substring of  $s_1$  matching r is replaced with  $s_2$ . The type of this expression is the computed, and is likely "smaller" or more constrained than the type of  $s_1$ . Libraries, frameworks or functions which construct and execute commands containing input can specify a safe subset  $stringin[r_{spec}]$  of strings, and input sanitation algorithms can construct such a string using rreplace or, optionally, by coercion (in which case a runtime check is inserted). We also show how this simple can be translated into a host language containing a regular expression library such that the safety guarantee of the extended language is preserved.

Summarily, we present a simple type system extension which ensures the absence of input sanitation vulnerabilities by statically checking input sanitation algorithms which use an underlying regular expression library. This approach is *composable* in the sense that it is a conservative extension. This approach is also *complementary* to existing input sanitation techniques which use string replacement for input sanitation.

## 1.1 Related Work and Alternative Approaches

The input sanitation problem is well-understood. There exist a large number of techniques and technologies, proposed by both practitioners and researchers, for preventing injection-style attacks. In this section, we explain how our approach to the input sanitation problem differs from each of these approaches. More important than these differences, however, is our more general assertion that language extensibility is a promising approach toward consideration of security goals in programming lanuage design.

Unlike frameworks and libraries provided by languages such as Haskell and Ruby, our type system provides a static guarantee that input is always properly sanitized before use. Doing so requires reasoning about the operations on regular languages corresponding to standard operations on strings; we are unaware of any production system which contains this form of reasoning. Therefore, even where frameworks and libraries provide a viable interface or wrapper around

input sanitation, our approach is complementary because it ensurees the correctness of the framework or library itself. Furthermore, our approach is more general than database abstraction layers because our mechanism is applicable to all forms of command injection (e.g. shell injection or remote file inclusion).

A number of research languages provide static guarantees that a program is free of input sanitation vulnerabilities [Jif][Ur/Web]. Our work differes from these contributions in the ways following:

- Our system is a light-weight solution to a single class of sanitation vulnerabilities (e.g. we do not address Cross-Site Scripting).
- Our system is defined as a library in terms of an extensible type system, as opposed to a stand-alone language. Instead of introducing new technologies and methodologies for addressing security problems, we provide a light-weight static analysis which complements approaches developers already understand well.
- Our implementation of the translation is implemented in Python and shares its grammar. Since Python is a popular programming language among web developers, the barrier between our research and adopted technologies is lower than for greenfield security-oriented languages.

We are also unaware of any extensible programming languages which emphasize applications to security concerns (TRUE?).

Incorporating regular expressions into the type system is not novel. The XDuce system [?] typechecks XML schemas using regular expressions. We differ from this and related work in at least two ways. First, our system is defined within an extensible type system; second, and more importantly, we have demonstrated that regular expression types are applicable to the web security domain.

In conclusion, our system is novel in at least two ways:

- The safety guarantees provided by libraries and frameworks in popular languages are not as (statically) justified as is often belived (or even claimed).
- Our extension is the first major demonstration of how an extensible type system may be used to provide lightweight, composable security analyses based upon idiomatic code.

#### 1.2 Outline

An outline of this paper follows:

 In §2, we define the type system which is embedded in Ace. We include a type safety proof for the string segment of this language and prove the correctness of a translation to an underlying language P. In our theory, P is a simply typed lambda calculus equipped with

- a minimal regular expression library; in an implementation, P stands in for Python or another underlying general-purpose programming language.
- In §3, we discuss our implemention of this translation as a type system extension within the Ace programming language.

# 2. A TYPE SYSTEM FOR STRING SANI-TATION

The  $\lambda_S$  language is characterized by a type of strings indexed by regular expressions, together with operations on such strings which correspond to common input sanitation patterns. This section presents the grammar, typing rules and operational semantics for  $\lambda_S$  as well as an underlying language  $\lambda_P$ .

The system  $\lambda_S$  2 is the simply typed lambda calculus extended with regular expression types, which are string types ensuring a string belongs to a specified language. For instance,  $S: \mathsf{stringin}[r]$  reads "s is a string matching r". the system includes an operation for replacing all instances of a pattern r in a string  $s_1$  with another string  $s_2$ . Input sanitation algorithms – as implemented by developers or within popular libraries and frameworks – are often implemented in terms of this replace operation. For instance, a developer might all potentially unsafe characters with excaped versions of the same character. Regular expression types are used both to specify input sanitation algorithms, and at use sites as specifications. Note that runtime error states (S err) are introduced by coercion, not by replacement.

The language  $\lambda_P$  2 is a simple functional language extended with a minimal regular expression library. Any general purpose programming language could stand in for  $\lambda_P$ ; for instance, SML has a regular expression library. In an implementation, our correctness results are modulo the underlying language's correct implementation of regular expression matching (see P-E-Replace).

Finally, we define a translation from our type system  $\lambda_S$  into  $\lambda_P$ .

$$\mathbf{r} \; ::= \; \epsilon \; | \; . \; | \; a \; | \; r \cdot r \; | \; r + r \; | \; r * \qquad \qquad a \in \Sigma$$

Figure 1: Regular expressions over the alphabet  $\Sigma$ .

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\begin{array}{ll} \psi ::= & \dots & \text{source types} \\ & | & \mathsf{stringin}[r] & \\ \mathbf{S} ::= & \dots & \text{source terms} \\ & | & \mathsf{rstr}[s] & s \in \Sigma^* \\ & | & \mathsf{rconcat}(S,S) \\ & | & \mathsf{rreplace}[r](S,S) \\ & | & \mathsf{rcoerce}[r](S) & \end{array}
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Figure 2: Syntax for the string sanitation fragment of our source language,  $\lambda_S$ .

Figure 8: Translation from source terms (S) to target terms (P). The translation is type-directed in the Tr-Coerce cases.

$$\begin{array}{ll} \theta & ::= \dots & \text{target types} \\ \mid & \text{string} \\ \mid & \text{regex} \end{array}$$
 
$$P & ::= \dots & \text{target terms} \\ \mid & \text{str}[s] \\ \mid & \text{rx}[r] \\ \mid & \text{concat}(P,P) \\ \mid & \text{preplace}(P,P,P) \\ \mid & \text{check}(P,P) \end{array}$$

Figure 3: Syntax for the fragment of our target language,  $\lambda_P$ , containing strings and statically constructed regular expressions.

Figure 4: Typing rules for our fragment of  $\lambda_S$ . The typing context  $\Psi$  is standard.

$$\begin{array}{c|c} S \Downarrow S & S \text{ err} \\ \hline \\ S\text{-E-RSTR} & S\text{-E-Concat} \\ \hline \\ r\text{str}[s] \Downarrow r\text{str}[s] & r\text{str}[s_1] & S_2 \Downarrow r\text{str}[s_2] \\ \hline \\ S\text{-E-REPLACE} & S\text{-E-REPLACE} \\ \hline \\ S1 \Downarrow r\text{str}[s_1] & S_2 \Downarrow r\text{str}[s_2] & r\text{eplace}(r,s_1,s_2) = s \\ \hline \\ r\text{replace}[r](S_1,S_2) \Downarrow r\text{str}[s] \\ \hline \\ S\text{-E-Coerce-OK} & S\text{-E-Coerce-Err} \\ \hline \\ S \Downarrow r\text{str}[s] & s \in \mathcal{L}\{r\} \\ \hline \\ r\text{coerce}[r](S) \Downarrow r\text{str}[s] & r\text{coerce}[r](S) \text{ err} \\ \hline \end{array}$$

Figure 5: Big step semantics for our fragment of  $\lambda_S$ . Error propagation rules are omitted.

$$\begin{array}{c|c} \Theta \vdash P : \theta & \Theta ::= \emptyset \ | \ \Theta, x : \theta \\ \\ \hline P\text{-T-STRING} & P\text{-T-REGEX} \\ \hline \Theta \vdash \mathsf{str}[s] : \mathsf{string} & \overline{\Theta} \vdash \mathsf{rx}[r] : \mathsf{regex} \\ \\ \hline \frac{P\text{-T-CONCAT}}{\Theta \vdash P_1 : \mathsf{string}} & \Theta \vdash P_2 : \mathsf{string} \\ \hline \Theta \vdash \mathsf{concat}(P_1, P_2) : \mathsf{string} \\ \hline \frac{P\text{-T-Replace}}{\Theta \vdash P_1 : \mathsf{regex}} & \Theta \vdash P_2 : \mathsf{string} \\ \hline \Theta \vdash \mathsf{preplace}(P_1, P_2, P_3) : \mathsf{string} \\ \hline \\ \hline \frac{P\text{-T-CHeck}}{\Theta \vdash P_1 : \mathsf{regex}} & \Theta \vdash P_2 : \mathsf{string} \\ \hline \Theta \vdash \mathsf{check}(P_1, P_2) : \mathsf{string} \\ \hline \end{array}$$

Figure 6: Typing rules for our fragment of  $\lambda_P$ . The typing context  $\Theta$  is standard.

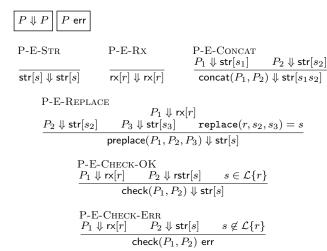


Figure 7: Big step semantics for our fragment of  $\lambda_P$ . Error propagation rules are omitted.

# 2.1 Properties of Regular Languages

Our type safety proofs for languages S and P and our translation correctness result all depend on some properties of regular languages. The crucial property is a relationship between string substitution – which is available in any regular expression library – and regular language substitution, which is a corresponding operation on languages instead of strings 5. The decidability of language substitution is what enables static analysis of sanitation algorithms implemented in terms of string replacement

Throughout this section, we fix an alphabet  $\Sigma$  over which strings s and regular expressions r are defined. throughout the paper,  $\mathcal{L}\{r\}$  refers to the language recognized by the expression r. This distinction between the expression and its language – typically elided in the literature – makes our definition and proofs about systems S and P more readable.

**Lemma 1.** Properties of Regular Languages and Expressions. The following are well-known properties of regular expressions which are necessary for our proofs:

- (1): If  $s_1 \in \mathcal{L}\{r_1\}$  and  $s_2 \in \mathcal{L}\{r_2\}$  then  $s_1s_2 \in \mathcal{L}\{r_1r_2\}$
- (2): For all strings s and expressions r, either  $s \in \mathcal{L}\{r\}$  or  $s \notin \mathcal{L}\{r\}$ .
- (3): Regular languages are closed under complements and concatenation.
- (4): The regular expressions correspond bijectively to the regular languages.

**Definition 2** (1subst). The function 1subst $(r, s_1, s_2)$  produces a string in which all substrings of  $s_1$  matching r are replaced with  $s_2$ .

**Definition 3** (Ireplace). The function Ireplace $(r, r_1, r_2)$  produces a regular expression in which any sublanguage  $\mathcal{L}\{r_1'\}$  of  $\mathcal{L}\{r_1\}$  satisfying the condition  $\mathcal{L}\{r_1'\}\subseteq \mathcal{L}\{r\}$  is replaced with  $\mathcal{L}\{r_2\}$ .

**Lemma 4.** Closure and Totality of Replacement. If  $r, r_1$  and  $r_2$  are regular expressions, then  $lreplace(r, r_1, r_2)$  is also a regular expression.

*Proof.* By induction on r and closure properties of regular expressions.  $\Box$ 

**Lemma 5.** Substitution Correspondence. If  $s_1 \in \mathcal{L}\{r_1\}$  and  $s_2 \in \mathcal{L}\{r_2\}$  then  $\mathtt{lsubst}(r, s_1, s_2) \in \mathtt{lreplace}(r, r_1, r_2)$ .

*Proof.* The proof proceeds by structural induction on r.

case  $r = \alpha$ . If  $s_1 = \alpha$  then  $\alpha \in \mathcal{L}\{r_1\}$  by assumption. Therefore,  $\mathtt{lsubst}(r,s_1,s_2) = \mathtt{lsubst}(\alpha,\alpha,s_2) = s_2$  and  $\mathtt{lreplace}(r,r_1,r_2) = \mathtt{lreplace}(\alpha,r_1,r_2)$ . Since  $s_1 = \alpha$  and  $\alpha \in \mathcal{L}\{r_1\}$ ,  $r_1 \cong \alpha | r_1'$  for some  $r_1'$ . Therefore,  $\mathtt{lreplace}(\alpha,r_1,r_2) \cong \mathtt{lreplace}(\alpha,\alpha | r_1',r_2)$  by Lemma X(1). Finally,  $s_2 \in \mathcal{L}\{r_2\}$  which implies  $s_1 \in \mathcal{L}\{r_2|r'\}$ . If  $s_1 \neq \alpha$  the  $\mathtt{lsubst}(r,s_1,s_2) = s_1$  and  $\mathtt{lreplace}(\alpha,r_1,r_2) = r_1$ .

case r=a|b|. Note that  $[a|b/s_1]s_2=\mathtt{lsubst}(a,\mathtt{lsubst}(b,s_1,s_2),s_2)$  and  $\mathtt{lsubst}(b,s_1,s_2)\in\mathtt{lreplace}(b,r_1,r_2)$  by induction. Therefore,  $\mathtt{lsubst}(a|b,s_1,s_2)\in\mathtt{lreplace}(a,\mathtt{lreplace}(b,r_1,r_2)$  by induction and the definition of lreplace. Finally, applying definitions once more,  $\mathtt{lsubst}(a|b,s_1,s_2)\in\mathtt{lreplace}(a|b,r_1,r_2)$ .

case r = ab. By a similar argument to the disjunctive case.

case r = a\*. By considering the once unwinding of a\*, noting that  $s_1$  and  $s_2$  are finite.

# **2.2** Safety of the Source and Target Languages Lemma 6. If $\Psi \vdash S$ : stringin[r] then r is a well-formed

**Lemma 6.** If  $\Psi \vdash S$ : stringin[r] then r is a well-formed regular expression.

*Proof.* The only non-trivial case is S-T-Replace, which follows from 4.  $\Box$ 

**Lemma 7.** If  $\Theta \vdash P$ : regex then  $P \Downarrow \mathsf{rx}[r]$  such that r is a well-formed regular expression.

We now prove safety for the string fragment of the source and target languages.

**Theorem 8.** Safety for the String Fragment of P. Let S be a term in the source language. If  $\Psi \vdash S$ : stringin[r] then  $S \Downarrow rstr[s]$  and rstr[s]: stringin[r], or else S err.

*Proof.* By induction on the derivation of  $\Psi \vdash S : \psi$ . The interesting case is S-T-Replace, which requires Lemma C.

- **S-T-Stringin-I:** If  $S = \mathsf{rconcat}(S_1, S_2)$ :  $\mathsf{stringin}[r]$  then  $S \Downarrow S$  by S-E-RStr, and  $\Psi \vdash S : \psi$  by assumption.
- S-T-Concat: Suppose  $S = \operatorname{rconcat}(S_1, S_2)$ : stringin $[r_1r_2]$ . By inversion,  $\Psi \vdash S_1$ : stringin $[r_1]$  and  $\Psi \vdash S_1$ : stringin $[r_2]$ . It follows by induction that either  $S_1$  err,  $S_2$  err, or  $S_1 \Downarrow \operatorname{rstr}[s_1]$  and  $S_2 \Downarrow \operatorname{rstr}[s_2]$  for some  $s_1 \in \mathcal{L}\{r_1\}$  and  $s_2 \in \mathcal{L}\{r_2\}$ . In the latter case  $S \Rightarrow \operatorname{rstr}[s_1s_2]$  by S-E-Concat and  $\Psi \vdash \operatorname{rstr}[s_1s_2]$ :  $\operatorname{str}[r_1r_2]$  by 1. In the former cases, S err.

- S-T-Replace: Suppose  $S = \text{rreplace}[r](S_1, S_2)$  and  $\Psi \vdash S$ : stringin[r']. By inversion  $\Psi \vdash S_1$ :  $\text{stringin}[r_1]$  and  $\Psi \vdash S_2$ :  $\text{stringin}[r_2]$  such that  $\text{lsubst}(r, r_1, r_2) = r'$ . By induction,  $S_1$  err,  $S_2$  err or  $S_1 \Downarrow \text{rstr}[s_1]$  and  $S_2 \Downarrow \text{rstr}[s_2]$  such that In the latter case, we know  $\text{lreplace}(r, s_1, s_2) \in \mathcal{L}\{\text{lsubst}(r, r_1, r_2)\}$  by Lemma C; therefore by S-E-Replace,  $S \Downarrow \text{rstr}[s]$  such that  $s \in \mathcal{L}\{\text{lsubst}(r, r_1, r_2)\} = \mathcal{L}\{r'\}$ . So by S-T-String-I, rstr[s]: stringin[r']. In the former cases, S err.
- **S-T-Coerce:** Suppose  $S = \operatorname{rcoerce}[r](S_1)$  and S: stringin[r]. By inversion,  $\Psi \vdash S_1$ : stringin[r']. By induction,  $S_1$  err or  $S_1 \Downarrow \operatorname{rstr}[s]$ . In the former case S err by propagation rules. In the latter case we have by property 2 of 1 that  $s \in \mathcal{L}\{r\}$  or else  $s \notin \mathcal{L}\{r\}$ . If  $s \in \mathcal{L}\{r\}$  then  $\operatorname{rstr}[s]$ : stringin[r]. If  $s \notin \mathcal{L}\{r\}$  then S err.

**Theorem 9.** Let P be a term in the target language. If  $\Theta \vdash P : \theta$  then  $P \Downarrow P'$  and  $P' : \theta$ .

*Proof.* The proof proceeds by induction on the typing relation and is trivial give and inversion lemma for the typing relation. We can write up this proof if we end up having enough space...

### 2.3 Translation Correctness

We now present the main correctness result.

**Theorem 10.** If S: rstr[r] then there exists a P such that ||s|| = P and either:

- (a)  $P \Downarrow \mathsf{str}[s] \ and \ S \Downarrow \mathsf{rstr}[s], \ and \ s \in langr.$
- (b) P err and S err.

*Proof.* The proof proceeds by induction on the typing relation for S. Throughout the proof, properties from the closure lemma for regular languages are necessary; for brevity, we elide these references.

- S-T-String-I: Let  $S = \mathsf{rstr}[s]$  and suppose  $\Psi \vdash \mathsf{rstr}[s]$ : stringin[r]. Choose  $T = \mathsf{string}s$  and note that  $[\![S]\!] = P$  by Tr-String. By P-E-String,  $P \Downarrow \mathsf{string}s$  and by S-E-String  $S \Downarrow \mathsf{rstr}[s]$ . Finally, by inversion of S-T-Stringin-I,  $s \in \mathcal{L}\{r\}$ .
- **S-T-Concat:** Let  $S = \operatorname{rconcat}(S_1, S_2)$  and suppose  $\Psi \vdash S : \operatorname{stringin}[r_1 r_2]$ . By inversion,  $\Psi \vdash S_1 : \operatorname{stringin}[r_1]$ . It follows by induction that there exists a  $P_1$  such that  $[S_1] = P_1$ . By a similar argument for  $S_2$  and  $r_2$ , there exists a  $P_2$  such that  $[S_2] = P_2$ . Choose  $P = \operatorname{concat}(P_1, P_2)$ .

We first prove property (a). Note that  $S_1$  and  $P_1$  are well typed (nrf ACTUALLY WE DON'T KNOW THAT  $P_1$  IS WELL-TYPED!) and do not result in errors. Therefore,  $S_1 \Downarrow \mathsf{rstr}[s_1]$  and  $P_1 \Downarrow \mathsf{string}s_1$  for some  $s_1 \in \mathcal{L}\{r_1\}$  by theorems 8 and 9 respectively. Similarly,  $S_2 \Downarrow \mathsf{rstr}[s_2]$  and  $P_2 \Downarrow \mathsf{string}s_2$  for some

 $s_2 \in \mathcal{L}\{r_2\}$ . Therefore,  $S \Downarrow \mathsf{rstr}[s_1s_2]$  by S-E-Concat and  $\mathsf{concat}(P_1, P_2) \Downarrow \mathsf{string}s_1s_2$  by P-E-Concat. Finally,  $s_1s_2 \in \mathcal{L}\{r_1\}r_2$  by 1.

Consider property (b). If  $S_1$  err then  $P_1$  err by induction, and it follows that S err and P err by respective error propagation rules. Similarly, if  $S_2$  err then  $P_2$  err and it follow that S err and P err by induction and propagation.

- S-T-Replace: Let  $S = \text{rreplace}[r](S_1, S_2)$  and suppose  $\Psi \vdash S : \text{stringin}[r']$  for some s. By inversion of S-T-Replace,  $\Psi S_1 : \text{stringin}[r_1]$  and  $\Psi : \text{stringin}[r_2]$  such that  $\mathbb{E}[r] : \mathbb{E}[r] : \mathbb$ 
  - If (a) holds then  $S_1 \Downarrow \operatorname{rstr}[s_1]$  and  $P_1 \Downarrow \operatorname{string} s_1$  for some  $s_1 \in \mathcal{L}\{r_1\}$ , and similarly for  $S_2, P_2$  and some  $s_2 \in \mathcal{L}\{r_2\}$ . Therefore, by S-E-Replace,  $S \Downarrow \operatorname{rstr}[s]$  for some  $s = \operatorname{lreplace}(r, s_1, s_2)$ . Choose  $P = \operatorname{preplace}(r, s_1, s_2)$ . By a similar argument and P-E-Replace,  $P \Downarrow \operatorname{string} s$  for some  $s = \operatorname{lreplace}(r, s_1, s_2)$ . What remains to be shown is  $\operatorname{lreplace}(r, s_1, s_2) \in \mathcal{L}\{\operatorname{lsubst}(r, r_1, r_2)\}$ , which follows from Leamm D since  $s_1 \in r_1$  and  $s_2 \in r_2$ .
  - If (b) holds for  $S_1$  and  $P_1$ , then S err and P err by propagation rules. Similarly, if (b) hols for  $S_2$  and  $P_2$  then S err and P err by propagation rules.
- **S-T-Coerce:** Let  $S = \mathsf{rcoerce}[r](S')$  and suppose  $\Psi \vdash \mathsf{rcoerce}[r](S)$ :  $\mathsf{stringin}[r]$ . By inversion  $\Psi \vdash S'$ :  $\mathsf{stringin}[r']$  for an arbitrary r'. By induction there exists a P' such that  $[\![S']\!] = P'$  and either (a) or (b) holds for S' and P'.

If (a) holds then  $S' \Downarrow \mathsf{rstr}[s']$  and  $P' \Downarrow \mathsf{string}s'$  for some  $s' \in \mathcal{L}\{r'\}$ . Note that either  $s' \in \mathcal{L}\{r\}$  or  $s' \not\in \mathcal{L}\{r\}$  by property 2 of 1. Suppose  $s' \in \mathcal{L}\{r\}$ . Then  $\mathsf{rcoerce}[r](S) \Downarrow \mathsf{rstr}[S']$  by S-E-Coerce. Choose  $P = \mathsf{rx}[r]P'$  and note that  $P \Downarrow \mathsf{string}s'$  by P-E-Coerce. Now suppose  $s' \not\in \mathcal{L}\{r\}$ . Then S err and P err by P-E-Check-Err and S-E-Coerce-Err.

Finally, if (b) holds then S err and P err by propagation.

Papers that needs to be cited in this section:

- Ur/Web OSDI paper
- Jif?

- OWASP
- XDuce and related papers.
- src?
- Ace or Wyvern paper?
- hotsos?
- Haskell extension paper
- Maybe some popular FOSS libraries/frameworks that do input sanitation?

r	$\lfloor r \rfloor_{\lambda}$	$\lfloor r  floor_{ m Ace}$
$\epsilon$	tremp	1111
	trdot	"."
a	$\mathtt{trchar}[a]$	"a"
$r_1 \cdot r_2$	$trseq(\lfloor r_1  floor_\lambda; \lfloor r_2  floor_\lambda)$	$\lfloor r_1 \rfloor_{\mathrm{Ace}} + \lfloor r_2 \rfloor_{\mathrm{Ace}}$
$r_1 + r_2$	$tror(\lfloor r_1  floor_\lambda; \lfloor r_2  floor_\lambda)$	"(" + $\lfloor r_1 \rfloor_{Ace}$ + " " + $\lfloor r_2 \rfloor_{Ace}$ + ")"
$\psi$	$\lfloor \psi  floor_{\lambda}$	$\lfloor \psi  floor$ Ace
$\mathtt{string\_in}[r]$	$STRINGIN[\lfloor r \rfloor_{\lambda}]$	$string\_in[\lfloor r \rfloor_{Ace}]$
S	$\lfloor S \rfloor_{\lambda}$	$\lfloor S \rfloor_{ ext{Ace}}$
$str_{\mathtt{-}}in[s]$	intro[str[s]]()	"s"
$\mathtt{concat}(S_1;S_2)$	$\lfloor S_1 \rfloor_{\lambda} \cdot elim[\mathbf{concat}](\lfloor S_2 \rfloor_{\lambda})$	$\lfloor S_1 \rfloor_{\mathrm{Ace}} + \lfloor S_2 \rfloor_{\mathrm{Ace}}$
$\mathtt{subst}[r](S_1;S_2)$	$\lfloor S_1 \rfloor_{\lambda} \cdot elim[\mathbf{subst} \ \lfloor r \rfloor_{\lambda}](\lfloor S_2 \rfloor_{\lambda})$	$\lfloor S_1  floor_{ m Ace}$ .subst( $\lfloor r  floor_{ m Ace}$ , $\lfloor S_2  floor_{ m Ace}$ )
$\mathtt{coerce}[r](S)$	$\lfloor S \rfloor_{\lambda} \cdot elim[\mathbf{coerce} \ \lfloor r \rfloor_{\lambda}]()$	$\lfloor S  floor_{ m Ace}$ .coerce( $\lfloor r  floor_{ m Ace}$ )

Table 1: Embeddings of the string\_in fragment into  $\lambda_{Ace}$  and Ace.

```
 \begin{array}{c|c} \hline \Gamma \vdash_{\Phi} e \Rightarrow \tau \sim i \end{array} & \hline \Gamma \vdash_{\Phi} e \Leftarrow \tau \sim i \\ \hline \\ ATT\text{-FLIP} & \Gamma \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \hline \Gamma \vdash_{\Phi} e \Leftrightarrow \tau \sim i \end{array} & \hline \\ ATT\text{-ELIM-SYN} & \Gamma \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ ATT\text{-ELIM-SYN} & \Gamma \vdash_{\Phi} e \Rightarrow \tau \sim i \end{array} & \hline \\ ATT\text{-ELIM-SYN} & \Gamma \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ T \vdash_{\Phi} e \Rightarrow \tau \sim i \end{array} & \hline \\ ATT\text{-ELIM-SYN} & \Gamma \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ T \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ ATT\text{-ELIM-SYN} & \Gamma \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ T \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ T \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ T \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ T \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ T \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ T \vdash_{\Phi} e \Rightarrow \tau \sim i \\ \hline \\ T \vdash_{\Phi} e \sim \text{elim}[\tau_{\text{opidx}}](e_1; \dots; e_n) \Rightarrow \tau \sim i' \\ \hline \\ T \vdash_{\Phi} e \sim i \\ \hline \\ T \vdash_{\Phi} e \sim \text{elim}[\tau_{\text{opidx}}](e_1; \dots; e_n) \Rightarrow \tau \sim i' \\ \hline \\ T \vdash_{\Phi} e \sim i \\ \hline \\ T \vdash_{\Phi} e \sim \text{elim}[\tau_{\text{opidx}}](e_1; \dots; e_n) \Rightarrow \tau \sim i' \\ \hline \end{array}
```

Figure 8: The bidirectional active typechecking and translation judgements.

```
tycon stringin of R  {
                                                                                                      (1)
    iana \{\lambda opidx: String. \lambda tyidx: R. \lambda a: list[Arg].
                                                                                                      (2)
        arity0 \ a \ (check \ opidx \ tyidx \ \rhd (\lhd(opidx)))
                                                                                                      (3)
    esyn \{\lambda opidx:1 + (R + R).\lambda a:list[Arg].
                                                                                                      (4)
        case opidx of inl(_-) \Rightarrow
                                                                                                      (5)
            \mathbf{arity2} \ \mathbf{a} \ \lambda \mathbf{a1} \text{:} \mathsf{Arg.} \lambda \mathbf{a2} \text{:} \mathsf{Arg.}
                                                                                                      (6)
                 rsyn a1 \lambdar1:R.\lambdai1:ITm.
                                                                                                      (7)
                 rsyn a2 \lambdar2:R.\lambdai2:ITm.
                                                                                                      (8)
                     (STRINGIN(rseq(r1; r2)),
                                                                                                      (9)
                      \triangleright (iconcat(\triangleleft(i1); \triangleleft(i2))))
                                                                                                    (10)
         |\inf(\mathbf{opidx'}) \Rightarrow d\}\};
                                                                                                    (11)
def \ \mathbf{concat} = \mathsf{inl}[1, \mathsf{R} + \mathsf{R}](());
                                                                                                    (12)
def \ \mathbf{subst} = \lambda \mathbf{r} : R.inr[1, R + R](inI[R, R](\mathbf{r}));
                                                                                                    (13)
\mathsf{def}\ \mathbf{coerce} = \lambda \mathbf{r} \mathsf{:R.inr}[1,\mathsf{R}+\mathsf{R}](\mathsf{inr}[\mathsf{R},\mathsf{R}](\mathbf{r}))
                                                                                                    (14)
```

Figure 10: Definition of  $\phi_S$ , which enables the embedding of fragment S into  $\lambda_{Ace}$ .

## 2.4 Background: Ace

TODO: Make a TR out of the OOPSLA submission.

- 2.5 Explicit Conversions
- 2.6 Adding Subtyping to Ace
- 2.7 Theory
- 3. RELATED WORK
- 4. DISCUSSION

Figure 9: Normalization semantics for the type-level language. Missing rules (including error propagation rules and normalization of quoted internal terms and types) are unsurprising and will be given later.