A Type System for String Sanitation Implemented Inside a Python

ABSTRACT

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1. INTRODUCTION

In web applications and other settings, incorrect input sanitation often causes security vulnerabilities. In fact, ...OWASP says it's important... Mention CVE stats. For this reason, modern web frameworks and libraries use various techniques to ensure proper sanitation of arbitrary user input. On the rare occasions when these methods are unavailable or insufficient, developers (hopefully) create ad hoc sanitation algorithms. Im most cases, sanitation algorithms – ad hoc or otherwise – are ultimately implemented using the language's regular expression capabilities. Therefore, a system capable of statically checking properties about operations performed using regular expressions will be expressive enough to capture real-world implementations of sanitation algorithms.

Input sanitation is the problem of ensuring that an arbitrary string is coerced into a safe form before potentially unsafe use. For example, preventing SQL injection attacks requires ensuring that any string coming from user input to a query does not contain unescaped SQL. The point at which arbitrary user input is concatenated into a SQL query is called a use site. Although we believe are general approach extends to a wider class of problems (e.g. sanitation algorithms for preventing XSS attacks might be definable using regular tree languages), these generalizations are beyond the scope of the present paper.

This paper presents a language extension, definable in the Ace programming language, for ensuring that input sanitation algorithms are implemented correctly with respect to use site specifications. If use site specifications are sufficient, then type checking ensures the absence of vulnerabilities and other bugs which arise from improper sanitation. Our extension focuses on sanitation algorithms which aim to prevent command-injection style attacks (e.g. SQL injection or RFI).

1.1 Related Work and Alternative Approaches

The input sanitation problem is well-understood. There exist a large number of techniques and technologies, proposed by both practitioners and researchers, for preventing injection-style attacks. In this section, we defend the novelty and significance of our approach with respect to the state of the art in practice and in research.

Unlike frameworks provided by languages such as Haskell and Ruby, our type system provides a *static* guarantee that input is always properly sanitized before use. We achieve this by defining a typing relation which captures idiomatic sanitation algorithms. Type safety in our system relies upon several closure and decidability results about regular languages.

Libraries and frameworks available in functional programming language communities often make claims about security and sometimes even sophistically mention sophisticated type systems as evidence of freedom from injection-style attacked. However, even the specification that input is always sanitized properly before use is not actually captured by the type system or anywhere else; in fact, the full specification of these algorithms is rarely characterized by anything more specific than the type String \rightarrow String, which is a class of safe input sanitation algorithms only in the most degenerate case.

A number of research languages provide actually static guarantees that a program is free of input sanitation vulnerabilities. Most rely on some form of information flow. TODO-nrf give citations and examples. Our extension to Ace differs from these systems in the ways following:

- Our system is a light-weight solution to a single class of sanitation vulnerabilities (e.g. we do not address Cross-Site Scripting). We present our system not as a comprehensive solution to the web security problem, but rather as evidence that composable, light-weight and simple analyses can address security problems.
- Our system is defined as a library in terms of an extensible type system, as opposed to a stand-alone language. This is important for two reasons. First, our system is one of the first large examples written in Ace, and serves as an extended case study. Second, although our approach requires developers to adopt a new language, it does not require developers to adopt a language specifically for web development.

- Ace is implemented in Python and shares its grammar. Since Python is a popular programming language among web developers, the barrier between our research and adopted technologies is far lower than is e.g. Ur/Web's.
- In general, our is a composable, light-weight and natural solution to a single problem rather than a comprehensive solution to the web security problem. Our goal is to demonstrate that extensible type systems can capture static properties of common idioms, and thereby ensure safety without introducing much additional complexity.

Finally, incorporating regular expressions into the type system is not novel. The XDuce system [?] typechecks XML schemas using regular expressions. We differ from this and related work in at least two ways. First, our system is defined within an extensible type system; this first difference introduced an interesting class of design problems (see §???). TODO-nrf this is the second time this is used as a warrant. Factor out this argument and place it at the top??? Second, our focus on security required novel design decisions; for instance, the filter elimination form is unique to Ace.

In conclusion, our system is novel in at least two ways:

- The safety guarantees provided by libraries and frameworks in popular languages are not as (statically) justified as is often belived (or even claimed).
- Our extension is the first major demonstration of how an extensible type system may be used to provide lightweight, composable security analyses based upon idiomatic code.

1.2 Outline

An outline of this paper follows:

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- In §2, we define the type system's static and dynamic semantics.
- Section 3 recalls some classical results about regular expressions and presents meta-theory for our system, including the main soundness theorem for λ_{CS} .
- Finally, §4 discusses our implemention of λ_{CS} as a type system extension within the Ace programming language.

2. A TYPE SYSTEM FOR STRING SANITATION

The λ_{CS} language is characterized by a type of strings indexed by regular expressions, together with operations on such strings which correspond to common input sanitation patterns.

This section presents the grammar and semantics of λ_{CS} . The semantics are defined in terms of an internal language with at least strings and a regex filter function. These constraints are captured by the internal term valuations. The internal language does not necessarily need a regex filter function because any dynamic conversion is easily definable using a combination of filters and safe casting.

Note that we never insert an internal check where the type of the string implies that a check must succeed. Furthermore, expensive calculations (such as language inclusion or dsubst, all occur at compile time. Since sanitation problems are generally expressible with smalle, simple expressions, we believe that the compile-time overhead is not significant enough to prohibiour target usecase. Informal experimentation with our implementation seems to support this assertion.

Due to Ei-Replace, all of our meta-theory depends upon a correct implementation of both regular expression replacement and inclusion checking in the internal language. We believe this assumption is okay for two reasons. First, our system is still superior to the status quo, which relies upon the correctness of these libraries in addition to correct application logic. Second, regular expression libraries are generally well-tested and there exist verified implementations.

$$\mathbf{r} \; ::= \; \epsilon \; | \; . \; | \; a \; | \; r \cdot r \; | \; r + r \; | \; r * \qquad \qquad a \in \Sigma$$

Figure 1: Regular expressions over the alphabet Σ .

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\begin{array}{ll} \psi ::= & \dots & \text{source types} \\ & | & \mathsf{stringin}[r] & \\ \mathbf{S} ::= & \dots & \text{source terms} \\ & | & \mathsf{rstr}[s] & s \in \Sigma^* \\ & | & \mathsf{rconcat}(S,S) \\ & | & \mathsf{rreplace}[r](S,S) \\ & | & \mathsf{rcoerce}[r](S) & \end{array}
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Figure 2: Syntax for the string sanitation fragment of our source language, λ_S .

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\begin{array}{lll} \theta & ::= & \dots & & \text{target types} \\ & | & \text{string} & | & \text{regex} & & & \\ P & ::= & \dots & & \text{target terms} \\ & | & \text{str}[s] & | & \text{rx}[r] & | & \text{concat}(P,P) & | & \text{replace}(P,P,P) & | & \text{check}(P,P) & \\ & | & & \text{check}(P,P) & & & \\ \end{array}
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Figure 3: Syntax for the fragment of our target language, λ_P , containing strings and statically constructed regular expressions.

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Figure 8: Translation from source terms (S) to target terms (P). The translation is type-directed in the Tr-Coerce cases.

[rcoerce[r'](S)] = check(rx[r'], P)

$$\begin{array}{lll} \Psi \vdash S : \psi & \Psi ::= \emptyset \mid \Psi, x : \psi & \Theta \vdash P : \theta & \Theta ::= \emptyset \mid \Theta, x : \theta \\ & & \frac{S \text{-T-STRINGIN-I}}{s \in \mathcal{L}\{r\}} & P \text{-T-STRING} & P \text{-T-REGEX} \\ & & \overline{\Psi} \vdash \operatorname{rstr}[s] : \operatorname{stringin}[r] & \overline{\Psi} \vdash S_2 : \operatorname{stringin}[r_2] \\ & & \overline{\Psi} \vdash \operatorname{rconcat}(S_1, S_2) : \operatorname{stringin}[r_1] & \Psi \vdash S_2 : \operatorname{stringin}[r_2] \\ & & \overline{\Psi} \vdash \operatorname{rstringin}[r_1] & \Psi \vdash S_2 : \operatorname{stringin}[r_2] \\ & & \overline{\Psi} \vdash \operatorname{rstringin}[r_1] & \Psi \vdash S_2 : \operatorname{stringin}[r_2] \\ & & \overline{\Psi} \vdash \operatorname{rreplace}[r](S_1, S_2) : \operatorname{stringin}[r'] \\ & & \overline{\Psi} \vdash \operatorname{rreplace}[r](S_1, S_2) : \operatorname{stringin}[r'] \\ & & \overline{\Psi} \vdash \operatorname{rcoerce}[r](S) : \operatorname{stringin}[r] \\ & & \underline{\Psi} \vdash \operatorname{rcoerce}[r](S) : \operatorname{stringin}[r] \\ & & \underline{\Psi} \vdash \operatorname{rcoerce}[r](S) : \operatorname{stringin}[r] \\ & & \underline{\Psi} \vdash \operatorname{rcoerce}[r](S) : \operatorname{rcoerce}[r](S)$$

Figure 4: Typing rules for our fragment of λ_S . The typing context Ψ is standard.

[rcoerce[r'](S)] = str[s]

$$\begin{array}{c|c} S \Downarrow S & \text{S err$} \\ \hline \\ S\text{-E-RSTR} & S\text{-E-CONCAT} \\ rstr[s] \Downarrow rstr[s] & rconcat(S_1,S_2) \Downarrow rstr[s_2] \\ \hline \\ S\text{-E-REPLACE} \\ S_1 \Downarrow rstr[s_1] & S_2 \Downarrow rstr[s_2] & replace(r,s_1,s_2) = s \\ \hline \\ rreplace[r](S_1,S_2) \Downarrow rstr[s] \\ \hline \\ S\text{-E-COERCE-OK} \\ S \Downarrow rstr[s] & s \in \mathcal{L}\{r\} \\ rcoerce[r](S) \Downarrow rstr[s] & S\text{-E-COERCE-ERR} \\ S \Downarrow rstr[s] & s \not\in \mathcal{L}\{r\} \\ \hline \\ rcoerce[r](S) \Downarrow rstr[s] & rcoerce[r](S) err \\ \hline \end{array}$$

Figure 5: Big step semantics for our fragment of λ_S . Error propagation rules are omitted.

$$\begin{array}{c|c} \hline P \Downarrow P & \hline P \text{ err} \\ \hline \\ P\text{-E-STR} & P\text{-E-Rx} & P\text{-E-Concat} \\ \hline str[s] \Downarrow str[s] & \hline \mathsf{rx}[r] \Downarrow \mathsf{rx}[r] & \hline \\ P^{1} \Downarrow \mathsf{str}[s_{1}] & P_{2} \Downarrow \mathsf{str}[s_{2}] \\ \hline \\ P^{1} \Downarrow \mathsf{rx}[r] & \hline \\ P^{2} \Downarrow \mathsf{str}[s_{2}] & P_{3} \Downarrow \mathsf{str}[s_{3}] & \mathsf{replace}(r,s_{2},s_{3}) = s \\ \hline \\ P^{2} \Downarrow \mathsf{str}[s_{2}] & P_{3} \Downarrow \mathsf{str}[s_{3}] & \mathsf{replace}(r,s_{2},s_{3}) = s \\ \hline \\ P^{2} \Downarrow \mathsf{rx}[r] & P_{3} \Downarrow \mathsf{rx}[r] \\ \hline \\ P^{2} \Downarrow \mathsf{rx}[r] & P_{2} \Downarrow \mathsf{rstr}[s] & s \in \mathcal{L}\{r\} \\ \hline \\ \mathsf{check}(P_{1},P_{2}) \Downarrow \mathsf{str}[s] & s \notin \mathcal{L}\{r\} \\ \hline \\ \mathsf{check}(P_{1},P_{2}) & \mathsf{err} \\ \hline \end{array}$$

Figure 6: Typing rules for our fragment of λ_P . The

typing context Θ is standard.

Figure 7: Big step semantics for our fragment of λ_P . Error propagation rules are omitted.

2.1 Properties of Regular Languages

Our type safety proofs for languages S and P and our translation correctness result all depend on some properties of regular languages. The crucial property is a relationship between string substitution – which is available in any regular expression library – and regular language substitution, which is a corresponding operation on languages instead of strings 5. The decidability of language substitution is what enables static analysis of sanitation algorithms implemented in terms of string replacement

Throughout this section, we fix an alphabet Σ over which strings s and regular expressions r are defined. throughout the paper, $\mathcal{L}\{r\}$ refers to the language recognized by the expression r. This distinction between the expression and its language – typically elided in the literature – makes our definition and proofs about systems S and P more readable.

Lemma 1. Properties of Regular Languages and Expressions. The following are well-known properties of regular expressions which are necessary for our proofs:

- (1): If $s_1 \in \mathcal{L}\{r_1\}$ and $s_2 \in \mathcal{L}\{r_2\}$ then $s_1s_2 \in \mathcal{L}\{r_1r_2\}$
- (2): For all strings s and expressions r, either $s \in \mathcal{L}\{r\}$ or $s \notin \mathcal{L}\{r\}$.
- $(3): \ Regular \ languages \ are \ closed \ under \ complements \ and \ concatenation.$
- (4): The regular expressions correspond bijectively to the regular languages.

Definition 2 (1subst). The function $lsubst(r, s_1, s_2)$ produces a string in which all substrings of s_1 matching r are replaced with s_2 .

Definition 3 (Ireplace). The function Ireplace (r, r_1, r_2) produces a regular expression in which any sublanguage $\mathcal{L}\{r'_1\}$ of $\mathcal{L}\{r_1\}$ satisfying the condition $\mathcal{L}\{r'_1\}\subseteq\mathcal{L}\{r\}$ is replaced with $\mathcal{L}\{r_2\}$.

Lemma 4. Closure and Totality of Replacement. If r, r_1 and r_2 are regular expressions, then $lreplace(r, r_1, r_2)$ is also a regular expression.

Lemma 5. Substitution Correspondence. If $s_1 \in \mathcal{L}\{r_1\}$ and $s_2 \in \mathcal{L}\{r_2\}$ then $\mathtt{lsubst}(r, s_1, s_2) \in \mathtt{lreplace}(r, r_1, r_2)$.

Proof. TODO-nrf \Box

2.2 Safety of the Source and Target Languages

Lemma 6. If $\Psi \vdash S$: stringin[r] then r is a well-formed regular expression.

Proof. The only non-trivial case is S-T-Replace, which follows from 4. $\hfill\Box$

Lemma 7. If $\Theta \vdash P$: regex then $P \Downarrow rx[r]$ such that r is a well-formed regular expression.

We now prove safety for the string fragment of the source and target languages.

Theorem 8. Safety for the String Fragment of P. Let S be a term in the source language. If $\Psi \vdash S$: stringin[r] then $S \Downarrow rstr[s]$ and rstr[s]: stringin[r], or else $S \Downarrow err$.

Proof. By induction on the derivation of $\Psi \vdash S : \psi$. The interesting case is S-T-Replace, which requires Lemma C.

- **S-T-Stringin-I:** If $S = \mathsf{rconcat}(S_1, S_2)$: $\mathsf{stringin}[r]$ then $S \Downarrow S$ by S-E-RStr, and $\Psi \vdash S : \psi$ by assumption.
- S-T-Concat: Suppose $S = \mathsf{rconcat}(S_1, S_2)$: $\mathsf{stringin}[r_1r_2]$. By inversion, $\Psi \vdash S_1$: $\mathsf{stringin}[r_1]$ and $\Psi \vdash S_1$: $\mathsf{stringin}[r_2]$. It follows by induction that either $S_1 \Downarrow \mathsf{err}$, $S_2 \Downarrow \mathsf{err}$, or $S_1 \Downarrow \mathsf{rstr}[s_1]$ and $S_2 \Downarrow \mathsf{rstr}[s_2]$ for some $s_1 \in \mathcal{L}\{r_1\}$ and $s_2 \in \mathcal{L}\{r_2\}$. In the latter case $S \Rightarrow \mathsf{rstr}[s_1s_2]$ by S-E-Concat and $\Psi \vdash \mathsf{rstr}[s_1s_2]$: $\mathsf{str}[r_1r_2]$ by 1. In the former cases, $S \Downarrow \mathsf{err}$.
- S-T-Replace: Suppose $S = \text{rreplace}[r](S_1, S_2)$ and $\Psi \vdash S$: stringin[r']. By inversion $\Psi \vdash S_1$: stringin $[r_1]$ and $\Psi \vdash S_2$: stringin $[r_2]$ such that $\texttt{lsubst}(r, r_1, r_2) = r'$. By induction, $S_1 \Downarrow \texttt{err}$, $S_2 \Downarrow \texttt{err}$ or $S_1 \Downarrow \texttt{rstr}[s_1]$ and $S_2 \Downarrow \texttt{rstr}[s_2]$ such that In the latter case, we know $\texttt{lreplace}(r, s_1, s_2) \in \mathcal{L}\{\texttt{lsubst}(r, r_1, r_2)\}$ by Lemma C; therefore by S-E-Replace, $S \Downarrow \texttt{rstr}[s]$ such that $s \in \mathcal{L}\{\texttt{lsubst}(r, r_1, r_2)\} = \mathcal{L}\{r'\}$. So by S-T-String-I, rstr[s]: stringin[r']. In the former cases, $S \Downarrow \texttt{err}$.
- **S-T-Coerce:** Suppose $S = \mathsf{rcoerce}[r](S_1)$ and $S : \mathsf{stringin}[r]$. By inversion, $\Psi \vdash S_1 : \mathsf{stringin}[r']$. By induction, $S_1 \Downarrow \mathsf{err}$ or $S_1 \Downarrow \mathsf{rstr}[s]$. In the former case $S \Downarrow \mathsf{err}$ by propagation rules. In the latter case we have by property 2 of 1 that $s \in \mathcal{L}\{r\}$ or else $s \notin \mathcal{L}\{r\}$. If $s \in \mathcal{L}\{r\}$ then $\mathsf{rstr}[s] : \mathsf{stringin}[r]$. If $s \notin \mathcal{L}\{r\}$ then $S \Downarrow \mathsf{err}$.

Theorem 9. Let P be a term in the target language. If $\Theta \vdash P : \theta$ then $P \Downarrow P'$ and $P' : \theta$.

Proof. The proof proceeds by induction on the typing relation and is trivial give and inversion lemma for the typing relation. We can write up this proof if we end up having enough space...

2.3 Translation Correctness

We now present the main correctness result.

Theorem 10. If $S : \mathsf{rstr}[r]$ then there exists a P such that ||s|| = P and either:

- (a) $P \Downarrow str[s]$ and $S \Downarrow rstr[s]$, and $s \in langr$.
- (b) P err and S err.

Proof. The proof proceeds by induction on the typing relation for S. Throughout the proof, properties from the closure lemma for regular languages are necessary; for brevity, we elide these references.

- S-T-String-I: Let $S = \mathsf{rstr}[s]$ and suppose $\Psi \vdash \mathsf{rstr}[s]$: stringin[r]. Choose $T = \mathsf{string}s$ and note that $[\![S]\!] = P$ by Tr-String. By P-E-String, $P \Downarrow \mathsf{string}s$ and by S-E-String $S \Downarrow \mathsf{rstr}[s]$. Finally, by inversion of S-T-Stringin-I, $s \in \mathcal{L}\{r\}$.
- **S-T-Concat:** Let $S = \operatorname{rconcat}(S_1, S_2)$ and suppose $\Psi \vdash S : \operatorname{stringin}[r_1 r_2]$. By inversion, $\Psi \vdash S_1 : \operatorname{stringin}[r_1]$. It follows by induction that there exists a P_1 such that $[S_1] = P_1$. By a similar argument for S_2 and r_2 , there exists a P_2 such that $[S_2] = P_2$. Choose $P = \operatorname{concat}(P_1, P_2)$.

We first prove property (a). Note that S_1 and P_1 are well typed (nrf ACTUALLY WE DON'T KNOW THAT P_1 IS WELL-TYPED!) and do not result in errors. Therefore, $S_1 \Downarrow \mathsf{rstr}[s_1]$ and $P_1 \Downarrow \mathsf{string}s_1$ for some $s_1 \in \mathcal{L}\{r_1\}$ by theorems 8 and 9 respectively. Similarly, $S_2 \Downarrow \mathsf{rstr}[s_2]$ and $P_2 \Downarrow \mathsf{string}s_2$ for some $s_2 \in \mathcal{L}\{r_2\}$. Therefore, $S \Downarrow \mathsf{rstr}[s_1s_2]$ by S-E-Concat and $\mathsf{concat}(P_1, P_2) \Downarrow \mathsf{string}s_1s_2$ by P-E-Concat. Finally, $s_1s_2 \in \mathcal{L}\{r_1\}r_2$ by 1.

Consider property (b). If S_1 err then P_1 err by induction, and it follows that S err and P err by respective error propagation rules. Similarly, if S_2 err then P_2 err and it follow that S err and P err by induction and propagation.

- S-T-Replace: Let $S = \mathsf{rreplace}[r](S_1, S_2)$ and suppose $\Psi \vdash S : \mathsf{stringin}[r']$ for some s. By inversion of S-T-Replace, $\Psi S_1 : \mathsf{stringin}[r_1]$ and $\Psi : \mathsf{stringin}[r_2]$ such that $\mathsf{lsubst}(r, r_1, r_2) = r'$. By induction, there exists some P_1, P_2 such that $[S_1] = P_1, [S_2] = P_2$ and either (a) or (b) holds.
 - If (a) holds then $S_1 \Downarrow \operatorname{rstr}[s_1]$ and $P_1 \Downarrow \operatorname{string} s_1$ for some $s_1 \in \mathcal{L}\{r_1\}$, and similarly for S_2, P_2 and some $s_2 \in \mathcal{L}\{r_2\}$. Therefore, by S-E-Replace, $S \Downarrow \operatorname{rstr}[s]$ for some $s = \operatorname{lreplace}(r, s_1, s_2)$. Choose $P = \operatorname{preplace}(r, s_1, s_2)$. By a similar argument and P-E-Replace, $P \Downarrow \operatorname{string} s$ for some $s = \operatorname{lreplace}(r, s_1, s_2)$. What remains to be shown is $\operatorname{lreplace}(r, s_1, s_2) \in \mathcal{L}\{\operatorname{lsubst}(r, r_1, r_2)\}$, which follows from Leamm D since $s_1 \in r_1$ and $s_2 \in r_2$.
 - If (b) holds for S_1 and P_1 , then S err and P err by propagation rules. Similarly, if (b) hols for S_2 and P_2 then S err and P err by propagation rules.
- S-T-Coerce: Let S = rcoerce[r](S') and suppose $\Psi \vdash \text{rcoerce}[r](S)$: stringin[r]. By inversion $\Psi \vdash S'$: stringin[r'] for an arbitrary r'. By induction there exists a P' such that [S'] = P' and either (a) or (b) holds for S' and P'.
 - If (a) holds then $S' \Downarrow \operatorname{rstr}[s']$ and $P' \Downarrow \operatorname{string}s'$ for some $s' \in \mathcal{L}\{r'\}$. Note that either $s' \in \mathcal{L}\{r\}$ or $s' \not\in \mathcal{L}\{r\}$ by property 2 of 1. Suppose $s' \in \mathcal{L}\{r\}$. Then $\operatorname{rcoerce}[r](S) \Downarrow \operatorname{rstr}[S']$ by S-E-Coerce. Choose $P = \operatorname{rx}[r]P'$ and note that $P \Downarrow \operatorname{string}s'$ by P-E-Coerce. Now suppose $s' \not\in \mathcal{L}\{r\}$. Then S err and P err by P-E-Check-Err and S-E-Coerce-Err.

Finally, if (b) holds then S err and P err by propagation