A Type System for String Sanitation Implemented Inside a Python

ABSTRACT

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1. INTRODUCTION

Improper input sanitation is a leading cause of security vulnerabilities in web applications [OWASP]. Command injection attacks exploit improper input sanitation by inserting malicious code into an otherwise benign command. Modern web frameworks, libraries, and database abstraction layers attempt to ensure proper sanitation of user input. When these methods are unavailable or insufficient, developers implement custom sanitation techniques. Im both cases, sanitation algorithms are implemented using the language's regular expression capabilities and usually replace potentially unsafe strings with equivalent escaped strings.

In this paper, we present a type system for implementing and statically checking input sanitation techniques. Our solution suggests a more general approach to the integration of security concerns into programming language design. This approach is characterized by *composable* type system extensions which *complement* existing and well-understood solutions with compile-time checks.

To demonstrate this approach, we present a simply typed lambda calculus with constrained strings; that is, a set of string types parameterized by regular expressions. If s: stringin[r], then s is a string matching the language r. Additionally, we include an operation $\text{rreplace}[r](s_1, s_2)$ which corresponds to the replace mechanism available in most regular expression libraries; that is, any substring of s_1 matching r is replaced with s_2 . The type of this expression is the computed, and is likely "smaller" or more constrained than the type of s_1 . Libraries, frameworks or functions which construct and execute commands containing input can specify a safe subset stringin $[r_{\text{spec}}]$ of strings, and input sanitation algorithms can construct such a string using rreplace or, optionally, by coercion (in which case a runtime check is inserted). We also show how this simple can be translated

into a host language containing a regular expression library such that the safety guarantee of the extended language is preserved.

Summarily, we present a simple type system extension which ensures the absence of input sanitation vulnerabilities by statically checking input sanitation algorithms which use an underlying regular expression library. This approach is *composable* in the sense that it is a conservative extension. This approach is also *complementary* to existing input sanitation techniques which use string replacement for input sanitation.

1.1 Related Work and Alternative Approaches

The input sanitation problem is well-understood. There exist a large number of techniques and technologies, proposed by both practitioners and researchers, for preventing injection-style attacks. In this section, we explain how our approach to the input sanitation problem differs from each of these approaches. More important than these differences, however, is our more general assertion that language extensibility is a promising approach toward consideration of security goals in programming lanuage design.

Unlike frameworks and libraries provided by languages such as Haskell and Ruby, our type system provides a static guarantee that input is always properly sanitized before use. Doing so requires reasoning about the operations on regular languages corresponding to standard operations on strings; we are unaware of any production system which contains this form of reasoning. Therefore, even where frameworks and libraries provide a viable interface or wrapper around input sanitation, our approach is complementary because it ensurees the correctness of the framework or library itself. Furthermore, our approach is more general than database abstraction layers because our mechanism is applicable to all forms of command injection (e.g. shell injection or remote file inclusion).

A number of research languages provide static guarantees that a program is free of input sanitation vulnerabilities [Jif][Ur/Web]. Our work differes from these contributions in the ways following:

- Our system is a light-weight solution to a single class of sanitation vulnerabilities (e.g. we do not address Cross-Site Scripting).
- Our system is defined as a library in terms of an ex-

tensible type system, as opposed to a stand-alone language. Instead of introducing new technologies and methodologies for addressing security problems, we provide a light-weight static analysis which complements approaches developers already understand well.

 Our implementation of the translation is implemented in Python and shares its grammar. Since Python is a popular programming language among web developers, the barrier between our research and adopted technologies is lower than for greenfield security-oriented languages.

We are also unaware of any extensible programming languages which emphasize applications to security concerns (TRUE?).

Incorporating regular expressions into the type system is not novel. The XDuce system [?] typechecks XML schemas using regular expressions. We differ from this and related work in at least two ways. First, our system is defined within an extensible type system; second, and more importantly, we have demonstrated that regular expression types are applicable to the web security domain.

In conclusion, our system is novel in at least two ways:

- The safety guarantees provided by libraries and frameworks in popular languages are not as (statically) justified as is often belived (or even claimed).
- Our extension is the first major demonstration of how an extensible type system may be used to provide lightweight, composable security analyses based upon idiomatic code.

1.2 Outline

An outline of this paper follows:

- In §2, we define the type system which is embedded in Ace. We include a type safety proof for the string segment of this language and prove the correctness of a translation to an underlying language P. In our theory, P is a simply typed lambda calculus equipped with a minimal regular expression library; in an implementation, P stands in for Python or another underlying general-purpose programming language.
- In §3, we discuss our implemention of this translation as a type system extension within the Ace programming language.

2. A TYPE SYSTEM FOR STRING SANI-TATION

The λ_S language is characterized by a type of strings indexed by regular expressions, together with operations on such strings which correspond to common input sanitation patterns. This section presents the grammar, typing rules and operational semantics for λ_S as well as an underlying language λ_P .

The system λ_S 2 is the simply typed lambda calculus extended with regular expression types, which are string types ensuring a string belongs to a specified language. For instance, S: stringin[r] reads "s is a string matching r". the system includes an operation for replacing all instances of a pattern r in a string s_1 with another string s_2 . Input sanitation algorithms – as implemented by developers or within popular libraries and frameworks – are often implemented in terms of this replace operation. For instance, a developer might all potentially unsafe characters with excaped versions of the same character. Regular expression types are used both to specify input sanitation algorithms, and at use sites as specifications. Note that runtime error states (S err) are introduced by coercion, not by replacement.

The language λ_P 2 is a simple functional language extended with a minimal regular expression library. Any general purpose programming language could stand in for λ_P ; for instance, SML has a regular expression library. In an implementation, our correctness results are modulo the underlying language's correct implementation of regular expression matching (see P-E-Replace).

Finally, we define a translation from our type system λ_S into λ_P .

$$\mathbf{r} ::= \epsilon \mid . \mid a \mid r \cdot r \mid r + r \mid r * \qquad \qquad a \in \Sigma$$

Figure 1: Regular expressions over the alphabet Σ .

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\begin{array}{ll} \psi \; ::= \; \dots & \text{source types} \\ & \mid \; \mathsf{stringin}[r] \\ \mathbf{S} \; ::= \; \dots & \text{source terms} \\ & \mid \; \mathsf{rstr}[s] & s \in \Sigma^* \\ & \mid \; \mathsf{rconcat}(S,S) \\ & \mid \; \mathsf{rreplace}[r](S,S) \\ & \mid \; \mathsf{rcoerce}[r](S) \end{array}
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Figure 2: Syntax for the string sanitation fragment of our source language, λ_S .

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\begin{array}{ll} \theta & ::= \ \dots & \text{target types} \\ \mid & \mathsf{string} \\ \mid & \mathsf{regex} \end{array} P & ::= \ \dots & \text{target terms} \\ \mid & \mathsf{str}[s] \\ \mid & \mathsf{rx}[r] \\ \mid & \mathsf{concat}(P, P) \\ \mid & \mathsf{preplace}(P, P, P) \\ \mid & \mathsf{check}(P, P) \end{array}
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Figure 3: Syntax for the fragment of our target language, λ_P , containing strings and statically constructed regular expressions.

Figure 8: Translation from source terms (S) to target terms (P). The translation is type-directed in the Tr-Coerce cases.

[rcoerce[r'](S)] = check(rx[r'], P)

$$\begin{array}{lll} \Psi \vdash S : \psi & \Psi ::= \emptyset \mid \Psi, x : \psi & \Theta \vdash P : \theta & \Theta ::= \emptyset \mid \Theta, x : \theta \\ & & \frac{S \text{-T-STRINGIN-I}}{s \in \mathcal{L}\{r\}} & P \text{-T-STRING} & P \text{-T-REGEX} \\ & & \overline{\Psi} \vdash \operatorname{rstr}[s] : \operatorname{stringin}[r] & \overline{\Psi} \vdash S_2 : \operatorname{stringin}[r_2] \\ & & \overline{\Psi} \vdash \operatorname{rconcat}(S_1, S_2) : \operatorname{stringin}[r_1] & \Psi \vdash S_2 : \operatorname{stringin}[r_2] \\ & & \overline{\Psi} \vdash \operatorname{rstringin}[r_1] & \Psi \vdash S_2 : \operatorname{stringin}[r_2] \\ & & \overline{\Psi} \vdash \operatorname{rstringin}[r_1] & \Psi \vdash S_2 : \operatorname{stringin}[r_2] \\ & & \overline{\Psi} \vdash \operatorname{rreplace}[r](S_1, S_2) : \operatorname{stringin}[r'] \\ & & \overline{\Psi} \vdash \operatorname{rreplace}[r](S_1, S_2) : \operatorname{stringin}[r'] \\ & & \overline{\Psi} \vdash \operatorname{rcoerce}[r](S) : \operatorname{stringin}[r] \\ & & \underline{\Psi} \vdash \operatorname{rcoerce}[r](S) : \operatorname{stringin}[r] \\ & & \underline{\Psi} \vdash \operatorname{rcoerce}[r](S) : \operatorname{stringin}[r] \\ & & \underline{\Psi} \vdash \operatorname{rcoerce}[r](S) : \operatorname{rcoerce}[r](S)$$

Figure 4: Typing rules for our fragment of λ_S . The typing context Ψ is standard.

[rcoerce[r'](S)] = str[s]

$$\begin{array}{c|c} S \Downarrow S & \text{S err$} \\ \hline \\ S\text{-E-RSTR} & S\text{-E-CONCAT} \\ rstr[s] \Downarrow rstr[s] & rconcat(S_1,S_2) \Downarrow rstr[s_2] \\ \hline \\ S\text{-E-REPLACE} \\ S_1 \Downarrow rstr[s_1] & S_2 \Downarrow rstr[s_2] & replace(r,s_1,s_2) = s \\ \hline \\ rreplace[r](S_1,S_2) \Downarrow rstr[s] \\ \hline \\ S\text{-E-COERCE-OK} \\ S \Downarrow rstr[s] & s \in \mathcal{L}\{r\} \\ rcoerce[r](S) \Downarrow rstr[s] & S\text{-E-COERCE-ERR} \\ S \Downarrow rstr[s] & s \not\in \mathcal{L}\{r\} \\ \hline \\ rcoerce[r](S) \Downarrow rstr[s] & rcoerce[r](S) err \\ \hline \end{array}$$

Figure 5: Big step semantics for our fragment of λ_S . Error propagation rules are omitted.

$$\begin{array}{c|c} \hline P \Downarrow P & \hline P \text{ err} \\ \hline \\ P\text{-E-STR} & P\text{-E-Rx} & P\text{-E-Concat} \\ \hline str[s] \Downarrow str[s] & \hline \mathsf{rx}[r] \Downarrow \mathsf{rx}[r] & \hline \\ P^{1} \Downarrow \mathsf{str}[s_{1}] & P_{2} \Downarrow \mathsf{str}[s_{2}] \\ \hline \\ P^{1} \Downarrow \mathsf{rx}[r] & \hline \\ P^{2} \Downarrow \mathsf{str}[s_{2}] & P_{3} \Downarrow \mathsf{str}[s_{3}] & \mathsf{replace}(r,s_{2},s_{3}) = s \\ \hline \\ P^{2} \Downarrow \mathsf{str}[s_{2}] & P_{3} \Downarrow \mathsf{str}[s_{3}] & \mathsf{replace}(r,s_{2},s_{3}) = s \\ \hline \\ P^{2} \Downarrow \mathsf{rx}[r] & P_{3} \Downarrow \mathsf{rx}[r] \\ \hline \\ P^{2} \Downarrow \mathsf{rx}[r] & P_{2} \Downarrow \mathsf{rstr}[s] & s \in \mathcal{L}\{r\} \\ \hline \\ \mathsf{check}(P_{1},P_{2}) \Downarrow \mathsf{str}[s] & s \notin \mathcal{L}\{r\} \\ \hline \\ \mathsf{check}(P_{1},P_{2}) & \mathsf{err} \\ \hline \end{array}$$

Figure 6: Typing rules for our fragment of λ_P . The

typing context Θ is standard.

Figure 7: Big step semantics for our fragment of λ_P . Error propagation rules are omitted.

2.1 Properties of Regular Languages

Our type safety proofs for languages S and P and our translation correctness result all depend on some properties of regular languages. The crucial property is a relationship between string substitution – which is available in any regular expression library – and regular language substitution, which is a corresponding operation on languages instead of strings 5. The decidability of language substitution is what enables static analysis of sanitation algorithms implemented in terms of string replacement

Throughout this section, we fix an alphabet Σ over which strings s and regular expressions r are defined. throughout the paper, $\mathcal{L}\{r\}$ refers to the language recognized by the expression r. This distinction between the expression and its language – typically elided in the literature – makes our definition and proofs about systems S and P more readable.

Lemma 1. Properties of Regular Languages and Expressions. The following are well-known properties of regular expressions which are necessary for our proofs:

- (1): If $s_1 \in \mathcal{L}\{r_1\}$ and $s_2 \in \mathcal{L}\{r_2\}$ then $s_1s_2 \in \mathcal{L}\{r_1r_2\}$
- (2): For all strings s and expressions r, either $s \in \mathcal{L}\{r\}$ or $s \notin \mathcal{L}\{r\}$.
- (3): Regular languages are closed under complements and concatenation.
- (4): The regular expressions correspond bijectively to the regular languages.

Definition 2 (1subst). The function $lsubst(r, s_1, s_2)$ produces a string in which all substrings of s_1 matching r are replaced with s_2 .

Definition 3 (Ireplace). The function Ireplace (r, r_1, r_2) produces a regular expression in which any sublanguage $\mathcal{L}\{r'_1\}$ of $\mathcal{L}\{r_1\}$ satisfying the condition $\mathcal{L}\{r'_1\}\subseteq \mathcal{L}\{r\}$ is replaced with $\mathcal{L}\{r_2\}$.

Lemma 4. Closure and Totality of Replacement. If r, r_1 and r_2 are regular expressions, then $lreplace(r, r_1, r_2)$ is also a regular expression.

Proof. By induction on r and closure properties of regular expressions.

Lemma 5. Substitution Correspondence. If $s_1 \in \mathcal{L}\{r_1\}$ and $s_2 \in \mathcal{L}\{r_2\}$ then $\mathtt{lsubst}(r, s_1, s_2) \in \mathtt{lreplace}(r, r_1, r_2)$.

Proof. The proof proceeds by structural induction on r.

case $r = \alpha$. If $s_1 = \alpha$ then $\alpha \in \mathcal{L}\{r_1\}$ by assumption. Therefore, $\mathtt{lsubst}(r,s_1,s_2) = \mathtt{lsubst}(\alpha,\alpha,s_2) = s_2$ and $\mathtt{lreplace}(r,r_1,r_2) = \mathtt{lreplace}(\alpha,r_1,r_2)$. Since $s_1 = \alpha$ and $\alpha \in \mathcal{L}\{r_1\}$, $r_1 \cong \alpha | r_1'$ for some r_1' . Therefore, $\mathtt{lreplace}(\alpha,r_1,r_2) \cong \mathtt{lreplace}(\alpha,\alpha | r_1',r_2)$ by Lemma X(1). Finally, $s_2 \in \mathcal{L}\{r_2\}$ which implies $s_1 \in \mathcal{L}\{r_2|r'\}$. If $s_1 \neq \alpha$ the $\mathtt{lsubst}(r,s_1,s_2) = s_1$ and $\mathtt{lreplace}(\alpha,r_1,r_2) = r_1$.

case r = a|b. Note that $[a|b/s_1]s_2 = \mathtt{lsubst}(a,\mathtt{lsubst}(b,s_1,s_2),s_2)$ and $\mathtt{lsubst}(b,s_1,s_2) \in \mathtt{lreplace}(b,r_1,r_2)$ by induction. Therefore, $\mathtt{lsubst}(a|b,s_1,s_2) \in \mathtt{lreplace}(a,\mathtt{lreplace}(b,r_1,r_2))$ by induction and the definition of lreplace. Finally, applying definitions once more, $\mathtt{lsubst}(a|b,s_1,s_2) \in \mathtt{lreplace}(a|b,r_1,r_2)$.

case r = ab. By a similar argument to the disjunctive case.

case r = a*. By considering the once unwinding of a*, noting that s_1 and s_2 are finite.

2.2 Safety of the Source and Target Languages

Lemma 6. If $\Psi \vdash S$: stringin[r] then r is a well-formed regular expression.

Proof. The only non-trivial case is S-T-Replace, which follows from 4. $\hfill\Box$

Lemma 7. If $\Theta \vdash P$: regex then $P \Downarrow \mathsf{rx}[r]$ such that r is a well-formed regular expression.

We now prove safety for the string fragment of the source and target languages.

Theorem 8. Safety for the String Fragment of P. Let S be a term in the source language. If $\Psi \vdash S$: stringin[r] then $S \Downarrow rstr[s]$ and rstr[s]: stringin[r], or else S err.

Proof. By induction on the derivation of $\Psi \vdash S : \psi$. The interesting case is S-T-Replace, which requires Lemma C.

- **S-T-Stringin-I:** If $S = \mathsf{rconcat}(S_1, S_2)$: $\mathsf{stringin}[r]$ then $S \Downarrow S$ by S-E-RStr, and $\Psi \vdash S : \psi$ by assumption.
- S-T-Concat: Suppose $S = \operatorname{rconcat}(S_1, S_2)$: stringin $[r_1r_2]$. By inversion, $\Psi \vdash S_1$: stringin $[r_1]$ and $\Psi \vdash S_1$: stringin $[r_2]$. It follows by induction that either S_1 err, S_2 err, or $S_1 \Downarrow \operatorname{rstr}[s_1]$ and $S_2 \Downarrow \operatorname{rstr}[s_2]$ for some $s_1 \in \mathcal{L}\{r_1\}$ and $s_2 \in \mathcal{L}\{r_2\}$. In the latter case $S \Rightarrow \operatorname{rstr}[s_1s_2]$ by S-E-Concat and $\Psi \vdash \operatorname{rstr}[s_1s_2]$: $\operatorname{str}[r_1r_2]$ by 1. In the former cases, S err.
- S-T-Replace: Suppose $S = \text{rreplace}[r](S_1, S_2)$ and $\Psi \vdash S : \text{stringin}[r']$. By inversion $\Psi \vdash S_1 : \text{stringin}[r_1]$ and $\Psi \vdash S_2 : \text{stringin}[r_2]$ such that $\text{lsubst}(r, r_1, r_2) = r'$. By induction, S_1 err, S_2 err or $S_1 \Downarrow \text{rstr}[s_1]$ and $S_2 \Downarrow \text{rstr}[s_2]$ such that In the latter case, we know $\text{lreplace}(r, s_1, s_2) \in \mathcal{L}\{\text{lsubst}(r, r_1, r_2)\}$ by Lemma C; therefore by S-E-Replace, $S \Downarrow \text{rstr}[s]$ such that $s \in \mathcal{L}\{\text{lsubst}(r, r_1, r_2)\} = \mathcal{L}\{r'\}$. So by S-T-String-I, rstr[s] : stringin[r']. In the former cases, S err.
- S-T-Coerce: Suppose $S = \operatorname{rcoerce}[r](S_1)$ and S: stringin[r]. By inversion, $\Psi \vdash S_1$: stringin[r']. By induction, S_1 err or $S_1 \Downarrow \operatorname{rstr}[s]$. In the former case S err by propagation rules. In the latter case we have by property 2 of 1 that $s \in \mathcal{L}\{r\}$ or else $s \notin \mathcal{L}\{r\}$. If $s \in \mathcal{L}\{r\}$ then $\operatorname{rstr}[s]$: stringin[r]. If $s \notin \mathcal{L}\{r\}$ then S err.

Theorem 9. Let P be a term in the target language. If $\Theta \vdash P : \theta$ then $P \Downarrow P'$ and $P' : \theta$.

Proof. The proof proceeds by induction on the typing relation and is trivial give and inversion lemma for the typing relation. We can write up this proof if we end up having enough space...

2.3 Translation Correctness

We now present the main correctness result.

Theorem 10. If $S : \mathsf{rstr}[r]$ then there exists a P such that ||s|| = P and either:

- (a) $P \Downarrow str[s]$ and $S \Downarrow rstr[s]$, and $s \in langr$.
- (b) P err and S err.

Proof. The proof proceeds by induction on the typing relation for S. Throughout the proof, properties from the closure lemma for regular languages are necessary; for brevity, we elide these references.

- S-T-String-I: Let $S = \mathsf{rstr}[s]$ and suppose $\Psi \vdash \mathsf{rstr}[s]$: stringin[r]. Choose $T = \mathsf{string}s$ and note that $[\![S]\!] = P$ by Tr-String. By P-E-String, $P \Downarrow \mathsf{string}s$ and by S-E-String $S \Downarrow \mathsf{rstr}[s]$. Finally, by inversion of S-T-Stringin-I, $s \in \mathcal{L}\{r\}$.
- **S-T-Concat:** Let $S = \operatorname{rconcat}(S_1, S_2)$ and suppose $\Psi \vdash S : \operatorname{stringin}[r_1 r_2]$. By inversion, $\Psi \vdash S_1 : \operatorname{stringin}[r_1]$. It follows by induction that there exists a P_1 such that $[S_1] = P_1$. By a similar argument for S_2 and r_2 , there exists a P_2 such that $[S_2] = P_2$. Choose $P = \operatorname{concat}(P_1, P_2)$.

We first prove property (a). Note that S_1 and P_1 are well typed (nrf ACTUALLY WE DON'T KNOW THAT P_1 IS WELL-TYPED!) and do not result in errors. Therefore, $S_1 \Downarrow \mathsf{rstr}[s_1]$ and $P_1 \Downarrow \mathsf{string}s_1$ for some $s_1 \in \mathcal{L}\{r_1\}$ by theorems 8 and 9 respectively. Similarly, $S_2 \Downarrow \mathsf{rstr}[s_2]$ and $P_2 \Downarrow \mathsf{string}s_2$ for some $s_2 \in \mathcal{L}\{r_2\}$. Therefore, $S \Downarrow \mathsf{rstr}[s_1s_2]$ by S-E-Concat and $\mathsf{concat}(P_1, P_2) \Downarrow \mathsf{string}s_1s_2$ by P-E-Concat. Finally, $s_1s_2 \in \mathcal{L}\{r_1\}r_2$ by 1.

Consider property (b). If S_1 err then P_1 err by induction, and it follows that S err and P err by respective error propagation rules. Similarly, if S_2 err then P_2 err and it follow that S err and P err by induction and propagation.

S-T-Replace: Let $S = \mathsf{rreplace}[r](S_1, S_2)$ and suppose $\Psi \vdash S : \mathsf{stringin}[r']$ for some s. By inversion of S-T-Replace, $\Psi S_1 : \mathsf{stringin}[r_1]$ and $\Psi : \mathsf{stringin}[r_2]$ such that $\mathsf{lsubst}(r, r_1, r_2) = r'$. By induction, there exists some P_1, P_2 such that $[S_1] = P_1, [S_2] = P_2$ and either (a) or (b) holds. If (a) holds then $S_1 \Downarrow \mathsf{rstr}[s_1]$ and $P_1 \Downarrow \mathsf{string}s_1$ for some $s_1 \in \mathcal{L}\{r_1\}$, and similarly for S_2, P_2 and some

 $s_2 \in \mathcal{L}\{r_2\}$. Therefore, by S-E-Replace, $S \downarrow \mathsf{rstr}[s]$ for

some $s = \mathtt{lreplace}(r, s_1, s_2)$. Choose $P = \mathtt{preplace}(r, s_1, s_2)$. By a similar argument and P-E-Replace, $P \Downarrow \mathtt{string}s$ for some $s = \mathtt{lreplace}(r, s_1, s_2)$. What remains to be shown is $\mathtt{lreplace}(r, s_1, s_2) \in \mathcal{L}\{\mathtt{lsubst}(r, r_1, r_2)\}$, which follows from Leamm D since $s_1 \in r_1$ and $s_2 \in r_2$. If (b) holds for S_1 and P_1 , then S err and P err by propagation rules. Similarly, if (b) hols for S_2 and P_2 then S err and P err by propagation rules.

S-T-Coerce: Let $S = \operatorname{rcoerce}[r](S')$ and suppose $\Psi \vdash \operatorname{rcoerce}[r](S)$: stringin[r]. By inversion $\Psi \vdash S'$: stringin[r'] for an arbitrary r'. By induction there exists a P' such that $[\![S']\!] = P'$ and either (a) or (b) holds for S' and P'.

If (a) holds then $S' \Downarrow \operatorname{rstr}[s']$ and $P' \Downarrow \operatorname{string} s'$ for some $s' \in \mathcal{L}\{r'\}$. Note that either $s' \in \mathcal{L}\{r\}$ or $s' \not\in \mathcal{L}\{r\}$ by property 2 of 1. Suppose $s' \in \mathcal{L}\{r\}$. Then rcoerce $[r](S) \Downarrow \operatorname{rstr}[S']$ by S-E-Coerce. Choose $P = \operatorname{rx}[r]P'$ and note that $P \Downarrow \operatorname{string} s'$ by P-E-Coerce. Now suppose $s' \not\in \mathcal{L}\{r\}$. Then S err and P err by P-E-Check-Err and S-E-Coerce-Err.

Finally, if (b) holds then S err and P err by propagation.

Papers that needs to be cited in this section:

- Ur/Web OSDI paper
- Jif?

- OWASP
- XDuce and related papers.
- src?
- Ace or Wyvern paper?
- hotsos?
- Haskell extension paper
- Maybe some popular FOSS libraries/frameworks that do input sanitation?