

## **1) Quicksort**

**a) Show, in the style of the trace given with partition(), how that method partitions the array I, L, O, V, E, A, L, G, O, R, I, T, H, M, S**

**VVV**

a) For partition method, we pick a pivot and utilize two increments. I will use first element as a pivot.

Repeat until  $i$  and  $j$  pointers cross

- scan  $i$  from left to right so long as  $(a[i] < a[lo])$
- scan  $j$  from right to left " "  $(a[j] > a[lo])$
- exchange  $a[i]$  with  $a[j]$

$\boxed{I}$  L O V E A L G O R I T H M S  
 $\downarrow$   $i$  stop  
 $\downarrow$   
 $\downarrow$   
 $\downarrow$   $j$  stop  
 I H O V E A L G O R I T L M S  
 $\downarrow$   $i$  stop  $\downarrow$   $j$  stop as  $a[j] = a[lo]$   
 $\downarrow$   
 I H I V E A L G O R O T L M S  
 $\downarrow$   $i$  stop  $\downarrow$   $j$  stop  
 $\downarrow$   
 $\downarrow$   $j$  stop  
 I H I G E A L V O R O T L M S  
 $\downarrow$   $i$   $\downarrow$   $j$   
 $i$   $j$  kisses ( $i$  stops)  
 swap  $lo$  with  $j$ :

I H I G E A L V O R O T L M S  
 $\boxed{A}$  H I G E  $\boxed{I}$  L V O R O T L M  $\boxed{S}$   
 $\downarrow$   $lo$   $\downarrow$   $hi$

partitioned !!

**b) Show, in the style of the quicksort trace discussed in the book, how quicksort sorts the array I, L, O, V, E, A, L, G, O, R, I, T, H, M, S (for the purpose of this exercise, ignore the initial shuffle.) Compare the best, worst, and average case scenarios for the quicksort algorithm.**

**VVV**

b) For quicksort, we will select the last value as our pivot

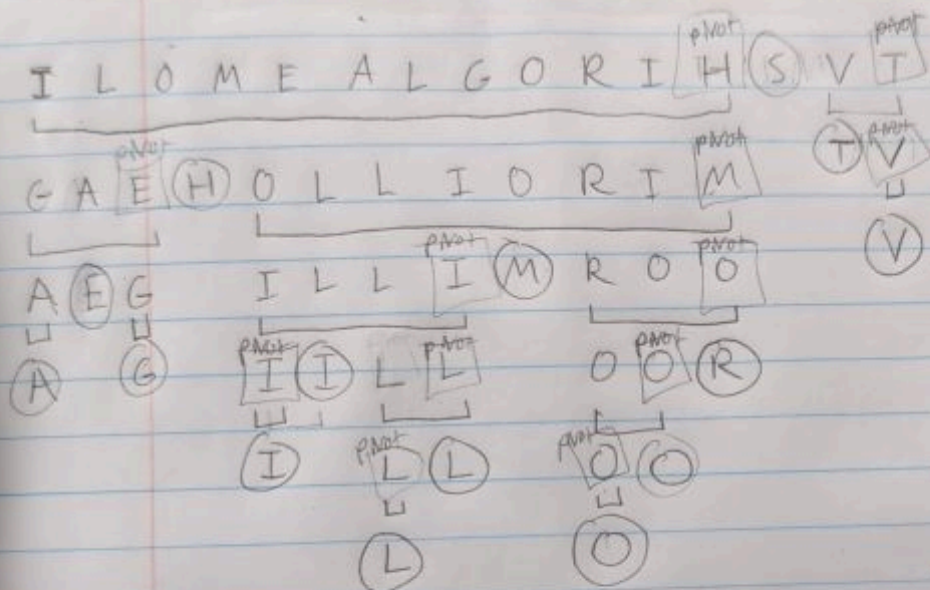
I L O M E A L G O R T T H M S

if  $i > \text{pivot}$  → pass

if  $i \leq \text{pivot}$  →  $j++$

if  $i > j$  →  $\text{Swap}(i, j)$

if  $i == j$  → pass



So the final indices become:

A E G H I L L M O O R S T V

Best case:  $O(n \log(n))$

each subarray must still be sorted after partitioning

Worst case:  $O(n^2)$

occurs when largest or smallest element is picked as the pivot for each run

Avg case:  $O(n \log(n))$

same reason as best case