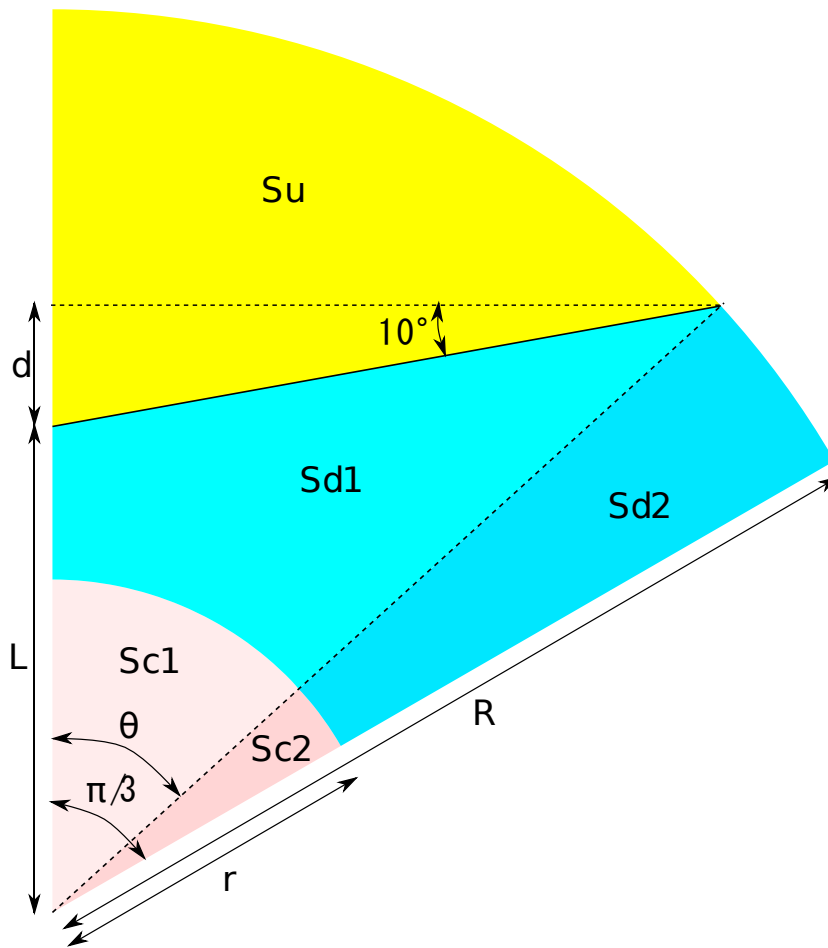


Derivation of the equation to equalize areas of the right upper region and the right lower region of a Tri-Bahtinov mask



$$d = R \cdot \sin \theta \cdot \tan 10^\circ$$

$$L = R \cdot \cos \theta - d = R \cdot (\cos \theta - \sin \theta \cdot \tan 10^\circ)$$

$$(S_u + S_{d1} + S_{d2}) = (R \cdot R - r \cdot r) \cdot (\pi/6)$$

$$(S_u + S_{d1} + S_{c1}) = R \cdot R \cdot \theta/2$$

$$(S_{c1} + S_{c2}) = \pi \cdot r \cdot r/6$$

$$(S_{d2} + S_{c2}) = (1/2) \cdot R \cdot R \cdot (\pi/3 - \theta)$$

$$(S_{d1} + S_{c1}) = (L/2) \cdot R \cdot \sin \theta$$

$$= (1/2) \cdot R \cdot R \cdot (\sin \theta \cdot \cos \theta - \sin \theta \cdot \sin \theta \cdot \tan 10^\circ)$$

$$(S_{d1} + S_{d2}) = (S_{d2} + S_{c2}) + (S_{d1} + S_{c1}) - (S_{c1} + S_{c2})$$

$$= (1/2) \cdot R \cdot R \cdot (\pi/3 - \theta + \sin \theta \cdot \cos \theta - \sin \theta \cdot \sin \theta \cdot \tan 10^\circ) - (\pi/6) \cdot r \cdot r$$

Equation on  $\theta$ :

$$(S_u + S_{d1} + S_{d2}) = 2 \cdot (S_{d1} + S_{d2})$$

$$(R \cdot R - r \cdot r) \cdot (\pi/6) = R \cdot R \cdot (\pi/3 - \theta + \sin \theta \cdot \cos \theta - \sin \theta \cdot \sin \theta \cdot \tan 10^\circ) - (\pi/3) \cdot r \cdot r$$

$$(1 - r \cdot r / (R \cdot R)) \cdot (\pi/6) = \theta - \sin \theta \cdot \cos \theta + \sin \theta \cdot \sin \theta \cdot \tan 10^\circ$$