# Map-Reduce Algorithms

What Can Go Wrong?
Reducer Size and Replication Rate
Mapping Schemas
Matrix Multiplication

Mining of Massive Datasets
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#### Mappers and Reducers

- Map-Reduce job = Map function + Reduce function.
- Map Task = Map-function execution on a chunk of inputs.
- Reduce Task = Reduce-function execution on one or more key-(list of values) pairs.
- Mapper = application of the Map function to a single input.
- Reducer = application of the Reduce function to a single key-(list of values) pair.

### Cost of Map-Reduce Jobs

- There are two principal costs:
  - Computation cost of mappers, reducers, and system.
    - System cost is principally sorting key-value pairs by key and merging them at Reduce tasks.
  - Communication cost shipping key-value pairs from mappers to reducers.
    - Assume Map tasks are executed where their input data resides, so no communication required.
    - Assume every key-value pair has to be moved.

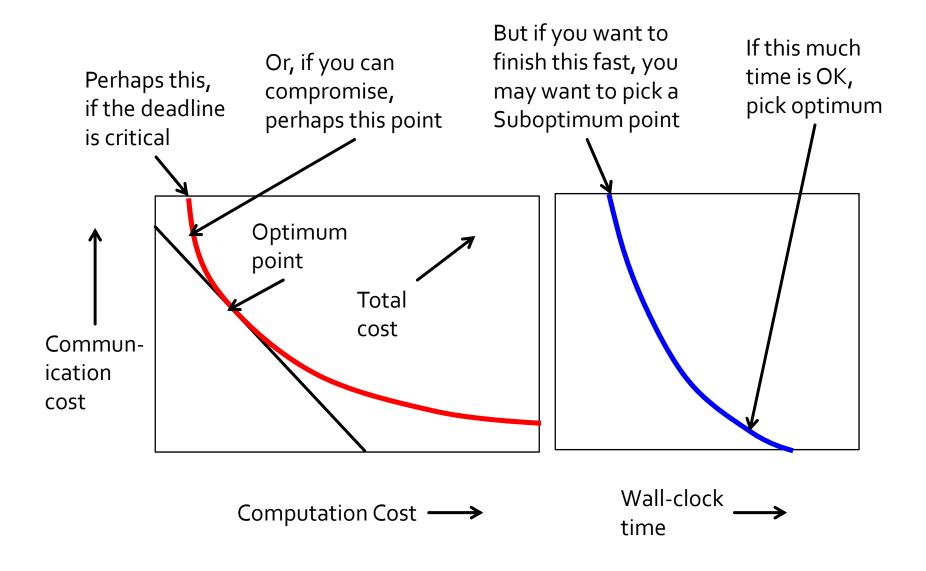
### Cost of Map-Reduce Jobs — (2)

- Computation at the mappers is usually a small fraction of the communication cost and can be neglected.
- System cost of sorting is typically proportional to the communication cost.
- Communication cost often dominates computation cost.

## Cost of Map-Reduce Jobs — (3)

- On a public cloud, you pay for computation and you also pay for communication.
  - Balancing the two is an important part of algorithm design.
- But you also want the job to finish fast, which requires a high degree of parallelism.
- Often, there is a second trade-off, with high parallelism pushing the communication higher than you would like for minimum cost.

#### A Picture of the Trade-Offs



#### Reducer Size – The Hidden Variable

- For some problems, the computation is the same no matter how you partition the problem.
- However, in many cases, the big issue is whether a reducer has too much input to operate in main memory.
  - To get reducers with small input size, you need a lot of communication.
  - Results in a step function of cost when communication gets too low.

### A Common Case

