

$$\tau = c\kappa.$$

$$c = 0, \text{ 则 } \gamma(s) = (\int_0^s (\cos \int_0^u \kappa(t) dt + a) du + b, \pm \int_0^s (\sin \int_0^u \kappa(t) dt + a) du + c)$$

$c > 0$  时, 令  $\theta(s)$  满足  $\theta'(s) = \kappa(s)$ , 从而

$$\begin{aligned} t_\theta &= t_s / \theta_s = n \\ n_\theta &= n_s / \theta_s = -t - cb \\ b_\theta &= b_s / \theta_s = cn \end{aligned}$$

从而  $n_{\theta\theta} + (1 + c^2)n = 0$ . 令  $c_0 = \sqrt{1 + c^2}$ , 则

$$n(\theta) = \cos(c_0\theta)e_1 + \sin(c_0\theta)e_2.$$

解得

$$\begin{aligned} b(\theta) &= \frac{c}{c_0} \sin(c_0\theta)e_1 - \frac{c}{c_0} \cos(c_0\theta)e_2 - \frac{1}{c_0}e_3. \\ t(\theta) &= \frac{1}{c_0} \sin(c_0\theta)e_1 - \frac{1}{c_0} \cos(c_0\theta)e_2 \pm \frac{c}{c_0}e_3. \end{aligned}$$

$\theta = 0$  时

$$\begin{pmatrix} t \\ n \\ b \end{pmatrix} = \begin{pmatrix} 0 & -1/c_0 & \pm c/c_0 \\ 1 & 0 & 0 \\ 0 & -c/c_0 & -1/c_0 \end{pmatrix} \begin{pmatrix} e_1 \\ e_2 \\ e_3 \end{pmatrix}$$

(转换矩阵为正交矩阵, 故应取正号).

此时

$$\begin{aligned} \gamma &= \int n ds \\ &= \frac{\int \left[ \sin \left( \frac{\int_0^u \kappa(s) + c_1}{\sqrt{1 + c^2}} \right) e_1 - \cos \left( \frac{\int_0^u \kappa(s) + c_1}{\sqrt{1 + c^2}} \right) e_2 + ce_3 \right] ds}{\sqrt{1 + c^2}} \end{aligned}$$