

(c) since for Jelinek-Mercer,

$$\text{score} \propto \sum_{w \in Q \cap D} c(w, Q) \log \left(1 + \frac{(1-\lambda) c(w, D)}{\lambda p(w|REF) \times |D|} \right)$$

$$\frac{c(w, D)}{|D|} = \text{const when doubling doc}$$

& $c(w, Q)$ will increase \Rightarrow

score should increase when doubling doc \Rightarrow

\Rightarrow no over constraint

For Dirichlet prior

$$\text{score} \propto \sum_{\substack{w \in d \\ w \in q}} \log \left[1 + \frac{c(w, d)}{\mu p(w|c)} \right] + \kappa \log \frac{\mu}{|d| + \mu} \quad \textcircled{A} \quad \textcircled{B}$$

when double doc, the increase in \textcircled{A} is more than the decrease in $\textcircled{B} \Rightarrow$

\Rightarrow score increases \Rightarrow no over constraints.