

2. (a) For Jelinek-Mercer,

$$p(w|d) = (1-\lambda) \frac{c(w,d)}{|d|} + \lambda p(w|REF)$$

$$\begin{aligned} \log p(q|d) &= \sum_{i=1}^m \log p(q_i|d) = \sum_{i=1}^{|v|} c(w_i, q) \log p(w_i|d) \\ &= \sum_{w \in q} c(w, q) \log p(w|d). \end{aligned}$$

plug in $p(w|d)$ we have

$$\log p(q|d) = \sum_{\substack{w \in q \\ w \in d}} c(w, q) \log \left[(1-\lambda) \frac{c(w,d)}{|d|} + \lambda p(w|REF) \right]$$

$$+ \sum_{\substack{w \in q \\ w \notin d}} c(w, q) \log [\lambda p(w|REF)]$$

$$= \sum_{\substack{w \in q \\ w \in d}} c(w, q) \log \left[(1-\lambda) \frac{c(w,d)}{|d|} + \lambda p(w|REF) \right]$$

$$- \sum_{\substack{w \in q \\ w \notin d}} c(w, q) \log [\lambda p(w|REF)]$$

$$+ \sum_{w \in q} c(w, q) \log [\lambda p(w|REF)]$$