

# CS 181 HW6 2021 CS181

CHARLES ZHANG

TOTAL POINTS

**27 / 25**

## QUESTION 1

### 1 CFG 7 / 5

✓ + **2 pts** Correct solution, and your CFG is unambiguous. You received 2 extra points.

- **0 pts** Correct solution, but your CFG is ambiguous, so you did not get the 2 bonus points.

- **1 pts** Minor mistake, your grammar cannot generate some of the strings in the language. We use following strings to test your solution:

-  $\epsilon$

- ab

- abbb

- b

- bbbb

- **1 pts** Minor mistake, your grammar generates some strings that are not in the given language. We use following strings to test your solution:

- a

- aa

- aab

- aaaabb

- ba

- bba

- baa

- **1 pts** Correct solution, but no explanation provided. You expected a brief explanation that explains how your grammar is designed to correctly represent the language.

- **1 pts** Did not define the start variable. You need to explicitly define which is the start variable.

- **5 pts** No answer provided.

## QUESTION 2

### 2 CFL Pumping Lemma 8 / 8

✓ + **8 pts** Correct or nearly correct

✓ + **1 pts** Appropriate string

✓ + **1 pts** Effective use of constraints on  $vxy$

- **0.5 pts** Does not explicitly state how  $|vxy| \leq p$  is used.

✓ + **2 pts** Clearly shows coverage of all cases

+ **1 pts** Partially shows coverage of all cases

+ **1 pts** Always pump down

+ **3 pts** Correct logic in every case

+ **2 pts** Partially correct logic in cases

+ **1 pts** Incorrect or weak logic in cases

+ **0 pts** No answer

+ **0 pts** Your string is not in the language.

+ **0 pts** Your string can be pumped and remain in the language.

## QUESTION 3

### Language Classification 12 pts

#### 3.1 a $R \cap L$ 2 / 2

✓ + **2 pts** Correct and complete or nearly so.

+ **1 pts** Correct classification.

+ **0.5 pts** Partially correct classification.

+ **1 pts** Correct or nearly correct brief justification.

+ **0.5 pts** Partially correct brief justification.

+ **0 pts** Incorrect

+ **0 pts** No answer.

#### 3.2 b $A = \text{Ambiguous Grammar}$ 2 / 2

✓ + **2 pts** Correct and complete or nearly so.

+ **1 pts** Correct classification.

+ **0.5 pts** Partially correct classification.

+ **1 pts** Correct or nearly correct brief justification.

+ **0.5 pts** Partially correct brief justification.

+ **0 pts** Incorrect

+ 0 pts No answer.

### 3.3 c $\bar{C}$ , C of PDA 2 / 2

- ✓ + 2 pts Correct and complete or nearly correct.
- + 1 pts Correct or nearly correct classification.
- + 0.5 pts Partially correct classification.
- + 1 pts Correct or nearly correct brief justification.
- + 0.5 pts Partially correct brief justification.
- + 0 pts Incorrect
- + 0 pts No answer.

### 3.4 d G of Unambiguous CFG 2 / 2

- ✓ + 2 pts Correct / Nearly Correct.
- + 1 pts Correct Classification.
- + 0.5 pts Partially Correct Classification.
- + 1 pts Correct Justification.
- + 0.5 pts Partially Correct Justification.
- + 0 pts Incorrect
- + 0 pts No answer.

### 3.5 e $\bar{L}$ 2 / 2

- ✓ + 2 pts Correct / Nearly Correct.
- + 1 pts Correct Classification.
- + 0.5 pts Partially Correct Classification.
- + 1 pts Correct Justification.
- + 0.5 pts Partially Correct Justification.
- + 0 pts Incorrect.
- + 0 pts No Answer.
- 0.25 pts L and  $\bar{L}$  cannot be FSL.

### 3.6 f X 2 / 2

- ✓ + 2 pts Correct / Nearly Correct.
- + 1 pts Correct Classification.
- + 0.5 pts Partially Correct Classification.
- + 1 pts Correct Justification.
- + 0.5 pts Partially Correct Justification.
- + 0 pts Incorrect.
- + 0 pts No Answer.

# CS 181 Homework 6

Charles Zhang, 305-413-659

May 9, 2021

## Problem 1

$$\Sigma = \{a, b\}$$
$$\{a^i b^j \mid 0 \leq i \leq j\}$$

**CFG:**

$G = (V, \Sigma, R, S)$ , with  $V = \{S, A, B\}$  and  $R$  = the rule set below.

$$S \rightarrow \epsilon \mid aAb$$

$$A \rightarrow aAb \mid B \mid \epsilon$$

$$B \rightarrow bB \mid b$$

**Justification:**

The specified language is made up of strings of  $as$  followed by  $bs$ , where the number of  $as$  is less than or equal to the number of  $bs$ . This CFG works by first accepting the empty string. Otherwise, it builds strings with equal numbers of  $as$  and  $bs$  using the rule  $A \rightarrow aAb$ , and then adds extra  $bs$  using the rule  $B \rightarrow bB \mid b$ . This allows us to say that there will be at least as many  $bs$  as  $as$ .

I believe this CFG is unambiguous, since there is only one way to generate a given number of  $as$  in the string using  $A \rightarrow aAb$ . Due to this, any extra  $bs$  must be generated using the rule  $B \rightarrow bB \mid b$ , which means there is also only one way to generate a given number of  $bs$  in the string. Finally, the empty string can only be generated by the rule  $S \rightarrow \epsilon$ . Taken together, this tells us there is only one way to generate each valid string.

## 1 CFG 7 / 5

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- 0 pts Correct solution, but your CFG is ambiguous, so you did not get the 2 bonus points.

- 1 pts Minor mistake, your grammar cannot generate some of the strings in the language. We use following strings to test your solution:

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- 1 pts Correct solution, but no explanation provided. You expected a brief explanation that explains how your grammar is designed to correctly represent the language.

- 1 pts Did not define the start variable. You need to explicitly define which is the start variable.

- 5 pts No answer provided.

## Problem 2

$$\Sigma = \{0, 1\}$$
$$L = \{xx^Rx \mid x \in \Sigma^*\}$$

**Proof (by contradiction):**

- Assume  $L$  is context-free.
- Let  $p$  be the pumping length given by the pumping lemma for CFLs.
- Let  $s = 0^p 1^p 1^p 0^p 1^p$ , noting that  $s \in L$ , as we can say that the substring  $x = 0^p 1^p$  and, as proved in HW1,  $x^R = 1^p 0^p$ , therefore,  $s = xx^Rx$ .
- With  $s$  being a member of  $L$  and having a length greater than  $p$ , the pumping lemma for CFLs guarantees that  $s$  can be split into five substrings of the form  $s = uvxyz$  such that
  - <sup>(1)</sup>for each  $i \geq 0$ ,  $uv^i xy^i z \in L$ ,
  - <sup>(2)</sup> $|vy| > 0$ , and
  - <sup>(3)</sup> $|vxy| \leq p$ .
- Note that  $s$  can be split into 3 substrings of length  $2p$ ,  $A = x$ ,  $B = x^R$ , and  $C = x$ .
- Note that each substring can be split into 2 substrings such that one substring contains  $p$  0s and the other contains  $p$  1s.
  - We will call these substrings  $A_0, A_1, B_0, B_1, C_0$ , and  $C_1$ , such that  $s = A_0 A_1 B_0 B_1 C_0 C_1$ .
- By condition (3) of the pumping lemma for CFLs, we know that  $|vxy|$  has length of at most  $p$ .
- This tells us that there are 2 general cases: one where  $|vxy|$  falls entirely within one of the substrings  $A, B$ , or  $C$ , and one where it doesn't.
- Create the string  $s'$  by pumping  $s$  using  $i = 2$ .
- Case 1:
  - In the case that  $vxy$  lies within 1 of the 3 substrings  $A, B$ , and  $C$ , there are 2 subcases:  $vxy$  is made up entirely of 1 symbol or  $vxy$  contains both symbols.
  - Case 1a:
    - \* In the first subcase, we know that one of  $A_0, A_1, B_0, B_1, C_0$ , or  $C_1$  will be pumped.
    - \* This means the total number of 0s or 1s will increase, while the other stays constant.
    - \* Note that all runs of 0s and 1s are separated by a run of the other symbol.
    - \* If the number of 0s or 1s increases, we know that the length of exactly 1 such run will increase.
    - \* However, in order to satisfy the condition that  $w = xx^Rx$ , this increase in length must be reflected in the other 2 runs of that symbol as well.
    - \* Therefore, the resulting string  $s'$  will not be in  $L$ .
  - Case 1b:
    - \* In the second subcase, we know a string containing 1 or more 0s and 1 or more 1s will be pumped.

- \* In this case, a pattern of alternating runs of 0s and 1s will emerge within the substring.
- \* However, this pattern will not occur in either of the other substrings.
- \* This clearly breaks the condition that  $w = xx^Rx$ .
- This tells us that the pumped string  $s'$  must no longer be a member of  $L$ .
- This tells us that pumped strings of this case fail the pumping lemma for CFLs.
- Case 2:
  - In the case that  $vxy$  lies between 2 of the 3 substrings  $A$ ,  $B$ , and  $C$ , there are 2 subcases:  $vxy$  lies between  $A$  and  $B$ , and  $vxy$  lies between  $B$  and  $C$ .
  - In both of the subcases, the substring disjoint from  $vxy$  is equal to  $x$ .
  - We know this substring remains the same between  $s$  and  $s'$ .
  - Note that  $x$  has an equal number of 0s and 1s, and, since strings in  $L$  have the form  $w = xx^Rx$ , we know that both  $s$  and  $s'$  must also have an equal number of 0s and 1s.
  - Since the substrings of the form  $A_0, A_1$ , etc. are each of length  $p$ , we know that, at most,  $vxy$  overlaps 2 such substrings.
  - Case 2a:
    - \*  $vxy$  crosses from  $A$  to  $B$ .
    - \* By the constraint that  $vxy$  only overlaps 2 of  $A_0, A_1$ , etc., we know that  $vxy$  must cross from  $A_1$  to  $B_1$ .
      - More explicitly, it is impossible for  $vxy$  to overlap with  $A_0$  or  $B_0$ .
    - \* This tells us that  $vxy$  is made up entirely of 1s
    - \* As a result, pumping  $vxy$  increases the number of 1s in the string, but keeps the number of 0s constant.
    - \* This violates the condition that the string  $s'$  has an equal number of 0s and 1s, telling us that  $s' \notin L$ .
  - Case 2b:
    - \*  $vxy$  crosses from  $B$  to  $C$ .
    - \* By the constraint that  $vxy$  only overlaps 2 of  $A_0, A_1$ , etc., we know that  $vxy$  must cross from  $B_0$  to  $C_0$ .
      - More explicitly, it is impossible for  $vxy$  to overlap with  $B_1$  or  $C_1$ .
    - \* This tells us that  $vxy$  is made up entirely of 0s
    - \* As a result, pumping  $vxy$  increases the number of 0s in the string, but keeps the number of 1s constant.
    - \* This violates the condition that the string  $s'$  has an equal number of 0s and 1s, telling us that  $s' \notin L$ .

- Both possible subcases fail to create a string  $s' \in L$  after pumping, telling us that pumped strings of this case fail the pumping lemma for CFLs.
- Both possible cases fail the pumping lemma for CFLs, which contradicts the assumption that  $L$  is context-free  $\Rightarrow \Leftarrow$

## 2 CFL Pumping Lemma 8 / 8

- ✓ + 8 pts Correct or nearly correct
- ✓ + 1 pts Appropriate string
- ✓ + 1 pts Effective use of constraints on  $vxy$ 
  - 0.5 pts Does not explicitly state how  $|vxy| \leq p$  is used.
- ✓ + 2 pts Clearly shows coverage of all cases
  - + 1 pts Partially shows coverage of all cases
  - + 1 pts Always pump down
  - + 3 pts Correct logic in every case
  - + 2 pts Partially correct logic in cases
  - + 1 pts Incorrect or weak logic in cases
  - + 0 pts No answer
  - + 0 pts Your string is not in the language.
  - + 0 pts Your string can be pumped and remain in the language.



## Problem 3

$R$  and  $S$  are FSLs

$C$  is a language which can be represented by a PDA

$G$  is a language which can be represented by an unambiguous CFG

$A$  is a language which can be represented by an ambiguous CFG

$I$  is an inherently ambiguous CFL

$L$  is a language which *cannot* be represented by a CFG

$X$ , given that  $X \cup S = L$

1 FSL | 2 CFL and not FSL | 3 Inherently Ambiguous CFL | 4 Non-CFL

**a)**  $R \cap L$ : It could be a non-CFL; so it could be 1, 2, 3, or 4. Since  $L$  is a non-CFL language, we can't apply any closure properties to narrow it down any further.

**b)**  $A$ : It could be 1, 2, or 3. Languages that can be represented by CFGs are CFLs by definition. If all we know is that  $A$  can be represented by an ambiguous CFG, we have no indication of if  $A$  is inherently ambiguous or not. In addition, we have no indication of if  $A$  is strictly a CFL.

**c)**  $\bar{C}$ : It could be 1, 2, 3, or 4. As discussed in lecture, languages that can be represented by a PDA are CFLs, which are not closed under complementation, so we have no indication of what the resulting language may be.

**d)**  $G$ : It could be 1 or 2. If  $G$  can be represented by an unambiguous CFG, then it's a CFL, and it's obviously not inherently ambiguous or non-CFL. However, FSLs are a subset of CFLs, so it may be an FSL.

**e)**  $\bar{L}$ : It could be 2, 3, or 4. Since FSLs are closed under complementation, and  $L$  cannot be represented by a CFG (meaning it's definitely not an FSL),  $\bar{L}$  can't be an FSL. CFLs and non-FSLs don't have the same restrictions, so it is possible for  $\bar{L}$  to be one of them.

**f)**  $X$ : It must be 4. Since CFLs and FSLs are closed under union, if  $X$  was a CFL or FSL, the result of unioning it with  $S$ , an FSL, would be a CFL or FSL. Instead, it's a non-CFL, so  $X$  must be a non-CFL too.

### 3.1 a R intersect L 2 / 2

- ✓ + 2 pts Correct and complete or nearly so.
- + 1 pts Correct classification.
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**f)**  $X$ : It must be 4. Since CFLs and FSLs are closed under union, if  $X$  was a CFL or FSL, the result of unioning it with  $S$ , an FSL, would be a CFL or FSL. Instead, it's a non-CFL, so  $X$  must be a non-CFL too.

### 3.2 b A = Ambiguous Grammar 2 / 2

- ✓ + **2 pts** Correct and complete or nearly so.
  - + **1 pts** Correct classification.
  - + **0.5 pts** Partially correct classification.
  - + **1 pts** Correct or nearly correct brief justification.
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  - + **0 pts** Incorrect
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### 3.3 c $\bar{C}$ , C of PDA 2 / 2

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**f)**  $X$ : It must be 4. Since CFLs and FSLs are closed under union, if  $X$  was a CFL or FSL, the result of unioning it with  $S$ , an FSL, would be a CFL or FSL. Instead, it's a non-CFL, so  $X$  must be a non-CFL too.

3.5 e  $L\bar{L}$  2 / 2

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**d)**  $G$ : It could be 1 or 2. If  $G$  can be represented by an unambiguous CFG, then it's a CFL, and it's obviously not inherently ambiguous or non-CFL. However, FSLs are a subset of CFLs, so it may be an FSL.

**e)**  $\bar{L}$ : It could be 2, 3, or 4. Since FSLs are closed under complementation, and  $L$  cannot be represented by a CFG (meaning it's definitely not an FSL),  $\bar{L}$  can't be an FSL. CFLs and non-FSLs don't have the same restrictions, so it is possible for  $\bar{L}$  to be one of them.

**f)**  $X$ : It must be 4. Since CFLs and FSLs are closed under union, if  $X$  was a CFL or FSL, the result of unioning it with  $S$ , an FSL, would be a CFL or FSL. Instead, it's a non-CFL, so  $X$  must be a non-CFL too.

3.6 f X 2 / 2

✓ + 2 pts Correct / Nearly Correct.

+ 1 pts Correct Classification.

+ 0.5 pts Partially Correct Classification.

+ 1 pts Correct Justification.

+ 0.5 pts Partially Correct Justification.

+ 0 pts Incorrect.

+ 0 pts No Answer.