Homework 2: assigned 10/14, LATEST due date 10/21 9 am (all pacific times)

All exercises that require an algorithm:

Write the algorithm in bullet form

Prove the correctness of your algorithm in bullet form

Analyze its time complexity

Justify the correctness of your time complexity

- 1. Exercise 8 b on Page 70 "You're doing some stress testing ..."
- 2. Exercise 5 on Page 108 "A binary tree is a rooted tree"
- 3. Exercise 7 on page 108 "Some friends of yours work on wireless networks...."
- 4. Exercise 10 on page 110 "A number of art museums around the country"
- 5. Suppose that you are given an algorithm as a blackbox. You cannot see how it is designed. The blackbox has the following properties: If you input any sequence of real numbers, and an integer \mathbf{k} , the algorithm will answer YES or NO indicating whether there is a subset of the numbers whose sum is exactly \mathbf{k} . Show how to use this blackbox to find the subset whose sum is \mathbf{k} , if it exists.

You should use the blackbox O(n) times (where n is the size of the input sequence).

- 6. An array of n elements contains all but one of the integers from 1 to n+1.
- a. Give the best algorithm you can for determining which number is missing if the array is sorted, and analyze its asymptotic worst-case running time.
- b. Give the best algorithm you can for determining which number is missing if the array is not sorted, and analyze its asymptotic worst-case running time.