

1/6: Introduction

- Start early, develop incrementally
- scp Desktop/Archive.zip charlesx@cs32.seas.ucla.edu:
- ssh charlesx@cs32.seas.ucla.edu
- unzip -j -a -d hw5 Archive.zip
- cd hw3
- ls
- g32 -o test *.cpp
- **#include <iostream>**
- **#include <cstdlib>**
- **#include <cmath>**
- **using namespace std;**
-
- **const double PI = 4 * atan(1.0);**
-
- **class Circle {**
 - **public:**
 - **Circle(double x, double y, double r);**
 - **void scale(double factor);**
 - **void draw() const;**
 - **double radius() const;**
 - **private:**
 - **// Class Invariants: m_r > 0**
 - **double m_x;**
 - **double m_y;**
 - **double m_r;**
- **};**
-
- **double area(const Circle& x);**
-
- **Circle::Circle(double x, double y, double r)**
- **: m_x(x), m_y(y), m_r(r)) { // member initialization list**
 - **if (r <= 0) {**
 - **cout << "Cannot create circle with radius " << r << endl;**
 - **exit(1);**
 - **}**
- **}**
-
- **bool Circle::scale(double factor) {**
 - **if (factor <= 0) {**
 - **return false;**
 - **}**

- `m_r *= factor;`
 - `return true;`
- `}`
-
- `void Circle::draw() const {`
 - ... code to draw the circle ...
- `}`
-
- `double Circle::radius() const {`
 - `return m_r;`
- `}`
-
- `double area(const Circle& x) {`
 - `return PI * x.radius() * x.radius();`
- `}`
-
- `int main() {`
 - `Circle blah(8, -3, 3.7);`
 - `Circle c(2, -5, 10);`
 - `c.scale(2);`
 - `c.draw();`
 - `cout << area(c) << endl;`
 - `cout << c.radius() << endl;`
 -
 - `double ff;`
 - `cin >> ff;`
 - `if (!c.scale(ff)) {`
 - ... error ...
 - `}`
- `} // guaranteed to return 0 if no number specified`
- Interface (what we can do) vs. Implementation (how do we do it)

1/8: Linking

- myapp.cpp:
 - **#include <iostream>**
 - **using namespace std;**
 - **void f(double x);** // needed to declare
 - **int main() {**
 - **double a = 3;**
 - **f(a);**
 - **cout << a;**
 - **}** // defines main
 - // needs f, cout, <<
- stuff.cpp
 - **#include <cmath>**
 - **using namespace std;**
 - **void f(double x) {**
 - **...**
 - **sin(x)**
 - **...**
 - **}** // defines f
 - // needs sin
- Libraries - collections of object files with code for library functions
 - Defines sin, cos, exponential, cout, cin, >>, <<, etc
 - Needs nothing
- Object files combine with libraries to create an executable file
 - Object file → executable is called the linker
- Nothing can be defined more than once → linker error
- Every need must be satisfied by some definition
- There must be exactly one main routine
- Convention - 2 files per C++ class
- myapp.cpp:
 - **#include "circle.h"**
 -
 - **int main() {**
 - **Circle c(-2, 5, 10);**
 - **c.draw();**
 - **}**
- **circle.h:** // class declaration
 - **class Circle {**
 - **public:**
 - **Circle(,,);**
 - **void draw() const;**
 - **private:**
 - **double m_x;**

- };
-
- **double area(Circle x);**
- **circle.cpp:** // implementation
 - **#include "circle.h"**
 - **#include <cmath>**
 - **using namespace std;**
 -
 - **Circle::Circle(,,)**
 - **: __ {**
 - ...
 - **}**
 -
 - **Circle::void draw() const {**
 - **sin(...);**
 - **}**
 -
 - **double area(Circle x) {**
 - ...
 - **}**
- **-o myapp myapp.cpp stuff.cpp** (no header files listed)
- Don't **#include ____.**cpp

1/13: Steps of Construction and Resource Management

- Steps of construction:
 - 1. -----
 - 2. Construct the data members, using the member initialization list; if a member is not listed:
 - If a data member is of a built in type, it is left uninitialized
 - If a data member is of a class type, the default constructor is called for it; error if there is none
 - If you declare no constructor for a class, the compiler writes a default constructor for you
 - 3. Execute the body of the constructor
- **class Circle {**
 - **public:**
 - **Circle(double x, double y, double r);**
 - ...
 - **private:**
 - **double m_x;**
 - **double m_y;**
 - **double m_r;**
- **};**
- **Circle::Circle(double x, double y, double r) : m_x(x), m_y(y), m_r(r) {**
 - **if (r <= 0) {**
 - **cerr << "...." << endl;**
 - **exit(1);**
 - **}**
- **}**
- **class StickFigure {**
 - **public:**
 - **StickFigure(double bl, double headDiameter, string nm, double hx, double hy);**
 - ...
 - **private:**
 - **string m_name;**
 - **Circle m_head;**
 - **double m_bodyLength;**
- **};**
- **StickFigure::StickFigure(double bl, double headDiameter, string nm, double hx, double hy) : m_name(nm), m_head(hx, hy, headDiameter/2), m_bodyLength(bl) {**

// must have m_head in initialization list, since Circle has no default constructor, and will error out if in the body of the constructor, m_name is in this list for performance reasons

- **if (bl <= 0) {**
 - **cerr << "....." << endl;**
 - **exit(1)**
 - **}**
- **}**
- Common to use member initialization lists to do as much of the initialization as possible
- **void f(String t) {**
 - **String u("Wow");**
 - **...**
- **}**
- **void h() {**
 - **String s = "Hello";**
 - **f(s);** // constructing a String using another String, needs a copy constructor
 - **...**
- **}**
- **int main() {**
 - **String t;**
 - **for (...)**
 - **h();**
 - **...**
- **}**
- **class String {**
 - **public:**
 - **String(const char* value = "");** // makes value "" if there is no argument provided (default parameter value), only works for parameters at the end
 - **String(const String& other);** // copy constructor
 - **String& operator=(const String& rhs);**
 - **~String();**
 - **private:** // Class Invariants: m_text points to a dynamically allocated array of m_len+1 characters
 - **m_len >= 0**
 - **m_text[m_len] == '\0'**
 - **char* m_text;**
 - **int m_len;**
- **};**

- **String::String(const char* value)** { // do not repeat the default parameter value(s) here
 - **m_len = strlen(value);**
 - **m_text = new char[m_len + 1];** // must dynamically allocate a new array, otherwise you risk the original array being changed, therefore changing string's m_text's value unintentionally
 - **strcpy(m_text, value);**
- }
- **String::String(const String& other)** {
 - **m_len = other.m_len;** // allowed
 - **m_text = new char [m_len+1];**
 - **strcpy(m_text, other.m_text)**
- }
- **String& String::operator=(const String& rhs)** { // by convention, this returns the new value of the left hand side, return a reference to the object
 - **delete [] m_text;**
 - **m_len = rhs.m_len;**
 - **m_text = new char[m_len+1];**
 - **strcpy(m_text, rhs.m_text);**
 - **return *this;**
- }
- **String::~~String()** { // ensure that all dynamically allocated objects are deleted when their local counterparts move out of scope
 - **delete [] m_text;** // make sure you match the form of delete to the form of new used (plain vs. array)
- }

1/15: Copy Constructors and Assignment Operators

- If you don't declare a copy constructor for a type, the compiler writes one for you
 - This copy constructor is made by copying all of the members
 - Creates problems with pointers:
 - Changing a value being pointed to inside a function that uses a copy also changes the original object
 - When other functions return, the destructor is called, and the value being pointed at is destructed
- If you write a destructor for a class, you likely have to write a copy constructor and assignment operator too
- Ok for any member functions to access private members of other objects of that class
- The copy constructor cannot be passed by value, as passing by value uses the copy constructor
- Assignment is not the same as the copy constructor

1/17: Discussion 1

- leetcode.com
- Dynamic Memory Allocation
 - Static memory allocation is inflexible
 - Assigns memory when compiling
 - **new** will automatically allocate the sequential memory space for the requested data type and size and return the starting address of the allocated memory space
 - Variables allocated with **new** will remain in the memory until deleted with **delete**
 - Dynamically allocated objects do not get deleted by the default destructor
- Copy Constructors
 - **School::School(const School &aSchool) {**
 - **m_name = aSchool.m_name;**
 - **m_numStudents = aSchool.m_numStudents;**
 - **m_students = new Students[m_numStudents]**
 - **for (int i = 0; i < m_numStudents; i++)**
 - **m_students[i] = aSchool.m_students[i];**
 - **}**
- Assignment Operator
 - **School& School::operator=(const School &aSchool) {**
 - **if (this != &aSchool) {**
 - **m_name = aSchool.m_name;**
 - **m_numStudents = aSchool.m_numStudents;**
 - **delete [] m_students;**
 - **m_students = new m_students[m_numStudents]**
 - **for (int i = 0; i < m_numStudents; i++)**
 - **m_students[i] = aSchool.m_students[i];**
 - **}**
 - **return *this;**
 - **}**

1/22: Linked Lists

- Arrays limited by methods of resizing and inserting items into the middle of the array
- **struct Node {**
 - **int value;**
 - **Node* next;**
- **};**
- **Node* head;**
- **Node* ptr = head**
- **while (ptr != nullptr) {**
 - **cout << ptr->value << endl;**
 - **ptr = ptr->next;**
- **}**
- **for (Node* p = head; p != nullptr; p = p->next) {**
 - **cout << p->value << endl;**
- **}**
- Usually preceded by a pointer (head) to the first element of the list
- Square bracket operators not valid
- When following a pointer, make sure it has previously been given a value and make sure that p is not the null pointer
- **Node* p;**
- **for (p = head; p != nullptr && p->value != 42; p = p->next) // evaluate left to right**
 - **;**
- **if (p != nullptr) {**
 - **cout << p->value << endl;**
- **} else {**
 - **cout << "There's no 42" << endl;**
- **}**
- **Node* p;**
- **for (p = head; p != nullptr && p->value != 42; p = p->next)**
 - **;**
- **if (p != nullptr) {**
 - **Node* newGuy = new Node**
 - **newGuy->value = 37;**
 - **newGuy->next = p->next;**
 - **p->next = newGuy; // order matters, set new node's values first**
- **}**

1/24: Linked Lists (cont.) and Aliasing

- Check normal case (middle), empty list, and boundary cases (first and last)
- **struct Node** { // doubly linked list
 - **int value;**
 - **Node* next;**
 - **Node* prev;**
- }
- **void transfer(Account& from, Account& to, double amt) {**
 - **if (&from != &to) {**
 - **if (from.balance >= amt) {**
 - **from.debit(amt);**
 - **to.credit(amt);**
 - **if (amt >= 10000) {**
 - **fileForm(...) {**
 - }
 - **} else {**
 - **cout << << endl;**
 - **}**
 - **}**
- **}**

1/27: Stacks and Queues

- Stack/LIFO:
 - Create an empty stack
 - Push an item onto the stack
 - Pop an item from the stack, undefined on an empty stack
 - The top of the stack keeps the same position
 - Look at the top item in the stack, undefined on an empty stack
 - Is the stack empty?
 - Maybe:
 - How many items are in the stack (C++ has)
 - Look at any item in the stack (C++ doesn't have)
- **#include <stack>**
- **using namespace std;**
- **int main() {**
 - **stack<int> s;**
 - **s.push(10);**
 - **s.push(20);** // adds 20 to top of stack
 - **int n = s.top()** // returns the top item of the stack
 - **s.pop();** // removes the top item of the stack, no return value
 - **if (!s.empty())** // asks if the stack is empty
 - **cout << s.size() << endl;**
- **}**
- Using a stack signifies that you are only using the top element
- Queue/FIFO:
 - Has a front/head and back/tail, 2 active ends
 - Create an empty queue
 - Enqueue an item (put it in the queue), can fail if there is a limited capacity
 - Dequeue an item (remove it from the queue), can fail if the queue is empty
 - Look at the front item in the queue
 - Is the queue empty?
 - Maybe:
 - How many items are in the queue
 - Look at any item in the queue
- **#include <queue>**
- **using namespace std**
- **int main() {**
 - **queue<int> q;**
 - **q.push(10);** // enqueues item
 - **q.push(20);**
 - **int n = q.front();** // n is 10

- `q.pop();`
 - `if(!q.empty())`
 - `cout << q.size() << endl;`
 - `cout << q.back() << endl;`
- `}`
- Queues and stacks have no limited capacity in C++
- String → numerical operations
 - Convert infix to postfix
 - If you hit an operand you append it to the result sequence
 - If you hit an operator and the operator stack is empty, push it onto the stack
 - Else if the top of the stack is an open parenthesis, push the operator
 - Else if the precedence of the current operator is greater than the operator at the top of the stack, push it
 - Else pop the top of the stack, appending it to the result sequence, and check again
 - Open parenthesis: always push
 - Close parenthesis: while top of stack is not an open parenthesis (operator) pop it and append it to the result sequence
 - Pop the open parenthesis
 - At end, pop each operator and append it to the sequence
 - Push operands onto a stack
 - When you hit an operator, you pop the operands and then push the result onto the stack

1/29: Inheritance

- Linked List vs. Array implementation of stacks
 - Harder to expand capacity with the array version
 - The array version takes up less memory
 - List version takes part in a lot of allocations and deallocations
- Linked List vs. Array implementation of queues
 - Use a doubly linked list for list implementation
 - Array:
 - Head and a tail (1 past the last element)
 - # items in queue is tail - head
 - When hit end of array, you can shift everything back to the beginning of the array
 - Downside if there are a lot of items constantly, many shifts
 - Can also wrap around to beginning of array - circular array
 - Head = tail if the list is empty or full
 - Make a size variable
 - Lists are easier when implemented as a doubly linked list
- Circular doubly linked lists are better for when you need to be able to insert/remove anywhere
 - Every node was guaranteed to have a node before and after it
 - Not very beneficial for queue implementation
- Inheritance:
- **class Circle {**
 - **void move(double xnew, double ynew);**
 - **void draw() const;**
 - **double m_x;**
 - **double m_y;**
 - **double m_r;**
- **};**
- **class Rectangle {**
 - **void move(double xnew, double ynew);**
 - **void draw() const;**
 - **double m_x;**
 - **double m_y;**
 - **double m_dx;**
 - **double m_dy**
- **};**
- **Circle ca[100];**
- **Rectangle ra[100];**
- **for (int i = 0; i < ...; i++)**

- `ca[i].draw();`
- `for (int i = 0; i < ...; i++) {`
 - `ra[i].draw();`
- `void f(Circle& x) {`
 - `x.move(10, 20);`
 - `x.draw();`
- `}`
- `void f(Rectangle& x) {`
 - `x.move(10, 20);`
 - `x.draw();`
- `}`
- This code contains a lot of duplicate code, and adding new classes is tedious and error prone
- `class Shape { // Shape is a superclass/base class of Circle and Rectangle`
 - `void move(double xnew, double ynew);`
 - `void draw() const;`
 - `double m_x;`
 - `double m_y;`
- `};`
- `class Circle : public Shape { // Circle and Rectangle are a subclass/derived classes of Shape`
 - `void draw() const;`
 - `double m_r;`
- `};`
- `class Rectangle : public Shape {`
 - `void draw() const;`
 - `double m_dx;`
 - `double m_dy`
- `};`
- `void Shape::move(double xnew, double ynew) {`
 - `m_x = xnew;`
 - `m_y = ynew;`
- `}`
- `Shape* pic[100];`

- **pic[0] = new Circle;** // if you have a pointer/reference of a derived type, it can be automatically converted to a pointer/reference of the base type
- **pic[1] = new Rectangle;**
- **pic[2] = new Circle;** // heterogeneous collection
- **for (int i = 0; i <...; i++) {**
 - **pic[i]->draw();**
- **}**
- **Circle c;**
- **f(c);** // x has to be another name for a Shape object
- **c.move(30, 40);** // Circle doesn't have a move function, compiler moves up and searches its base class

1/31: Discussion 2

- **Linked Lists**
 - Minimum:
 - Key component as unit: Node with a value and pointer to the next Node
 - Head pointer → points to the first term
 - Loop-free (except in circular linked list)
 - Regular Operations:
 - Insertion, Search, Removal
 - Pros and cons:
 - Efficient insertion, flexible memory allocation, simple implementation
 - Arrays have to occupy contiguous memory locations
 - High complexity of search
 - Insertion:
 - Steps: Create a new Node, make its next pointer point to the first item, make the head pointer point to the new Node
 - Search:
 - Steps: Find matching Node and return, if no match then return
 - Removal:
 - Remember to set the previous Node's next pointer to point to the Node following the deleted Node
 - Consider what happens if the selected Node is the head or the last Node in the list
 - Suggestions:
 - Draw pictures and carefully trace through your code
 - Check any operations for the beginning of the list, end of the list, empty lists, and one-element lists
- **Stack**
 - FILO: First in, last out
 - A standard stack implementation:
 - push() and pop()
 - Other methods: top(), count()
 - Applications:
 - Stack memory: function call
 - Check expressions: matching brackets
 - Depth-first graph search
 - How do you implement stacks with linked lists?
 - push(): Insert Node before head
 - pop() : Remove head and return the head value
 - top(): Read head Node
 - count(): Maintain a private int data member to keep track
- **Queue**
 - FIFO: First in, first out
 - Basic methods:

- enqueue(), dequeue()
 - front(), back()
 - count()
- Applications:
 - Data streams
 - Process scheduling (DMV service request)
 - Breadth-first graph search
- How to implement queue with linked lists?
- Suggestions on stacks and queues
 - Draw pictures and carefully trace the code
 - Infix to postfix conversion is very important
 - Stacks and queues can be applied to trees/graphs
 - You can use the given Standard Template Library to implement stacks and queues

2/3: Inheritance (cont.)

- Every derived object has a base object embedded in it
 - Base object is constructed first
- Calling a member function of a derived object in a function that takes a base object as the parameter will not compile
 - These kind of functions can only access functions that the base object can definitely access
-
- **void Shape::draw() const {**
 - ... draw a cloud centered at (m_x, m_y) // not the right implementation for derived objects
- **}**
- **void Circle::draw() const {**
 - draw a circle of radius m_r centered at (m_x, m_y)
- **}**
- **void f(Shape& x) {**
 - x.move(10, 20);
 - x.draw();
- **}**
- Static binding vs. dynamic binding
 - Connecting the name and the function
 - Static binding - function decided in compile time - uses Shape's draw()
 - C++ default
 - Dynamic binding - function decided in runtime - uses derived type's draw()
- Use **virtual** to make function dynamically bound
- **class Shape {**
 - **void move(double xnew, double ynew);**
 - **virtual void draw() const;**
 - **double m_x;**
 - **double m_y;**
- **}**
- **Shape::move(...)** // calling the base class' function
- **class Rectangle : public Shape {**
 - **void draw() const;**
 - **virtual double diag() const;**
 - **double m_dx;**

- **double m_dy;**
- **}**
- **double Rectangle::diag() const {**
 - **return sqrt(m_x*m_x + m_y*m_y);**
- **}**
- **class Shape {**
 - **void move(double xnew, double ynew);**
 - **virtual void draw() const = 0;** // function introduced as virtual, but not implemented, pure virtual function
 - **double m_x;**
 - **double m_y;**
- **}**
- You cannot create objects that have pure virtual functions
 - You can create pointers to these objects
 - If an object has at least one pure virtual function, it is an abstract class cannot be constructed)
- Abstract classes still have objects, they are just never created by themselves
- **class Shape {**
 - ...
- **};**
- **class Polygon : public Shape {**
 - ...
 - **~Polygon()** // necessary for Polygon, not Shape
 - **Node* head;**
 - ...
- **};**
- **Shape* sp;**
- **sp = new Polygon**
- **delete sp;** // calls the Shape destructor, not Polygon's, must declare Shape to have a virtual destructor (must also be implemented)
- Destruction: 1) Execute the body of the destructor, 2) Destroy the data members, 3) Destroy the base part
- If a class is designed to be a base class, declare and implement a virtual destructor for that class
- **class Shape {**

- **public:**
 - **Shape(double x, double y)**
 - ...
 - **private:**
 - **double m_x;**
 - **double m_y;**
- **};**
- **Shape::Shape(double x, double y) : m_x(x), m_y(y) {}**
- **class Circle : public Shape {**
 - **public:**
 - **Circle (double x, double y, double r);**
 - ...
 - **private:**
 - **double m_r;**
- **};**
- **Circle::Circle (double x, double y, double r) : m_x(x), m_y(y), m_r(r) {}** // doesn't compile, m_x and m_y are private members of Shape, Circle cannot access them
- Construction: 1) Construct the base part, 2) Construct the data members, 3) Execute the body of the constructor
- **Circle::Circle (double x, double y, double r) : Shape(x, y), m_r(r) {}** // fixed

2/5: Recursion

- Base cases: can be solved without making a recursive call
- Recursive cases: make one or more recursive calls for strictly smaller (closer to a base case) instances of the problem
- Verify there's at least one base case and that each recursive call works towards that base case

- **int arr[5];**
- ...
- **sort(arr, 0, 5);**
- **void sort(int a[], int b, int e) { // sort a[b] to a[e - 1]**
 - **if (e - b > 1) {**
 - **int mid = (b + e) / 2;**
 - **sort(a, b, mid);** // sort left half
 - **sort(a, mid, e);** // sort right half
 - **merge(a, b, mid, e);** // merges sequences b → mid and mid → e that produces a sorted final array
 - **}**
- **}**

- If tracing code, start tracing small, the problem should appear early on
- Divide and conquer - solve the problem by breaking it up (see above)
- The first and the rest - divide collection into first and the rest, then solve and combine
 - Sometimes more convenient to last and the rest

- **bool has(const int a[], int n, int target) {**
 - **if (n <= 0) return false;**
 - **if (a[0] == target) return true;**
 - **return has(a + 1, n - 1, target)**
- **}**

- When you have a function returning a boolean using recursion above (returning the recursive call) make sure the return is not left off

- **bool solve(start, goal) { // base cases: at the goal or surrounded by walls**
 - **if (start == goal) return true;**
 - **// mark this position as visited**
 - **// for each direction {**
 - **// if moving one step in that direction is possible and hasn't been visited {**
 - **// if(solve(pos reached by moving, goal) return true;**
 - **}**
 - **}**
 - **return false;**

2/10: Template Functions and Class Templates

- **int minimum(int a, int b) {**
 - **if (a < b) return a;**
 - **else return b;**
- **}**
- **double minimum(double a, double b) {** // effectively the same code as the int minimum at the C++ language level
 - **if (a < b) return a;**
 - **else return b;**
- **}**
- **int main() {**
 - **int k;**
 - **cin >> k;**
 - **cout << minimum(k, 10) / 2;**
 - **double x;**
 - **...**
 - **double y = 3 * minimum(x * x, x + 10);**
 - **...**
 - **int z = minimum(0, 3 * k - k + 4);**
- **}**
- **template<typename T>** // declare T to be used in template, T is now a placeholder for a type name
- **T minimum(T a, T b) {** // both functions fit into this template
 - **if (a < b) return a;**
 - **else return b;**
- **} // this function can replace both the int and double declarations above**
- “Instantiate the template”
 - You have to match some template
 - The instantiated template compiles
 - The instantiated template has to do what you want
- You cannot mix types in the example above (passing an int and a double doesn't work)
- **template<typename T1, typename T2>**
- **bool isEqualTo(T1 a, T2 b) {** // this function can take 2 different types as parameters
 - **return a == b;**
- **}**
- **template<typename T1, typename T2>**
- **??? minimum (T1 a, T2 b) {** // no way to give a correct return type

- **if (a < b) return a;**
 - **else return b;**
- **}**
- **Conversions:**
 - Boolean compared to int/double → boolean converted to int/double
 - Int compared to double → int converted to double
- **Chicken c1, c2;**
- **minimum(c1, c2);** // how do you compare 2 chickens? fits template but probably won't compile
- **char ca1[100];**
- **char ca2[100];**
- **char* ca3 = minimum(ca1, ca2);** // minimum would compare the addresses of the pointers, not the values they point to, will compile, wouldn't do what you want
- Given a function vs. a template for a function, the language will choose the function
- Passing by const reference is common
- **template<typename T>**
- **T sum(const T a[], int n) {**
 - **T total = 0;** // won't compile with string call, no conversion between string and int, solution: *builtinType()* gives the "default" value, change to **T total = T();**
 - **for (int k = 0; k < n; k++) {**
 - **total += a[k];**
 - **}**
 - **return total;**
- **}**
- **int main() {**
 - **double da[100];**
 - **...**
 - **cout << sum(da, 100);**
 - **...**
 - **string sa[10] = {"This ", "is ", "a ", "test."};**
 - **string s = sum(sa, 4)**
- **}**

2/12: STL

- **<vector>**

- **push_back(n)** // adds an index to the vector that contains n
- **pop_back()** // deletes the last index of the vector
- **.size(), .front(), .back()** // same as queues
- **[]** // access elements, undefined for subscripts out of range
- **.at()** // access elements, throws an exception for subscripts out of range
- **vector<double> vd(10)** // 10 doubles, each is 0.0
- **vector<string> vs(10, "Hello")** // 10 strings, each is "Hello"
- **vector<int> vx(a, a+5)** // vx.size() is 5, vx[0] is 10, vx[1] is 20, ... , vx[4] is 50
- **vector<int>::iterator q = vi.insert(p, 40);** // inserts 40 before p, returns iterator to new element
 - vector iterators support using +=/-= i
- **p = vi.erase(q);** // erases the value at q, returns iterator to new element in that spot

- **<list>**

- **list<int> li;**
- **li.push_back(20);**
- **li.push_back(30);**
- **li.push_front(10);**
- **cout << li.size();** // writes 3
- **cout << li.front();** // writes 10
- **cout << li.back();** // writes 30
- **li.push_front(40);**
- **li.pop_front();**
- **for (list<int>::iterator p = li.begin(); p != li.end(); p++)**
 - **cout << *p << endl;** // writes 10 20 30
- **list<double> ld(10);** // ld.size() is 10, each element is 0.0
- **vector<string> ls(10, "Hello");** // ls.size() is 10, each element is "Hello"
- **vector<string> vs(ls.begin(), ls.end());** // vs.size() is 10, each element is "Hello"
- **list<int>::iterator p = li.end();**
- **p--;**
- **p--;**
- **p += 2;** // won't compile
- **list<int>::iterator q = li.insert(p, 40);** // inserts 40 before p, returns iterator to new element
- **list<int>::iterator q = li.erase(p);** // erases element at p and using p is now undefined, returns iterator to element after

- **<set>**

- **set<string> s;**
- **s.insert("Fred");**
- **s.insert("Ethel");**
- **s.insert("Fred");**

- `cout << s.size(); // 2`
- `s.insert("Desi");`
- `s.erase("Ethel");`
- `for(set<string>::iterator ptr = s.begin(); ptr != s.end(); ptr++) {`
 - `cout << *ptr << endl; // prints using < (Desi is first)`
- `}`
- `template<typename T>`
- `T* find(T* b, T* e, const T& target) {`
 - `for (; b != e; b++) {`
 - `if (*b == target) break;`
 - `}`
 - `return b;`
- `}`
- `int main() {`
 - `int a[5] = {10, 40, 50, 20, 30};`
 - `int k;`
 - `cin >> k;`
 - `int* p = find(a, a + 5, k);`
 - `if (p == a + 5)`
 - `... not found ...`
 - `else`
 - `... found, p points to the first element with that value ...`
 - `string sa[4] = {"Lucy", "Ricky", "Fred", "Ethel"};`
 - `string* sp = find(sa, sa + 4, "Fred") // won't compile, "Fred" is a pointer to a char[]`
- `}`
- `template<typename Iter, typename T>`
- `Iter find(Iter b, Iter e, const T& target) {`
 - `for (; b != e; b++) {`
 - `if (*b == target) {`
 - `break;`
 - `}`
 - `}`
 - `return b;`
- `}`
- `int main() {`
 - `int a[5] = {10, 40, 50, 20, 30};`
 - `int k;`
 - `cin >> k;`

- `int* p = find(a, a+5, k);`
- `if (p == a+5)`
- `... not found ...`
- `else`
- `... found, p points to the first element with that value ...`
- `list<string> ls;`
- `list<string>::iterator q = find(ls.begin(), ls.end(), "Fred");`
- `if (q == ls.end()) \`
- `... not found ...`
- `vector<int> vi;`
- `vector<int>::iterator r = find(vi.begin(), vi.begin() + 5, 42);`
- `if (r == vi.begin() + 5)`
- `... not found ...`
- `}`

- `template<typename Iter, typename Func>`
- `Iter find_if(Iter b, Iter e, Func f) {`
 - `for (; b != e; b++) {`
 - `if (f(*b)) break;`
 - `}`
 - `return b;`
- `}`

- `bool isNegative(int k) {`
 - `return k < 0;`
- `}`

- `bool isEmpty(string s) {`
 - `return s.empty();`
- `}`

- `int main() {`
 - `vector<int> vi;`
 - `...`
 - `vector<int>::iterator p = find_if(vi.begin(), vi.end(), isNegative);` // function name by itself acts as a pointer to the function
 - `if (p == vi.end())`
 - `... not found ...`
 - `list<string> ls;`
 - `...`
 - `list<string>::iterator q = find_if(ls.begin(), ls.end(), isEmpty)`
- `}`

2/24: Big-O

- `for (int i = 0; i < N; i++) { // O(N)`
 - `c[i] = a[i] * b[i]; // O(1)`
- `}`
- Work from the inside out
- `for (int i = 0; i < N; i++) { // O(N^2)`
 - `a[i] *= 2; // O(1)`
 - `for (int j = 0; j < N; j++) { // O(N)`
 - `d[i][j] = a[i] * c[j]; // O(1)`
 - `}`
- `}`
- `for (int i = 0; i < N; i++) { // O(N)`
 - `a[i] *= 2; // O(1)`
 - `for (int j = 0; j < 100; j++) { // O(1) → still a constant, not reliant on N`
 - `d[i][j] = a[i] * c[j]; // O(1)`
 - `}`
- `}`
- `for (int i = 0; i < N; i++) { // O(N^2)`
 - `a[i] *= 2; // O(1)`
 - `for (int j = 0; j < i; j++) { // O(i) → proportional to 0 + 1 + 2 + ... + (N-1) = (N-1)N/2`
 - `d[i][j] = a[i] * c[j]; // O(1)`
 - `}`
- `}`
- `for (int i = 0; i < N; i++) { // O(N^2)`
 - `if (std::find(a, a+N, 10*i) != a+N) { // takes time proportional to O(N)`
 - `count++;`
 - `}`
- `}`
- `for (int i = 0; i < N; i++) { // O(N^2 log N)`
 - `a[i] *= 2;`
 - `for (int j = 0; j < N; j++) { // O(N log N)`
 - `d[i][j] = f(a, N); // suppose f(a, N) is O(log N)`
 - `}`
- `}`
- `for (int i = 0; i < N; i++) { // O(RC log C)`

- `a[i] *= 2;`
 - `for (int j = 0; j < N; j++) { // O(C log c)`
 - `d[i][j] = f(C); // suppose f(C) is O(log C)`
 - `}`
- `}`
- Selection Sort: $O(N^2)$
- Bubble Sort:
 - Worst Case: $O(N^2)$
 - Average Case: $O(N^2)$
- Insertion Sort: $O(N^2) \rightarrow$ best of the N^2 sorts
- Shell Sort: $O(N^{1.47})$
- Merge Sort: $O(N \log N)$

3/2: Hash Tables

- Use a formula to set up a data structure that can contain a lot of data and is inexpensive to search/insert
- Always expect collisions
 - If load factor (# of items/# of buckets) > 1, there is guaranteed to be a collision
- Using a prime number of buckets allows there to be no common factor → more equal distribution
- Hash function
 - **unsigned int hash(string s) {** // numbers greater than the max size for unsigned ints are just represented by their last 32? digits
 - **unsigned int h = 216613261U;** // U makes the compiler treat it as an unsigned integer constant
 - **for (int i = 0; i != s.size(); i++) {**
 - **h += s[i];**
 - **h *= 16777619;**
 - **}**
 - **return h;**
 - **}**
- Hash table with N items: lookup/insert/erase for fixed # of buckets: O(N) with low constant of proportionality
- Hash table with N items + rehashing: lookup/insert/erase: O(1) on average
- **unordered_set**
- **unordered_multiset** // allows duplicates
- **unordered_map**
- **unordered_multimap** // allows duplicate keys
- **#include <unordered_map>**
- **using namespace std;**
- **unordered_map<string, double> ious;**
- **string name;**
- **double amt;**
- **while (cin >> name >> amt) {**
 - **ious[name] += amt;**
- **}**
- **if (ious.find("ricky") == ious.end()) {**
 - **cout << "Ricky doesn't owe me anything" << endl;**
- **}**
- **#include <functional>**
- **#include <string>**

- `string s;`
- `cin >> s;`
- `unsigned int h = std::hash<std::string>()(s);`
- `unsigned int h2 = std::hash<double>()(3.75);`
- `unsigned int h3 = std::hash<string*>()(&s);`

3/4: Binary Trees

- Made up of nodes connected by edges, stemming from a root node, and paths that connect one node to another
 - There is a unique path from the root node to any other node in the tree
 - Nodes follow a parent/child relationship
 - A leaf node has no children, interior nodes do
 - The depth of a node is determined by how many edges away from the root node a node is
 - Any program with a tree that goes down multiple paths is most likely best implemented with recursion
- **struct Node {**
 - **string data;**
 - **vector<Node*> children;**
 - **Node* parent;** // not always necessary, returning to parent may or may not be relevant
- **};**
- **Node* root;**
- **int count(const Node* p) {** // base cases: empty tree and leaf nodes
 - **if (p == nullptr) {**
 - **return 0;**
 - **}**
 - **int total = 1;** // count self
 - **for (int k = 0; k != p->children.size(); k++) {**
 - **total += count (p->children[k]);**
 - **}**
 - **return total;**
- **}**
- **cout << count(root) << endl;**
- **void printTree(const Node* p, int depth) {**
 - **if (p == nullptr) {**
 - **return;**
 - **}**
 - **cout << string(2 * depth, ' ') << p->data << endl;**
 - **for (int i = 0; i < p->children.size(); i++) {**
 - **printTree(p->children[i], depth + 1);**
 - **}**
- **}**
- Preorder traversal: process the node before you process the children
- Postorder traversal: process the node after you process the children

- A binary tree is either:
 - Empty
 - Or is a node with 2 binary subtrees (a left subtree and a right subtree)
- **struct Node {**
 - **string data;**
 - **Node* left;**
 - **Node* right;**
- **};**
- A binary search tree (BST) is either:
 - Empty
 - A node with a left BST and a right BST such that the value at every node on the left subtree is < the value at this node, and every node in the right subtree is > the value at this node
 - Assuming no duplicates
- **set<string> visitors;**
- **...**
- **string name;**
- **...**
- **visitors.insert(name)** // inserts if name is not already in the set
- **...**
- **if (visitors.find("Ricky") == visitors.end());**
 - **cout << "not found" << endl;**
- **for (set<string>::iterator p = visitors.begin(); p!= visitors.end(); p++) {**
 - **cout << *p << endl;**
- **}**
- **...**
- **set<string>::iterator p = visitors.find("Fred");**
- **if (p != visitors.end()) {**
 - **cout << "Bye, Fred" << endl;**
 - **visitors.erase(p)** // harmless to pass erase the end iterator
- **}**
- **...**
- **visitors.remove("Lucy");**
- In-order traversal:
 - **void printTree(const Node* p) {**
 - **if (p != nullptr) {**
 - **printTree(p->left);**
 - **cout << p->data << endl;**
 - **printTree(p->right);**

- }
 - }

- Insertion/deletion/search - $O(\log N)$ in a relatively balanced BST
- Deletion:
 - Leaf node - delete the node
 - Node with one child - delete the node, move the child up
 - Node with two children - delete the node and take either the greatest value in the left subtree or the least value in the right subtree to replace it
- AVL Tree:
 - A BST where for every node, the height of the left subtree and the height of the right subtree differ by at most 1
 - Guarantees $\log N$ behavior
- 2-3 Tree:
 - Every node has 2 or 3 children
 - Nodes with 3 children contain 2 values, the 3rd child is between these 2 values
 - All leaf nodes have the same depth
- Red-black tree:
 - Used by STL for set, map, multiset, multimap
 - $\log N$ data structures