

CS 181 HW8 2021 CS181

CHARLES ZHANG

TOTAL POINTS

12 / 12

QUESTION 1

1 Two left-most reductions in CFG **4 / 4**

✓ - **0 pts** Perfectly correct

- **1.5 pts** One of your reductions is wrong

- **3 pts** Both of your reductions are wrong

- **1 pts** Reduction is correct, but one of your reductions is not left-most

- **2 pts** Reduction is correct, but both of your reductions are not left-most

- **4 pts** Did not answer this question

QUESTION 2

TM (mixed) Construction **8 pts**

2.1 a. Procedure **6 / 6**

✓ + **6 pts** Correct

+ **4 pts** Partially correct

+ **2 pts** Attempted

+ **5 pts** Almost Correct

+ **0 pts** Not attempted

2.2 b. Brief explanation **2 / 2**

✓ + **2 pts** Correct

+ **1 pts** Attempted, partially correct

+ **0 pts** Not attempted or wrong

CS 181 Homework 8

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Problem 1

Leftmost Reduction #1:

baabba

Baabba

BAabba

BAAbbba

BCbbba

Abba

ABba

ABBa

ADa

Ba

BA

S

Leftmost Reduction #2:

baabba

Baabba

BAabba

BAAbbba

BAABba

BASba

BAba

BABa

BSa

Ba

BA

S

1 Two left-most reductions in CFG 4 / 4

✓ - 0 pts Perfectly correct

- 1.5 pts One of your reductions is wrong
- 3 pts Both of your reductions are wrong
- 1 pts Reduction is correct, but one of your reductions is not left-most
- 2 pts Reduction is correct, but both of your reductions are not left-most
- 4 pts Did not answer this question

Problem 2

a) Proof (by construction):

- Let M_P be a Turing Machine that recognizes L_P .
- Let M_A be a Turing Machine that decides L_A .
- Construct M for $L_P \cup L_A$.
- Use UTM to simulate M_A on a given input w .
 - Since M_A decides a language, it's guaranteed to halt.
- If M_A halts and accepts, M halts and accepts.
- Else (M_A has halted and rejected):
 - Use UTM to simulate M_P on w (this may enter an infinite loop).
 - If M_P halts and accepts, M halts and accepts.
 - If M_P halts and rejects, M halts and rejects.

b) Justification:

By definition, a machine that recognizes the language $L_P \cup L_A$, must recognize every string in L_P . Since L_P is an RE language, we cannot guarantee that all strings recognized by M_P cause M_P to halt. As a result, we must account for the possibility that some strings in L_P cannot be decided, only recognized. Therefore, the language $L_P \cup L_A$ cannot be assumed to be recursive, it must be RE.

2.1 a. Procedure 6 / 6

✓ + **6 pts** Correct

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+ **2 pts** Attempted

+ **5 pts** Almost Correct

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2.2 b. Brief explanation 2 / 2

✓ + 2 pts Correct

+ 1 pts Attempted, partially correct

+ 0 pts Not attempted or wrong