# Quiz 5

| <b>Due</b> Nov 16 at 11:59pm | Points 7 | Questions 7 | Time Limit None |  |
|------------------------------|----------|-------------|-----------------|--|
|                              |          |             |                 |  |

# **Attempt History**

|        | Attempt   | Time       | Score      |
|--------|-----------|------------|------------|
| LATEST | Attempt 1 | 47 minutes | 4 out of 7 |

Score for this quiz: **4** out of 7 Submitted Nov 12 at 12:18pm This attempt took 47 minutes.

## **Question 1**

1 / 1 pts

Given  $\mathbf{x} \in R^3$ , what is the corresponding mapping function  $\phi(\mathbf{x})$  for the kernel function  $K(\mathbf{x}, \mathbf{y}) = \phi(\mathbf{x})^T \phi(\mathbf{y}) = (1 + \mathbf{x}^T \mathbf{y})^2$ .

(A) 
$$\phi(\mathbf{x}) = [1, x_1, x_2, x_3, x_1x_2, x_1x_3, x_2x_3]$$

(B) 
$$\phi(\mathbf{x}) = [1, x_1, x_2, x_3, x_1x_2, x_1x_3, x_2x_3, x_1^2, x_2^2, x_3^2]$$

(C) 
$$\phi(\mathbf{x}) = [1, 2x_1, 2x_2, 2x_3, 2x_1x_2, 2x_1x_3, 2x_2x_3, x_1^2, x_2^2, x_3^2]$$

(D) 
$$\phi(\mathbf{x}) = [1, \sqrt{2}x_1, \sqrt{2}x_2, \sqrt{2}x_3, \sqrt{2}x_1x_2, \sqrt{2}x_1x_3, \sqrt{2}x_2x_3, x_1^2, x_2^2, x_3^2]$$

A

B

C

Correct!

D

# **Question 2**

1 / 1 pts

Which of the following statements about kernels are true?

- (A) After applying the mapping function  $\phi(\mathbf{x}) = [\mathbf{x}, \mathbf{x}^2]$ , the data always become linearly separable.
- (B)  $\mathbf{x}, \mathbf{y} \in R^2, K(\mathbf{x}, \mathbf{y}) = (1 + 8\mathbf{x}^T\mathbf{y})^2$  is a valid kernel.
- (C) Let  $K(\mathbf{x}, \mathbf{y}) = \phi(\mathbf{x})^T \phi(\mathbf{y})$ . Computing the inner product between  $\phi(\mathbf{x})$  and  $\phi(\mathbf{y})$  using kernel function  $K(\mathbf{x}, \mathbf{y})$  is always slower than directly estimating from  $\phi(\mathbf{x})^T \phi(\mathbf{y})$ .
- (D) A kernel function may allow us to map feature vectors in to another space where the data is linearly separable.

### Select all that apply

A

Correct!

- ✓ B
- \_ C

Correct!

✓ D

Question 3 1 / 1 pts

Given a set of training data, Hard SVM returns a model with the hyper-plane  $\mathbf{w}^T\mathbf{x} + b = 0$ , where  $\mathbf{w} = [-1, -1]$  and b = 1. Which data point(s) **cannot** belong to the training dataset?

(A) 
$$\mathbf{x} = (0, 0.5), y = 1.$$

(B) 
$$\mathbf{x} = (0,0), y = 1.$$

(C) 
$$\mathbf{x} = (2,1), y = -1.$$

(D) 
$$\mathbf{x} = (2, 2), y = 1.$$

### select all that apply

Correct!

A

В

\_ C

Correct!

D

# **Question 4**

1 / 1 pts

As we see in the lecture, Soft SVM identifies a hyper-plane  $\mathbf{w}^T\mathbf{x} + b = 0$  by solving the following optimization problem.

$$\min_{w,b,\xi_i} \quad \frac{1}{2} \mathbf{w}^T \mathbf{w} + C \cdot \sum_{i=1}^N \xi_i$$

$$s.t \ \forall i, \ y(\mathbf{w}^T\mathbf{x}_i + b) \ge 1 - \xi_i$$

$$\xi_i \ge 0$$

Let  $\mathbf{w} = [-1, -1]$  and b = 1 are the solution of the above optimization problem. Given two positive data points  $\mathbf{x}_1 = (0,0)$  and  $\mathbf{x}_2 = (1,0)$ ,  $y_1 = y_2 = 1$ , what are their corresponding slack variables  $\xi_1$  and  $\xi_2$ , respectively?

(A) 
$$\xi_1 = 0, \, \xi_2 = 0.5$$

(B) 
$$\xi_1 = 0, \, \xi_2 = 1$$

(C) 
$$\xi_1 = 1, \, \xi_2 = 0$$

(D) 
$$\xi_1 = 1, \, \xi_2 = 0.5$$

A

Correct!

B

\_ C

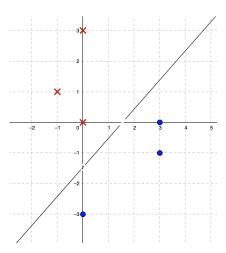
D

# **Question 5**

0 / 1 pts

Assume you have datapoints and labels as  $X=\{[0,0],[0,3],[-1,1],[3,0],[3,-1],[0,-3]\}$  and  $Y=\{-1,-1,-1,1,1\}$ .

We train a hard SVM classifier as shown in below.



What is w1? (round to 2 decimal places)

ou Answered

1

orrect Answers

0.67 (with margin: 0.01)

# Question 6 Follow the previous question. What is w2? (round to 2 decimal places) w2= \_\_\_\_ pu Answered -1 -0.67 (with margin: 0.01)

|                | Question 7                                | 0 / 1 pts |
|----------------|---|-----------|
|                | What is b? (round to 2 decimal places) b= |           |
| ou Answered    | -1.5                                      |           |
| orrect Answers | -1 (with margin: 0)                       |           |

Quiz Score: 4 out of 7