

Exercise 21.53

✓ Complete

■ Review | Constants

An electric dipole with dipole moment  $\vec{p}$  is in a uniform external electric field  $\vec{E}$ .

▼ Part A

Find the orientations of the dipole for which the torque on the dipole is zero measured counterclockwise from the electric field direction.

Enter your answers in degrees separated by a comma.

$\theta = 180,0^\circ$

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✓ Correct

▼ Part B

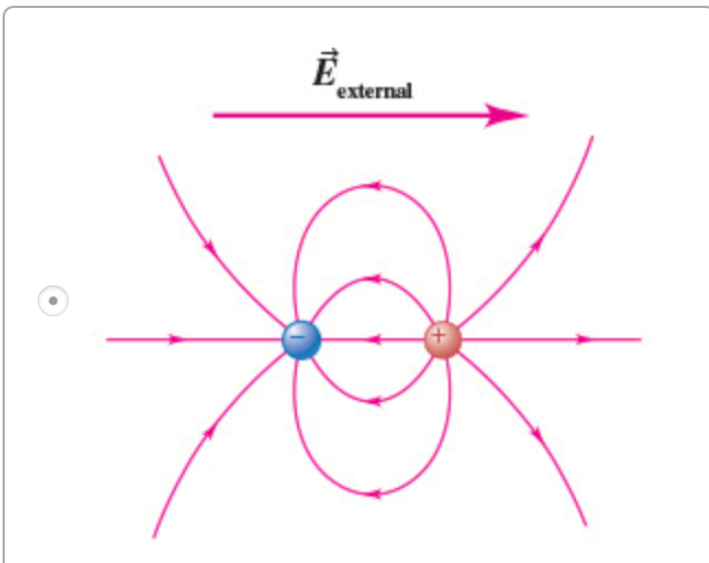
Which of the orientations in part A is stable, and which is unstable? (*Hint:* Consider a small rotation away from the equilibrium position and see what happens.)

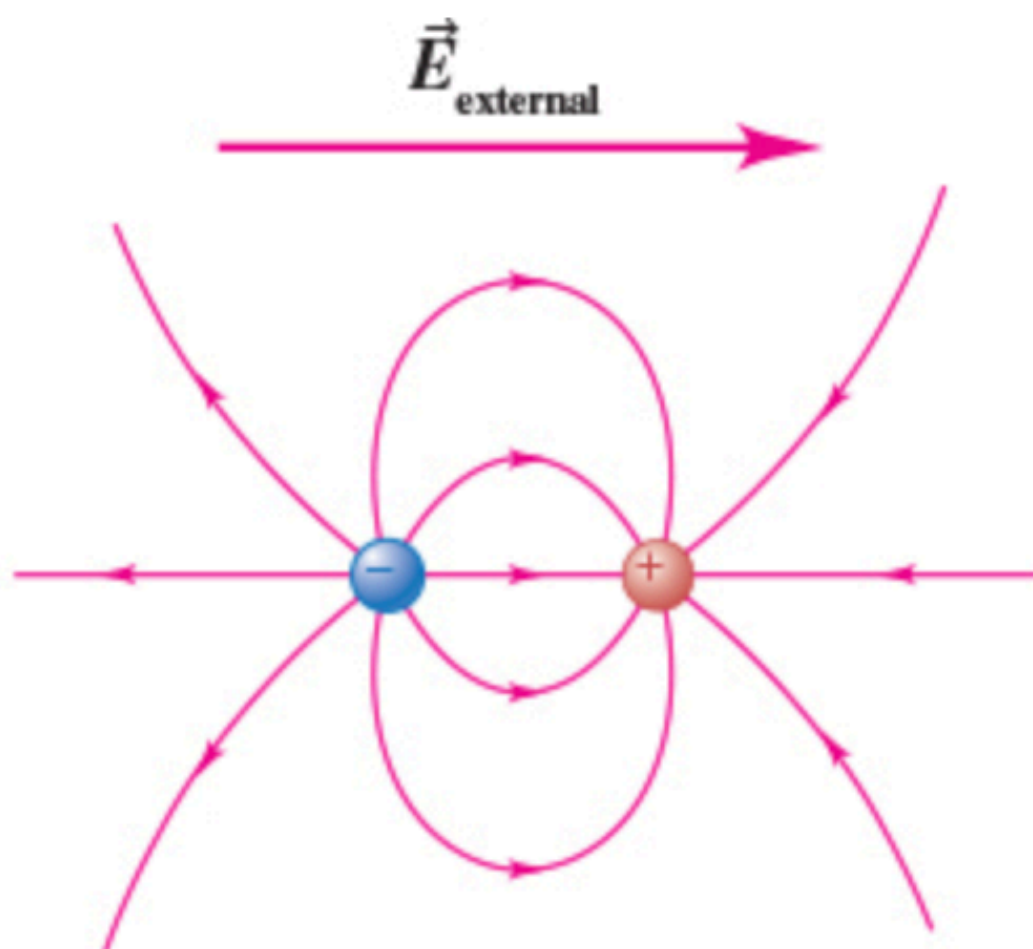
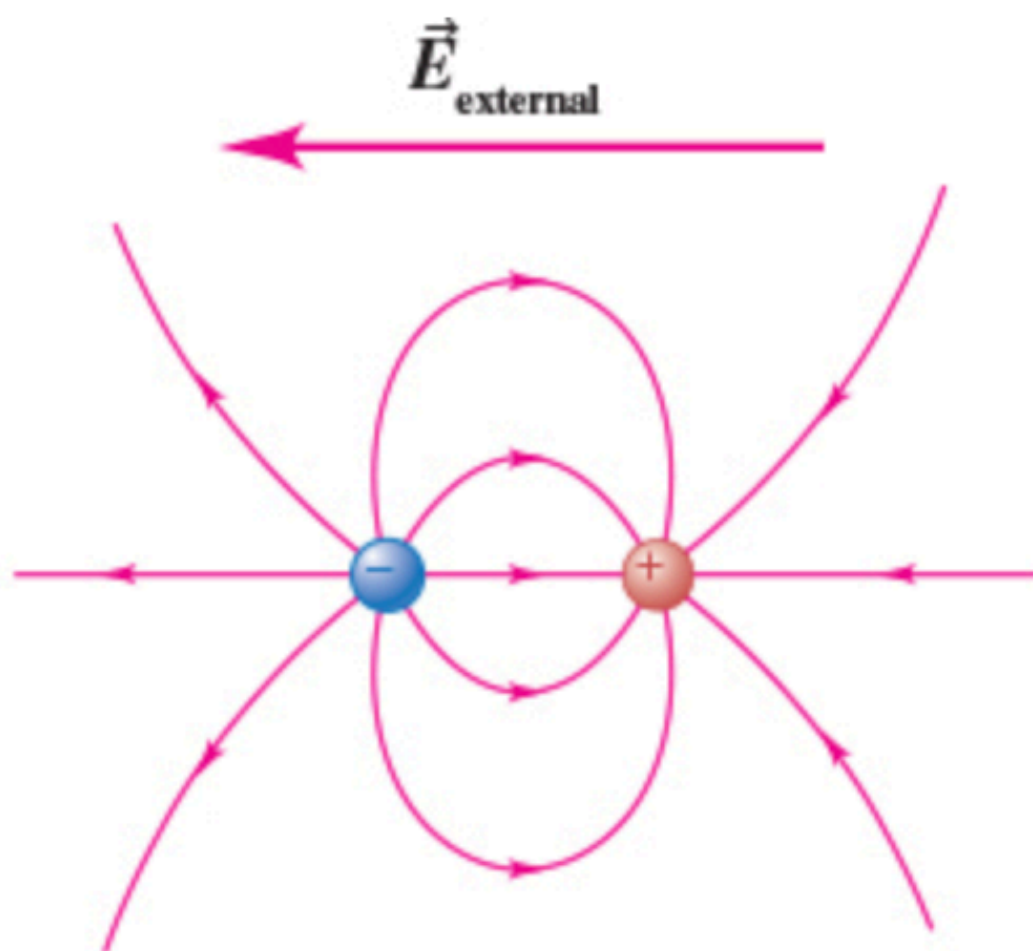
- ☐ The orientation is stable only when  $\vec{p}$  and  $\vec{E}$  point in opposite directions.
- ☒ The orientation is stable only when  $\vec{p}$  and  $\vec{E}$  point in the same direction.
- ☐ Both orientations in part A are stable.
- ☐ Both orientations in part A are unstable.

▼ Part C

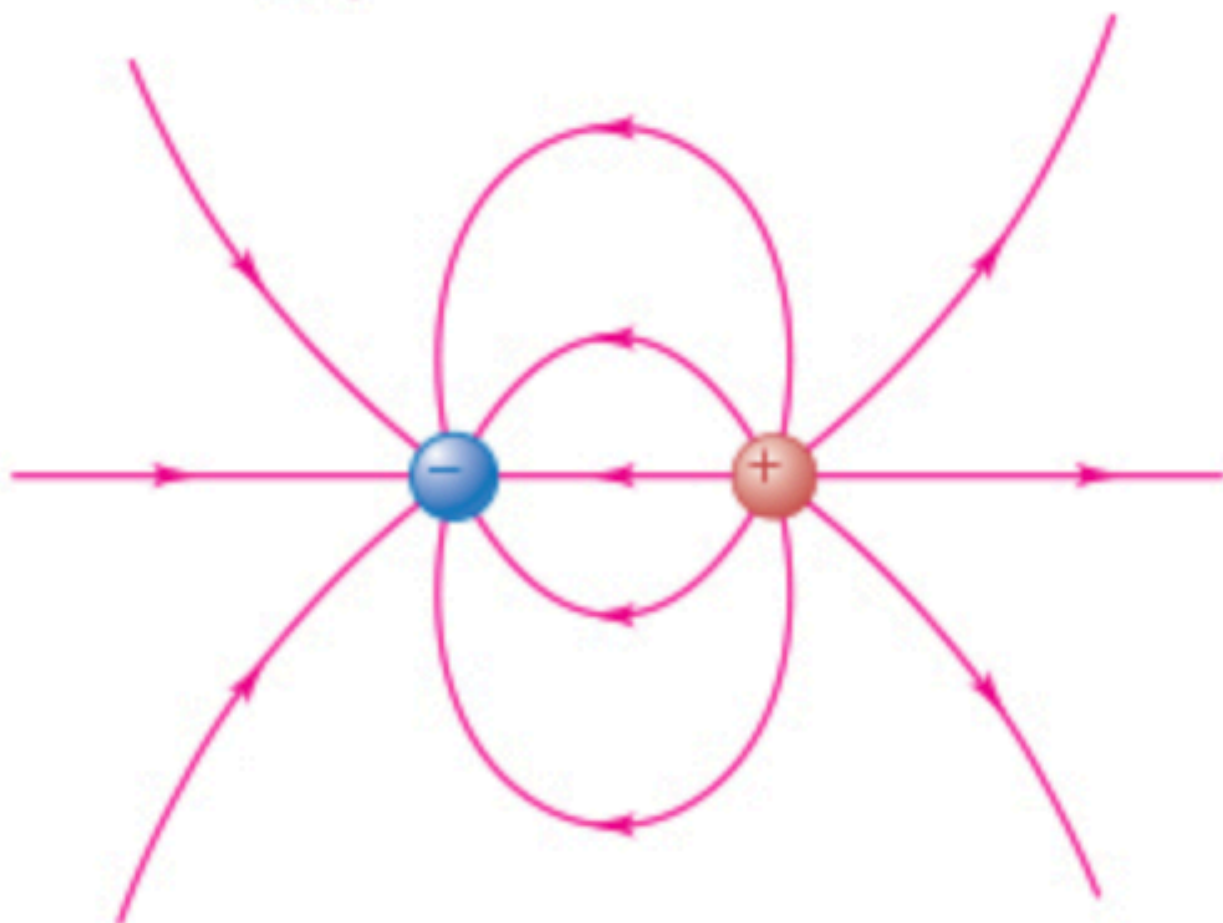


Choose a figure that correctly shows the dipole's own electric field and the external electric field for the stable orientation in part B.





$\vec{E}_{\text{external}}$



# Exercise 21.55 - Enhanced - with Solution

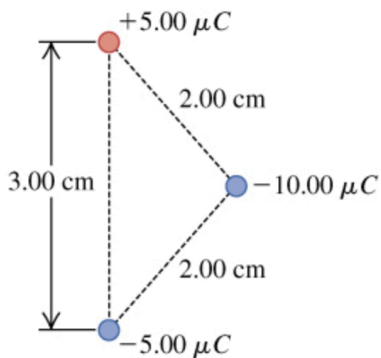
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Three charges are at the corners of an isosceles triangle as shown in (Figure 1). The  $\pm 5.00 \mu\text{C}$  charges form a dipole. Suppose that the  $+y$ -axis is directed upward and the  $+x$ -axis is directed rightward.

For related problem-solving tips and strategies, you may want to view a Video Tutor Solution of [Force and torque on an electric dipole](#).

Figure

1 of 1



[Review](#) | [Constants](#)

## Part A

Find the magnitude of the force the  $-10.00 \mu\text{C}$  charge exerts on the dipole.

Express your answer with the appropriate units.

$F =$

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## Part B

Find the direction angle of the force the  $-10.00 \mu\text{C}$  charge exerts on the dipole. The angle is measured from the  $+x$ -axis toward the  $+y$ -axis.

Express your answer in degrees to three significant figures.

$\theta =$    $^\circ$

▼ **Part C**

For an axis perpendicular to the plane of the figure at the midpoint of the line connecting the  $\pm 5.00 \mu\text{C}$  charges, find the magnitude of the torque exerted on the dipole by the  $-10.00 \mu\text{C}$  charge.

**Express your answer with the appropriate units.**

$\mu\text{A}$

↶

↷

↺

?

$\tau =$

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▼ **Part D**

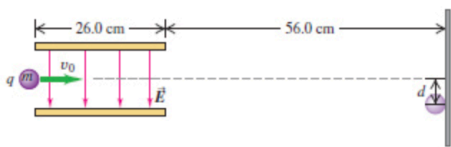
What is the direction of the torque in part C?

- ☐ Clockwise
- ☐ Counterclockwise

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A small object with mass  $m$ , charge  $q$ , and initial speed  $v_0 = 4.00 \times 10^3 \text{ m/s}$  is projected into a uniform electric field between two parallel metal plates of length  $26.0 \text{ cm}$  (Figure 1). The electric field between the plates is directed downward and has magnitude  $E = 600 \text{ N/C}$ . Assume that the field is zero outside the region between the plates. The separation between the plates is large enough for the object to pass between the plates without hitting the lower plate. After passing through the field region, the object is deflected downward a vertical distance  $d = 1.35 \text{ cm}$  from its original direction of motion and reaches a collecting plate that is  $56.0 \text{ cm}$  from the edge of the parallel plates. Ignore gravity and air

1 of 1



Express your answer in coulombs per kilogram.

$q/m =$   C/kg

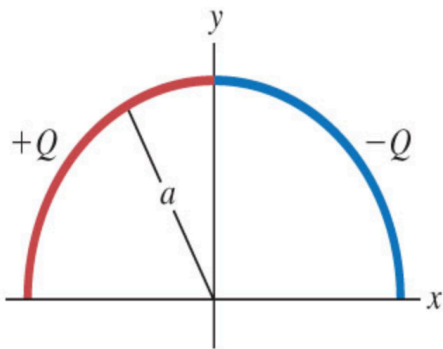
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Next &gt;

A semicircle of radius  $a$  is in the first and second quadrants, with the center of curvature at the origin. Positive charge  $+Q$  is distributed uniformly around the left half of the semicircle, and negative charge  $-Q$  is distributed uniformly around the right half of the semicircle in the following figure.(Figure 1)

Figure

1 of 1



Review | Constants

Part A

What is the magnitude of the net electric field at the origin produced by this distribution of charge?

Express your answer in terms of the variables  $Q$ ,  $a$ , and constant  $k$ .

$$|E| = \frac{4kQ}{\pi a^2}$$

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Previous Answers

Correct

Part B

What is the direction of the net electric field at the origin produced by this distribution of charge?

- ☒  $+x$  direction
- ☐  $-x$  direction
- ☐  $+y$  direction
- ☐  $-y$  direction
- ☐ another direction



Exercise 22.9 - Enhanced - with Feedback

[Review](#) | [Constants](#)

A charged paint is spread in a very thin uniform layer over the surface of a plastic sphere of diameter 18.0 cm, giving it a charge of  $-59.0\ \mu\text{C}$ .

▼ Part A

Find the electric field just inside the paint layer.

Express your answer with the appropriate units. Enter positive value if the field is directed away from the center of the sphere and negative value if the field is directed toward the center of the sphere.

$\mu\text{A}$

↶

↷

↺

⌨

?

$E =$

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▼ Part B

Find the electric field just outside the paint layer.

Express your answer with the appropriate units. Enter positive value if the field is directed away from the center of the sphere and negative value if the field is directed toward the center of the sphere.

$\mu\text{A}$

↶

↷

↺

⌨

?

$E =$

▼ Part C



Find the electric field 6.00 cm outside the surface of the paint layer.

**Express your answer with the appropriate units. Enter positive value if the field is directed away from the center of the sphere and negative value if the field is directed toward the center of the sphere.**

$$E = -2.36 \times 10^7 \frac{\text{N}}{\text{C}}$$

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✓ Correct

Exercise 22.19 - Enhanced - with Feedback

[Review | Constants](#)

A hollow, conducting sphere with an outer radius of 0.260 m and an inner radius of 0.200 m has a uniform surface charge density of  $+6.17 \times 10^{-6} \text{ C/m}^2$ . A charge of  $-0.400 \mu\text{C}$  is now introduced into the cavity inside the sphere.

▼ Part A

What is the new charge density on the outside of the sphere?

Express your answer with the appropriate units.

$\mu\text{A}$

↶

↷

↺

⌨

?

$\sigma =$ 

Value

Units

Submit

[Request Answer](#)

▼ Part B

Calculate the strength of the electric field just outside the sphere.

Express your answer with the appropriate units.

$\mu\text{A}$

↶

↷

↺

⌨

?

$E =$ 

Value

Units

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For related problem-solving tips and strategies, you may want to view a Video Tutor Solution of [Field of a uniformly charged sphere](#).

▼ **Part A**

$\rho =$   C/m<sup>3</sup>

**Request Answer**

▼ **Part B**

$E =$   N/C

Problem 22.45

An insulating hollow sphere has inner radius  $a$  and outer radius  $b$ . Within the insulating material the volume charge density is given by  $\rho(r) = \frac{\alpha}{r}$ , where  $\alpha$  is a positive constant.

Review | Constants

Part A

What is the magnitude of the electric field at a distance  $r$  from the center of the shell, where  $a < r < b$ ?

Express your answer in terms of the variables  $\alpha$ ,  $a$ ,  $r$ , and electric constant  $\epsilon_0$ .

$E =$

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Part B

A point charge  $q$  is placed at the center of the hollow space, at  $r = 0$ . What value must  $q$  have (sign and magnitude) in order for the electric field to be constant in the region  $a < r < b$ ?

Express your answer in terms of the variables  $\alpha$ ,  $a$ , and appropriate constants.

$q =$

▼ **Part C**

What then is the value of the constant field in this region?

**Express your answer in terms of the variable  $\alpha$  and electric constant  $\epsilon_0$ .**



$\Lambda \Sigma \Phi$



$E =$

**Submit**

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Problem 22.46

In the early years of the 20th century, a leading model of the structure of the atom was that of the English physicist J. J. Thomson (the discoverer of the electron). In Thomson's model, an atom consisted of a sphere of positively charged material in which were embedded negatively charged electrons, like chocolate chips in a ball of cookie dough. Consider such an atom consisting of one electron with mass  $m$  and charge  $-e$ , which may be regarded as a point charge, and a uniformly charged sphere of charge  $+e$  and radius  $R$ .

Review | Constants

Part A



Is equilibrium position of the electron at the center of the nucleus.

- ☒ Yes  
☐ No

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✓ Correct

Part B

In Thomson's model, it was assumed that the positive material provided little or no resistance to the motion of the electron. If the electron is displaced from equilibrium by a distance  $r$  less than  $R$ , find the net force on the electron.

Express your answer in terms of the variables  $R$ ,  $e$ , vector  $\mathbf{r}$  and constants  $\pi$  and  $\epsilon_0$ . Use the 'vec' button to denote vectors in your answers.



▼ Part C



Will the resulting motion of the electron be simple harmonic. (*Hint:* Review the definition of simple harmonic motion in Section 13.2 from the textbook. If it can be shown that the net force on the electron is of this form, then it follows that the motion is simple harmonic. Conversely, if the net force on the electron does not follow this form, the motion is not simple harmonic.)

- ☒ Yes, it will be.
- ☐ No, it will not be.

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✓ Correct

▼ Part D



Calculate the frequency of oscillation.

Express your answer in terms of the variables  $m$ ,  $R$ ,  $e$ , and constants  $\pi$  and  $\epsilon_0$ .

$$f = \frac{1}{2\pi} \sqrt{\frac{e^2}{4\pi m \epsilon_0 R^3}}$$

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▼ Part E



By Thomson's time, it was known that excited atoms emit light waves of only certain frequencies. In his model, the frequency of emitted light is the same as the oscillation frequency of the electron or electrons in the atom. What would the radius of a Thomson-model atom have to be for it to produce red light of frequency  $4.54 \times 10^{14}$  Hz ? (see Appendix F from the textbook for data about the electron)

Express your answer in meters.

$$R = 3.14 \times 10^{-10} \text{ m}$$

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✓ Correct

▼ Part F



Compare your answer in the previous part to the radii of real atoms, which are of the order of  $10^{-10}$  m.

- ☒ The atom radius in this model is the correct order of magnitude.
- ☐ The atom radius in this model is the invalid order of magnitude.

▼ Part G



If the electron were displaced from equilibrium by a distance greater than  $R$ , would the electron oscillate? Would its motion be simple harmonic? Explain your reasoning. (*Historical note:* In 1910, the atomic nucleus was discovered, proving the Thomson model to be incorrect. An atom's positive charge is not spread over its volume as Thomson supposed, but is concentrated in the tiny nucleus of radius  $10^{-14}$  to  $10^{-15}$  m.)

- ☒ The electron would still oscillate. But the motion would not be simple harmonic.
- ☐ The electron would not oscillate.
- ☐ The electron would still oscillate. The motion would be simple harmonic.

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Challenge Problem 22.62

A region in space contains a total positive charge  $Q$  that is distributed spherically such that the volume charge density  $\rho(r)$  is given by

$$\rho(r) = 3\alpha r / (2R) \quad \text{for } r \leq R/2$$
$$\rho(r) = \alpha [1 - (r/R)^2] \quad \text{for } R/2 \leq r \leq R$$
$$\rho(r) = 0 \quad \text{for } r \geq R$$

Here  $\alpha$  is a positive constant having units of  $\text{C}/\text{m}^3$ .

Review | Constants

Part A

Determine  $\alpha$  in terms of  $Q$  and  $R$ .

Express your answer in terms of variables  $R$ ,  $Q$  and appropriate constants.

$\sqrt[n]{\phantom{x}}$

$\Delta \Sigma \Phi$

$\curvearrowright$

$\curvearrowleft$

$\refresh$

$\text{⌨}$

$?$

$\alpha =$

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Part B

Using Gauss's law, derive an expression for the magnitude of the electric field as a function of  $r$  for  $r \leq R/2$ . Express your answers in terms of the total charge  $Q$ .

Express your answer in terms of variables  $r$ ,  $R$ ,  $Q$  and appropriate constants.

$\sqrt[n]{\phantom{x}}$

$\Delta \Sigma \Phi$

$\curvearrowright$

$\curvearrowleft$

$\refresh$

$\text{⌨}$

$?$

$E_1 =$

▼ Part C



Using Gauss's law, derive an expression for the magnitude of the electric field as a function of  $r$  for  $R/2 \leq r \leq R$ . Express your answers in terms of the total charge  $Q$ .

Express your answer in terms of variables  $r$ ,  $R$ ,  $Q$  and appropriate constants.

$$E_2 = \frac{1}{4\pi r^2 \epsilon_0} \frac{1920Q}{233} \left[ \left( \frac{r^3}{3R^3} - \frac{r^5}{5R^5} \right) - \frac{23}{1920} \right]$$

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✓ Correct

▼ Part D

Using Gauss's law, derive an expression for the magnitude of the electric field as a function of  $r$  for  $r \geq R$ . Express your answers in terms of the total charge  $Q$ .

Express your answer in terms of variables  $r$ ,  $R$ ,  $Q$  and appropriate constants.



$E_3 =$

▼ Part E

What fraction of the total charge is contained within the region  $R/2 \leq r \leq R$ ?

$\sqrt[n]{\square}$   $\Lambda \Sigma \Phi$  ↶ ↷ ↺  ?

$\frac{Q_0}{Q} =$

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▼ Part F

What is the magnitude of  $\vec{E}$  at  $r = R/2$ ?

Express your answer in terms of variables  $R$ ,  $Q$  and appropriate constants.

$\sqrt[n]{\square}$   $\Lambda \Sigma \Phi$  ↶ ↷ ↺  ?

$E =$

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