

# Matlab/Octave basics

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# Vectors

The `row` and `column` vectors are `different` !

creating row-vectors:

The vector  $a = (-1.2, 3.1, 4.7, 1.9)$  can be created by listing its elements enclosed by square brackets, separating them by `comma` :

```
a = [-1.2, 3.1, 4.7, 1.9]
```

or by `space` :

```
a = [-1.2 3.1 4.7 1.9]
```

# Vectors

- 1 The indexing starts at `1`.
- 2 the  $i$ -th element of the vector is `a(i)`.
- 3 `length(a)` returns the number of elements in `a`.
- 4 the empty vector is `[]`

# Vectors as regular sequences

## the colon operator:

It is the most useful syntax for defining vectors.

- for the vector  $b = (1, 2, 3, 4, 5)$  simply use: `b = 1:5`
- for  $c = (5, 4, 3, 2, 1)$ : `c = 5:-1:1`
- for  $d = (2, 2.2, 2.4, 2.6, 2.8, 3)$ : `d = 2:0.2:3`

the colon syntax:

```
x = first:stepsize:last
```

where the default value of stepsize is `one`, that is

```
x = first:last
```

is the shorter form of

```
x = first:1:last
```

the `linspace` function:

- the vector  $e = (1, 1.2, 1.4, 1.6, 1.8, 2)$  can be created by:

```
e = linspace(1,2,6)
```

- for a 100 element vector  $f$ :

```
f = linspace(1,2)
```

`linspace` syntax:

```
x = linspace(first, last, numberOfElements)
```

The elements in the resulting vector are `equally spaced`. The `default` number of elements is `100`:

```
x = linspace(first, last)
```

is the shorter form of

```
x = linspace(first, last, 100)
```

# Column-vectors

## creation:

- by listing the elements separated by `semicolon`, enclosing them in square brackets:

```
m = [-3; 0; 7]
```

- transposing a row-vector:

```
n=[1 -2 4 -1]'
```



**Note that:** the operator `'` is the conjugate-transpose operator, so the result is not the expected one for complex valued vectors. For "transposing only" complex vectors use the function `transpose`

# Column-vectors

The usage of `x(i)` and `length(x)` is the same as for row-vectors.

The call `size(x)` returns the vector

```
[numOfRows, numOfColumns]
```

where `numOfRows=1` for row-vectors and `numOfColumns=1` for column-vectors. In Octave/Matlab the vectors are 2-dimensional objects.

## Common ways of defining vectors

- `[a, b]` : extending along the 2nd-dimension, the sizes of the 1st dimension must agree
- `[m;n]` : extending along the 1st-dimension, the sizes of the 2nd dimension must agree
- `[-4 a 3 -1]` : extending along the 2nd dimension by listing the new elements
- `[1;m;-3]` : extending along the 1st dimension by listing the new elements
- `h(2:4)` : extract a subvector by specifying the indices of the desired elements
- `h([1 4 5])` : extract a subvector by specifying the indices of the desired elements
- `h(2)=[]` : clear individual elements
- `h([2 4])=[]` : clear elements specified by an index vector

**Important!** For `a=[-1 3 2]` the result of the command `a(6)=4` is the vector `a=[-1 3 2 0 0 4]`. Not that one could expect. The undefined new elements will be set to zero. There is no warning issued by the system!

# Some useful functions

- `min(x)` and `max(x)` returns the smallest and the largest element of  $x$
- `sort(x)` returns the sorted instance of  $x$  (the default order: increasing)
- `sort(x, 'descend')` returns the reversely sorted instance of  $x$
- `flip(x)` returns a new vector (matrix) with elements of  $x$  in reverse order (for matrices the elements are the rows by default)
- `length(x)` number of elements
- `sum(x)` sum of the elements
- `prod(x)` product of the elements
- `mean(x)` arithmetic mean of the elements of  $x$
- `x(end)` in vector (matrix) context the `end` has special meaning: the last element of the object

# Vector operations

For the same shaped vectors `a` and `b`

- `a+b` and `a-b` is the elementwise sum and difference
- `x=a+1` for convenience the basic operations with a scalar defined elementwise
- `x=a.^ 2` see above
- `x=a.*b` it is the elementwise product, results in a new vector  $a_i b_i$
- `x=a./b` see above
- `x=1./a` shorter version of `ones(size(a))./a`
- `dot(a,b)` the scalar, inner product, the sum-product of the vectors

**Important!** The dot before the operator results elementwise operations.

The builtin functions `sin`, `cos`, `tan`, `exp`, `log`, `sqrt`, `abs`, can have vector and matrix parameters, resulting the function called elementwise.

`NaN` : Not a Number is a result of undefined operation. For example `0/0`, `Inf/Inf` )

# Matrices in Octave/Matlab

## Defining matrices by listing

$A = [1, 2, 3; 4, 5, 6; 7, 8, 9]$  or  $A = [1 \ 2 \ 3; \ 4 \ 5 \ 6; \ 7 \ 8 \ 9]$  results in:

$$A = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$

The **comma** separates the elements of the row, the **semicolon** separates the rows

The indexing for matrices is **one** based, as for vectors.

$A(i, j)$  is the  $(i, j)$ -th element of  $A$

# Defining matrices from vectors

For vectors `a=[1 -2 0]` ; `b=[2 -11 7]` ; `m=[-3;0;7]` ;

`n=[1; -2; 0]` ;

the result of

`B=[a;b]` :

$$B = \begin{pmatrix} 1 & -2 & 0 \\ 2 & -11 & 7 \end{pmatrix}$$

`C=[a' b']` and `D=[m' a']` :

$$C = \begin{pmatrix} 1 & 2 \\ -2 & -11 \\ 0 & 7 \end{pmatrix} \quad D = \begin{pmatrix} -3 & 1 \\ 0 & -2 \\ 7 & 0 \end{pmatrix}$$

## Extending matrices

For matrices and vectors defined above the result of `E=[A;a]` (or `E=[A;[1,-2,0]]`):

$$E = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 1 & -2 & 0 \end{pmatrix}$$

The result of `F=[A m]` (or `F=[A, m]`):

$$F = \begin{pmatrix} 1 & 2 & 3 & -3 \\ 4 & 5 & 6 & 0 \\ 7 & 8 & 9 & 7 \end{pmatrix}$$



## Extending matrices

For  $G=[C \ D]$  and  $H=[C;D]$  we get:

$$G = \begin{pmatrix} 1 & 2 & -3 & 1 \\ -2 & -11 & 0 & -2 \\ 0 & 7 & 7 & 0 \end{pmatrix} \quad H = \begin{pmatrix} 1 & 2 \\ -2 & -11 \\ 0 & 7 \\ -3 & 1 \\ 0 & -2 \\ 7 & 0 \end{pmatrix}$$

For  $C(4,5)=9$ :

$$C = \begin{pmatrix} 1 & 2 & 0 & 0 & 0 \\ -2 & -11 & 0 & 0 & 0 \\ 0 & 7 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 9 \end{pmatrix}$$

**The size of matrix has changed without warning!**

# Accessing elements, rows, columns and submatrices

- `size(A)` : the number of rows and columns in  $A$
- `length(A) = max(size(A))`
- `numel(A)` the number of elements in  $A$
- `A(i,j)` the  $i,j$ -th element
- `A(i,:)` the  $i$ -th row-vector
- `A(:,j)` the  $j$ -th column
- `A(2:3,:)` the 2-nd and 3-rd rows
- `A([1 2 4],:)` the 1., 2. and 4. rows
- `A(:, [1 3])` the 1. and 3. columns
- `A(2:3, [1 3])` the 1. and 3. elements of the 2. and 3. rows

# Manipulating matrices

## Deleting rows and columns

- `A(i,:)=[]` will delete the  $i$ -th row
- `A(:,j)=[]` will delete the  $j$ -th column
- `A([1 3],:)=[]` will delete the 1-st and 3-rd rows
- `A(:, [1 3])=[]` will delete the 1-st and 3-rd columns

## Exchanging rows, columns

Swapping the  $i$ -th and  $j$ -th column:

`A([i,j],:)=A([j,i],:)` , and `A(:, [i,j])=A(:, [j,i])` respectively.

## Transforming to vector:

`A(:)` the elements of  $A$  listed in column major order:

`[A(:,1);...;A(:,end)]`

# Predefined matrices

<code>eye(n)</code>	the identity matrix of size $n \times n$
<code>eye(n,m)</code>	the identity matrix of size $n \times m$
<code>ones(n)</code>	the $n \times n$ array of all ones
<code>ones(n,m)</code>	the $n \times m$ array of all ones
<code>zeros(n)</code>	the $n \times n$ array of all zeros
<code>zeros(n,m)</code>	the $n \times m$ array of all zeros

# Matrix-vector operations

For matrices  $A$  and  $B$  and a scalar  $c$ , the operations

`A+B`

`A-B`

`c*A`

`A*B`

`A^2`

are performed in the usual way (as we learned in mathematics). The operation

`A+c`

is defined for convenience, it is a shorter form of `A+c*ones(size(A))`.  
The result of

`A/B`

and

`A\B`

$A \cdot B^{-1}$  and  $A^{-1} \cdot B$  respectively.

# Matrix-vector operations

## Elementwise operations

The `.` before the operator results in elementwise operation, so the  $ij$ -th element of

- `A.*B` is  $a_{ij} * b_{ij}$ ,
- `A.^2` is  $a_{ij}^2$ ,
- `A./B` is  $a_{ij}/b_{ij}$ .

Most of the built-in functions can be called with matrix argument, with elementwise evaluation.

## Some more builtins

- `det(A)` : determinant of  $A$
- `inv(A)` : inverse of  $A$
- `dot(a,b)` : scalar (inner) product of  $a$  and  $b$
- `norm(A)` 2-norm of  $A$  (also for vectors)
- `norm(A,inf)`  $\infty$ -norm of  $A$
- `norm(A,1)` 1-norm of  $A$

Solving the system  $Ax = b$ :

```
x=A\b
```

## Some more builtins

### diag

- `diag(a)` gives a square matrix whose main diagonal is  $a$
- `diag(a,k)` returns a square matrix whose  $k$ -th diagonal is  $a$ .
- `diag(A,k)` returns the  $k$ -th diagonal of  $A$

### Note

The main diagonal is the 0-th one. The diagonal above the  $k$ -th one is the  $k + 1$ -th one.



## Some more builtins

### `tril` and `triu`

- `tril(A)` : returns the lower triangle part of  $A$ .
- `triu(A)` : returns the upper triangle part of  $A$ .
- `tril(A,k)` : return the matrix  $A$  with elements above the  $k$ -th diagonal set to `0`.
- `triu(A,k)` : return the matrix  $A$  with elements below the  $k$ -th diagonal set to `0`.

# Defining functions

The structure (syntax) of Octave/Matlab functions:

```
function outVariables = funName( inVariables )  
    % body of the function  
end
```

**Important!** The name of file to which your function saved should be `funName.m`.

# Defining functions

## Example 1

```
function y=myquad(x)
    y=2*x.^2-3*x+5;
end
```

The result of the command `y=myquad(x)` is the value of  $2x^2 - 3x + 5$ , where  $x$  can be a vector or matrix, because we used elementwise operations in the definition.

# Important!

You can define several functions within a script. They must be lexically at the end of the script and they are visible only within the script (helper functions).

# Logical operators, functions

- `<`, `<=`, `>`, `>=`, `==`, `~=` (for vectors, matrices the comparison is done elementwise)
- `A&B`, `A|B`, `~A`, `xor(A,B)` (elementwise evaluation)
- `all(x)` : is true if all elements of `v` is nonzero.
- `all(A)` : is a row vector `[all(A(:,1)), ..., all(A(:,end))]`, that is `all` is applied column-wise.
- `all(A,2)` `all` is applied row-wise.
- `any(x)` : is true if some element of `v` is nonzero.
- `any(A)` : is a row vector `[any(A(:,1)), ..., any(A(:,end))]`, that is `any` is applied column-wise.
- `any(A,2)` `any` is applied row-wise.

# The `find` function

- `ind=find(A)` returns the indices of nonzero elements of  $A$  (column-wise ordering is used).
- `ind=find(A,n)` returns the indices of the first  $n$  nonzero elements of  $A$  (column-wise ordering is used).
- `ind=find(A,n,last)` returns the indices of the last  $n$  nonzero elements of  $A$  (column-wise ordering is used).
- `[rowI,colI]=find(A)` returns the row-column indices of nonzero elements of  $A$ .
- `[rowI,colI,elem]=find(A)` same as the previous, except that it catches also the nonzero elements.

# The `find` function

The `find` can be called with logical vector, matrix argument:

- `find(A<=B)`
- `find(A==5)`
- `find(A>5,4)`
- `find(A>5,4,last)`
- `find(A<5 & A>4)`
- `find(abs(A-2)<=0.01)`

`logical(A)` converts  $A$  to a logical array, the nonzeros map to the logical 1.

# Branching, if-else

```
if logicalExpression
    % body
else
    % body
end
```

## Example 2

```
N=input('Type an integer: ');
if mod(N,3)==0
    disp('divisible by 3');
else
    disp(sprintf('the remainder after dividing by 3 is: %d', mod(N,3) ))
end
```



# Useful structures, functions

- `break`: immediately exits the execution of the containing `for` or `while` loop
- `continue`: stops the execution of the body's statements, and then continues with the next iteration
- `pause`: waits for press a key
- `pause(n)`: waits for  $n$  seconds
- `return`: stops the execution of the script (or function)
- `error('message')`: stops the execution of the script (or function) displaying 'message'