

Matlab/Octave basics

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Vectors

The **row** and **column** vectors are **different**!

creating row-vectors:

The vector $a = (-1.2, 3.1, 4.7, 1.9)$ can be created by listing its elements enclosed by square brackets, separating them by **comma**:

`a = [-1.2, 3.1, 4.7, 1.9]`

or by **space**:

`a = [-1.2 3.1 4.7 1.9]`

Vectors

- 1 The indexing starts at 1.
- 2 the i -th element of the vector is a(i) .
- 3 length(a) returns the number of elements in a.
- 4 the empty vector is []

Vectors as regular sequences

the colon operator:

It is the most useful syntax for defining vectors.

- for the vector $b = (1, 2, 3, 4, 5)$ simply use: `b = 1:5`
- for $c = (5, 4, 3, 2, 1)$: `c = 5:-1:1`
- for $d = (2, 2.2, 2.4, 2.6, 2.8, 3)$: `d = 2:0.2:3`

the colon syntax:

```
x = first:stepsize:last
```

where the default value of stepsize is one , that is

```
x = first:last
```

is the shorter form of

```
x = first:1:last
```

the `linspace` function:

- the vector $e = (1, 1.2, 1.4, 1.6, 1.8, 2)$ can be created by:

```
e = linspace(1,2,6)
```

- for a 100 element vector f :

```
f = linspace(1,2)
```

linspace syntax:

```
x = linspace(first, last, numberOfElements)
```

The elements in the resulting vector are **equally spaced**. The **default** number of elements is **100**:

```
x = linspace(first, last)
```

is the shorter form of

```
x = linspace(first, last, 100)
```

Column-vectors

creation:

- by listing the elements separated by **semicolon**, enclosing them in square brackets:

```
m = [-3; 0; 7]
```

- transposing a row-vector:

```
n=[1 -2 4 -1]'
```

Note that: the operator `apostrophe` is the conjugate-transpose operator, so the result is not the expected one for complex valued vectors. For "transposing only" complex vectors use the function `transpose`

Column-vectors

The usage of `x(i)` and `length(x)` is the same as for row-vectors.

The call `size(x)` returns the vector

`[numOfRows, numOfColumns]`

where `numOfRows=1` for row-vectors and `numOfColumns=1` for column-vectors. In Octave/Matlab the vectors are 2-dimensional objects.

Common ways of defining vectors

- `[a, b]` : extending along the 2nd-dimension, the sizes of the 1st dimension must agree
- `[m;n]` : extending along the 1st-dimension, the sizes of the 2nd dimension must agree
- `[-4 a 3 -1]` : extending along the 2nd dimension by listing the new elements
- `[1;m;-3]` : extending along the 1st dimension by listing the new elements
- `h(2:4)` : extract a subvector by specifying the indices of the desired elements
- `h([1 4 5])` : extract a subvector by specifying the indices of the desired elements
- `h(2)=[]` : clear individual elements
- `h([2 4])=[]` : clear elements specified by an index vector

Important! For `a=[-1 3 2]` the result of the command `a(6)=4` is the vector `a=[-1 3 2 0 0 4]`. Note that one could expect. The undefined new elements will be set to zero. There is no warning issued by the system!

Some useful functions

- `min(x)` and `max(x)` returns the smallest and the largest element of `x`
- `sort(x)` returns the sorted instance of `x` (the default order: increasing)
- `sort(x, 'descend')` returns the reversely sorted instance of `x`
- `flip(x)` returns a new vector (matrix) with elements of `x` in reverse order (for matrices the elements are the rows by default)
- `length(x)` number of elements
- `sum(x)` sum of the elements
- `prod(x)` product of the elements
- `mean(x)` arithmetic mean of the elements of `x`
- `x(end)` in vector (matrix) context the `end` has special meaning: the last element of the object

Vector operations

For the same shaped vectors `a` and `b`

- `a+b` and `a-b` is the elementwise sum and difference
- `x=a+1` for convenience the basic operations with a scalar defined elementwise
- `x=a.^ 2` see above
- `x=a.*b` it is the elementwise product, results in a new vector $a;b$;
- `x=a./b` see above
- `x=1./a` shorter version of `ones(size(a))./a`
- `dot(a,b)` the scalar, inner product, the sum-product of the vectors

Important! The dot before the operator results elementwise operations.

The builtin functions `sin`, `cos`, `tan`, `exp`, `log`, `sqrt`, `abs`, can have vector and matrix parameters, resulting the function called elementwise.

`NaN` : Not a Number is a result of undefined operation. For example $0/0$,
`Inf/Inf`)

Matrices in Octave/Matlab

Defining matrices by listing

$A = [1, 2, 3; 4, 5, 6; 7, 8, 9]$ or $A = [1 \ 2 \ 3; \ 4 \ 5 \ 6; \ 7 \ 8 \ 9]$ results in:

$$A = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{pmatrix}$$

The `comma` separates the elements of the row, the `semicolon` separates the rows

The indexing for matrices is `one` based, as for vectors.

$A(i, j)$ is the (i, j) -th element of A

Defining matrices from vectors

For vectors $a = [1 \ -2 \ 0]$; $b = [2 \ -11 \ 7]$; $m = [-3; 0; 7]$;

$n = [1; \ -2; \ 0]$;

the result of

$B = [a; b] :$

$$B = \begin{pmatrix} 1 & -2 & 0 \\ 2 & -11 & 7 \end{pmatrix}$$

$C = [a' \ b']$ and $D = [m' \ a'] :$

$$C = \begin{pmatrix} 1 & 2 \\ -2 & -11 \\ 0 & 7 \end{pmatrix} \quad D = \begin{pmatrix} -3 & 1 \\ 0 & -2 \\ 7 & 0 \end{pmatrix}$$

Extending matrices

For matrices and vectors defined above the result of $E=[A; a]$ (or
 $E=[A; [1, -2, 0]]$):

$$E = \begin{pmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \\ 1 & -2 & 0 \end{pmatrix}$$

The result of $F=[A \ m]$ (or $F=[A, \ m]$):

$$F = \begin{pmatrix} 1 & 2 & 3 & -3 \\ 4 & 5 & 6 & 0 \\ 7 & 8 & 9 & 7 \end{pmatrix}$$

Extending matrices

For $G = [C \ D]$ and $H = [C; D]$ we get:

$$G = \begin{pmatrix} 1 & 2 & -3 & 1 \\ -2 & -11 & 0 & -2 \\ 0 & 7 & 7 & 0 \end{pmatrix} \quad H = \begin{pmatrix} 1 & 2 \\ -2 & -11 \\ 0 & 7 \\ -3 & 1 \\ 0 & -2 \\ 7 & 0 \end{pmatrix}$$

For $C(4,5)=9$:

$$C = \begin{pmatrix} 1 & 2 & 0 & 0 & 0 \\ -2 & -11 & 0 & 0 & 0 \\ 0 & 7 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 9 \end{pmatrix}$$

The size of matrix has changed without warning!

Accessing elements, rows, columns and submatrices

- `size(A)` : the number of rows and columns in A
- `length(A) = max(size(A))`
- `numel(A)` the number of elements in A
- `A(i,j)` the i,j -th element
- `A(i,:)` the i -th row-vector
- `A(:,j)` the j -th column
- `A(2:3,:)` the 2-nd and 3-rd rows
- `A([1 2 4],:)` the 1., 2. and 4. rows
- `A(:,[1 3])` the 1. and 3. columns
- `A(2:3,[1 3])` the 1. and 3. elements of the 2. and 3. rows

Manipulating matrices

Deleting rows and columns

- $A(i,:) = []$ will delete the i -th row
- $A(:,j) = []$ will delete the j -th column
- $A([1 3], :) = []$ will delete the 1-st and 3-rd rows
- $A(:, [1 3]) = []$ will delete the 1-st and 3-rd columns

Exchanging rows, columns

Swapping the i -th and j -th column:

$A([i,j], :) = A([j,i], :)$, and $A(:, [i,j]) = A(:, [j,i])$ respectively.

Transforming to vector:

$A(:)$ the elements of A listed in column major order:

$[A(:,1); \dots; A(:,\text{end})]$

Predefined matrices

`eye(n)`

the identity matrix of size $n \times n$

`eye(n,m)`

the identity matrix of size $n \times m$

`ones(n)`

the $n \times n$ array of all ones

`ones(n,m)`

the $n \times m$ array of all ones

`zeros(n)`

the $n \times n$ array of all zeros

`zeros(n,m)`

the $n \times m$ array of all zeros

Matrix-vector operations

For matrices A and B and a scalar c , the operations

$A+B$ $A-B$ $c*A$ $A*B$ A^2

are performed in the usual way (as we learned in mathematics). The operation

$A+c$

is defined for convenience, it is a shorter form of `A+c*ones(size(A))`.
The result of

A/B and $A\backslash B$

$A \cdot B^{-1}$ and $A^{-1} \cdot B$ respectively.

Matrix-vector operations

Elementwise operations

The `.` before the operator results in elementwise operation, so the ij -th element of

- `A.*B` is $a_{ij} * b_{ij}$,
- `A.^2` is a_{ij}^2 ,
- `A./B` is a_{ij}/b_{ij} .

Most of the built-in functions can be called with matrix argument, with elementwise evaluation.

Some more builtins

- `det(A)` : determinant of A
- `inv(A)` : inverse of A
- `dot(a,b)` : scalar (inner) product of a and b
- `norm(A)` 2-norm of A (also for vectors)
- `norm(A,inf)` ∞ -norm of A
- `norm(A,1)` 1-norm of A

Solving the system $Ax = b$:

$$x = A \setminus b$$

Some more builtins

diag

- `diag(a)` gives a square matrix whose main diagonal is a
- `diag(a,k)` returns a square matrix whose k -th diagonal is a .
- `diag(A,k)` returns the k -th diagonal of A

Note

The main diagonal is the 0-th one. The diagonal above the k -th one is the $k + 1$ -th one.

Some more builtins

tril and triu

- `tril(A)` : returns the lower triangle part of A .
- `triu(A)` : returns the upper triangle part of A .
- `tril(A,k)` : return the matrix A with elements above the k -th diagonal set to `0`.
- `triu(A,k)` : return the matrix A with elements below the k -th diagonal set to `0`.

Defining functions

The structure (syntax) of Octave/Matlab functions:

```
function outVariables = funName( inVariables )
    % body of the function
end
```

Important! The name of file to which your function saved should be `funName.m`.

Defining functions

Example 1

```
function y=myquad(x)
    y=2*x.^2-3*x+5;
end
```

The result of the command `y=myquad(x)` is the value of $2x^2 - 3x + 5$, where x can be a vector or matrix, because we used elementwise operations in the definition.

Important!

You can define several functions within a script. They must be lexically at the end of the script and they are visible only within the script (helper functions).

Logical operators, functions

- $<$, \leq , $>$, \geq , $=$, $\sim=$ (for vectors,matrices the comparison is done elementwise)
- $A \& B$, $A | B$, $\sim A$, $\text{xor}(A, B)$ (elementwise evaluation)
- $\text{all}(x)$: is true if all elements of v is nonzero.
- $\text{all}(A)$: is a row vector $[\text{all}(A(:,1)), \dots, \text{all}(A(:,\text{end}))]$, that is all is applied column-wise.
- $\text{all}(A, 2)$ all is applied row-wise.
- $\text{any}(x)$: is true if some element of v is nonzero.
- $\text{any}(A)$: is a row vector $[\text{any}(A(:,1)), \dots, \text{any}(A(:,\text{end}))]$, that is any is applied column-wise.
- $\text{any}(A, 2)$ any is applied row-wise.

The `find` function

- `ind=find(A)` returns the indices of nonzero elements of A (column-wise ordering is used).
- `ind=find(A,n)` returns the indices of the first n nonzero elements of A (column-wise ordering is used).
- `ind=find(A,n,last)` returns the indices of the last n nonzero elements of A (column-wise ordering is used).
- `[rowI,colI]=find(A)` returns the row-column indices of nonzero elements of A .
- `[rowI,colI,elem]=find(A)` same as the previous, except that it catches also the nonzero elements.

The `find` function

The `find` can be called with logical vector, matrix argument:

- `find(A<=B)`
- `find(A==5)`
- `find(A>5,4)`
- `find(A>5,4,last)`
- `find(A<5 & A>4)`
- `find(abs(A-2)<=0.01)`

`logical(A)` converts A to a logical array, the nonzeros map to the logical 1.

Branching, if-else

```
if logicalExpression  
    % body  
else  
    % body  
end
```

Example 2

```
N=input('Type an integer:');  
if mod(N,3)==0  
    disp('divisible by 3');  
else  
    disp(sprintf('the remainder after dividing by 3 is: %d', mod(N,3) ))  
end
```

Useful structures, functions

- `break` : immediately exits the execution of the containing for or while loop
- `continue` : stops the execution of the body's statements, and then continues with the next iteration
- `pause` : waits for press a key
- `pause(n)` : waits for *n* seconds
- `return` : stops the execution of the script (or function)
- `error('message')` : stops the execution of the script (or function) displaying 'message'