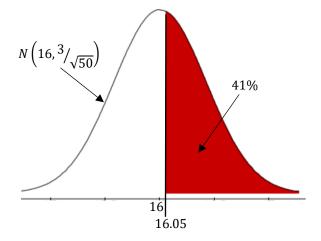
## ST517 Sample Midterm—Solutions

- 1. C
- 2. A
- 3. C
- 4. B5. B
- 6. B  $\left[ \int_0^{0.4} 2x dx = 0.4^2 \right]$
- 7. D
- 8. D
- 9. D
- 10. B
- 11. C
- 12. D
- 13. A
- 14. B
- 15. D
- 16. C
- 17. D
- 18. D
- 19. B
- 20. Note: this is a question about the distribution of the sample average; since n = 50 > 30, the CLT holds and we know that the sampling distribution of  $\bar{x}$  will be normal!



- 21. While np = (50)(0.95) = 47.5 meets the large sample condition, n(1-p) = (50)(0.05) = 2.5 does not. Thus the shape of the sampling distribution of p-hat will not be normal; rather it will be left-skewed. We can say that the center will be 0.95, and the standard deviation will be  $\sqrt{\frac{(0.95)(0.05)}{50}} = 0.03$ .
- 22.
- a.  $30 \pm t_{74} \times \frac{5}{\sqrt{75}}$
- b. 90% of possible random samples of 75 homes from this county would produce a 90% confidence interval that contains the true average amount of lawn space allowed for pets.

$$E(\widehat{\Theta}) = E\left(\frac{n+1}{n}Y\right) = \frac{n+1}{n}E(Y) = \frac{n+1}{n}\frac{n}{n+1}\theta = \theta$$

Since  $E(\widehat{\Theta}) = \theta$ ,  $\widehat{\Theta}$  is unbiased for  $\theta$ .

24. The group should use method 2. Method 1 is a convenience sample, and convenience samples tend to be biased. Method 2 is a cluster random sample where classes are the clusters. Cluster random samples tend to be unbiased. Since method 1 would likely be biased and method 2 would likely be unbiased, the group should use method 2.

$$25. \ P(X \ge 2) = 1 - P(X < 2) = 1 - \left[ \binom{20}{0} (0.06^0)(0.94^{20}) + \binom{20}{1} (0.06^1)(0.94^{19}) \right]$$

Note: you could solve  $P(X \ge 2)$  directly, but this would waste a lot of time!

$$P(X \ge 2) = {20 \choose 2} (0.06^2) (0.94^{18}) + {20 \choose 3} (0.06^3) (0.94^{17}) + \dots + {20 \choose 20} (0.06^{20}) (0.94^0)$$