

How to
Interpret (or not)
a
Machine Learning
model

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2 topics

Interpretability

Model Selection

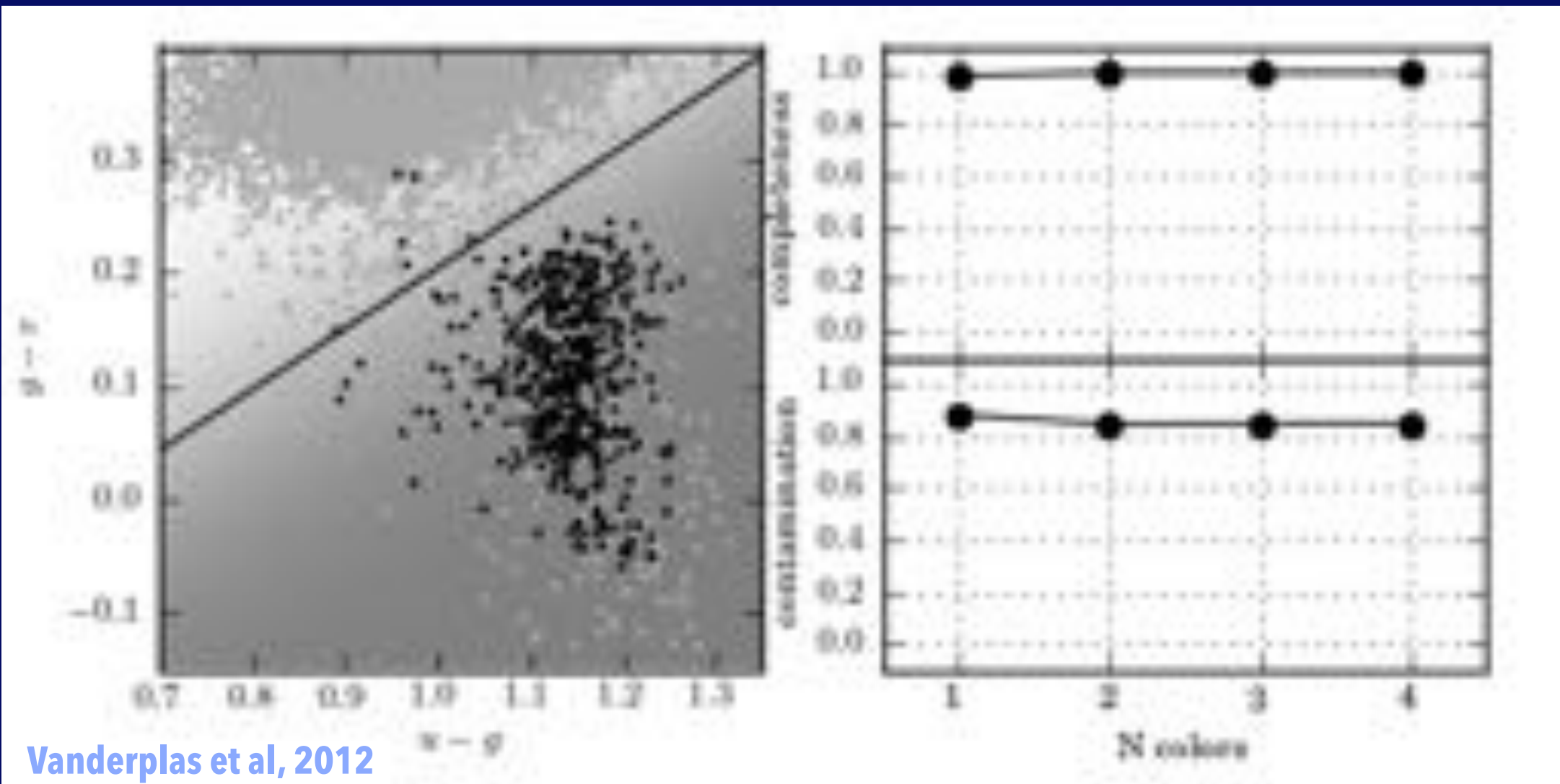
Interpretability

YOUR MODEL IS INTERESTING...



BUT WHAT DOES IT MEAN?

Logistic Regression of RR Lyrae Stars



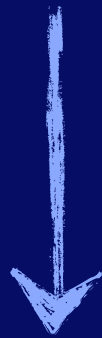
... now what?

**What does interpretability
mean to you?**

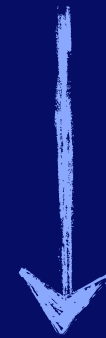
2 main goals:
inference versus prediction

2 main goals:

inference **versus prediction**



statistics!



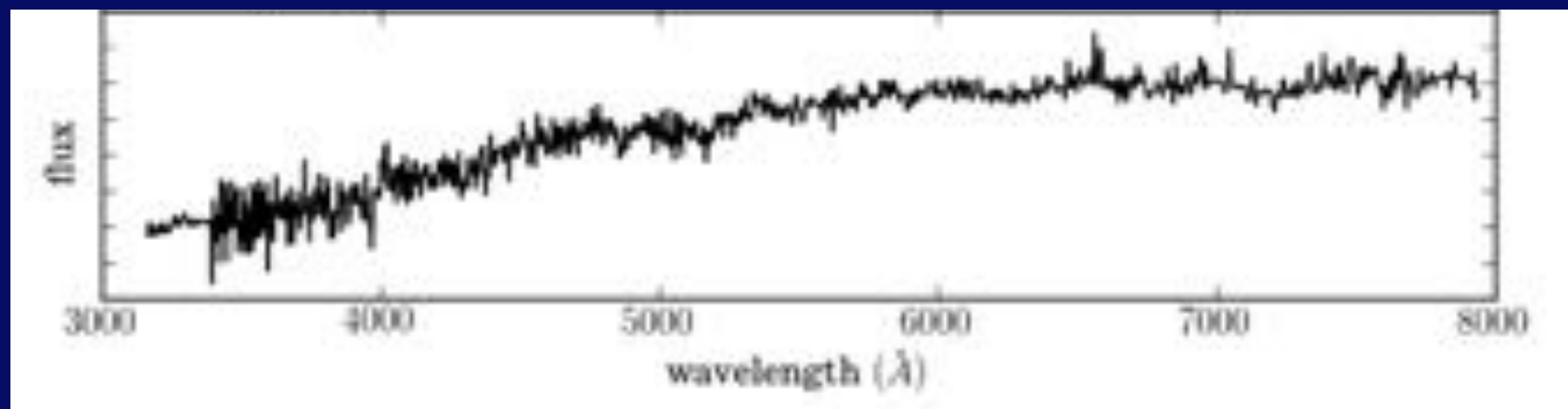
machine learning

Inference

“a conclusion reached on the basis of evidence and reasoning”

Inference

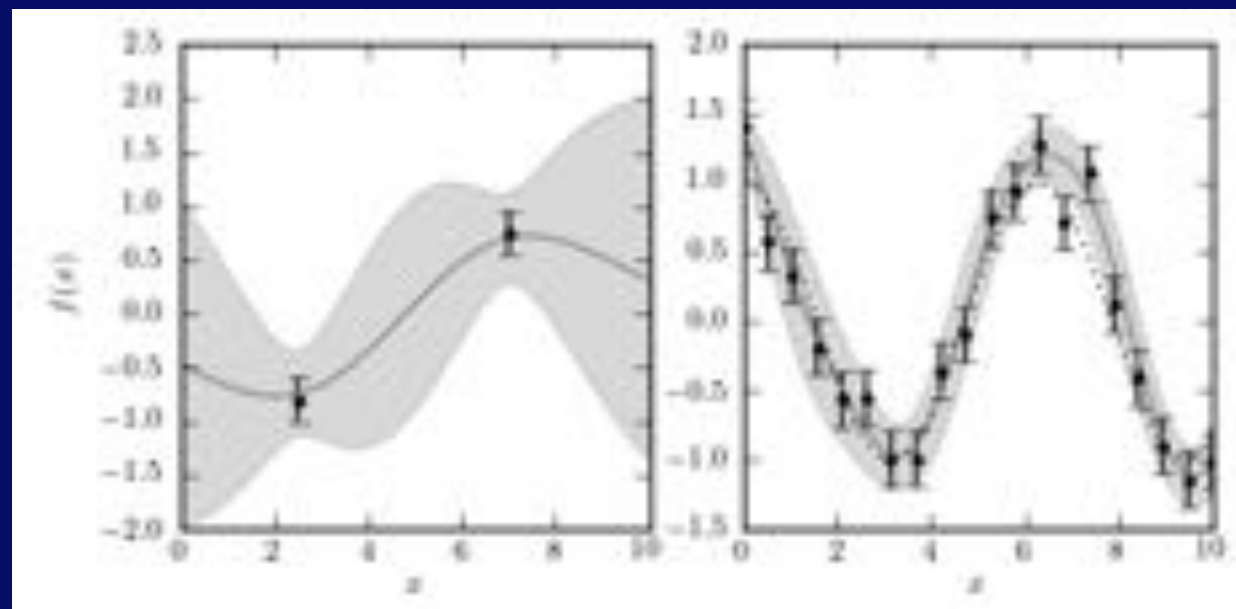
“Why do stars have different colours from galaxies?”



Vanderplas et al, 2012

Prediction

"Given my data points X and outcomes y , what outcome will I predict for a new data point x ?"



Vanderplas et al, 2012

Z. Lipton: The Mythos of Model Interpretability
<https://arxiv.org/abs/1606.03490>

**Scientific goal: uncover
causal relationship**

≠

**ML goal: minimize
prediction error**

Motives

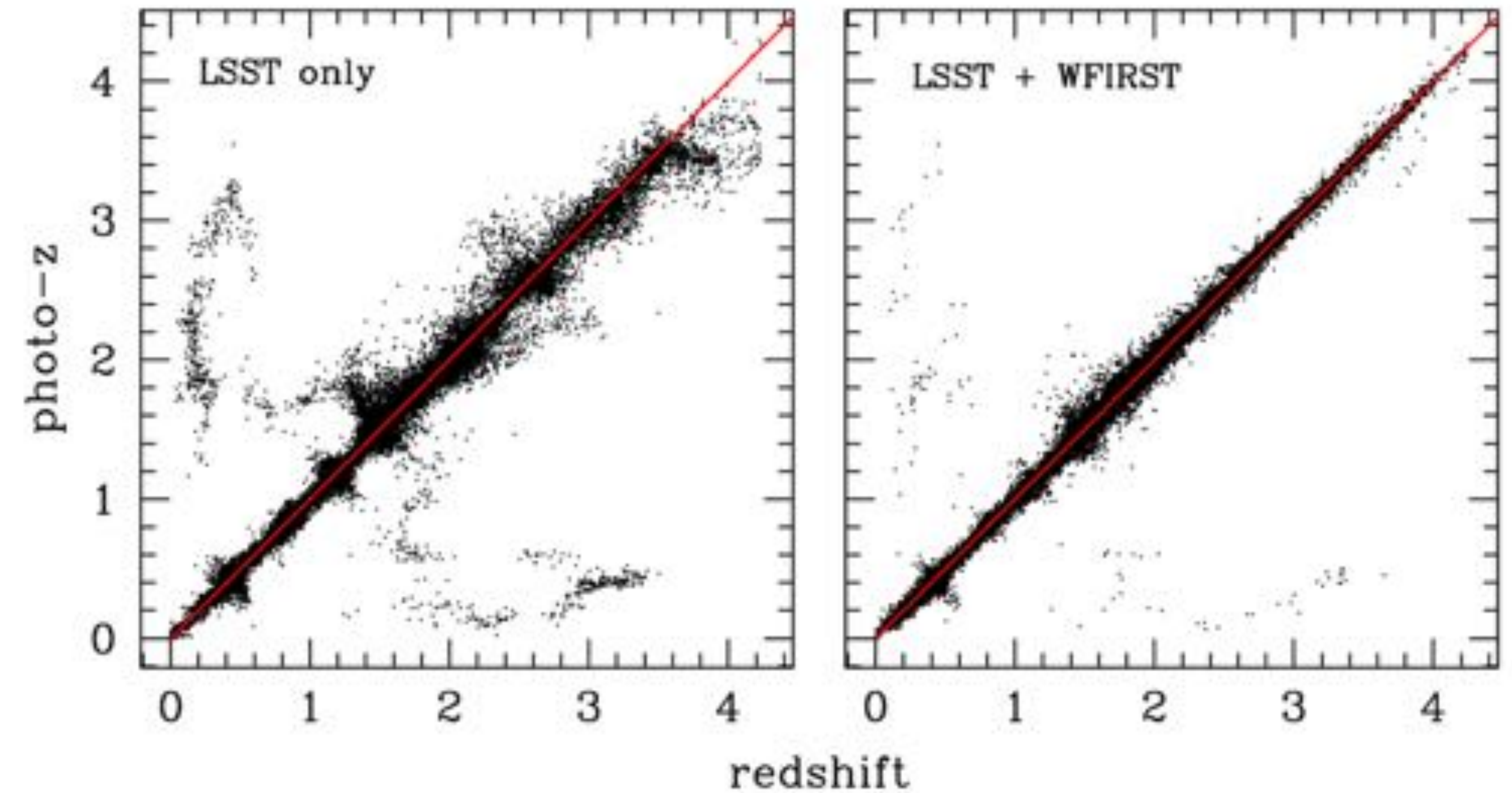
Trust

**Understandability? Of features? Parameters?
Models? Algorithms?**

Low test error?

**Does training data match deployment
environment?**

Trust



Causality



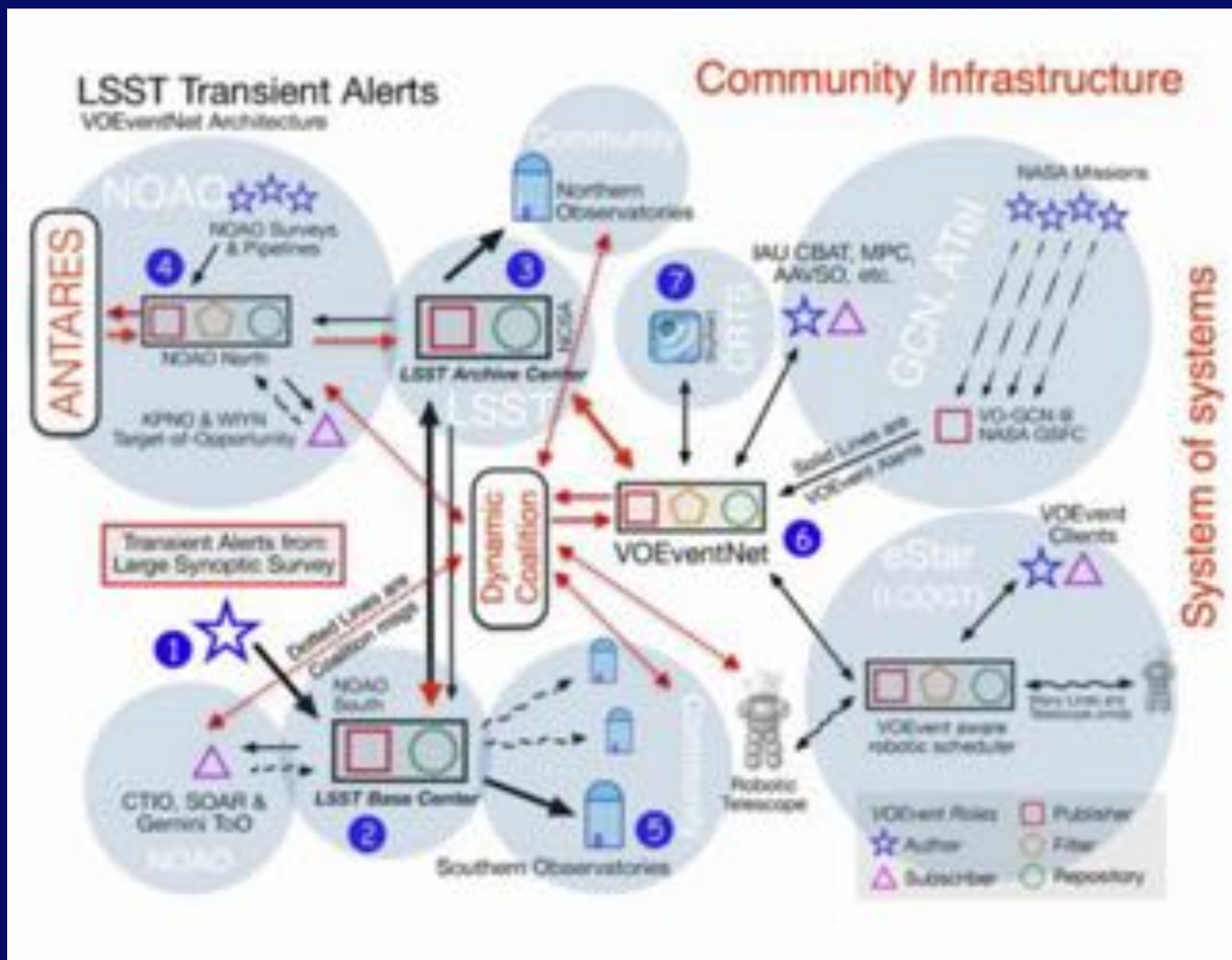
Transferability



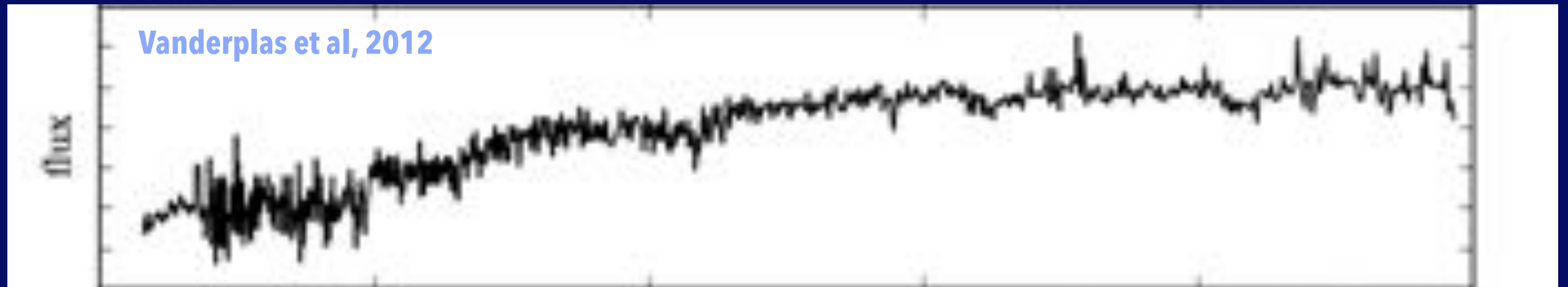
<http://emedicine.medscape.com/article/360090-overview>

See also: Caruana et al, 2015

Transferability

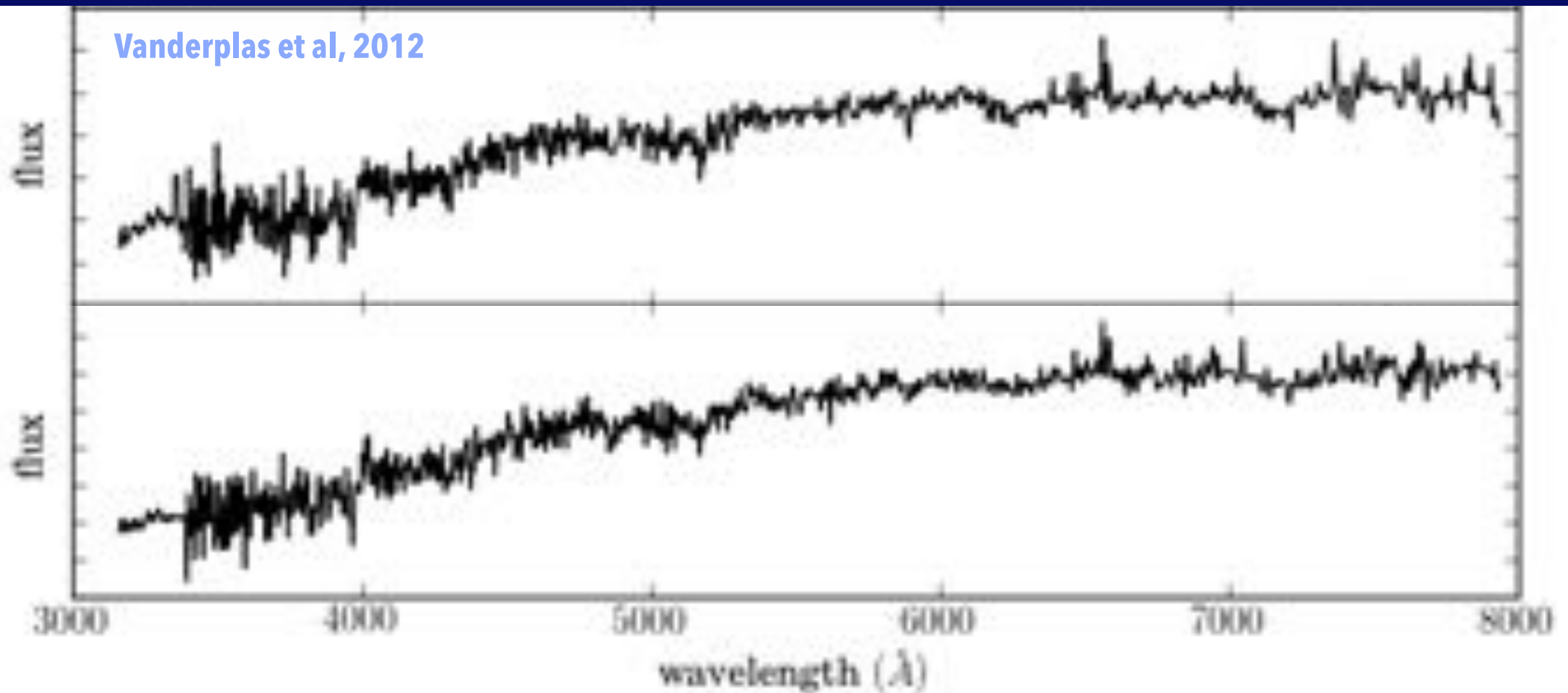


Informativeness



Informativeness

Vanderplas et al, 2012

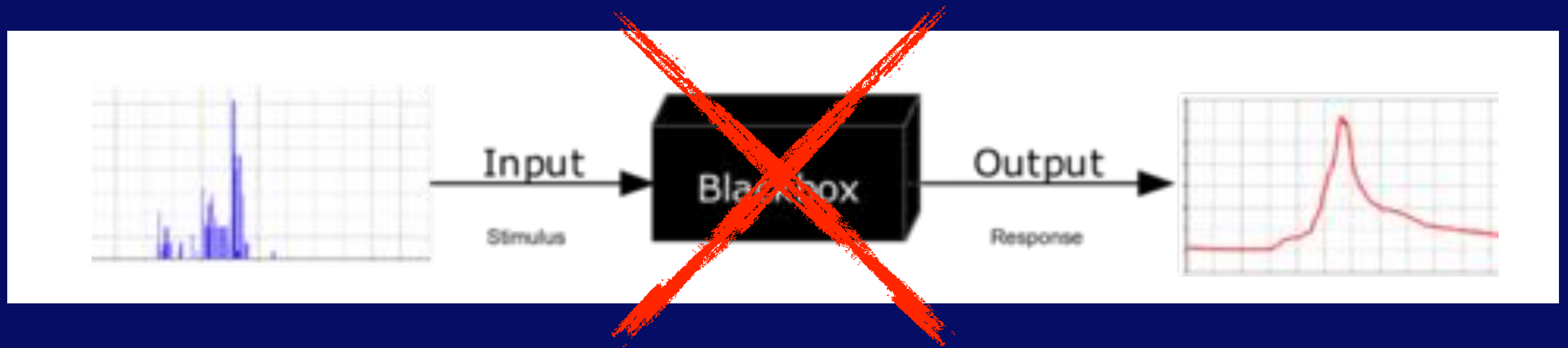


Properties of an interpretable model

1) Transparency



1) Transparency



Simulatability

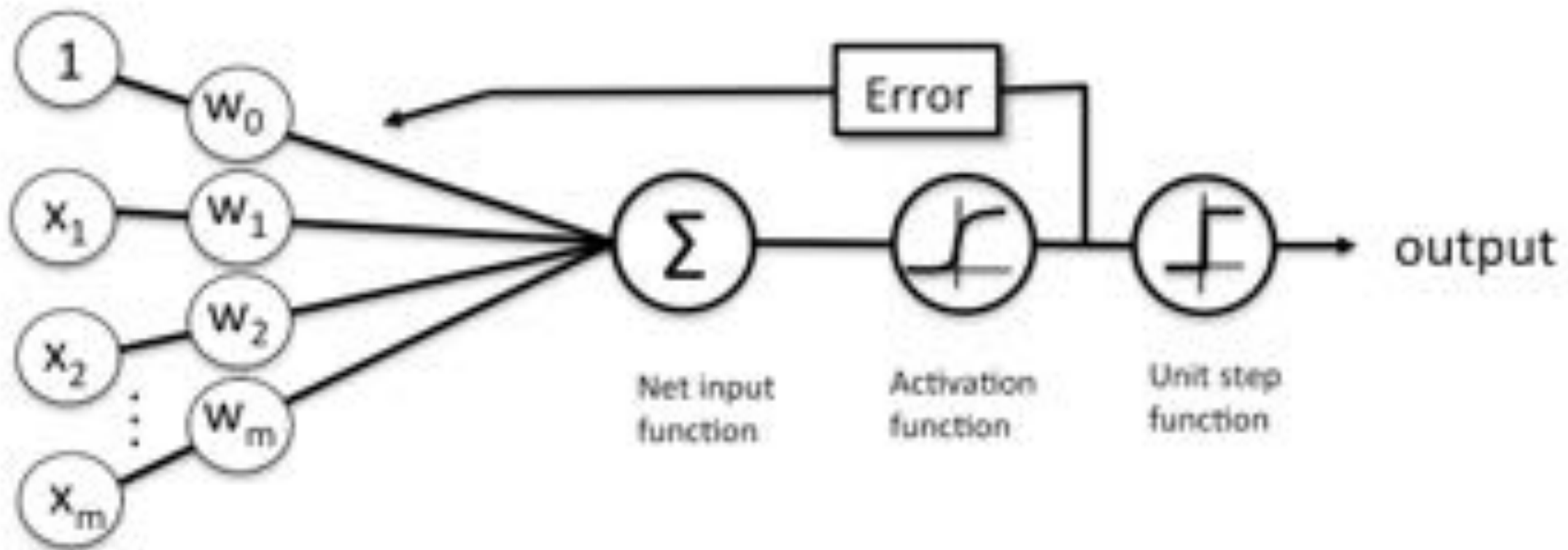


= ability to understand model in your head

Example: Decision Trees



Decomposability



Schematic of a logistic regression classifier.

= ability to understand model components

Algorithmic Transparency*

The image shows a handwritten mathematical derivation of the Central Limit Theorem for a binomial distribution. The derivation starts with the binomial probability mass function and uses Stirling's approximation to simplify the factorials. It then shows the standardization of the binomial variable, leading to the normal distribution. The final result is the Central Limit Theorem for a binomial distribution.

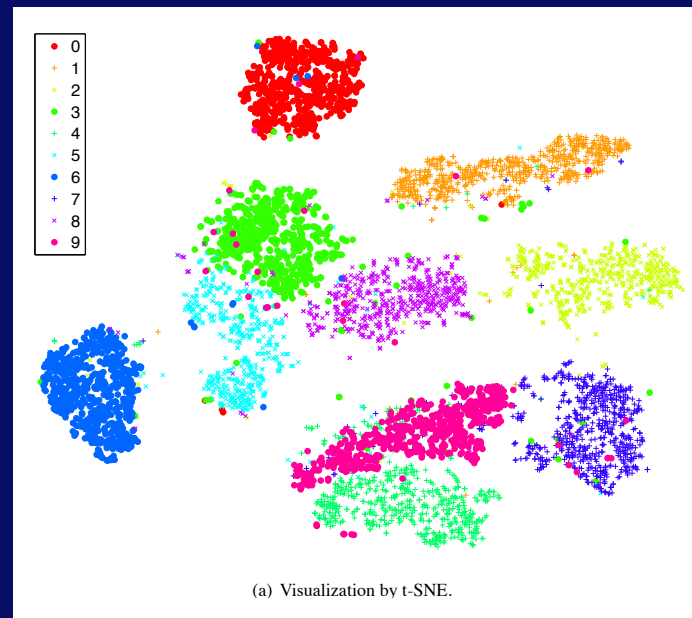
$$P(X = k) = \binom{n}{k} p^k (1-p)^{n-k}$$
$$\approx \frac{1}{\sqrt{2\pi np(1-p)}} \exp\left(-\frac{(k - np)^2}{2np(1-p)}\right)$$
$$P\left(\frac{X - np}{\sqrt{np(1-p)}} < \frac{t}{\sqrt{n}}\right) \rightarrow \Phi\left(\frac{t}{\sqrt{n}}\right)$$
$$(X - np)^2 < t^2 np(1-p)$$
$$X^2 - 2npX + n^2p^2 < t^2 np(1-p)$$

***note: humans have no algorithmic transparency whatsoever!**

2) Post-Hoc Interpretability



**natural language
explanations**

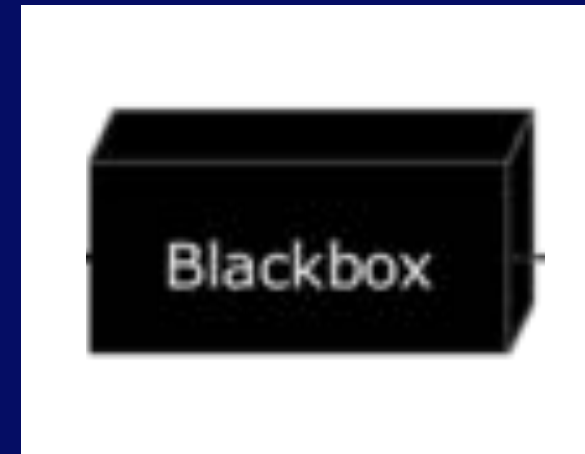
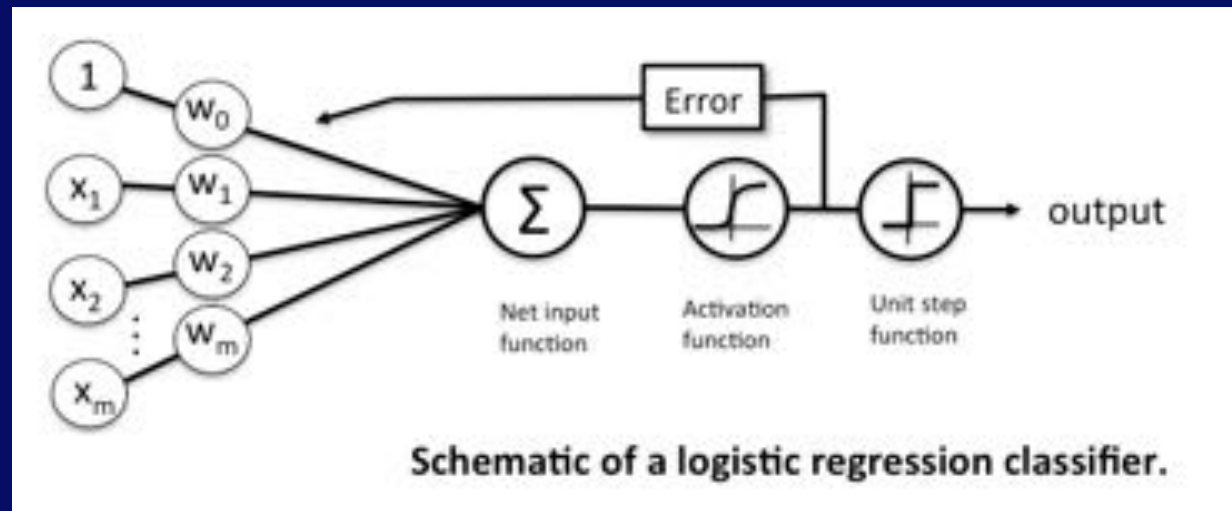


visualization



learning by example

Black Box Benchmarking

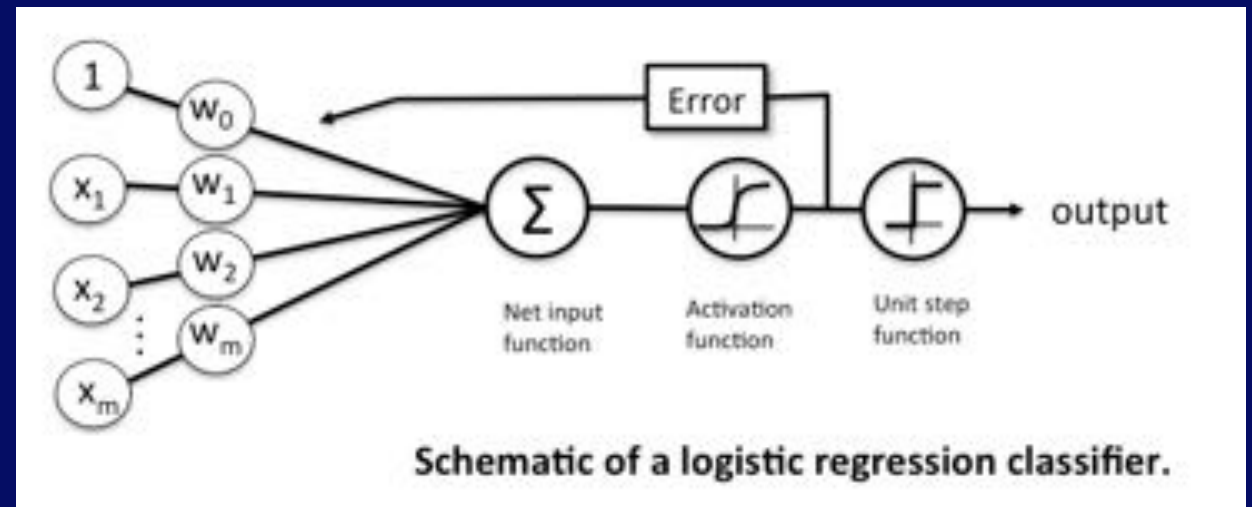
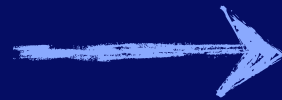
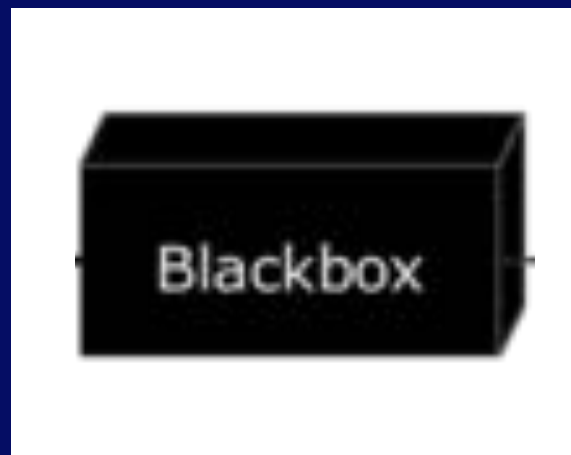


1) train linear model

2) train blackbox model

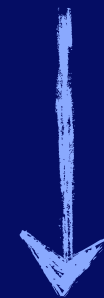
compare!

Surrogate Models



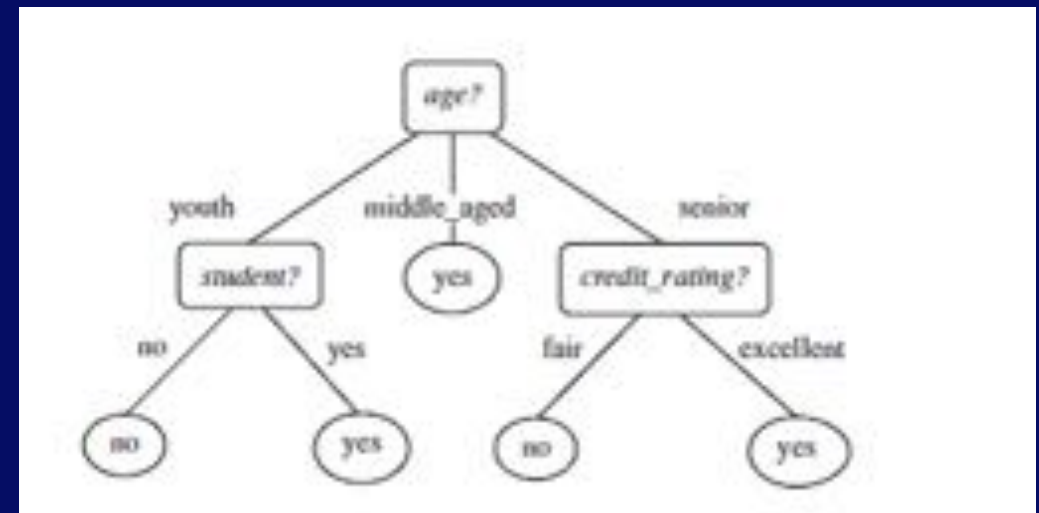
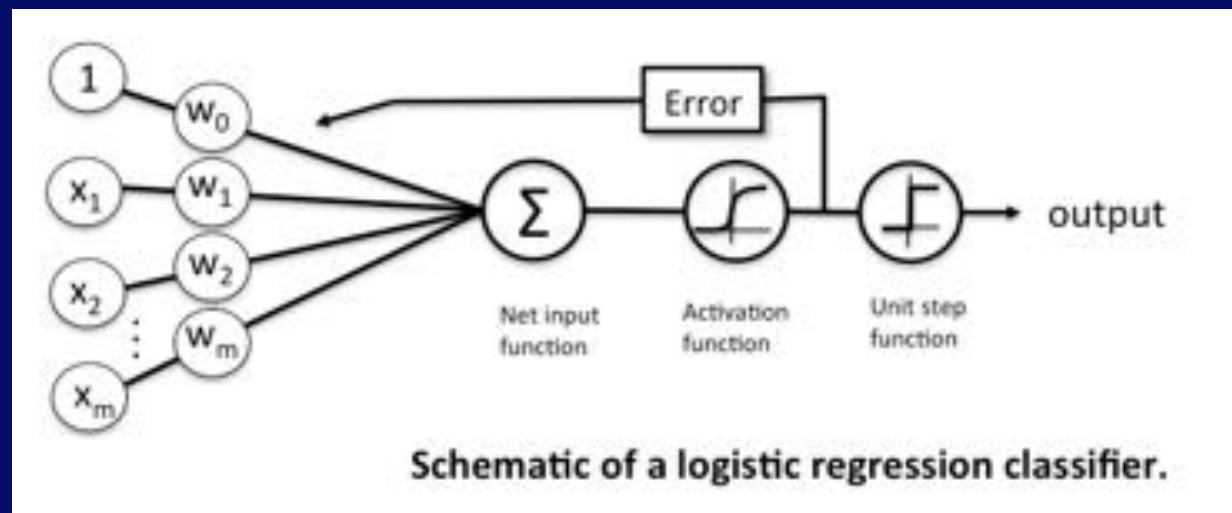
**1) train blackbox
model**

**2) train interpretable
model on predictors**



interpret

Ensemble of Models

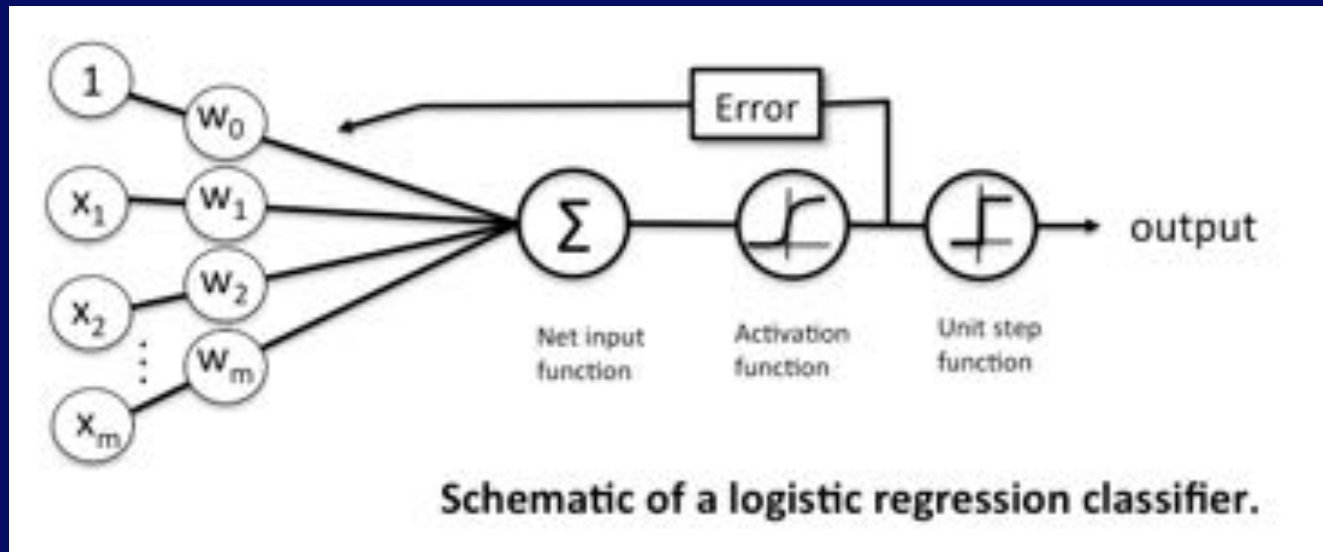


1) train interpretable
linear model

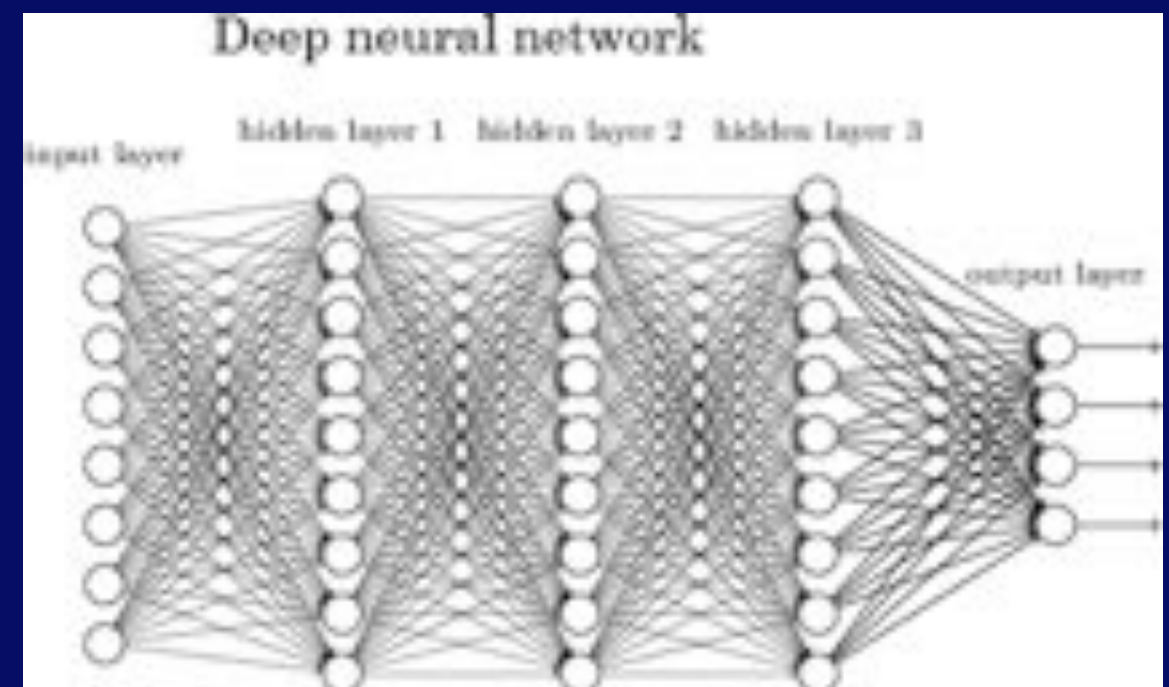
2) train interpretable
decision tree

compare

Which is easier to interpret?



or



Answer: it depends!

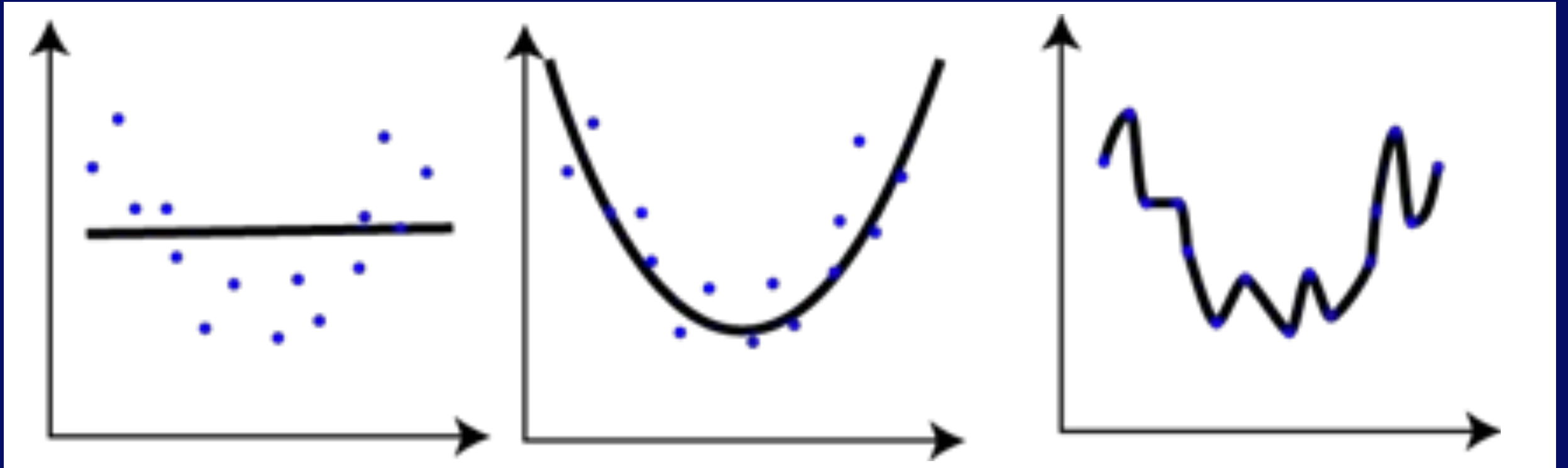
A linear model with highly engineered features and high-dimensional variables may not be very interpretable

but: linear models have a better track record for modelling the natural world and identifying weaknesses in the training data

**Think carefully about your goals,
your features, and your feature
engineering!**

Model Selection

Model Selection



- 1) **avoid overfitting** (prediction)
- 2) **decide between (physical) models** (inference)

Possible models?

- 1) **algorithms**
- 2) **algorithm-specific parameters**
- 3) **regularization parameters**
- 4) **feature selection**

Cross-validation

- 1) **hold-out cross-validation**
- 2) **k-fold cross-validation**
- 3) **leave-one-out (LOO) cross validation**
- 4) **random subset cross validation**

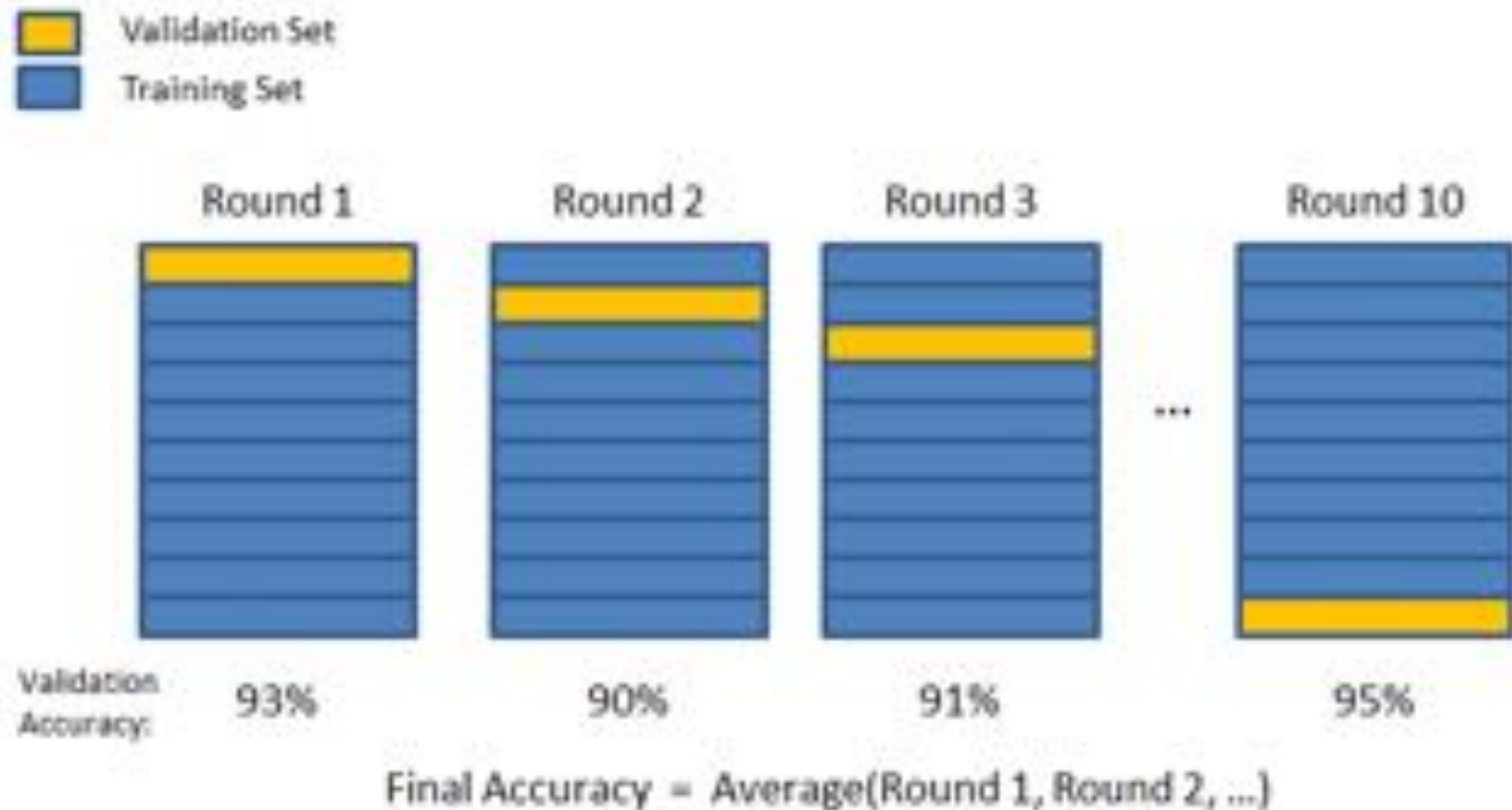
Nomenclature

training set: a data set to train your algorithm on

validation set: a data set to use for comparing the performance of different models

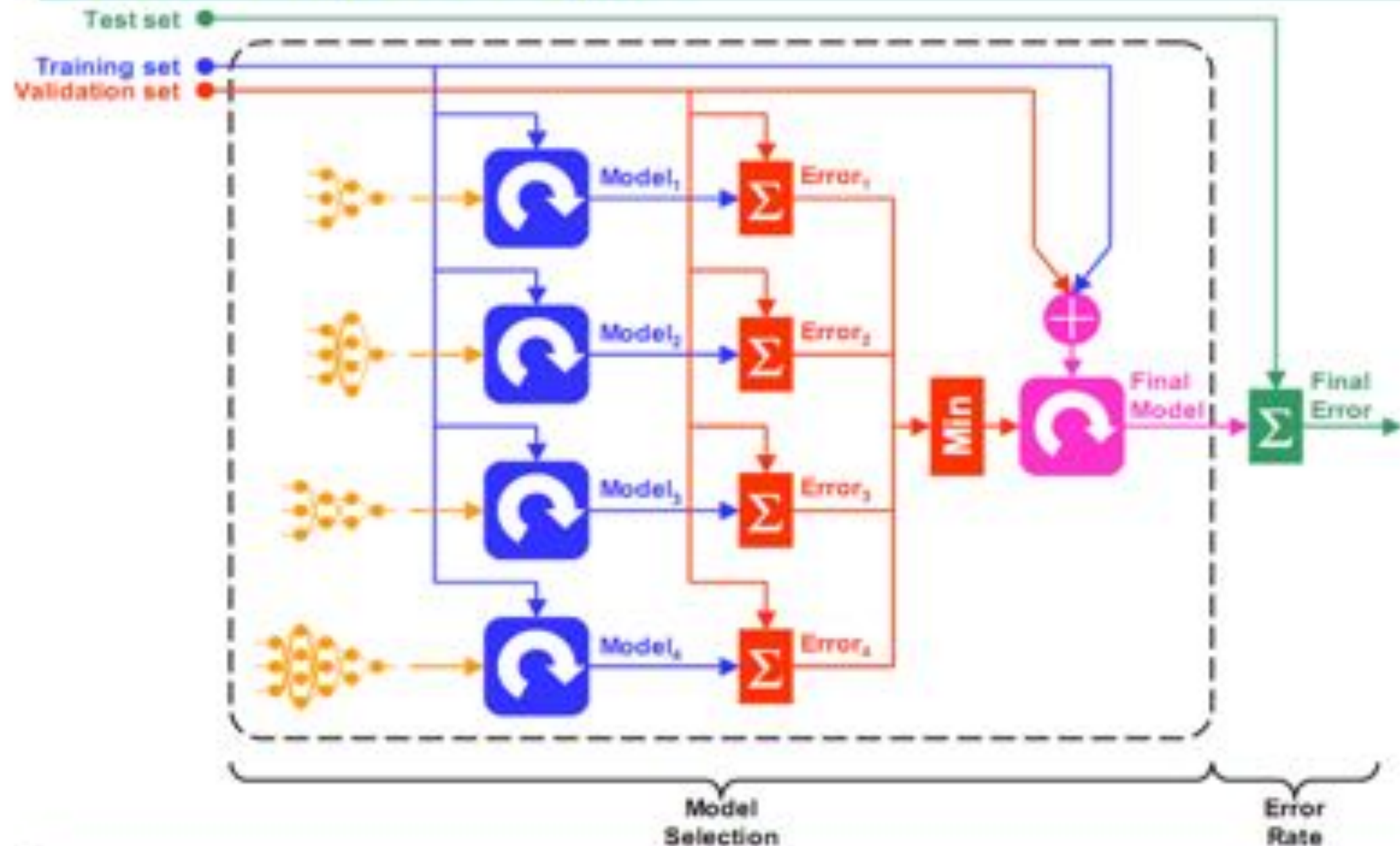
test set: a data set reserved to compute the error estimate of the final chosen model

Hold-out + k-fold cross-validation

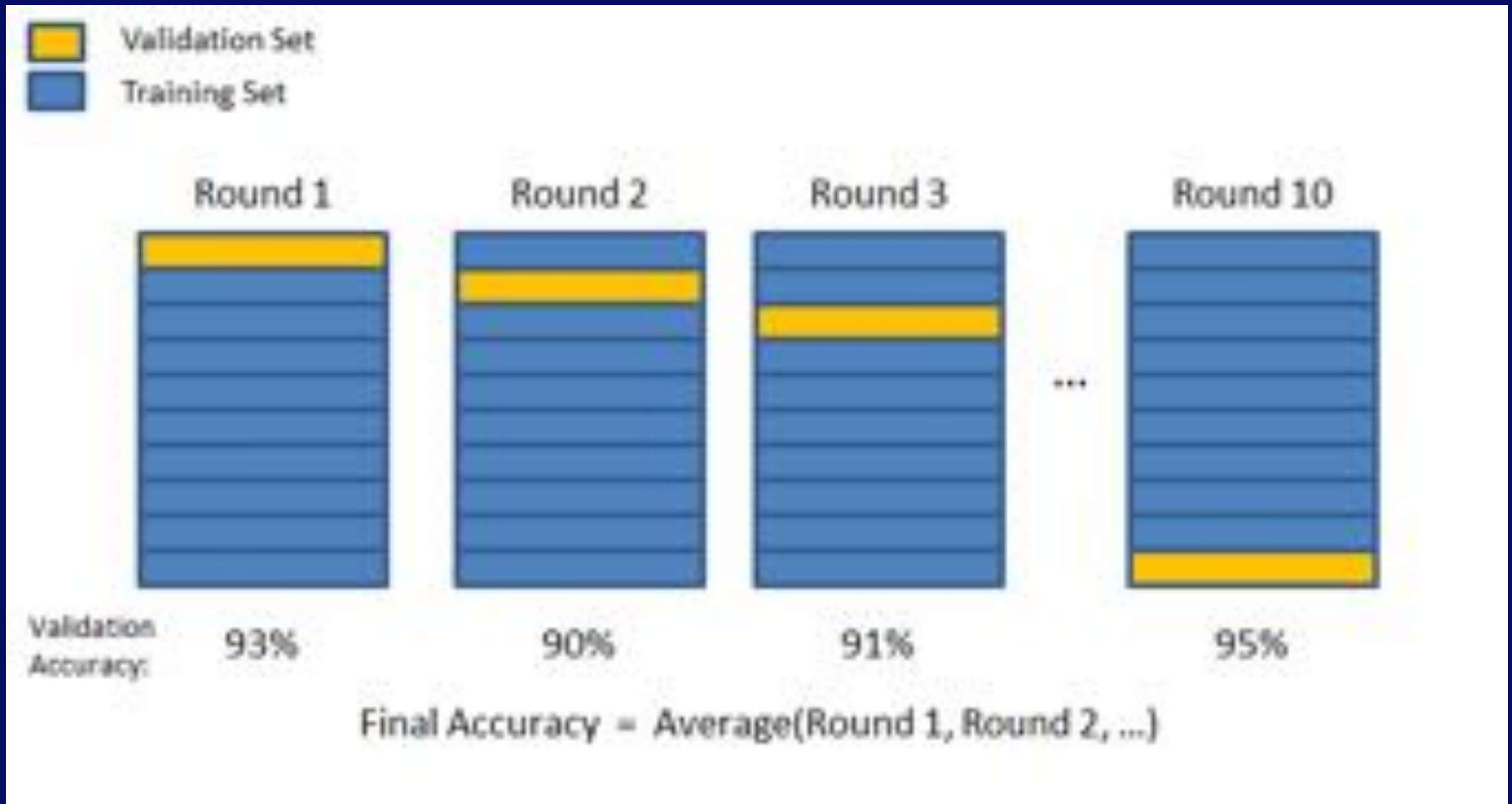


Hold-out + k-fold cross-validation

Three-way data splits



Leave one out cross validation



special case: $k = N$

Random subset cross validation

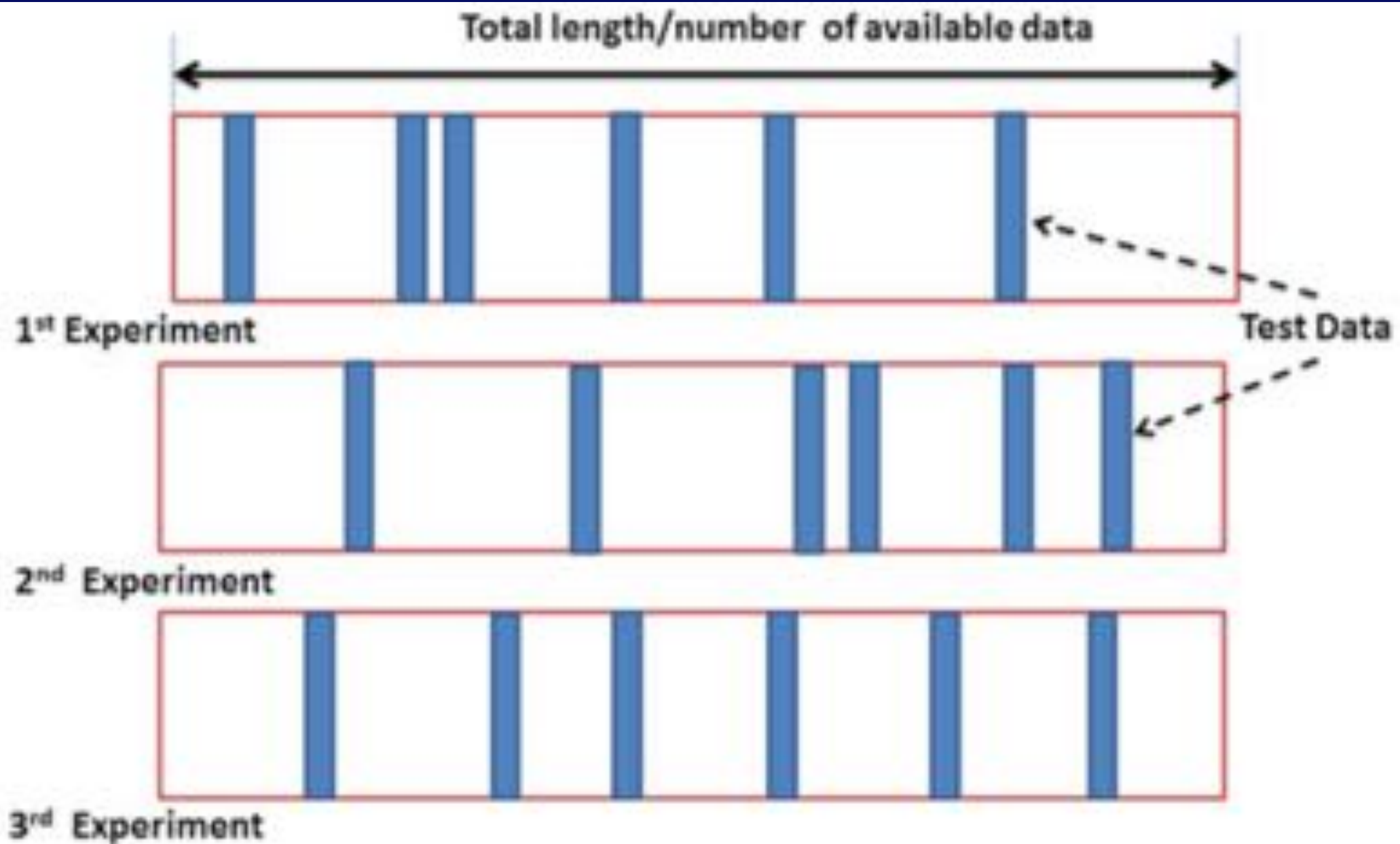


Fig. 3.7 Data splitting in the random sub-sampling approach

**What do you compare during
cross validation?**

Example: LSST alerts!



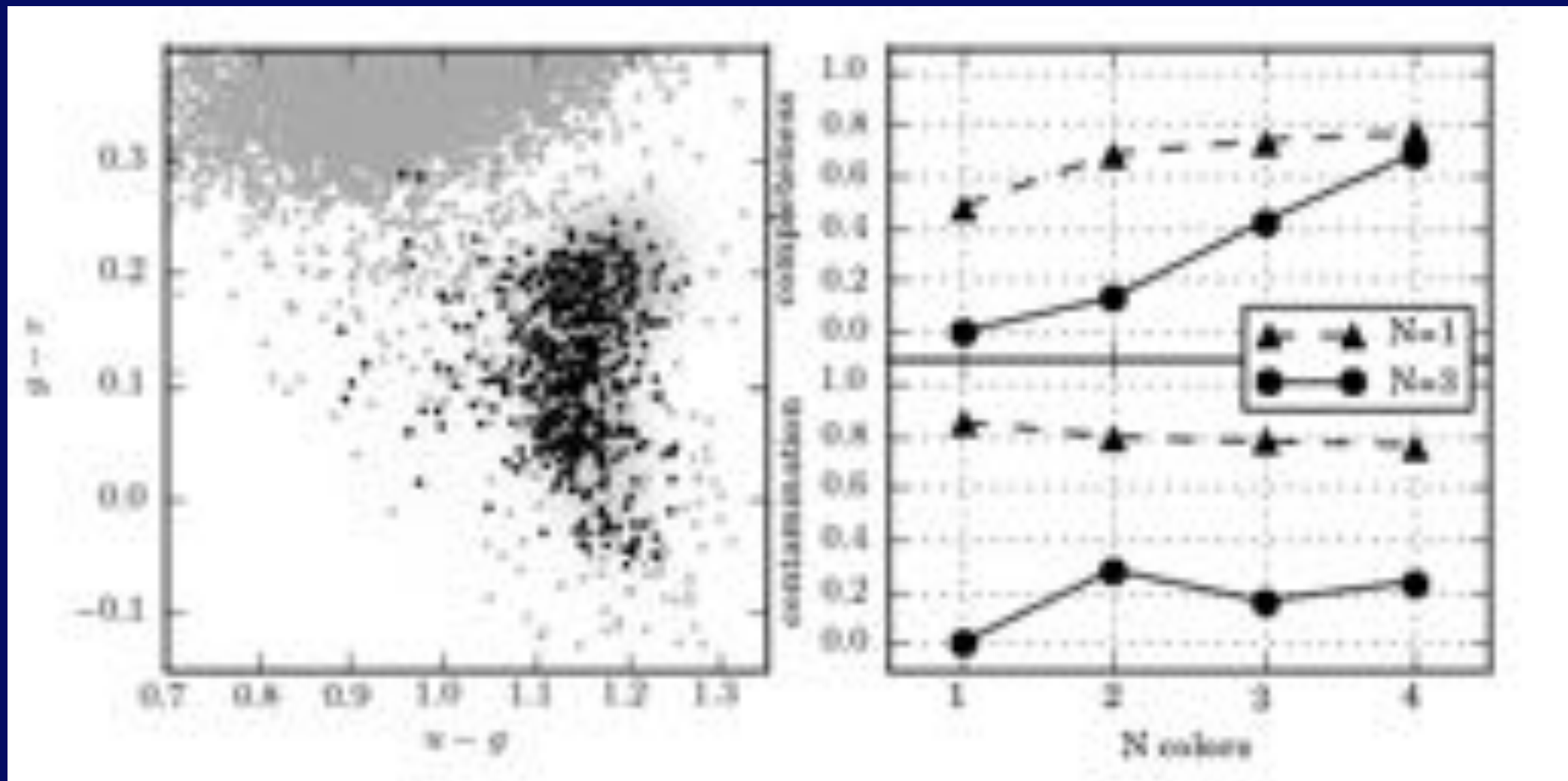
10 million alerts per night
0.1% interesting

		Predicted	
		+	-
Actual	+	5000	0
	-	200	1

Accuracy Paradox

**different metrics are useful for
different use cases!**

Unsupervised classification

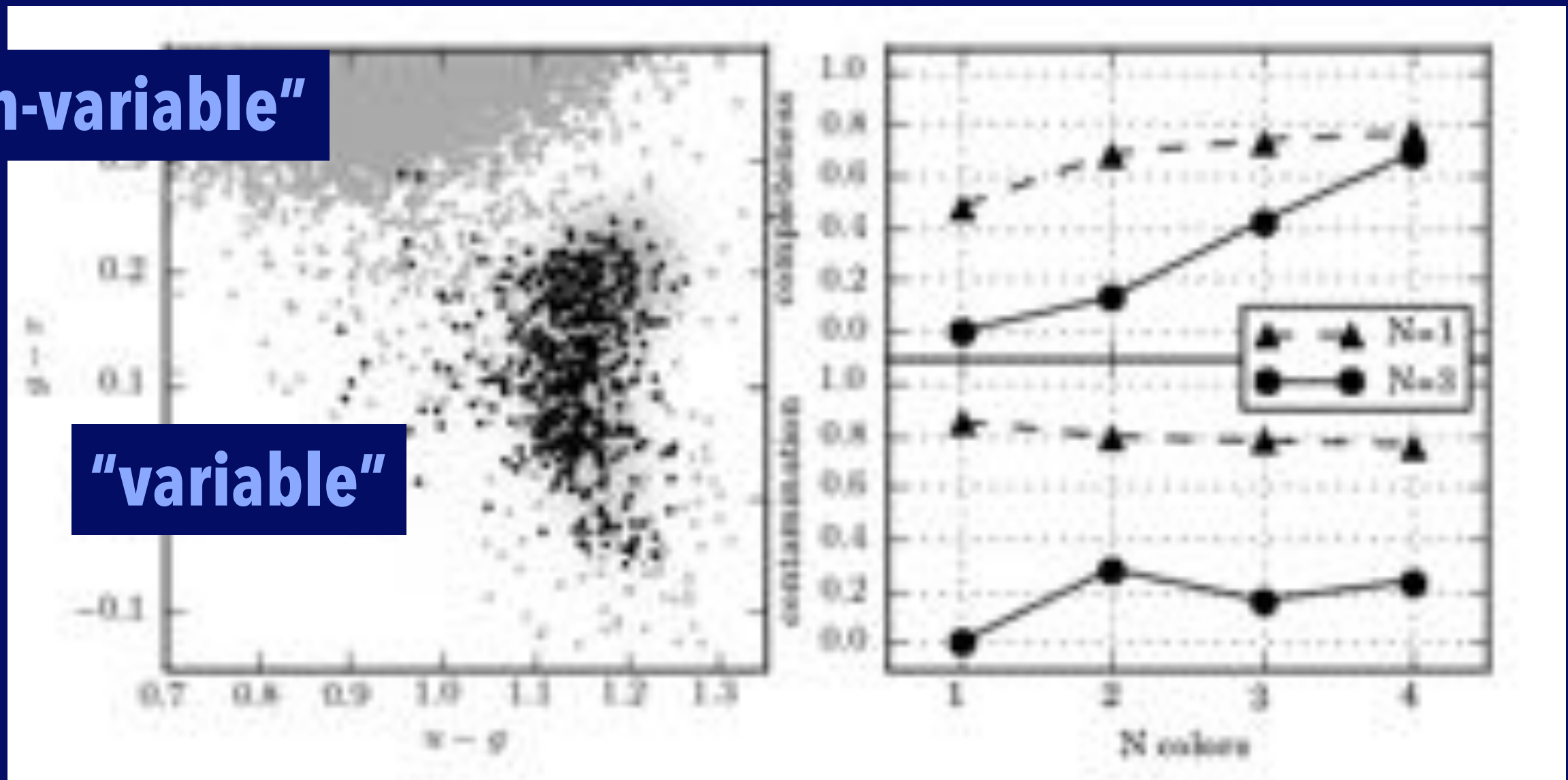


Unsupervised classification

Human:

"non-variable"

"variable"



Unsupervised classification

Human:

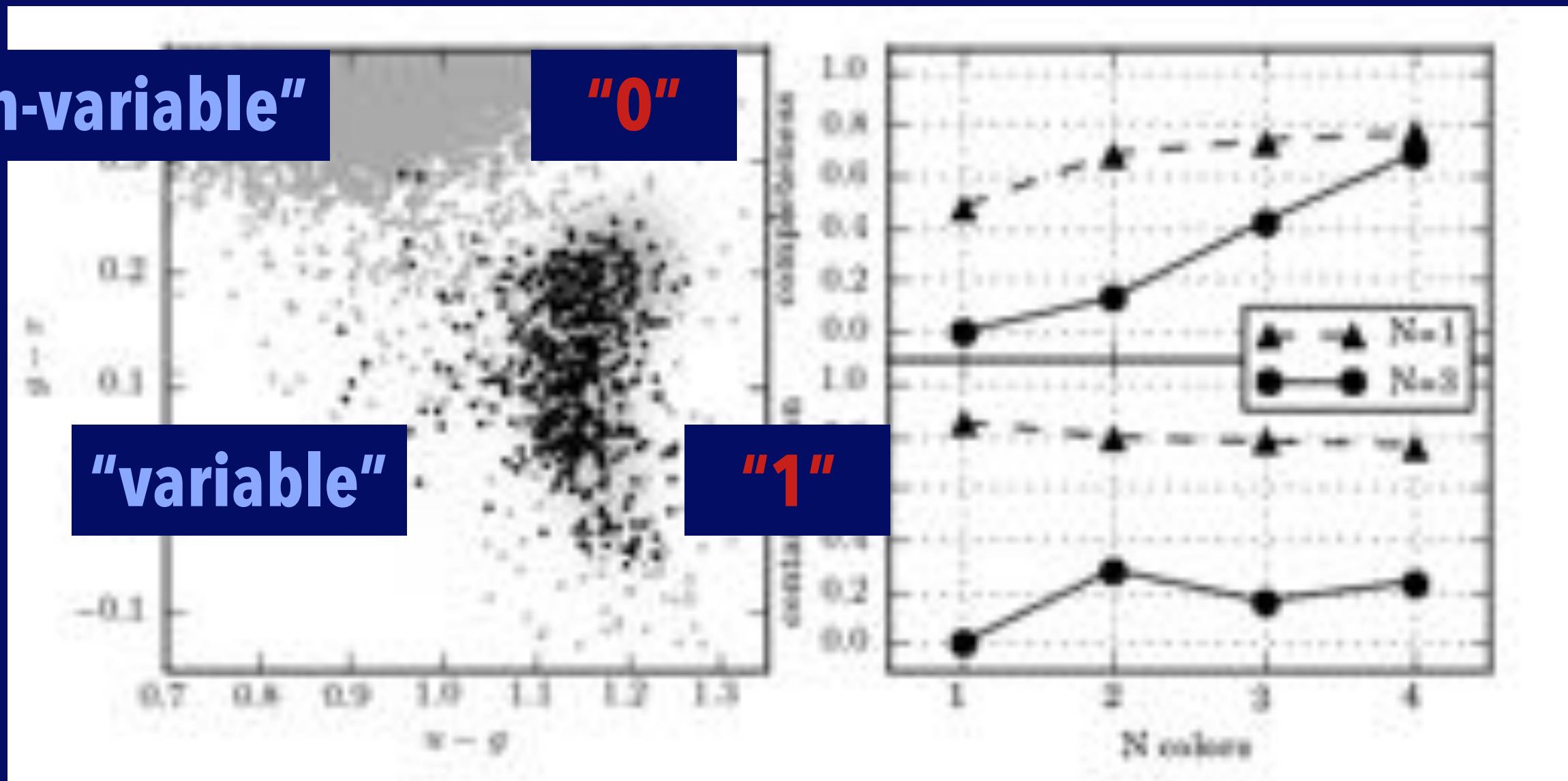
Computer:

"non-variable"

"0"

"variable"

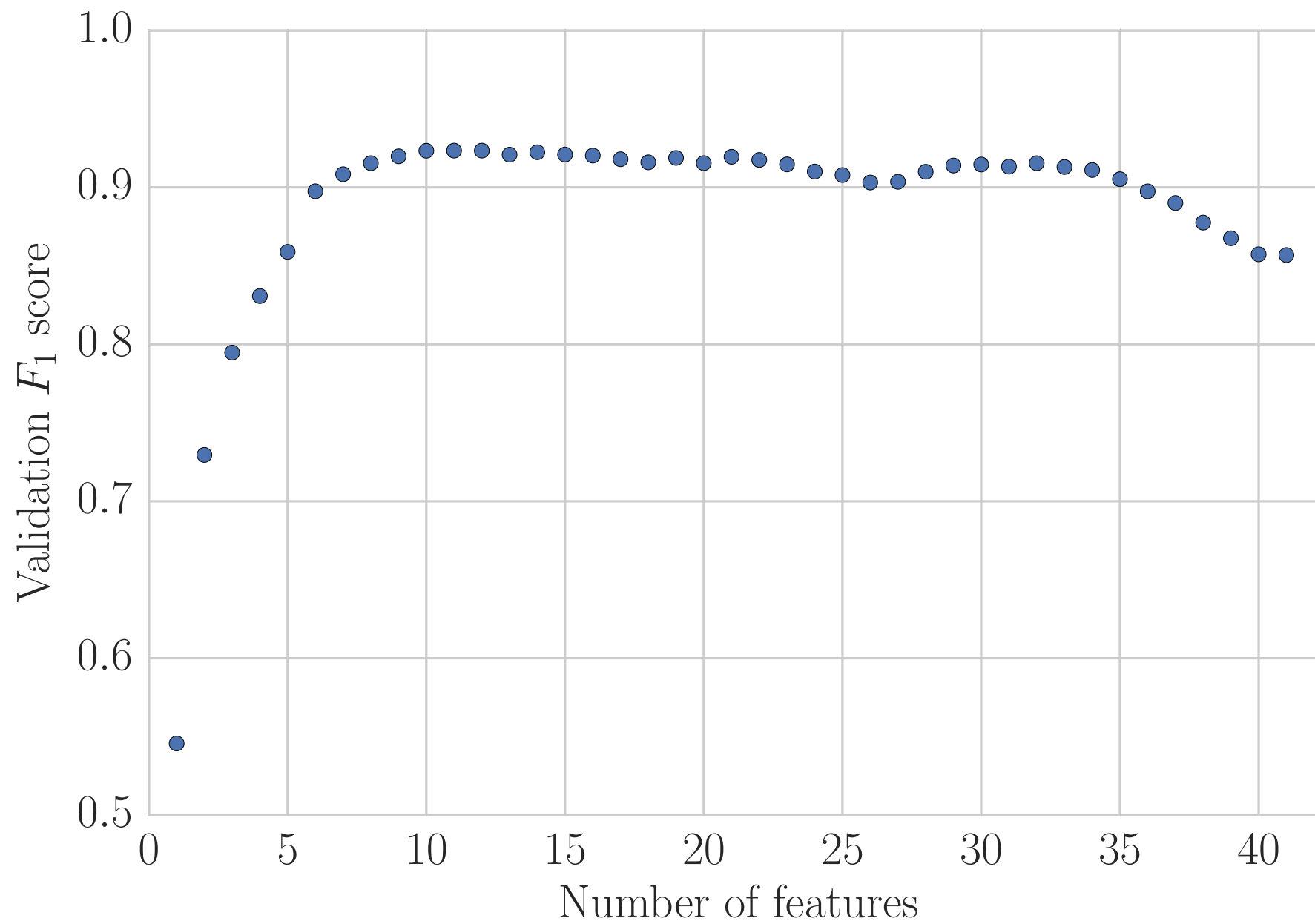
"1"



Unsupervised classification

- 1) **adjusted Rand index (ARI)**
- 2) **adjusted mutual information score**
- 3) **Silhouette coefficient**
- 4) **Information criteria**

Feature Selection



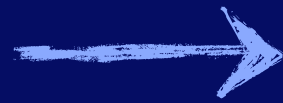
**Maybe only a subset of
available features is predictive!**

Exhaustive search:
 $>2^n$ model evaluations

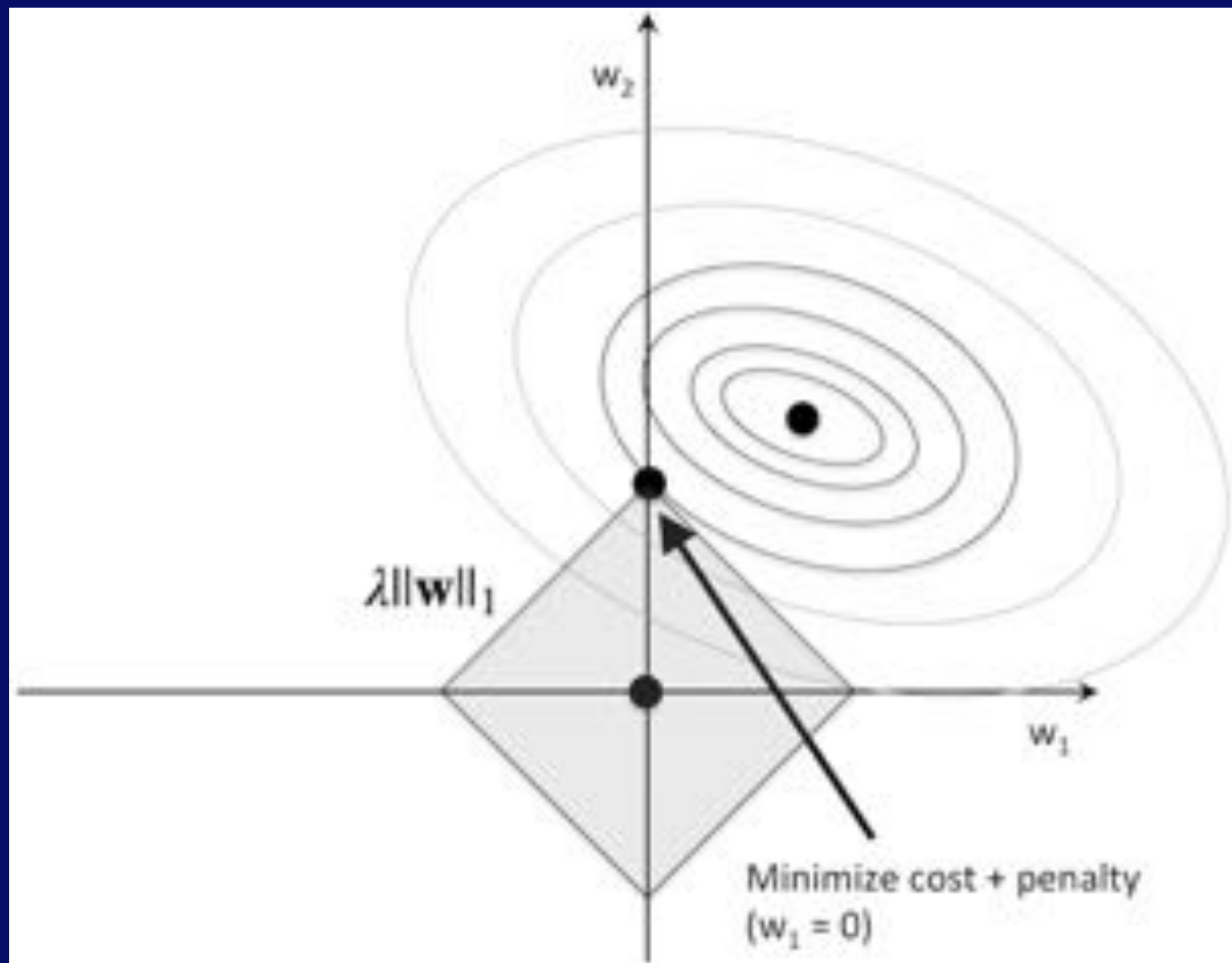
Linear models:

L1 regularization

$$L1 : \lambda \|\mathbf{w}\|_1 = \lambda \sum_{j=1}^m |w_j|$$



$$SSE = \sum_{i=1}^n (\text{target}^{(i)} - \text{output}^{(i)})^2 + L1$$

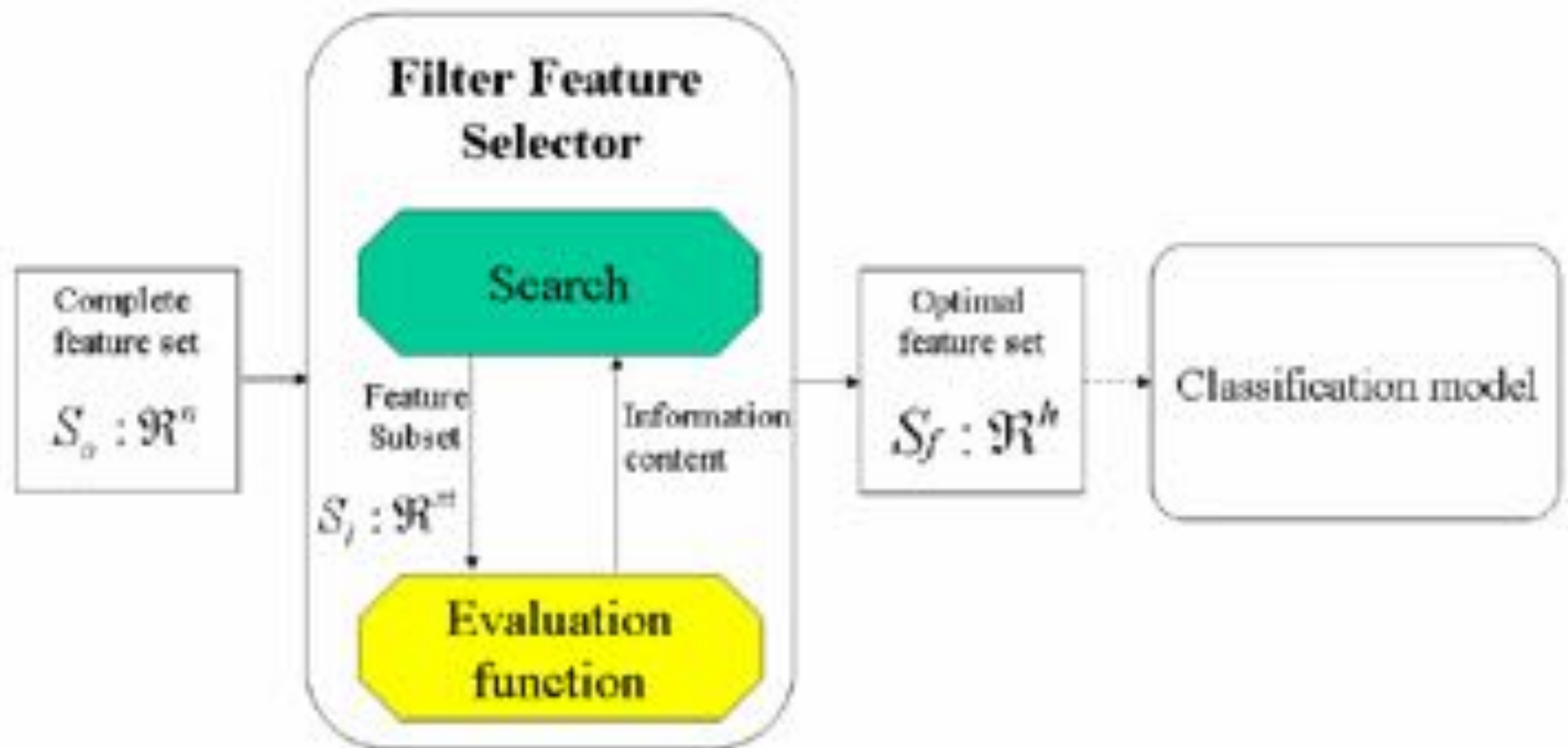


Forward or backward search:
 $>n^2$ model evaluations

search procedure is called **forward search**:

1. Initialize $\mathcal{F} = \emptyset$.
2. Repeat {
 - (a) For $i = 1, \dots, n$ if $i \notin \mathcal{F}$, let $\mathcal{F}_i = \mathcal{F} \cup \{i\}$, and use some version of cross validation to evaluate features \mathcal{F}_i . (I.e., train your learning algorithm using only the features in \mathcal{F}_i , and estimate its generalization error.)
 - (b) Set \mathcal{F} to be the best feature subset found on step (a).}
3. Select and output the best feature subset that was evaluated during the entire search procedure.

Filter feature selection:
>n model evaluations



**e.g. correlation between features and labels,
Kullback-Leibler divergence, ...**

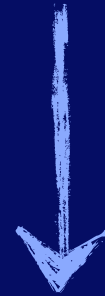
The Bayesian Perspective

**"I have a generative model and
a likelihood"**

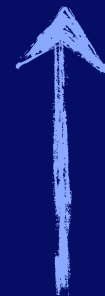
**+ usually easier to interpret
and reason about**

**– usually much more
computationally expensive**

approximation of the Bayes factor

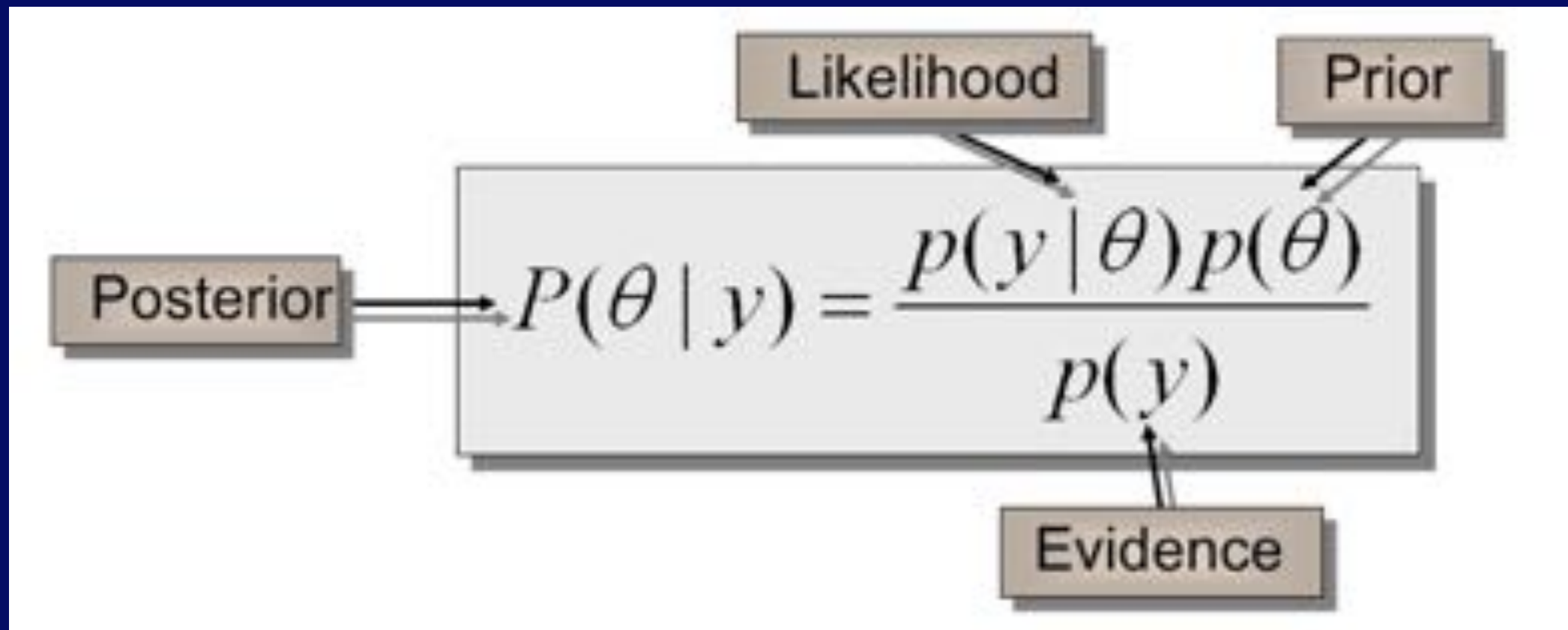


Information Criteria

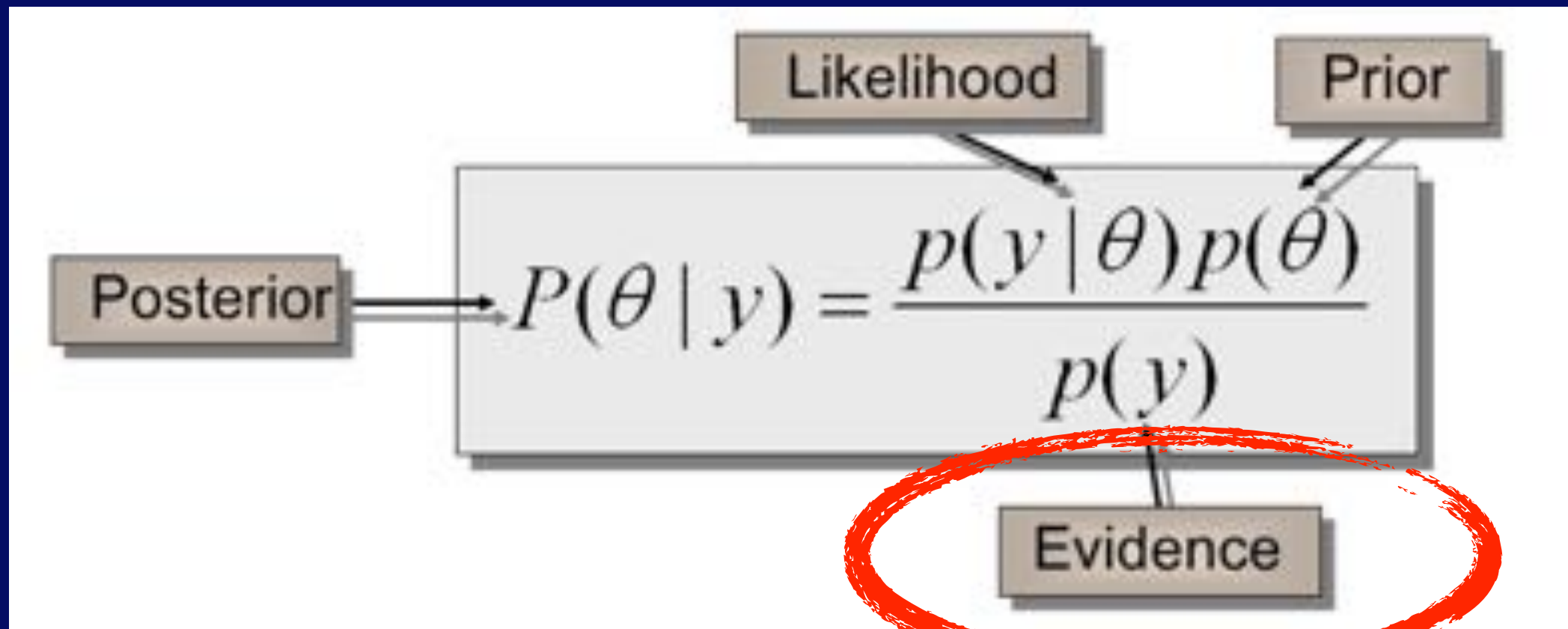


approximation of Bayesian cross validation

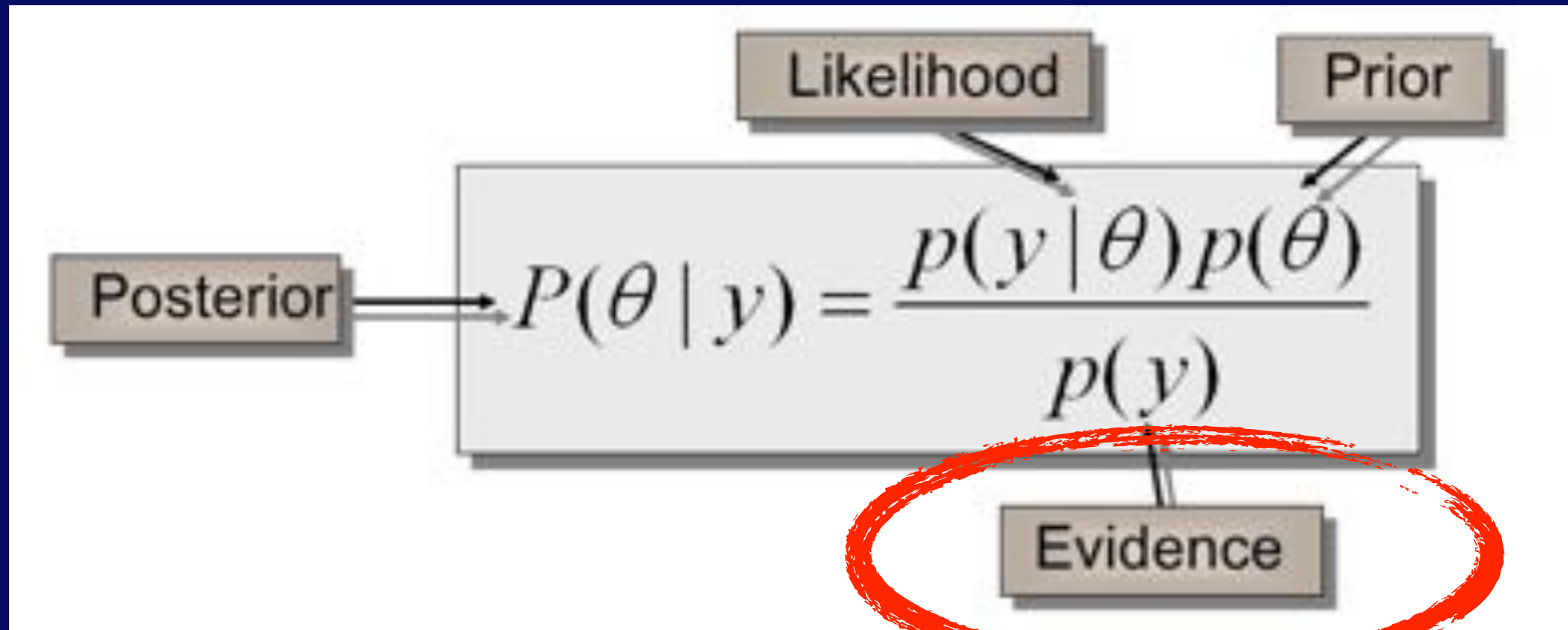
approximation of the Bayes factor



approximation of the Bayes factor



approximation of the Bayes factor



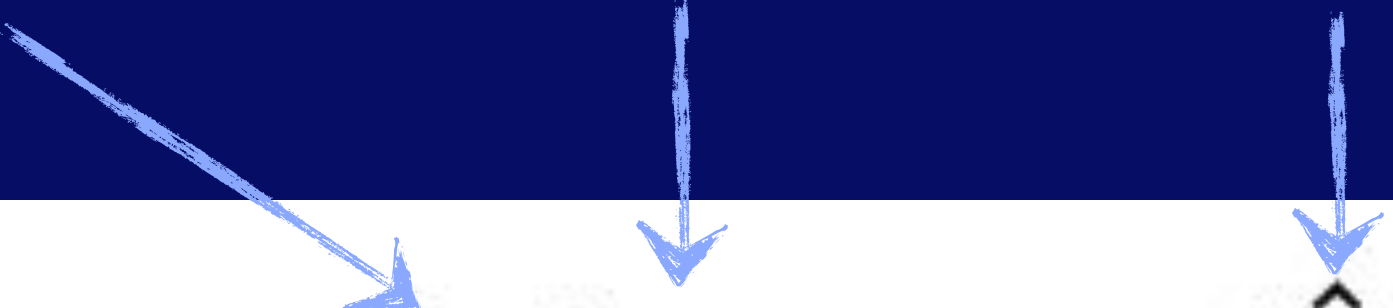
$$P(m|\mathbf{y}) = \frac{P(\mathbf{y}|m)P(m)}{P(\mathbf{y})}$$

Bayesian Information Criterion

data points

parameters

likelihood



$$\text{BIC} = \ln(n)k - 2 \ln(\hat{L}).$$

- rough approximation of the Bayes factor (for unit uniform prior)
- conservative estimate
- useful as a baseline

approximation of Bayesian CV

Akaike Information Criterion (AIC)*

Deviance Information Criterion (DIC)

Widely Applicable Information Criterion (WAIC)


are all approximation to leave-one-out cross-validation in Bayesian models (Gelman et al, 2013)

Akaike Information Criterion

$$\text{AIC} = 2k - 2 \ln(\hat{L})$$

**only works for linear models with flat priors or
models with a normally distributed posterior**

Deviance Information Criterion

$$\text{AIC} = 2k - 2 \ln(\hat{L})$$


**replace with data-
based bias correction**

**replace with
posterior mean**

$$\text{computed } p_{\text{DIC}} = 2 \left(\log p(y|\hat{\theta}_{\text{Bayes}}) - \frac{1}{S} \sum_{s=1}^S \log p(y|\theta^s) \right).$$

Resources:

- http://www.stat.columbia.edu/~gelman/research/published/waic_understand3.pdf
- <https://github.com/marcotcr/lime>
- <https://arxiv.org/abs/1606.03490>
- <https://www.stat.washington.edu/raftery/Research/PDF/kass1995.pdf>
- Gelman et al, Bayesian Data Analysis, 2004
- Bishop, Pattern Recognition + Machine Learning
- <http://users.isr.ist.utl.pt/~wurmd/Livros/school/Bishop%20-%20Pattern%20Recognition%20And%20Machine%20Learning%20-%20Springer%20%202006.pdf>
- <https://www.stat.washington.edu/research/reports/1999/tr347.pdf>