## Design Theory of Relational DBr.

- · What makes a good database?
  - · Normalization
  - · Avoid "anomalies"

Functional Dependencies (FD)

· A FD is a constraint between two set of attributer of a relation.

· Given R, a set of attributes X in R is said to functionally determine another set of attributes Y in R (X > Y) iff 2 tiples have the same values of attributes X then they must have the same values for attributes Y.

We write them as:

A... An > B... Bm

Attributes written as list.

Example: title Le ar 977 124 Star Wars Sci Fi Carry Fisher Fox Star Wars 977 SG Fi 124 Fox Mark Hamill 977 Star Wars Sci Fi Fox 124 Harrison Ford 972 The God father 175 Drama Paramount Robert Duvall 972 The God father 175 Drama Marlon Brandon Paramount 1953 Apocalyte Now 153 Zoetrope Marlon Brandon War I claim by design that title, year -> lenght, genre, studio Name title, year /> star Name Superkey (SK) A set of attributes of A...Angis a superkey of Riff A...Angis a Candidate ken ( key) A candidate key is a superker that is minimal: there is no proper subset of C of AA...And s.t C > R One candidate Key becomes the Primary Key!

For ar example:

- · All attributes of R are always a SK.
- · title, year, starhame is a candidate title, year, star Name -> R
- · Any superset of a candidate key is

Leasoning about FD's.

. aiven a relation R two sets of FDs

A & B are equivalent it.

The set of instances of 12 that satisfy A is exactly the same that

· A follows from B if every instance of 12 that satisfies Balso satisfies A.

- A & B are equivalent ild.

A follows B and B follows A

Armstrong's Axioms (3.2 page 81)

Given relation 12 with subsets of attributer X, Y, Z C R

Reflexivity (Trivial)
YCX then X >> Y

Agmentation:

Algmentation: If X > Y then XZ > YZ for any Z Transituity:

If X > Y, Y > Z then X > Y

Additional Rules. They can be derived from axioms.

Union:

If X > Y, X > Z then X > YZ Decomposition

If X => YZ then X => Y and X => Z

Ex:

Y Z -> 2

 $\times \rightarrow Y$ 

 $\times \rightarrow 2$ 

Derive Union from axioms

X = Y, X = 12

XZ = YZ Augmentation

XX = XZ Augmentation

X = XZ = YZ Transituity

X = YZ M

Derive decomposition

X = YZ

YZ = YZ

YZ = YZ

Deliverthe

(3.2.4)Closure of attributes Given a relation R and a set of of FDs, what other FDs can be computed from a set of attributer of R? The closure of a set of attributes

A...An denoted fa...An It is the set of attr. that can be derived from A...An rsing +. Hard to do and error prone via axioms! 1) Rewrite FDs in f in canonical form 2) X 
A1.. An 3) for each B<sub>1</sub>... B<sub>m</sub>... C in FDs If B. . Bm EX and C X add C to X 1) Repeat (3) until X does not change X is h A, ... Any+

Ex; R(ABC DE) AB-C BC -> A F= AB > C BC > AD D > E CF > B BC > D D->E CF-B Compute 4B3+ X & AB First pass:  $x \in ABC$  fd1  $X \in ABCDE$  fd3 fd4all attributes hence X will change any more (AB)+ = 4 ABCDEY AB is a SK of R. Is it a candidate key? Closure of attr. can help us find CKs of a relation: Compute hart land 413-4+

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Closure of set of FDs.

Given a set of FDs, its closure

473+ is the set of all FDs derived from f. I=/A>B A > C E f+ \ \ B→C Two sets A&B of

iff (A) + = (B) + FDs are equivalent  $\begin{cases} A \rightarrow B \\ B \rightarrow C \end{cases} = \begin{cases} A \rightarrow B \\ A \rightarrow C \end{cases}$ 

We can easily test if X > Y e ft

X > Y e ft iff Y c f x y t using f.

 $A \rightarrow C = A \rightarrow B$   $A \rightarrow C = A \rightarrow B$   $A \rightarrow C = A \rightarrow B$   $A \rightarrow A \rightarrow B$   $A \rightarrow A \rightarrow A \rightarrow B C$ 

A -> C 2 8

Basis of a relation

Given a relation E and FDs f we say that any set g s.t. ft = gt is a basis of R.

Minimal Basis of FDs. (3.2.7)

Any relation R has many equivalent set of FDs. (many basis-es).

To avoid an explosion of FDs we usually use a minimal basis

A minimal basis B of a relation R is a basis of R s.t.

- 1) All FD's in B are in canonical form
- 2) If any FD is removed from B, the result is no longer a basis
- 3) If for any FD we remove one or more attr. from the left hand side the result is no longer a basis,

Ex: Is A a minimal basis of B 0  $A \Rightarrow B$   $B \Rightarrow C$   $C \Rightarrow B$ CAA 6 C >B AB -> C AC >B BC-A GNEN FDs in A, can we generate FDs in B? (1), (3), (6) already in A. 4A7+= {ABC}. > 2 can be generated, and also 3, 8 by using augmentation. (or compute 1AByt, 4ACyt) (5?(13+=4CBA) > yes (3) and 9 (augmentation) can be generated. So from A we can generate B. Hence A is a basis of B

Bis also a basis of A (ACB)

Is A minimal?

Can we drop A > B?

A > B be generated from C > B B > C) A) + = AA) so no A > B cannot be removed.

· Com we drop B > A?

B > A be generated from C > B

B > C

B > C

B > C

1B7+=1BCZ, so no, it can not be removed.

· Repeat for C > B and B > C.
Yes, it is minimal.

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Projection of FDs (3.2.8) aven R and set F of FDS the projection of Fon R1=TLK is the set of FDs that follows from F this involve only attributes in R. Algorithm:  $T \leftarrow \emptyset$ for each subset X EL compute \X\for every attribute A in 1 X3+ add X > A to T iff A E L and A & X (non-trivial)

 $F = \begin{pmatrix} A \rightarrow B \\ B \rightarrow C \\ C \rightarrow D \end{pmatrix}$ Ex: R(ABCD) Compute FDs of MACD R closure 3) Remove RHS att not in L. 4) Remove trivial For Pesult: / AC → D AD → C  $A \rightarrow C$   $A \rightarrow D$   $C \rightarrow D$ Is it a minimal basis? No ABOOC can be ABOOC ABOOC ABOOC Prove st!!

## Design of Relational DBs (3.3)title 977 Star Wars 124 Sci Fi Fox Carry Fisher Star Wars 977 124 Sci Fi Fox Mark Homill Star Wars 977 124 Sci Fi Fox Harrison Ford 972 The God father 175 Robert Duvall Orama Paramount

Drama

War

Paramount

Zoetrope

Marlon Brandon

Marlon Brandon

FDs: title, year -> length, studio Name

175

153

972

1953

## Anomalies

The God father

Apocalyte Now

- · Redundancy: Unnecessary repeated
- · Update anomalies: If we change one typle we might have to change another: Ex: change length of a movie.
  - · Deletion anomalies: If we delete a typle we might lose other info: Ex: Remove M. Brandon from Ap. Now.

Decomposing Relations To deal with anomalies we decompose relations.

Given  $R(A_1...A_n)$  a decomposition into  $S(B_1...B_m)$  and  $T(C_1...C_k)$  s.t.

1) {A, ... An } = 1B, ... Bm } U 1 C1 ... Cx }
and

2)  $S = \prod_{B_1 \dots B_m} R$  and  $T = \prod_{C_1 \dots C_K} R$ 

We can decompose Moures into S(title, year, length, genre, statio Name)

T (title, year, star Name)

Call this Movies 2

Standana title Le ar Star Wars Carry Fisher 1977 1977 Mark Hamill Star Wars 1977 Harrison Ford Star Wars The God father 1972 Robert Duvall The God father Marlon Brandon 1972 1953 Marlon Brandon Apocalyte Now

Call this Movies 3

Good de compositions.

Given a relation R we want to decompose it into two relations S and T s.t.

- 1) R = SMT lossless join
- 2) The projection of FDs Fr of R into S (F's) and T (FT)

Dependency preserving.

Boyce Codd Normal Form (BCNF)

A relation R is in BCNF iff for every non-trivial FD A...An > B...Bm A...An is a Superkey.

Ex:

Movies is not BCNF

title, year -> lenght, studio Name
is a not a SK of Movies

If a relation R; s not BCNF then decompose into relations  $R_1...R_n$  s.t  $R_1 \bowtie R_2...\bowtie R_n = R$   $\Rightarrow Loss-less$  join decomposition.

Algorithm to de compose into BCNF relations

Given R and set F of FDs:

R is not BCNF.

1) Choose one FD X → Y not in BCNF 2). De compose:

$$P_{i} = \sqrt{\times j^{+}} \times \rightarrow Y$$

$$P_{2} = \times \cup (P - P_{i})$$

- 3) Compute FDs for R, and Bz (projection of FDs of R into P1, P2)
- 4) If R1 or R2 are not BCNF recursively decompose.

Graranteed to be lossless join but not FD preserving.

Any non BCNF relation has a BCNF loss-less join decomposition but not a BCNF FD preserving de composition. Ex: e(TCH)  $H \rightarrow C$ TC -9H. not BCNF. H-> C HU TCH-C3 4 H3+= HC ← any 2 attrel 1. HT FDs is BCNF FDs HC HC HT HTC -H-H& H HC

## 3rd Normal Form (3NF)

If we cannot decompose a relation into BCNF relations that are FD preserving we are happy if they can be decompose into 3NF relations.

Any relation R with a set of FDs F has a 3NF decomposition that is loss-less join and FD preserving.

A relation R with FDs Fisin 3NF

if for every non-trivial FD

A1...An → B1...Bm

- · it is a:SK
- · CE {B, ... Bm} is either

C E hA1.. And or

C is part of some candidate key.

Ex: B(ABCDE) Isit 3NF? AB -> C AB rota Sk. is C partofa Ck? Need to compute candidate keys of R · Heuristic: AE never on righthand side of > always part of a key Use closure of attr. to compute SKs. all combination of atter. closure. AE BCD AEBCD BC BP AE BC D all SK. AE BD C AEBCD AECDB AECBD AFD AED . > Candidate Keyr. JAEC Back to testing if Ris 3NF.

AB > C c is part of Ck. V

C > B C is not SK. but

B is part of CK.

A > D A is not SK.

D is not part of CK

> 2 is not 3NF.

Decomposition of a Relation into 3NF relations that is loss-less join and FD preserving: (Synthesis alg 3.5.2)

Given R with set of FDs F

1) Fmd G, a minimal bass of F

2) For each FD A...An → B in G.

add a relation with schema

 $A_1...A_n$  B with FD  $A_1...A_n \rightarrow B$ 

3) If none of the addied relations in step 2 is a SK of R add another relation whose schema is a Key of R.