

Date:

Name 1:

Name 2:

Compute the minimum closure of this set of FDs:

$$F = \{ A \rightarrow BC, B \rightarrow CE, A \rightarrow E, AC \rightarrow H, D \rightarrow B \}$$

1) $A \rightarrow B \quad B \rightarrow C \quad A \rightarrow E \quad AC \rightarrow H \quad D \rightarrow B$
 $A \rightarrow C \quad B \rightarrow E$ (In canonical form)

2) See if any attribute in the left hand side is redundant. We only have to check

$$AC \rightarrow H \quad A^+ = \{ABC H\}$$

$\Rightarrow C$ is redundant

$$\Rightarrow A \rightarrow H$$

We now have.

$$\begin{array}{ccccc} A \rightarrow B & B \rightarrow C & A \rightarrow E & A \rightarrow H & D \rightarrow B \\ A \rightarrow C & B \rightarrow E & & & \end{array} \left. \vphantom{\begin{array}{ccccc} A \rightarrow B & B \rightarrow C & A \rightarrow E & A \rightarrow H & D \rightarrow B \\ A \rightarrow C & B \rightarrow E & & & \end{array}} \right\} \text{New FDs}$$

3) Remove any redundant FDs.

Test to see if an FD can be generate from the others

$$\text{Test } A \rightarrow B \quad A^+ = \{ACH\} \quad \text{Needed!}$$

$$\text{Test } A \rightarrow C \quad A^+ = \{ABCEH\} \quad \text{Redundant!}$$

$$\Rightarrow \begin{array}{ccccc} A \rightarrow B & B \rightarrow C & A \rightarrow E & A \rightarrow H & D \rightarrow B \\ & B \rightarrow E & & & \end{array} \left. \vphantom{\begin{array}{ccccc} A \rightarrow B & B \rightarrow C & A \rightarrow E & A \rightarrow H & D \rightarrow B \\ & B \rightarrow E & & & \end{array}} \right\} \text{New FDs}$$

Test $B \rightarrow C$

$B^+ = \{B, E\} \Rightarrow$ Needed

Test $B \rightarrow E$

$B^+ = \{B, C\} \Rightarrow$ Needed

Test $A \rightarrow E$

$A^+ = \{A, B, C, E, H\}$ Redundant

$\Rightarrow A \rightarrow B \quad B \rightarrow C$
 $B \rightarrow E$

$A \rightarrow H \quad D \rightarrow B$ } New FDs

Test $A \rightarrow H$

$A^+ = \{A, B, C, E\}$ Needed

Test $D \rightarrow B$

$D^+ = \{D\}$ Needed

\Rightarrow Minimal Cover:

$A \rightarrow B$

$A \rightarrow H$

$B \rightarrow C$

$D \rightarrow B$

$B \rightarrow E$

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