

Model Tuning: Regularization

Motivation: Overfitting often caused by overly-complex models capturing idiosyncrasies in training set.

Regularization: Adding penalty score for complexity to cost function

$$\text{cost}_{\text{reg}} = \text{cost} + \frac{\alpha}{2} \text{penalty}$$

Automated way to find the right balance between the important features and the overfitting of the model.

Example: Regularization - cost is the sum of the squared errors

Complicated model: 100s of thousands of features
- penalty could be the sum of the weight of each feature

α - regularization strength: larger α means larger penalty

Weight - denotes relative importance of the variable

Idea: large weights correspond to higher complexity
Regularize by penalizing large weights

Two standard types:

L1 regularization, Lasso: $\text{penalty} = \|\vec{w}\|_1 = \sum_{j=1}^m |w_j|$

L2 regularization, Ridge:
 $\text{penalty} = \|\vec{w}\|_2^2 = \sum_{j=1}^m w_j^2$

Now we minimize total cost

L2 popular, but L1 useful as feature selection approach since most weights shrink to 0 (sparsity)
Note: important to scale features first!

scikit-learn: Models that support regularization typically provide parameters for type and strength.

Sklearn

L2 Ridge regression `sklearn.linear_model.Ridge`

L1 Lasso regression `sklearn.linear_model.Lasso`

Both: `sklearn.linear_model.ElasticNet`

The strength of regularization $C = \frac{1}{\alpha}$
inverse of the reg strength

Logistic regression, add in a penalty of L2 with $C = 1$