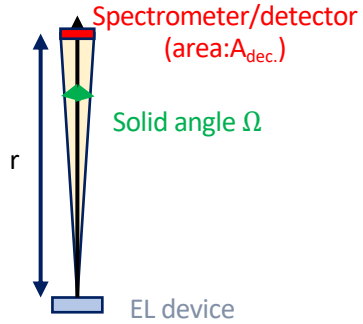


Method (1)



- (a) the total outcoupling efficiency from device to far field, η_{total}
- (b) normalized far field's pattern, $\bar{I}_{FF}(\theta, \phi) [\frac{1}{sr}]$ (without λ dependent)
- (c) normalized spectrum at normal direction, $\bar{\bar{S}}p_{FF}(\lambda, \theta = 0^\circ) [\frac{1}{nm}]$

- The relation between the injection current ($I_{inj.}$) and far field photon number (N_{FF})

$$\frac{N_{FF}}{\Delta t} = IQE \times (I_{inj.} \times 6.241 \times 10^{18}) \times \eta_{total} \left[\frac{1}{s} \right]$$

- N_{FF} should also equal to the integration of far field intensity with absolute value.
 - Assume the spectra are same over all the angles. As a result, the angular dependent far field spectrum with absolute value should equal to (α strength)

$$\alpha \bar{\bar{S}}p_{FF}(\lambda, \theta = 0^\circ) \bar{I}_{FF}(\theta, \phi) \left[\frac{W}{nm \cdot sr} \right]$$

Then,

$$\left(\frac{hc}{\lambda} \right)_{avg.} \frac{N_{FF}}{\Delta t} [W] = \int \int \alpha \bar{\bar{S}}p_{FF}(\lambda, \theta = 0^\circ) \bar{I}_{FF}(\theta, \phi) d\lambda d\Omega$$

Method (2)

$$\frac{N_{FF}}{\Delta t} = \frac{1}{\left(\frac{hc}{\lambda}\right)_{peak}} \int \int \alpha \overline{\overline{S p}}_{FF}(\lambda, 0^\circ) \overline{\overline{I}}_{FF}(\theta, \phi) d\lambda d\Omega = IQE \times (I_{inj.} \times 6.241 \times 10^{18}) \times \eta_{total}$$

Then,

$$\alpha = \left(\frac{hc}{\lambda}\right)_{avg.} \frac{IQE \times (I_{inj.} \times 6.241 \times 10^{18}) \times \eta_{total}}{\int \overline{\overline{S p}}_{FF}(\lambda, 0^\circ) d\lambda \int \overline{\overline{I}}_{FF}(\theta, \phi) d\Omega}$$

As a result, the spectrum at normal direction with absolute value is

$$\alpha \overline{\overline{S p}}_{FF}(\lambda, 0^\circ) \overline{\overline{I}}_{FF}(0^\circ) \left[\frac{W}{nm \cdot sr} \right]$$

Then current efficiency would become

$$\begin{aligned} \eta_{cd}(0^\circ) &= \frac{K \int_{\lambda} \alpha \overline{\overline{S p}}_{FF}(\lambda, 0^\circ) \overline{\overline{I}}_{FF}(0^\circ) V(\lambda) d\lambda}{I_{inj.}} \left[\frac{lm}{sr \cdot A} = \frac{cd}{A} \right] \\ &= \frac{K}{I_{inj.}} \left(\frac{hc}{\lambda} \right)_{avg.} \frac{IQE \times (I_{inj.} \times 6.241 \times 10^{18}) \times \eta_{total}}{\int \overline{\overline{S p}}_{FF}(\lambda, 0^\circ) d\lambda \int \overline{\overline{I}}_{FF}(\theta, \phi) d\Omega} \overline{\overline{I}}_{FF}(0^\circ) \int_{\lambda} \overline{\overline{S p}}_{FF}(\lambda, 0^\circ) V(\lambda) d\lambda \end{aligned}$$

α

Method (3)

$$\eta_{cd}(0^\circ) = K \left(\frac{hc}{\lambda} \right)_{avg.} \frac{IQE \times \eta_{total} \times 6.241 \times 10^{18}}{\int \overline{\overline{Sp}}_{FF}(\lambda, 0^\circ) d\lambda \int \bar{I}_{FF}(\theta, \phi) d\Omega} \bar{I}_{FF}(0^\circ) \int_{\lambda} \overline{\overline{Sp}}_{FF}(\lambda, 0^\circ) V(\lambda) d\lambda$$

Rearrange

$$\eta_{cd}(0^\circ) = \underbrace{IQE \times \eta_{total}}_{EQE} \times 6.241 \times 10^{18} \left(\frac{hc}{\lambda} \right)_{avg.} \frac{\bar{I}_{FF}(0^\circ)}{\int \bar{I}_{FF}(\theta, \phi) d\Omega} \frac{K \int_{\lambda} \overline{\overline{Sp}}_{FF}(\lambda, 0^\circ) V(\lambda) d\lambda}{\int \overline{\overline{Sp}}_{FF}(\lambda, 0^\circ) d\lambda}$$

,where

$$\left(\frac{hc}{\lambda} \right)_{avg.} = \frac{\int_{\lambda} \left(\frac{hc}{\lambda} \right) \overline{\overline{Sp}}_{FF}(\lambda, 0^\circ) d\lambda}{\int_{\lambda} \overline{\overline{Sp}}_{FF}(\lambda, 0^\circ) d\lambda}$$
$$\int \bar{I}_{FF}(\theta, \phi) d\Omega = \int \int \bar{I}_{FF}(\theta, \phi) \sin \theta d\theta d\phi \approx 2\pi \int \bar{I}_{FF}(\theta, \phi) \sin \theta d\theta$$
