Assignment 8:

- A crime is committed by one of two suspects, A and B. Initially, there is equal evidence
 against both of them. In further investigation at the crime scene, it is found that the guilty
 party had a blood type found in 10% of the population. Suspect A does match this blood
 type, whereas the blood type of Suspect B is unknown.
- (a) Given this new information, what is the probability that A is the guilty party?
- (a) Let M be the event that A's blood type matches the guilty party's and for brevity, write A for "A is guilty" and B for "B is guilty". By Bayes' Rule,

$$P(A|M) = \frac{P(M|A)P(A)}{P(M|A)P(A) + P(M|B)P(B)} = \frac{1/2}{1/2 + (1/10)(1/2)} = \frac{10}{11}.$$

(We have P(M|B) = 1/10 since, given that B is guilty, the probability that A's blood type matches the guilty party's is the same probability as for the general population.)

- (b) Given this new information, what is the probability that B's blood type matches that found at the crime scene?
- (b) Let C be the event that B's blood type matches, and condition on whether B is guilty. This gives

$$P(C|M) = P(C|M,A)P(A|M) + P(C|M,B)P(B|M) = \frac{1}{10} \cdot \frac{10}{11} + \frac{1}{11} = \frac{2}{11}.$$