Programming Math in Java

Lessons from Apache Commons Math

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Agenda

- Commons Math Overview
- Examples and problems
- Lessons learned
- Getting involved

Disclaimer

Apache Commons Math is a community-based, open development project.

The discussion of problems, challenges and lessons learned represents one contributor's views.

Goals

- Self-contained, ASL-licensed Java
- Provide simple solutions to common problems
- Implement standard, well-documented algorithms
- Balance ease of use and good design
- Stay well-tested and maintained
- Maintain a strong community

Some Statistics (as of March 11, 2015)...

- 67 packages
  - 908 classes
  - 84,057 lines of code
- 54,629 lines of comments
  - 99.7% documented API
- 5862 unit tests
  - 92% of code covered
- 80 open issues
  - Average 216 issues resolved per year
- 6 active committers
- 70+ contributors
- 0 dependencies

Quick Tour

Building Blocks - util, special, complex packages

- FastMath (pure java replacement for java.lang.Math)
- Dfp (arbitrary precision arithmetic)
- Continued fractions
- Special functions (Beta, Gamma, Bessel, Erf)
- Array utilities (norms, normalization, filling, etc)
- Basic combinatorics ($\binom{n}{k}$, $n!$, Stirling numbers...)
- Basic integer arithmetic (checked ops, gcd, lcm, primality...)
- Complex numbers

Linear Algebra - linear package

- Vector and Matrix operations (dense, sparse, field)
- Decompositions (LU, QR, Cholesky, SVD, Eigenvalue)
- Solvers

Basic Numerical Analysis - analysis package

- Automatic Differentiation
- Numerical Integration
- Interpolation
- Root finders

Probability and Statistics - distributions, stat and random packages

- Probability distributions (Gaussian, Exponential, Poisson...)
- Random number generators (Well, ISAAC, Mersenne twister...)
- Random data generators (samplers, random vectors...)
- Univariate statistics (storeless and in-memory)
- Regression (matrix-based and storeless)
- Correlation
- Inference (T-, G-, ChiSquare, Kolmogorov-Smirnov tests...)

Optimization and Geometry - optim, fitting, ode, transform, geometry packages

- Fitting (non-linear least-squares, curve fitting)
- Ordinary differential equations (ODE)
- Linear/Non-linear optimization
- Computational Geometry
- Fast Fourier transform

AI / Machine learning - genetics, filter and ml packages

- Genetic algorithms
- Neural networks
- Clustering
- Kalman filter

Examples and Challenges

Example 1 - Root finding

Find all roots of the polynomial

$$p(x) = x^5 + 4x^3 + x^2 + 4 = (x + 1)(x^2 - x + 1)(x^2 + 4)$$

Example - Root finding (cont)

How about this one?

$$p(x) = \prod_{i=1}^{50} 15,000(i + ix + ix^2 + ix^3)$$

As of 3.4.1, this will appear to hang.
Two problems:

1. Complex iterates "escape to NaN"
2. Default max function evaluations is set to Integer.MAX_VALUE

Example 1 - Root finding (cont)

First problem: escape to NaN

- Long and painful history debating C99x Annex G
- Desire: clear, self-contained, open documentation
- Desire: simple, performant code
- Result: use standard definitions and let NaNs propagate

Second problem: hanging

- Ongoing debate about what to make defaults, whether to have defaults at all...
- Ease of use vs foot-shooting potential
- OO vs procedural / struct / primitives design

Example 2 - Kolmogorov-Smirnov Test

Problem: Given two samples S_1 and S_2, are they drawn from the same underlying probability distribution?

K-S Test Implementation Challenges

Test statistic $= D_{m,n} =$ maximum difference between the empirical distribution functions of the two samples.

- The distribution of $D_{m,n}$ is asymptotically an easy-to-compute distribution
- For very small m, n, the distribution can be computed exactly, but expensively
- What to do for mid-size samples $(100 < m \times n < 10,000)$?
- Should this distribution be in the distributions package?
- Reference data / correctness very hard to verify

Example 3 - Multivariate optimization

Find the minimum value of $100(y - x^2)^2 + (1 - x)^2$, starting at the point $(-1, 1)$

Works OK in this case, but...

Example 3 - Optimization (cont)

User question: How do I choose among the available optimizers?
Developer question: How do we define a consistent API?

Another solution for Example 3:
Note additional parameter to optimize.

Example 3 - Optimization (cont)

To allow arbitrary parameter lists, we settled on varargs ...

Optimization (cont) - version 4 direction

Refactor all classes in "o.a.c.m.optim"

- Phase out "OptimizationData"
- Use "fluent" API
- Separate optimization problem from optimization procedure

Experimentation has started with least squares optimizers:

- LevenbergMarquardtOptimizer
- GaussNewtonOptimizer

Optimization (cont) - version 4 direction

New classes/interfaces in "o.a.c.m.fitting.leastsquares":

- LeastSquaresProblem and LeastSquaresProblem.Evaluation
- LeastSquaresOptimizer and LeastSquaresOptimizer.Optimum
- LeastSquaresFactory and LeastSquaresBuilder

Usage:

Yet to be done: Refactor all the other optimizers.

Example 3 - Optimization (cont)

Some additional challenges:

- Stochastic algorithms are tricky to test
- FORTRAN ports create awful Java code, but "fixing" can create discrepancies
- BOBYQAOptimizer port has never really been fully supported
- Answering user questions requires expertise and time

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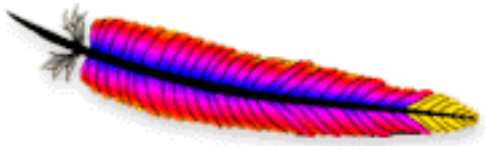
- Math is interesting!
- Bugs are interesting!
- People are interesting!



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Example 4 - Aggregated statistics

Problem: Aggregate summary statistics across multiple processes

- SummaryStatistics instances handle large data streams
- StatisticalSummary is reporting interface

Question: how to distribute instances / workload?

Threading and workload management

Questions:

1. Should we implement multi-threaded algorithms?
2. How can we be more friendly for Hadoop / other distributed compute environments?

- So far (as of 3.4.1), we have not done 1.
- So far, answer to 2 has been "leave it to users."

Could be both answers are wrong...

Example 5 - Genetic algorithm

Another example where concurrent execution would be natural...

Question: how to distribute "evolve" workload?

Example 6 - OLS regression

Three ways to do it

OLSMultipleRegression (stat.regression) in-memory

MillerUpdatingRegression (stat.regression) streaming

LevenbergMarquardtOptimizer (fitting.leastsquares) in-memory

1. How to make sure users discover the right solution for them?
2. How much dependency / reuse / common structure to force?

Example 6 - OLS regression (cont)

Simplest, most common: Question: What happens if design matrix is singular?

Example 6 - OLS regression (cont)

Answer: if it is "exactly" singular,

If it is near-singular, garbage out
So make singularity threshold configurable:

- What exactly is this threshold?
- What should exception error message say?
- How to doc it?
- What if we change underlying impl?

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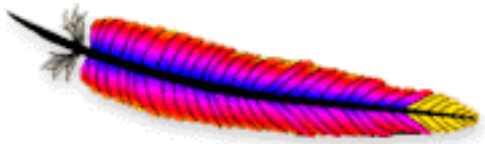

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Example 7 - Rank correlation

Given two double arrays and , we want a statistical measure of how well their rank orderings match.

Use Spearman's rank correlation coefficient.
How are ties in the data handled?
What if one of the arrays contains NaNs?

Example 7 - Rank correlation (cont)

- As of 3.4.1, by default ties are averaged and NaNs cause NotANumberException
- Both are configurable via RankingAlgorithm constructor argument
- RankingAlgorithm is a ranking implementation plus
  - TiesStrategy - what ranks to assign to tied values
  - NaNStrategy - what to do with NaN values
- Default in Spearman's is natural ranking on doubles with ties averaged and NaNs disallowed

Example 7 - Rank correlation (cont)

NaNStrategies:

- MINIMAL - NaNs are treated as minimal in the ordering
- MAXIMAL - NaNs are treated as maximal in the ordering
- REMOVED - NaNs are removed
- FIXED - NaNs are left "in place"
- FAILED - NaNs cause NotANumberException

Problems:

1. What if user supplies a NaturalRanking with the NaN strategy that says remove NaNs?
2. How to doc clearly and completely?

Example 8 - Random Numbers

Commons Math provides alternatives to the JDK PRNG and a pluggable framework

- RandomGenerator interface is like j.u.Random
- All random data generation within Commons Math is pluggable

Low-level example:

Example 8 - Random Numbers (cont)

High-level example:
Problems:

1. Well generators (used as defaults a lot) have some initialization overhead. How / when to take this hit?
2. Distribution classes also have sample() methods, but that makes them dependent on generators

Example 9 - Linear Programming

Maximize $7x_1 + 3x_2$ subject to
$3x_1 - 5x_3 \leq 0$
$2x_1 - 5x_4 \leq 0$
... (more constraints)

Example 9 - Linear Programming (cont)

Question: What happens if the algorithm does not converge?
Answer:

What if I want to know the last ?
(Rejected) Alternatives:

1. Don't throw, but embed some kind of status object in return
2. Shove context data in exception messages

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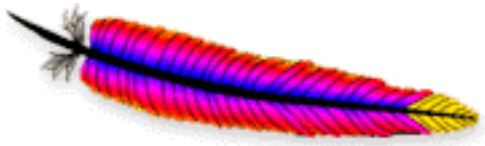

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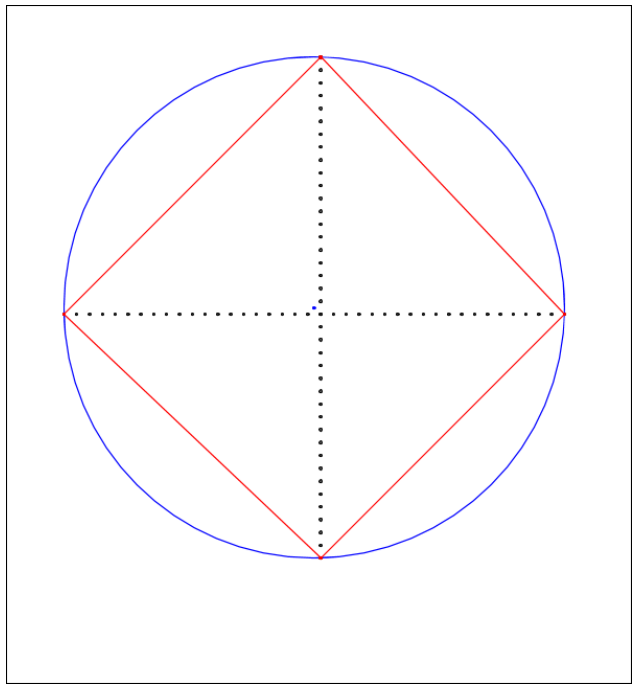
Example 10 - Geometry

Calculate the convex hull and enclosing ball of a set of 2D points:
Problems:

1. algorithms are prone to numerical problems
2. important to specify a meaningful tolerance, but depends on input data
3. does it make sense to support a default tolerance?



Lessons Learned

Key Challenges Recap...

- Balancing performance, mathematical correctness and algorithm fidelity
- Fully documenting behavior and API contracts
- Steering users toward good solutions as simply as possible
- Balancing OO design and internal reuse with approachability
- Obscure and abandoned contributions
- Reference implementations and / or data for validation
- Backward compatibility vs API improvement

Some lessons learned

- Let practical use cases drive performance / accuracy / fidelity decisions
- Be careful with ports and large contributions
- Limit public API to what users need
- Prefer standard definitions and algorithms
- Take time to fully research bugs and patches
- Constantly improve javadoc and User Guide
- Try to avoid compatibility breaks, but bundle into major version releases when you have to

Get Involved!

Using Apache Commons Math

Maven:
Download:
http://commons.apache.org/math/download_math.cgi

Watch for new versions!

Links

- Project homepage: http://commons.apache.org/math/
- Issue tracker:
  https://issues.apache.org/jira/browse/MATH
- Mailinglists: dev@commons.apache.org &
  user@commons.apache.org
  e-mail subject: [math]
- Wiki: http://wiki.apache.org/commons/MathWishList

How to contribute?

- Check out the user guide
  http://commons.apache.org/math/userguide
- Ask - and answer - questions on the user mailing list
- Participate in discussions on the dev list
- Create bug reports / feature requests / improvements in JIRA
- Create and submit patches (code, documentation, examples)
- Look at
  http://commons.apache.org/math/developers.html
- Run and review CheckStyle, Findbugs reports when creating patches
- Don't be shy asking for help with maven, git, coding style, math ... anything

- Questions?