CS340 Cheat Sheet Tristan Rice 2016-12-12

Assignment 1

Decision Trees:

- Classify by walking tree
- Greedy recursive splitting
- Information gain as score, entropy
- O(mnd log n),

Decision Stump Rule Search:

- Ignore rules outside feature ranges.
- Sort examples O(n log n)
- O(n) score updates
- Total cost: O(nd log n), data size: O(nd)

Learning Theory:

- THE TEST DATA CANNOT INFLUENCE THE TRAINING PHASE IN ANY WAY.
- Fundamental Trade-Off:
- 1. How small you can make the training error.
- 2. How well training error approximates the test error.
- Simple models have good approximation of test error, but fit training data poorly.
- Cross validation, test on your training data, use each point as test once.
- No free lunch theorem: no best machine learning model for every problem

Naive Bayes:

$$p(y_i = |x_i|) = \frac{p(x_i | y_i = |x_i|)p(y_i = |x_i|)}{p(x_i)}$$

- Compute p(y="spam"|xi) > p(y="not spam",xi)
- Need to estimate p(xi|y="spam")

Descriptive Statistics:

- Mean, Median, Quantiles (v s.t. x% < v)
- Box Plot

Assignment 2

KNN:

- Non-parametric
- Distance fn: Euclidean, L1 Dist, Jaccard similarity, Cosine, Distance after dimension reduction, Metric learning

Jaccard similarity: D(x1,x2)=(x1 x2)/(x1 U x2)

Ensemble Methods: Boosting, Averaging

Random Forests:

- Train number of deep decision trees on bootstrapped samples from the main dataset + small random subset of features on each stump
- Very fast, good out of the box classifier
- Bayesian Model Averaging
- Train O(tmnd log n), t = #trees, m = depth, d = #features, can be sqrt(d)
- Classify one is O(tm)

Clustering: No best method, no test error

K-Means:

- k clusters, random center
- add one point and update mean based on assignment
- initialization important, need to know k
- Total cost: O(ndk), updating means O(nd)
- vector quantization: cluster colors
- K-Medians: Can also use L1-norm + median
- K-Means++, init clusters by furthest distance
- Convex clusters

Density based clustering:

- Non-convex clusters

DBSCAN:

- Radius, if at least minPoints of same type become "core"
- Merge clusters if reachable
- Can have outliers
- Sensitive to boundaries
- need lots of points in high dimensions

$$\left\|\mathbf{x}
ight\|_p := igg(\sum_{i=1}^n \left|x_i
ight|^pigg)^{1/p}.$$

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Assignment 3

Linear regression (adding bias, change of basis, RBFs, regularization, cost of training/testing, effect of basis parameters).

- 1D
$$f(w) = \sum_{i=1}^n (wx_i - y_i)^2$$
 - Minimize least squares
$$w = \frac{\sum_{i=1}^n y_i x_i}{\sum_{i=1}^n x_i^2}$$
 - Solution

- Bias variable, add row with 1s
- Change of basis, linear least squares
- each row: $[1 \times x^2 \dots x^p]$; $[1 \times \sin(6x)]$
- Radial basis functions: non-parametric

- Can combine both

Assignment 4:

Convex and MLE/MAP estimation (showing functions are convex, connection between probabilities and losses/regularizers)

- likelihood function: p(y|X,w)
- minimize negative log-likelihood

$$f(w) = -\sum_{i=1}^{n} \log(p(y_i|x_i, w))$$

$$p(w|X,y) \propto p(y|X,w)p(w)$$

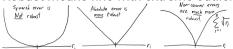
$$(p(w|X,y)) = -\sum_{i=1}^{n} \log(p(y_i|x_i,w)) - \sum_{j=1}^{d} \log(p(w_j)) + const$$

Sigmoid: $h(z) = 1/(1 + \exp(-z))$

Logistic Regression:

Robust regression (weighted least squares, smooth approximations, computing gradients).

- Robust means fine with extreme outliers



- Absolute is most robust convex error function
- Weighted least squares: weight on each training example

Convexity:

- 1-variable, twice-differentiable function is convex iff $f''(w) \ge 0$ for all 'w'.
- A convex function multiplied by non-negative constant is convex.
- Norms and squared norms are convex.
- The sum of convex functions is a convex function.
- The max of convex functions is a convex function.
- Composition of a convex function and a linear function is convex.
- Not true: composition of convex and convex is convex

Regularizers:

- "robust" = less influenced by large values

 $p(y_i|x_i, w) = \frac{1}{1 + \exp(-y_i w^T x_i)}$ $f(w) = \sum_{i=1}^n \log(1 + \exp(-y_i w^T x_i)) + \frac{\lambda}{2} ||w||^2$

- L0 sparsity, non-convex
- L1 makes things more sparse, non-convex
- Huber loss:

-12

$$L_\delta(a) = egin{cases} rac{1}{2}a^2 & ext{for } |a| \leq \delta, \ \delta(|a| - rac{1}{2}\delta), & ext{otherwise}. \end{cases}$$

- L Infinite = max, log-sum-exp is smooth approx
- LSE(x1,...,xn) = log(exp(x1)+...+exp(xn))

0-1 Loss: Number of classification errors

- Hinge: Convex, max{0, 1-y_iw^Tx_i}
- SVM is hinge loss + L2-regularizer
- Logistic: smooth approximation to hinge, differentiable

Regularized logistic regression (loss functions for binary classification, effect of different regularizers on overfitting and sparsity)

Multi-class Logistic (one-vs-all, softmax loss derivatives and implementation)

Vectors/matrices/norms (summation and vector/matrix/norm notation, minimizing quadratic functions as linear systems)

Assignment 5:

PCA (computing 1st PC, scaling issue, PCA for visualization, PCA for compression)

- $-||w||_2 = 1$
- X=ZW
- $f(Z,W) = sum_{i=1}^n(w*z_i-x_i)^2$
- reduce dimensionality

Beyond PCA (different loss functions, effect of regularizers)

Multi-dimensional scaling (basic model, ISOMAP and geodesic distance)

Assignment 6:

PageRank (random walk model)

- Probability of landing on page as t->inf
- Add small probability of going to random webpage
- At each step follow random link on page

Stochastic gradient and neural networks (effect of step-size, effect of standardization, effect of initialization, effect of non-linearity, effect of regularization)

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Inner product $a^Tb = b^Ta$ $a^T(b+c) = a^Tb + a^Tc$ Orthogonal $a^Tb = 0$ Orthonormol $a^Tb = 1$ Matrix Multiplication A(BC) = (AB)CA(B+C) = AB + AC $AB \neq BC$ $(AB)^T = B^T A^T$ $(AB)^2 = ABAB$ Matrix * vector = vector $x^T A y = x^T (A y) = (A y)^T x = y^T A^T x$ Inverses $A^{-1}A = I = AA^{-1}$ $(A^{-1})^T = (A^T)^{-1}$ $(AB)^{-1} = \gamma^{-1}A^{-1}$ $(AB)^{-1} = B^{-1}A^{-1}$

Operation	Input	Output	Algorithm	Complexity
Matrix multiplication	Two <i>n×n</i> matrices	One <i>n×n</i> matrix	Schoolbook matrix multiplication	O(n ³)
			Strassen algorithm	O(n ^{2.807})
			Coppersmith–Winograd algorithm	O(n ^{2.376})
			Optimized CW-like algorithms ^{[14][15][16]}	O(n ^{2.373})
Matrix multiplication	One <i>n×m</i> matrix & one <i>m×p</i> matrix	One <i>n×p</i> matrix	Schoolbook matrix multiplication	O(nmp)
Matrix inversion*	One <i>n×n</i> matrix	One <i>n×n</i> matrix	Gauss-Jordan elimination	O(n ³)
			Strassen algorithm	O(n ^{2.807})
			Coppersmith–Winograd algorithm	O(n ^{2.376})
			Optimized CW-like algorithms	O(n ^{2.373})
Singular value decomposition	One <i>m×n</i> matrix	One mxm matrix, one mxn matrix, & one nxn matrix		O(mn ²) (m ≤ n)
		One mxr matrix, one rxr matrix, & one nxr matrix		
Determinant	One <i>n×n</i> matrix	One number	Laplace expansion	O(n!)
			Division-free algorithm ^[17]	O(n ⁴)
			LU decomposition	O(n ³)
			Bareiss algorithm	O(n ³)
			Fast matrix multiplication ^[18]	O(n ^{2.373})
Back substitution	Triangular matrix	n solutions	Back substitution ^[19]	O(n ²)