Witness

 $\phi = (x \vee y \vee z)(\bar{x} \vee \bar{y})(x \vee \bar{z})$ <- Conjuntive normal form

 $\phi \in SAT \equiv \phi$ has a satisfying truth assignment

Witness is a truth statement.

If it's satisfiable, there has to be a witness.

 $\phi \in Co-Sat \equiv \phi$ has no satisfying assignment iff $\phi \in SAT$.

NP-Completeness

L is NP-complete \equiv L is in NP and L is NP-hard.

 $\mathrm{NP} \equiv \exists \ \mathrm{witness}$

 $CoNP \equiv \forall \text{ witnesses}$

 $\exists x \forall y \text{ verifyable in poly time} \equiv \sum_z$

 $\forall x\exists y=\Pi_z$

True Quantified Boolean Formulas

 $\forall x \exists y \forall z (x \vee y \vee z) (\bar{x} \vee \bar{y})$