Computer Science 221

Practice Questions - Set 3 Solutions: Data Structures, etc.

1. Use a doubly linked list. Why? We need to update the node before the last.

```
int height( Bnode* node)

{
    if ( node == NULL ||
        (node->left == NULL && node->right == NULL) )
        return 0;

    int leftHeight = height( node -> left );

    int rightHeight = height( node -> right );

    if (leftHeight > rightHeight)
        return leftHeight + 1;

    else
    return rightHeight + 1;
```

}

- 3. If the sequences are not sorted then the worst-case running time is O(n). If they are stored in sorted order, then the worst-case running time is $O(n^2)$.
- 4. To count the number of 1's in A, we can do a binary search on each row of A to determine the position of the last 1 in that row. Then we can simply sum up these values to obtain the total number of 1's in A. This takes O(lg n) time to find the last 1 in each row. Done for each of the n rows, then this takes O(n lg n) time.
- 5. First, we sort the objects of A. Then, we can go through the sorted sequence and remove all duplicates. This takes O(n lg n) time to sort and O(n) time to remove the duplicates. Overall, this is an O(n lg n) algorithm.
- 6. We know that $m \le C(n,2) = n(n-1)/2$ is $O(n^2)$. It follows, therefore, that $O(\lg(n^2)) = O(2 \lg(n)) = O(\lg n)$.