

# CIS560

Obtaining a Good Database Design – Part 2

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Computer Science



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## What's next?

- We briefly discussed the 3NF and BCNF.
- They are defined using:
  - Functional Dependencies
  - Keys
- We defined functional dependencies.
- We defined closures and how they help us find all functional dependencies.
- Now let's review keys.

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## Superkeys and Keys

- A **superkey** is a set of attributes  $A_1, \dots, A_n$  s.t. for any other attribute  $B$ , we have  $A_1, \dots, A_n \rightarrow B$
- A **key** is a minimal superkey
  - set of attributes which is a superkey
  - for which no subset is a superkey



## Computing Keys

- Compute  $X^+$  for all sets  $X$
- If  $X^+ =$  all attributes, then  $X$  is a superkey
- We only want the keys  
(*minimal superkeys*)



## Example - What are the key(s)?

Enrollment(student, address, course, room, time)

student  $\rightarrow$  address  
room, time  $\rightarrow$  course  
student, course  $\rightarrow$  room, time

*HINT:* You can have more than one key.

Keys: {student, room, time}, {student, course}



## How do we use keys to eliminate anomalies?

Each attribute must provide a fact  
about the **key**,  
the **whole key**,  
and **nothing but the key**.

Chris Date's adaptation to William Kent's summary



# Boyce-Codd Normal Form

- A relation R is in BCNF if and only if for every functional dependency  $X \rightarrow A$ :
  - $X \rightarrow A$  is a trivial functional dependency  
or
  - X is a superkey for R
- Equivalently:  $\forall X$ , where X is a set of attributes, either  $(X^+ = X)$  or  $(X^+ = \text{all attributes})$



## Example

Name	ID	Phone	Department
Fred	123	206-555-1234	CIS
Fred	123	206-555-6543	CIS
Joe	987	908-555-2121	Math
Joe	987	206-151-7839	Math

$ID \rightarrow \text{Name, Department}$

What is the key?  
{ID, Phone}

Hence  $ID \rightarrow \text{Name, Department}$   
is a “bad” dependency



## BCNF Decomposition – Using FDs

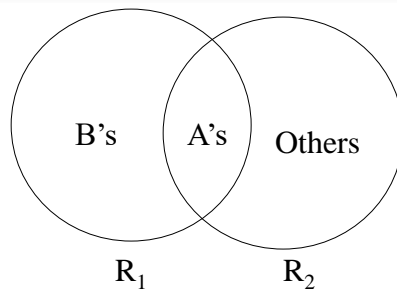
**repeat**

choose  $A_1, \dots, A_m \rightarrow B_1, \dots, B_n$  that violates BCNF (bad FD)

split  $R$  into  $R_1(A_1, \dots, A_m, B_1, \dots, B_n)$  and  $R_2(A_1, \dots, A_m, [\text{others}])$

continue with both  $R_1$  and  $R_2$

**until** no more violations



A two-attribute relation  
is always in BCNF.

## Example

Name	ID	Phone	Department
Fred	123	206-555-1234	CIS
Fred	123	206-555-6543	CIS
Joe	987	908-555-2121	Math
Joe	987	206-151-7839	Math

$ID \rightarrow \text{Name, Department}$  is a bad functional dependency

## Relation Decomposition

Name	<u>ID</u>	Department	Phone
Fred	123	CIS	206-555-1234
Fred	123	CIS	206-555-6543
Joe	987	Math	908-555-2121
Joe	987	Math	206-151-7839



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## Relation Decomposition

Name	<u>ID</u>	Department
Fred	123	CIS
Joe	987	Math

<u>ID</u>	Phone
123	206-555-1234
123	206-555-6543
987	908-555-2121
987	206-151-7839



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## BCNF Decomposition – Using Closures

**repeat**

find  $X$  s.t.:  $X \neq X^+ \neq [\text{all attributes}]$

**if** (not found) **then** “ $R$  is in BCNF”

**let**  $Y = [\text{all attributes}] - X^+$

decompose  $R$  into  $R_1(X^+)$  and  $R_2(X \cup Y)$

continue with both  $R_1$  and  $R_2$

**until** no  $X$  is found



## Example BCNF Decomposition – Using Closures

**Student**(name, ID, age, hairColor, phoneNumber)

$ID \rightarrow \text{name, age}$

$\text{age} \rightarrow \text{hairColor}$

Iteration 1: **Student**  $X = ID$

$ID^+ = \{ID, \text{name}, \text{age}, \text{hairColor}\}$

Decompose into: **Student1**(ID, name, age, hairColor)

**Phone**(ID, phoneNumber)

Iteration 2: **Student1**  $X = \text{age}$

$\text{age}^+ = \{\text{age}, \text{hairColor}\}$

Decompose: **Hair**(age, hairColor)

**Student2**(ID, name, age)

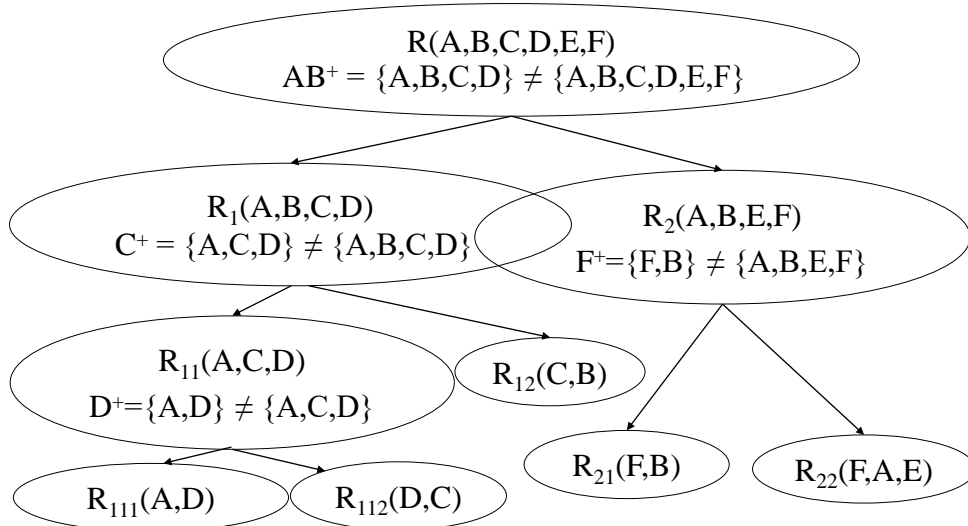


## Example

 $R(A,B,C,D,E,F)$ 

$AB \rightarrow C$
$C \rightarrow D$
$F \rightarrow B$
$D \rightarrow A$

What are the keys ?



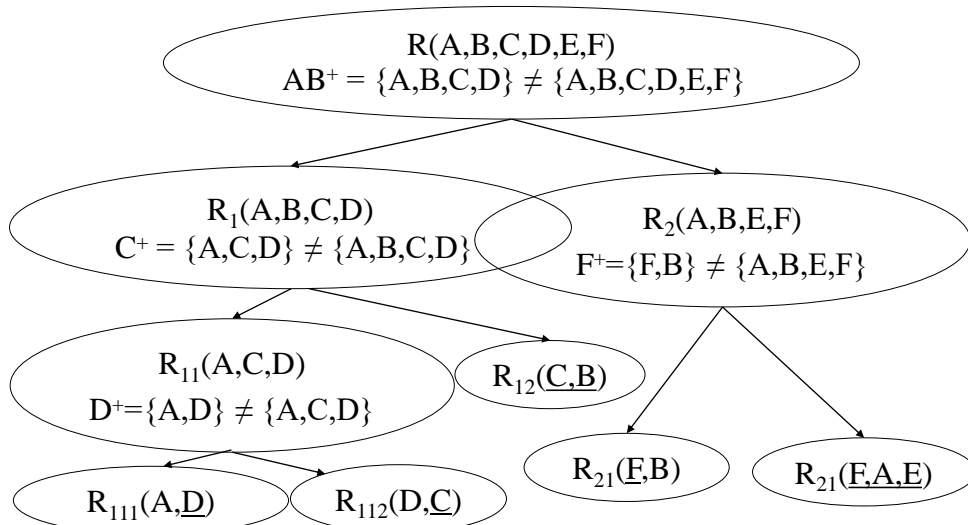
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## Example

 $R(A,B,C,D,E,F)$ 

$AB \rightarrow C$
$C \rightarrow D$
$F \rightarrow B$
$D \rightarrow A$

What are the keys ?



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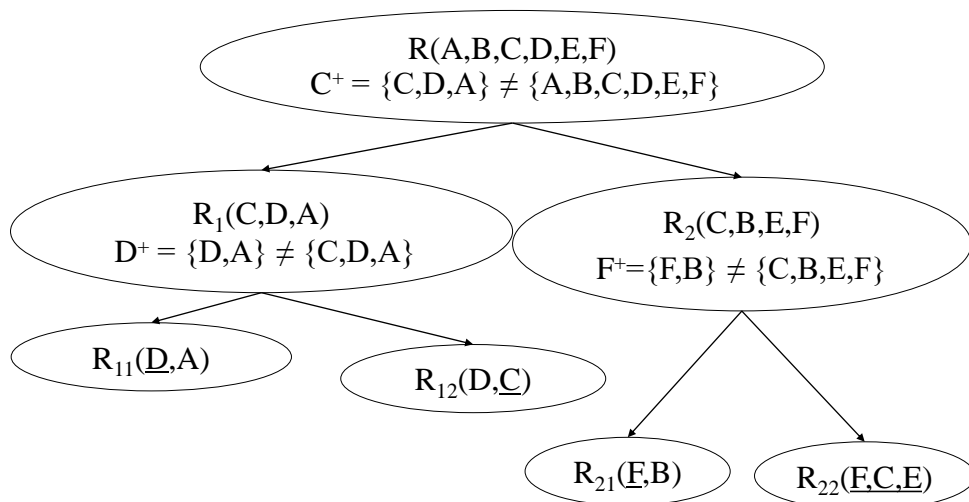
# Is the resulting BCNF schema unique?



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## Example – Solution 2

$R(A,B,C,D,E,F)$	$AB \rightarrow C$
	$C \rightarrow D$
	$F \rightarrow B$
	$D \rightarrow A$



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Which solution is better?

$$R_{111}(A, \underline{D}), R_{112}(D, \underline{C}), R_{12}(\underline{C}, \underline{B}), R_{21}(\underline{E}, B), R_{22}(\underline{E}, \underline{A}, \underline{E})$$

OR

$$R_{11}(A, \underline{D}), R_{12}(D, \underline{C}), R_{21}(\underline{E}, B), R_{22}(\underline{E}, \underline{C}, \underline{E})$$


Which solution is better?

- From the theoretical point of view...  
Both solutions are good.
- From a practical point of view...  
It depends.
- Look at the common ways they are queried, for example.

