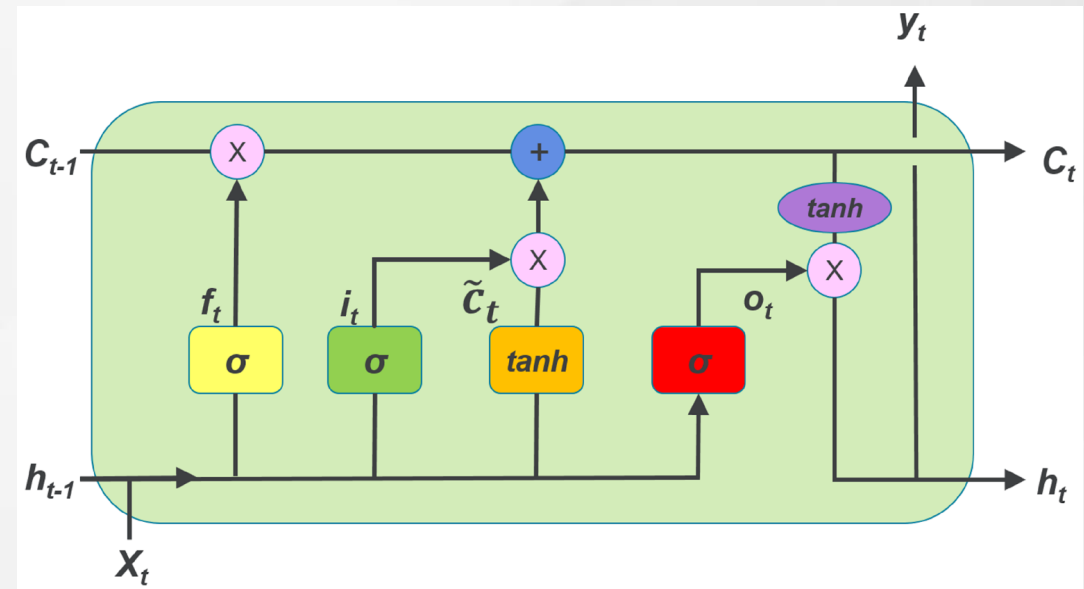


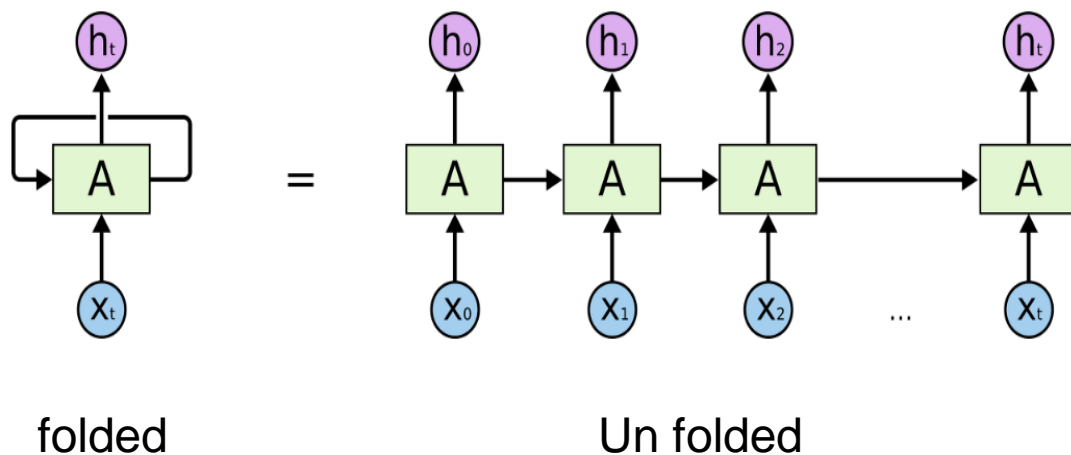
Chapter 09. 시계열을 활용한 딥러닝 (Time Sequence Processing)

RNN, Seq2Seq, LSTM, GRU



Recurrent Neural Network

- **Recurrent** : 반복되는 -> 시퀀스의 모든 요소에 대해 동일한 작업을 수행하고 출력은 이전 계산에 의존하기 때문에 *반복적*이라고 합니다.
- RNN은 지금까지 계산 된 것에 대한 정보를 캡처하는 "**메모리**"가 있다는 것입니다



RNN 의 특징 :

1) 장점 :

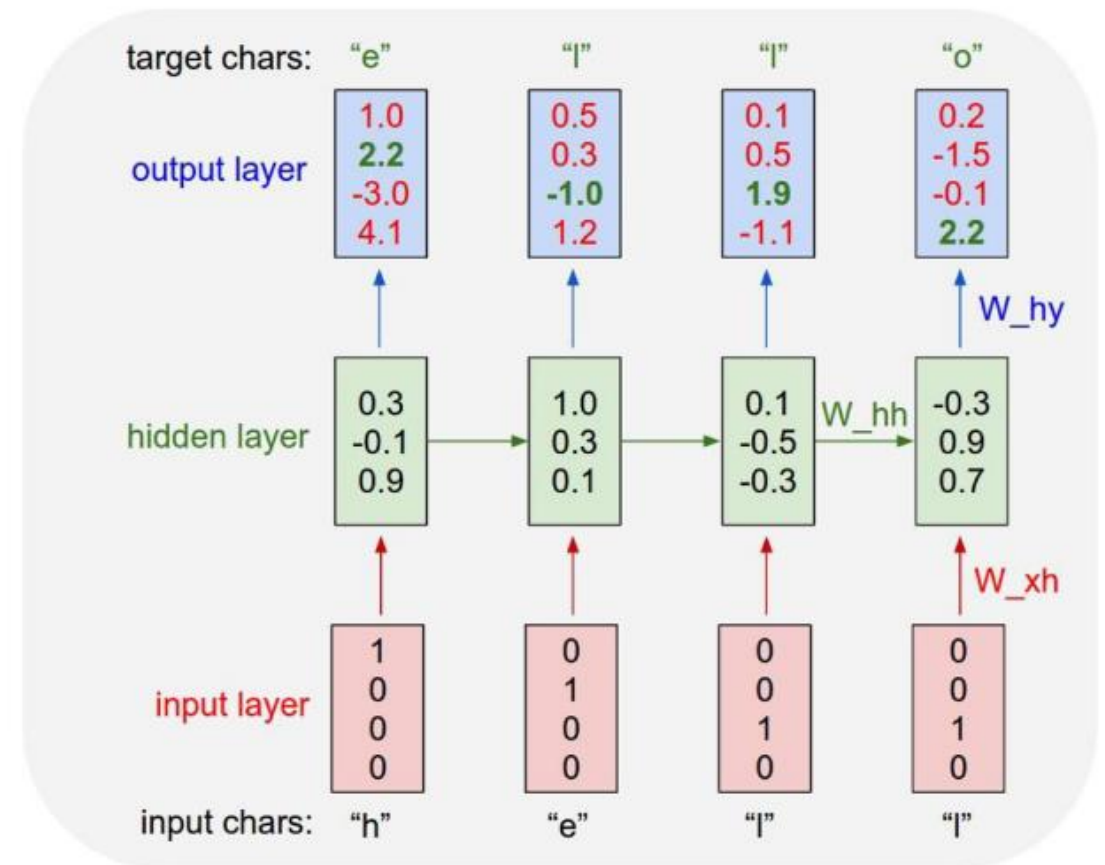
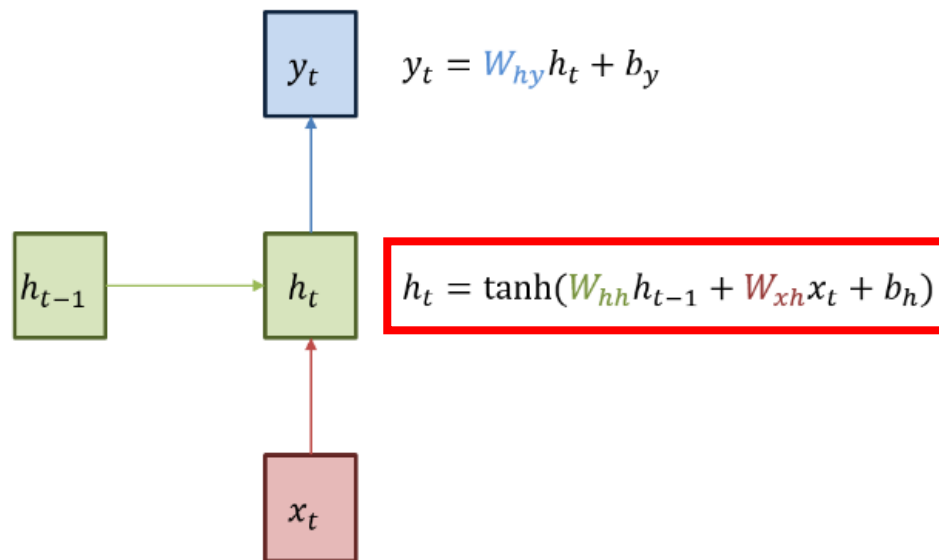
- 시퀀스 길이에 관계없는 input/output

2) 단점 :

- Gradient Vanishing : 상대적으로 짧은 sequence 학습

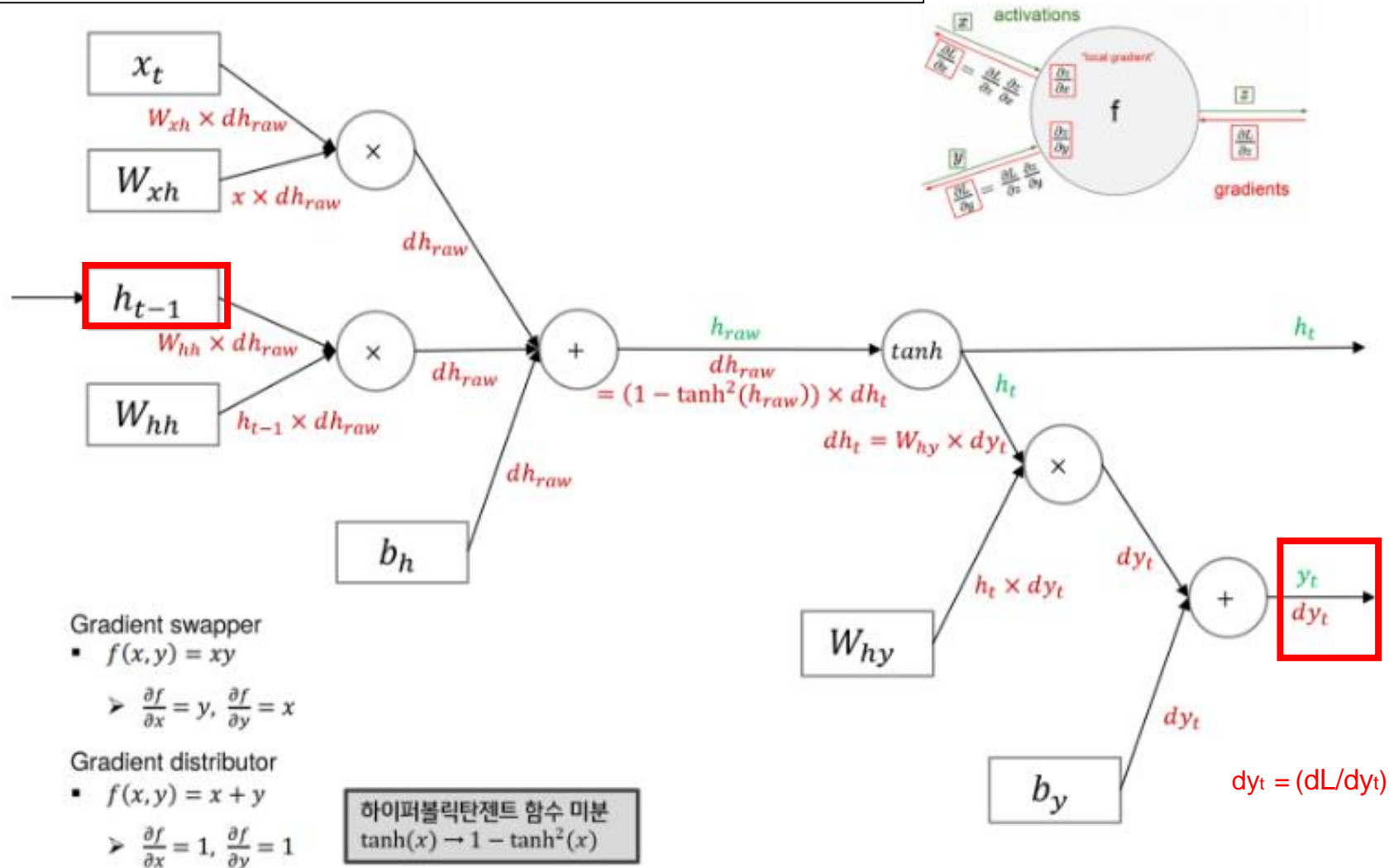
RNN forward propagation

- RNN 은 “입력층“, “은닉층(Hidden layer)“, “출력층“ 으로 구성되있다.



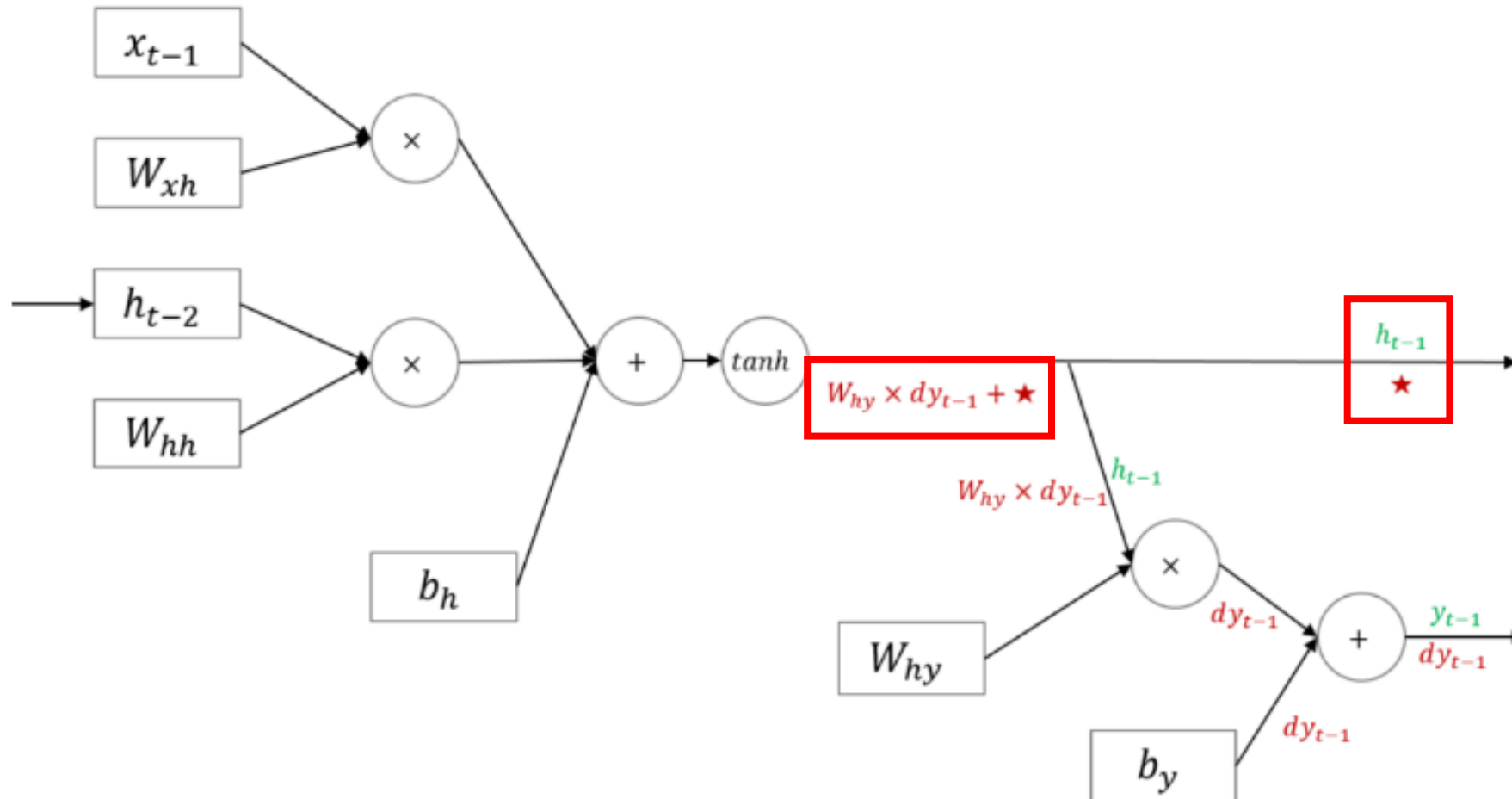
RNN backward propagation

<https://ratsgo.github.io/natural%20language%20processing/2017/03/09/rnnlstm/>



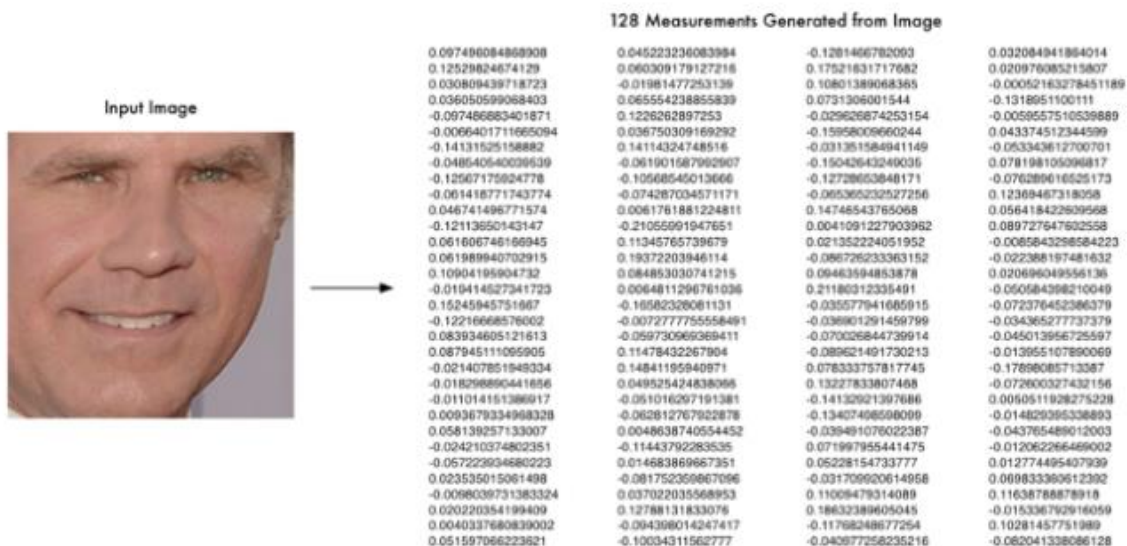
RNN backward propagation

<https://ratsgo.github.io/natural%20language%20processing/2017/03/09/rnnlstm/>

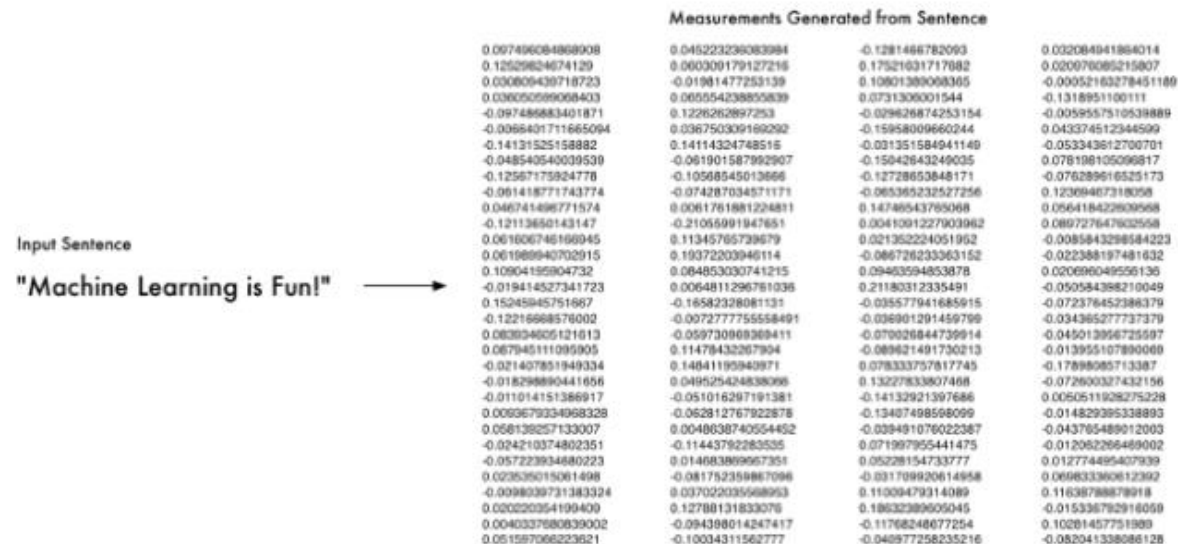


Sequence to Sequence

Encoding : 매우 복잡한 무엇인가를 단순한 것으로 표현할 수 있게 해줍니다.



이러한 얼굴 특징 측정값들은 다른 사람들의 얼굴이 다른 결과값으로 나오도록 훈련 된 신경망에 의해 생성됩니다.

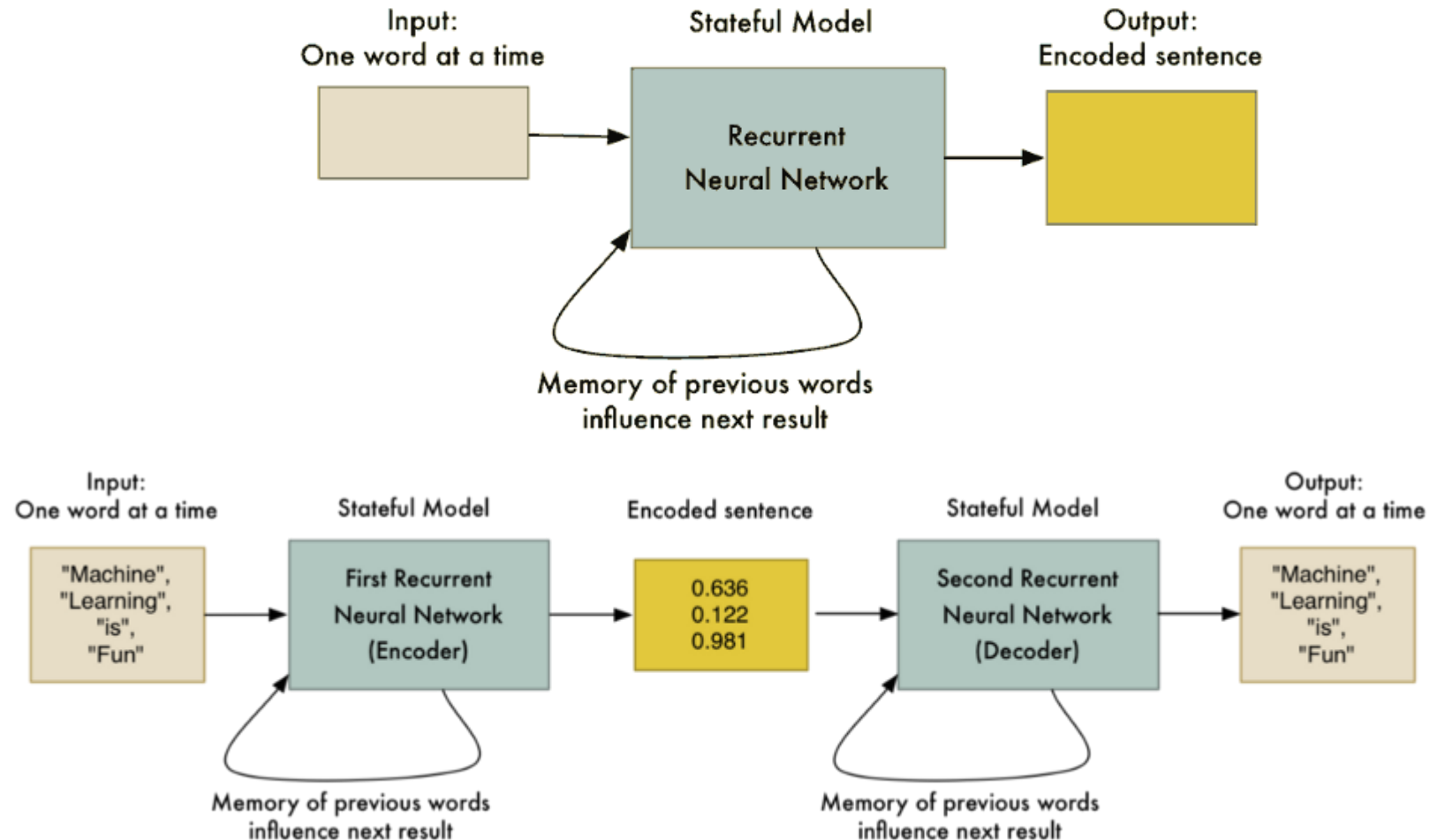


이 숫자 목록은 영어 문장인 "Machine Learning is Fun!"을 나타냅니다. 다른 문장은 다른 숫자의 집합으로 표현될 것입니다.

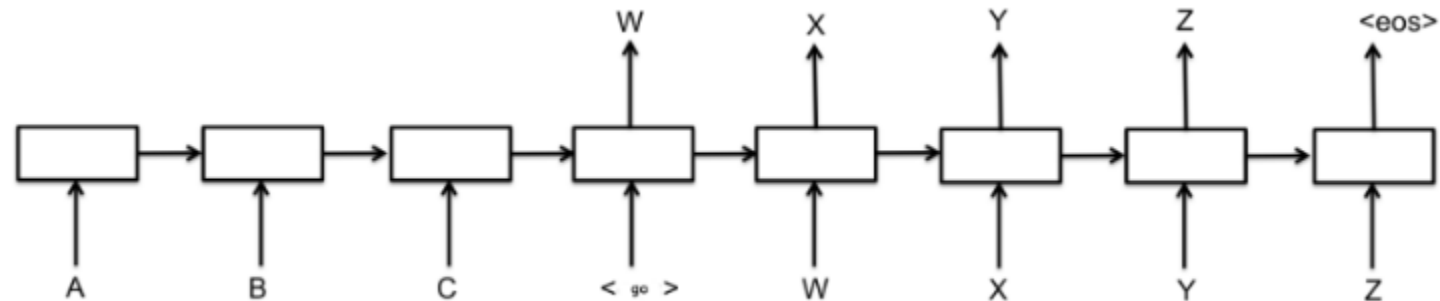
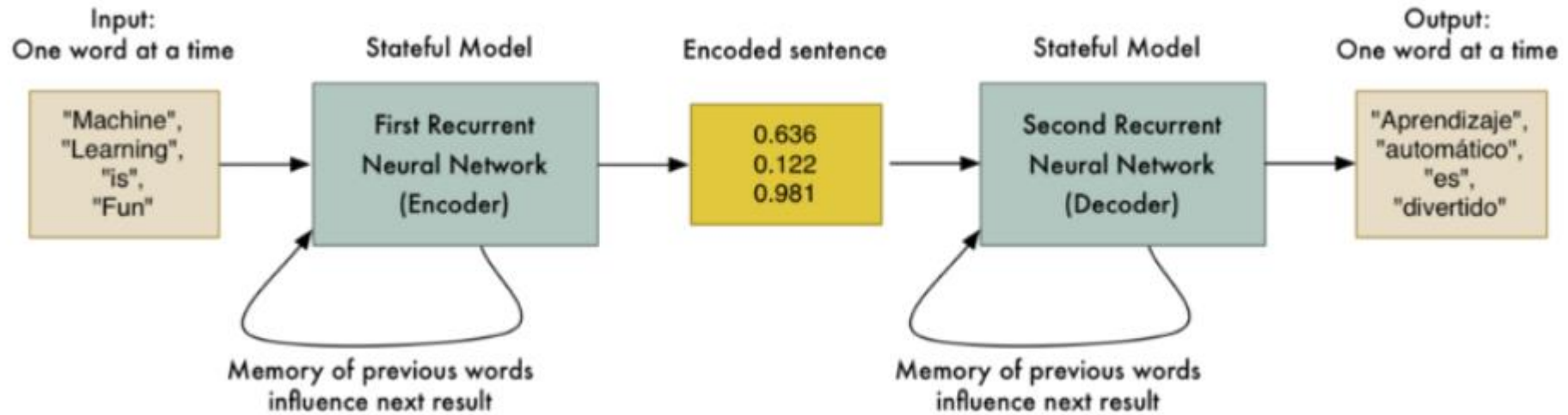
복잡한 그림, 문장을 일련의 고유한 숫자들로 표현 한다 !

Sequence to Sequence

Sequence 2 Sequence : RNN 도 Encoder / Decoder 역할을 할 수 있다.



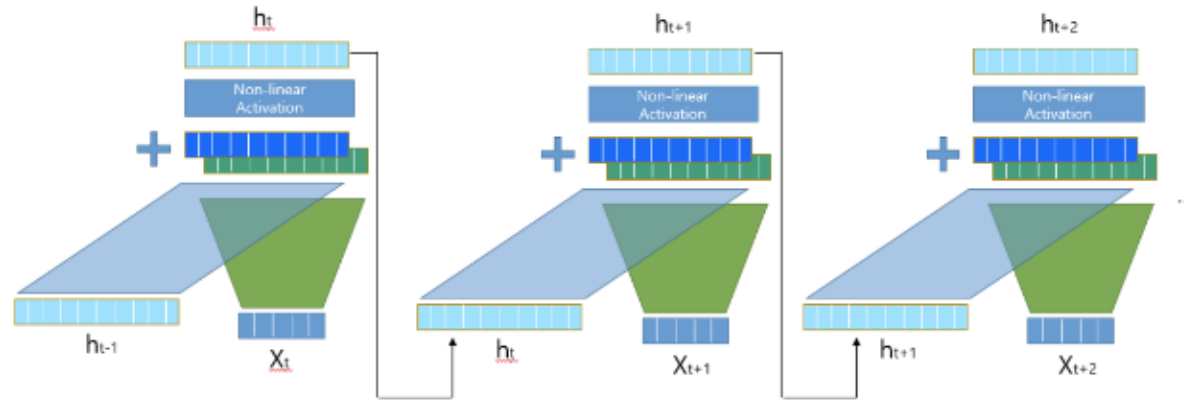
Sequence to Sequence



RNN Problem

<https://github.com/heartcore98/Standalone-DeepLearning/blob/master/Lec8/Lec8-A.pdf>

Vanishing Gradient Problem



$$h_{t-2} = \tanh(W[h_{t-3}, x_{t-2}])$$

$$h_{t-1} = \tanh(W[h_{t-2}, x_{t-1}])$$

$$h_t = \tanh(W[h_{t-1}, x_t])$$

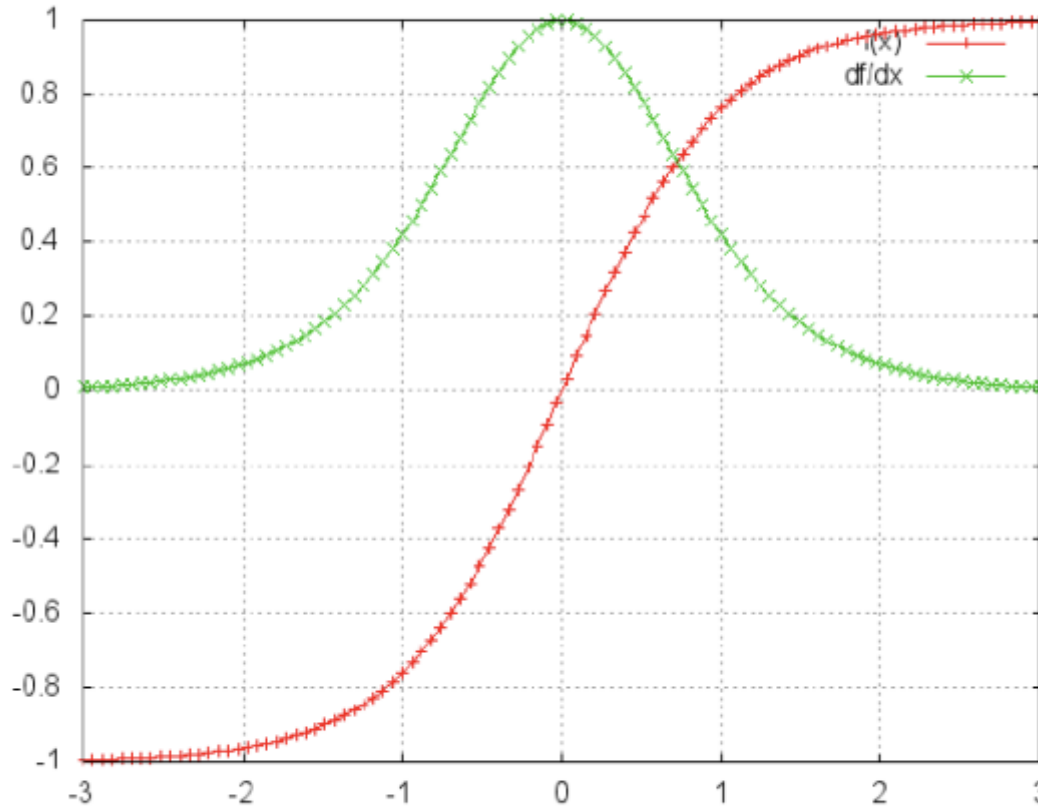
$$h_t = \tanh(W[\tanh(\dots \tanh(\dots h_{t-3})), x_t])$$

So many $\tanh(x)$!

RNN Problem

<https://github.com/heartcored98/Standalone-DeepLearning/blob/master/Lec8/Lec8-A.pdf>

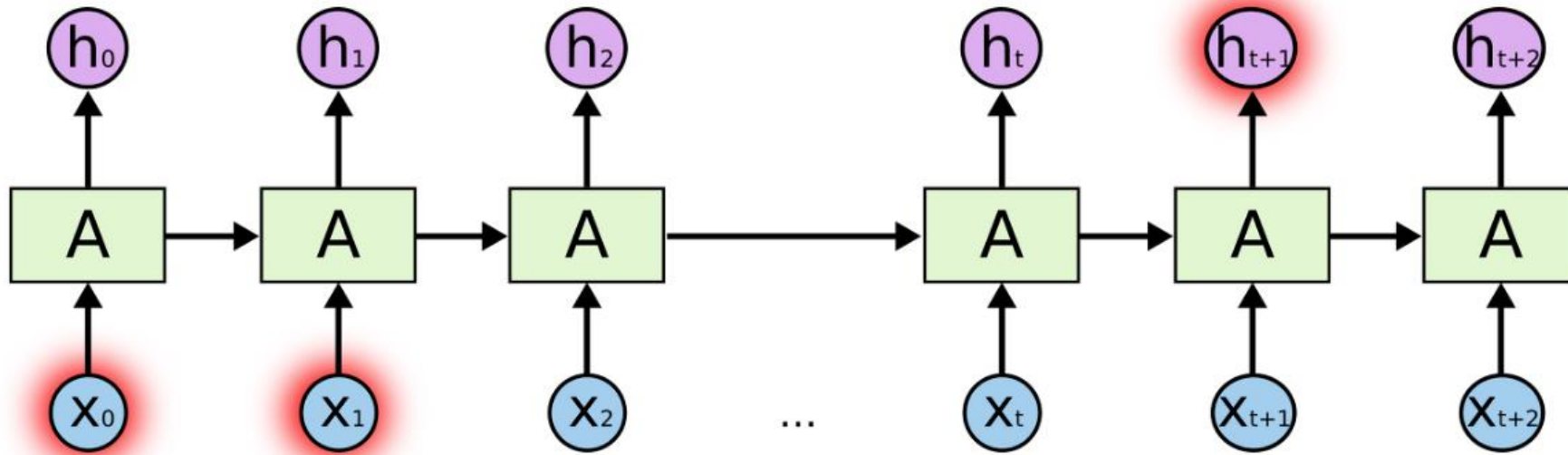
Vanishing Gradient Problem



Graph of $\tanh(x)$ (red) $\frac{d}{dx}\tanh(x)$ (green)

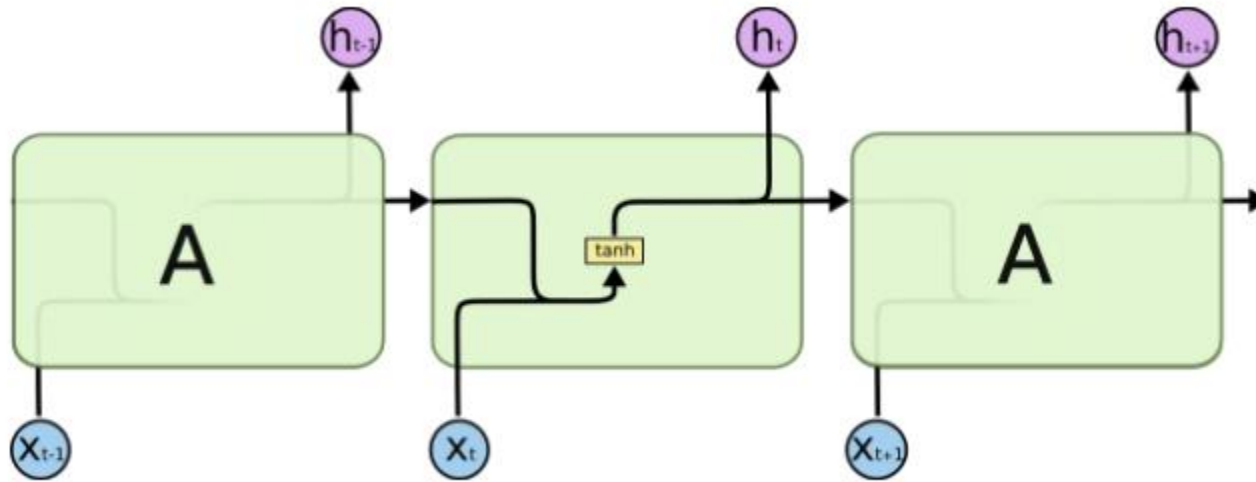
LSTM

RNN 의 문제점 : Gradient Vanishing 문제로 장기간에 걸친 시간의존성은 학습시킬 수 없다.



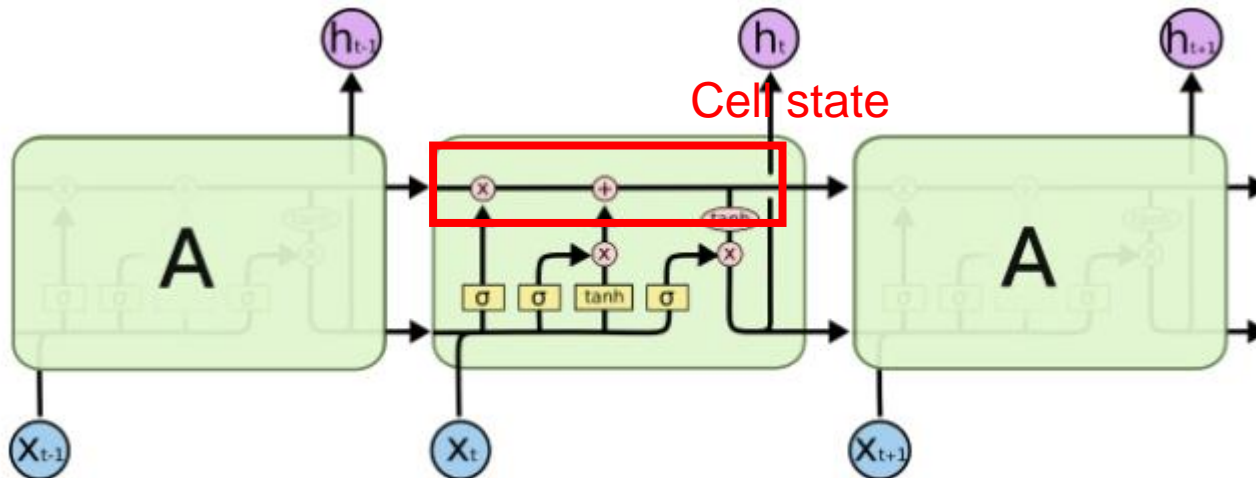
Long Short Term Memory : 장시간에 걸친 시간 의존성, 단 시간에 걸친 시간의존성 모두를 학습시킬 수 있는 기법.

LSTM



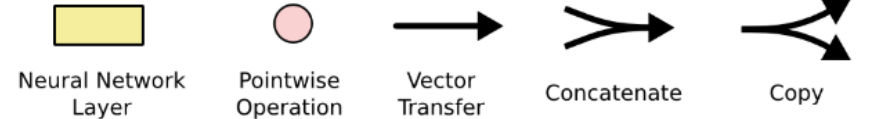
싱글 레이어를 가지고 있는 반복되는 표준 RNN 모듈

: RNN

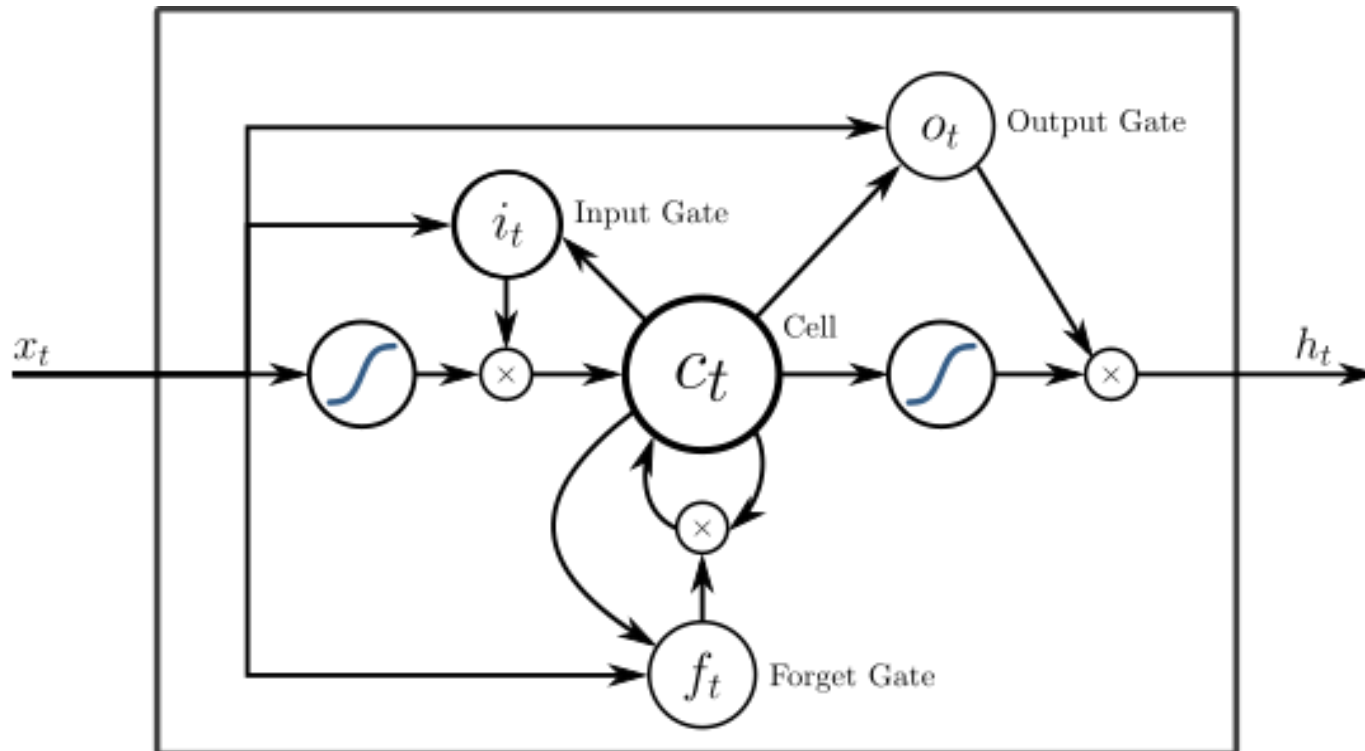


LSTM에 들어있는 4개의 상호작용하는 레이어가 있는 반복되는 모듈

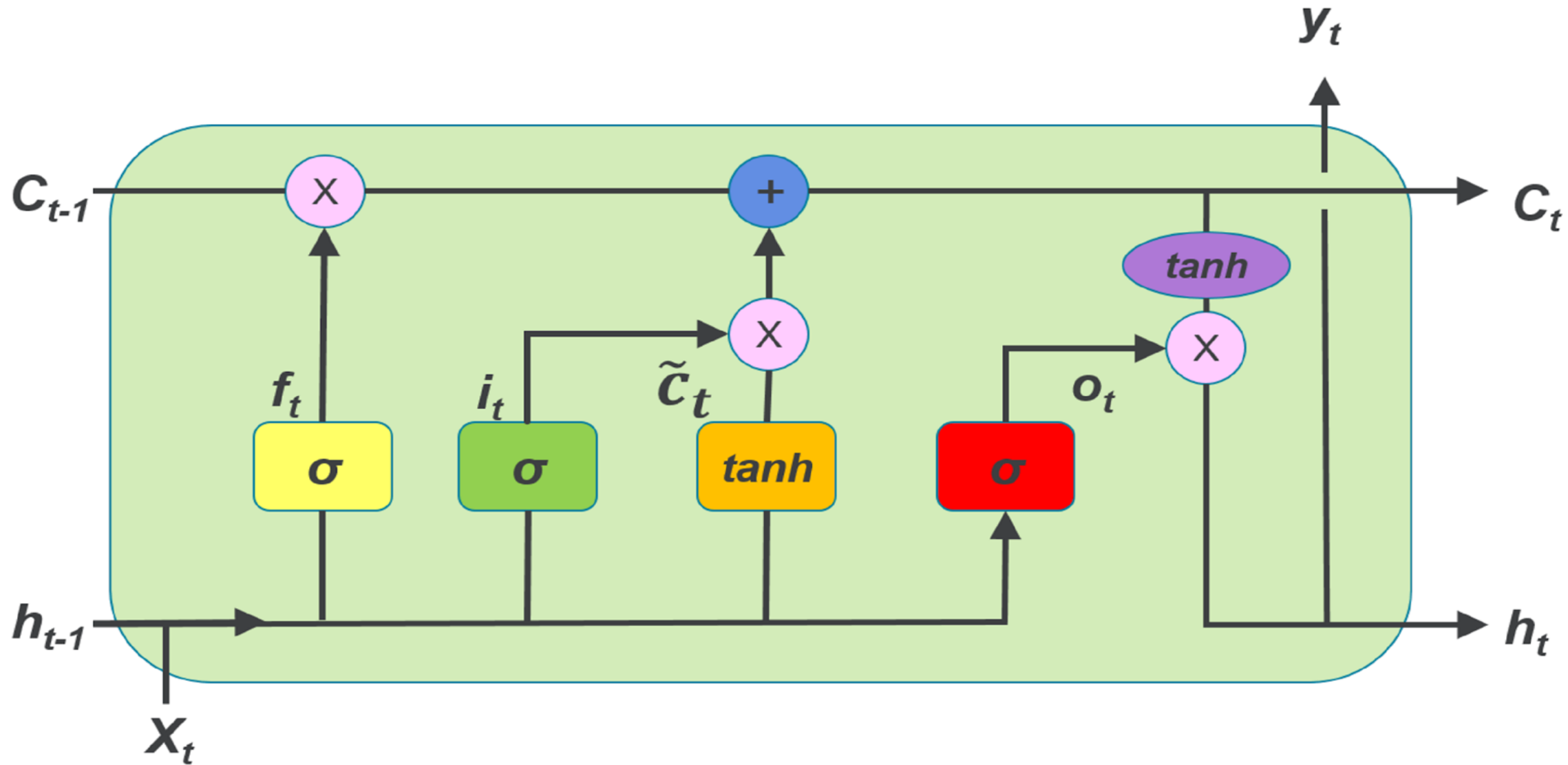
: LSTM



LSTM

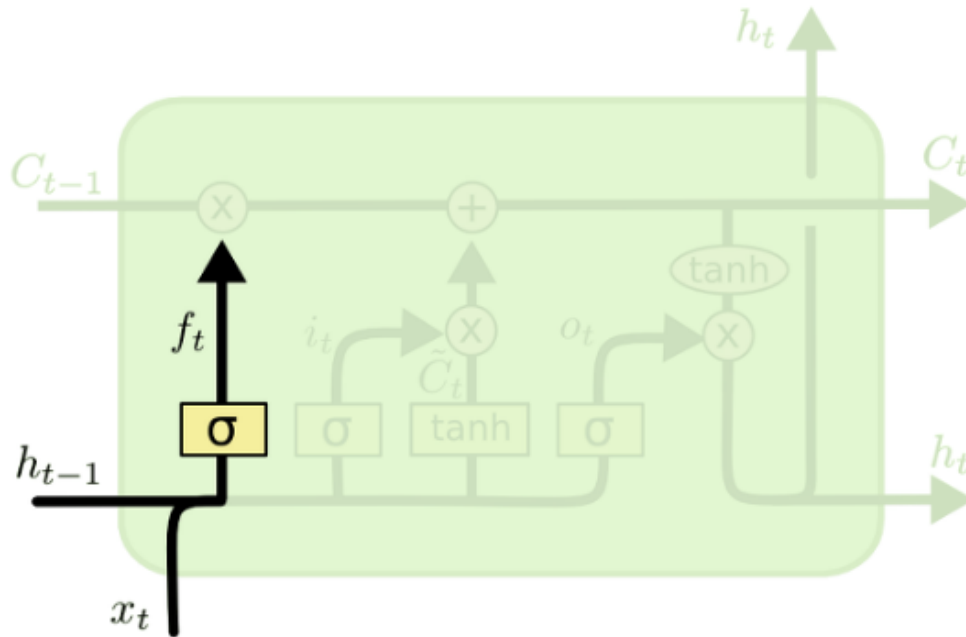


- **Input gate**
- **Forget gate**
- **Output gate**



LSTM

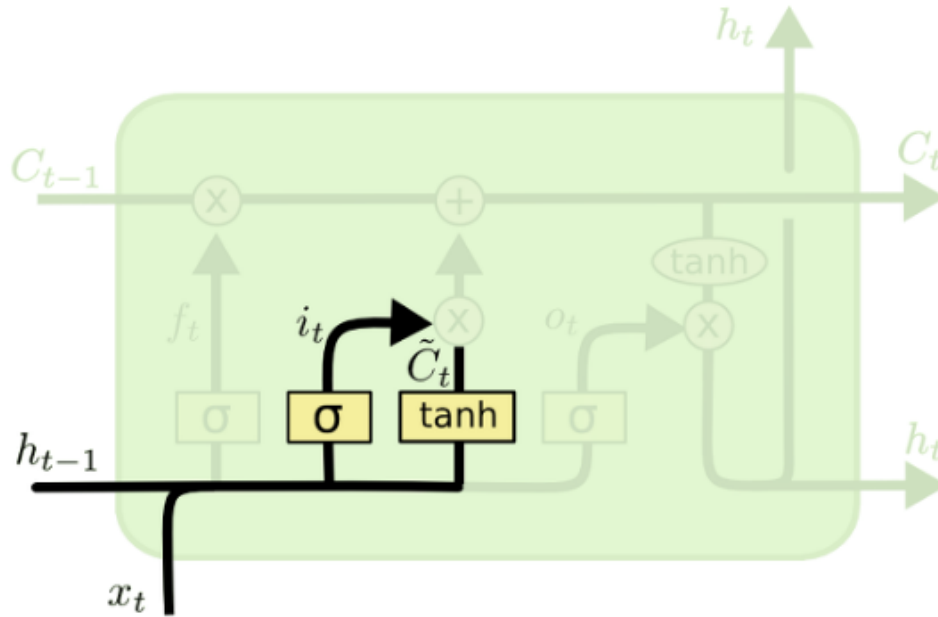
- **forget gate** : 시간 t 에서의 정보의 중요도에 따른 망각 결정



$$f_t = \sigma(W_f \cdot [h_{t-1}, x_t] + b_f)$$

LSTM

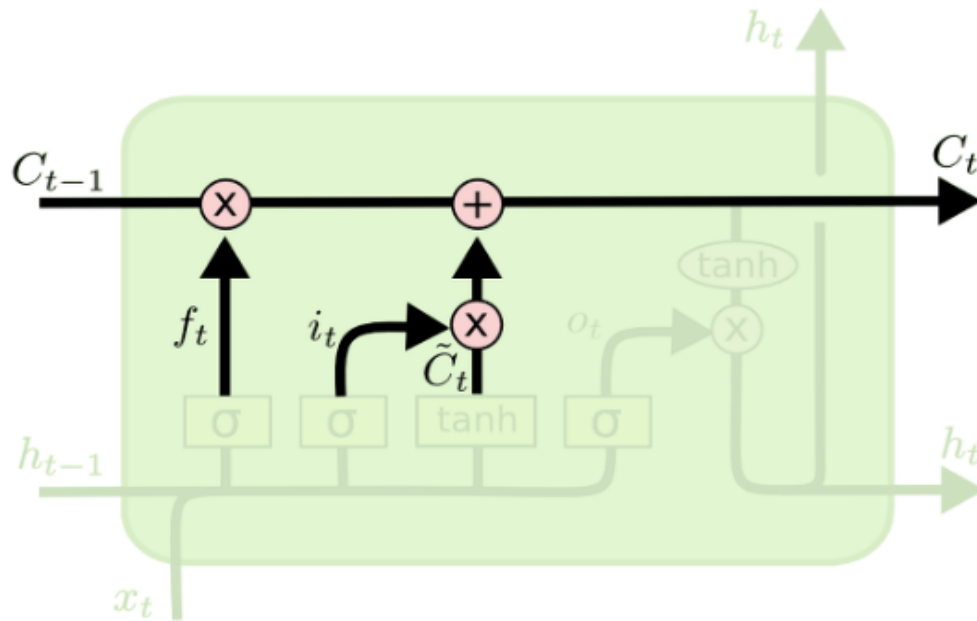
- **Input gate:** 시간 t 에서의 정보를 받아들이는 양 결정



$$i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i)$$
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

LSTM

- **Cell state** : 내부 기억에 관련된 state

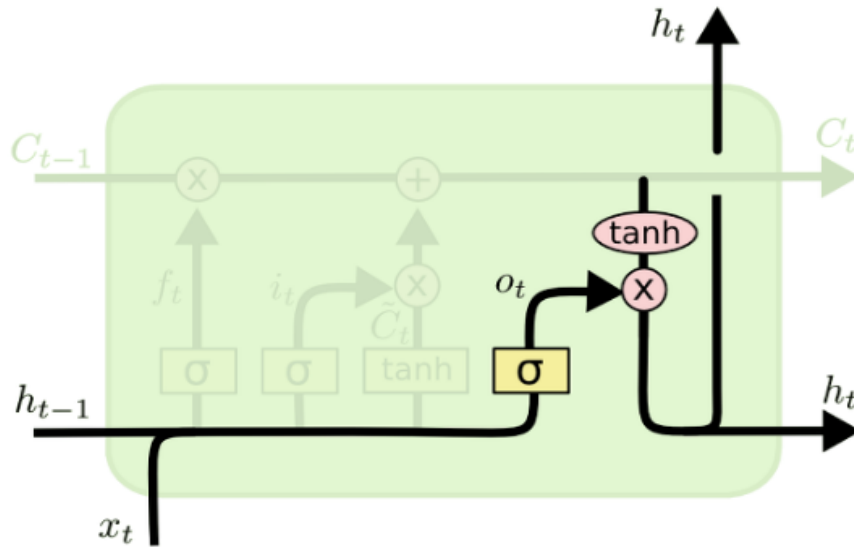


Input 정보를 얼마나 받아들일지
이전 cell state 를 얼마나 망각할
지 결정

$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

LSTM

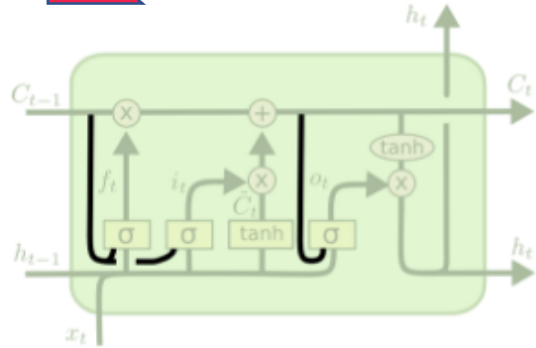
- **Output gate** : 다음 연속된 모듈에 hidden state 결정



$$o_t = \sigma (W_o [h_{t-1}, x_t] + b_o)$$

$$h_t = o_t * \tanh (C_t)$$

LSTM and others

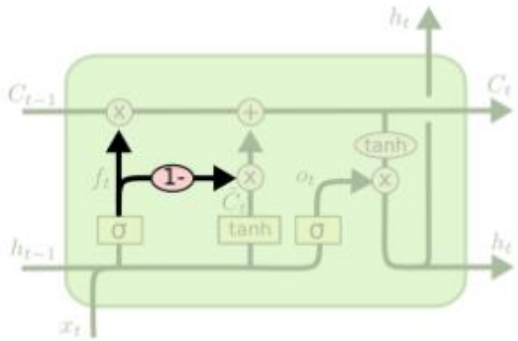


$$f_t = \sigma(W_f \cdot [C_{t-1}, h_{t-1}, x_t] + b_f)$$

$$i_t = \sigma(W_i \cdot [C_{t-1}, h_{t-1}, x_t] + b_i)$$

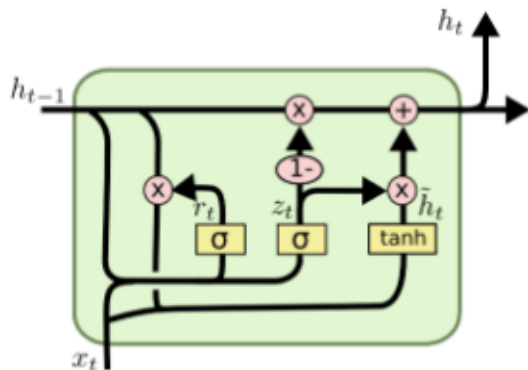
$$o_t = \sigma(W_o \cdot [C_t, h_{t-1}, x_t] + b_o)$$

: **펍홀 변형** – cell state 의 제어를
보다 용이하게한 구조



$$C_t = f_t * C_{t-1} + (1 - f_t) * \tilde{C}_t$$

: **merge input / forget gate 변형**



$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$

$$r_t = \sigma(W_r \cdot [h_{t-1}, x_t])$$

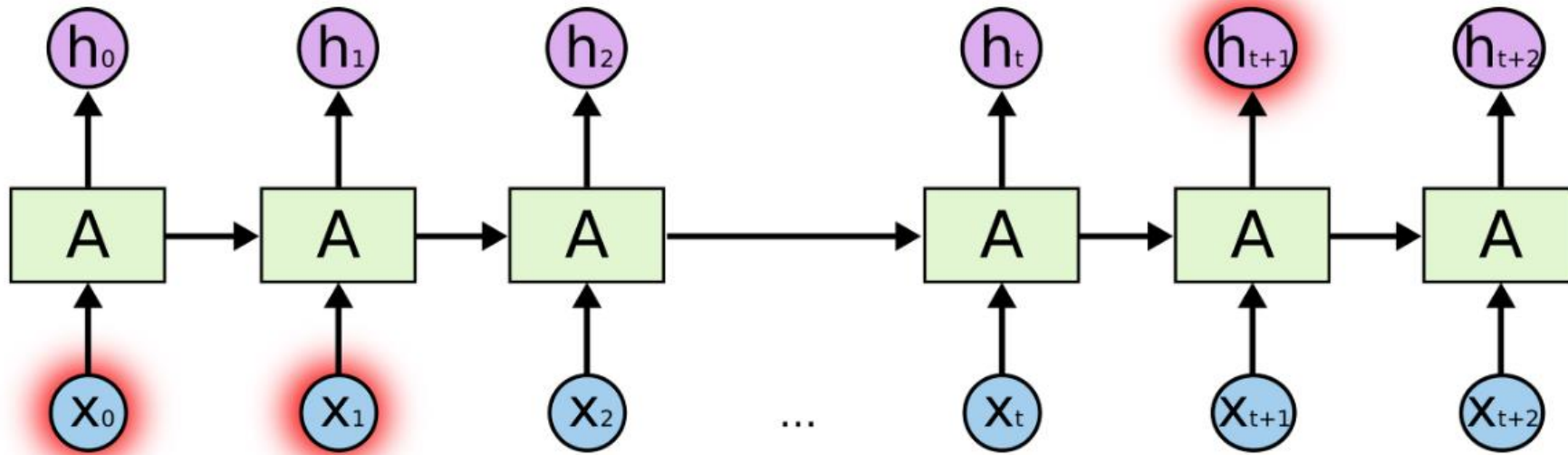
$$\tilde{h}_t = \tanh(W \cdot [r_t * h_{t-1}, x_t])$$

$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$

: **GRU 변형** – reset / update gate 만
을 사용한 간소화

LSTM

RNN 의 문제점 : Gradient Vanishing 문제로 장기간에 걸친 시간의존성은 학습시킬 수 없다.



Long Short Term Memory : 장시간에 걸친 시간 의존성, 단기간에 걸친 시간의존성 모두를 학습시킬 수 있는 기법.

LSTM

<https://github.com/heartcored98/Standalone-DeepLearning/blob/master/Lec8/Lec8-A.pdf>

Long Short Term Memory Network

1. C_{t-1} 에서 불필요한 정보를 지운다. $f_t = \sigma(W_f \cdot [h_{t-1}, x_t] + b_f)$
2. C_{t-1} 에 새로운 인풋 x_t 와 h_{t-1} 를 보고 중요한 정보를 넣는다. $i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i)$
3. 위 과정을 통해 C_t 를 만든다. $\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$
4. C_t 를 적절히 가공해 해당 t 에서의 h_t 를 만든다. $C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$
5. C_t 와 h_t 를 다음 스텝 $t+1$ 로 전달한다. $o_t = \sigma(W_o [h_{t-1}, x_t] + b_o)$
 $h_t = o_t * \tanh(C_t)$

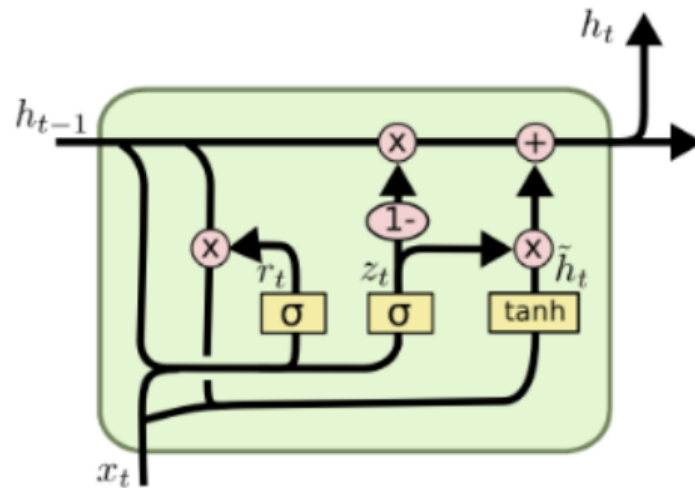
뭔가 너무 중복되는 느낌..?

→ 더 간단하게 forget gate, input gate, output gate를 해결 할 수는 없을까?

GRU

<https://github.com/heartcored98/Standalone-DeepLearning/blob/master/Lec8/Lec8-A.pdf>

Gated Recurrent Unit (GRU)



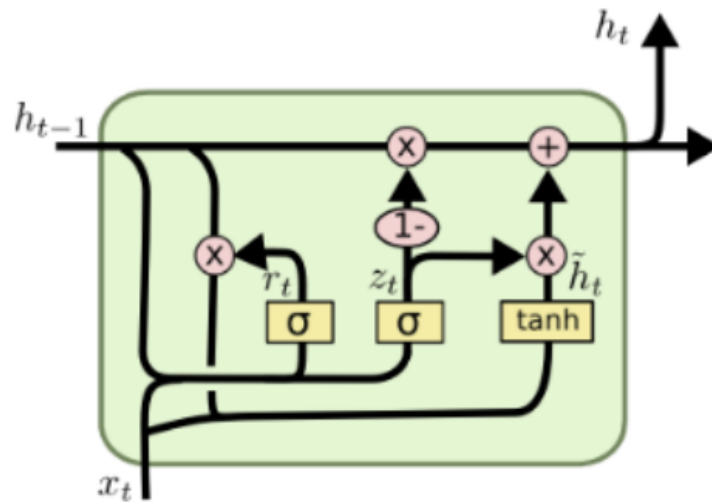
$$r_t = \sigma(W_r \cdot [h_{t-1}, x_t])$$

$$\tilde{h}_t = \tanh(W \cdot [r_t * h_{t-1}, x_t])$$

1. Reset gate를 계산해서 임시 h_t 를 만든다.

GRU

<https://github.com/heartcored98/Standalone-DeepLearning/blob/master/Lec8/Lec8-A.pdf>

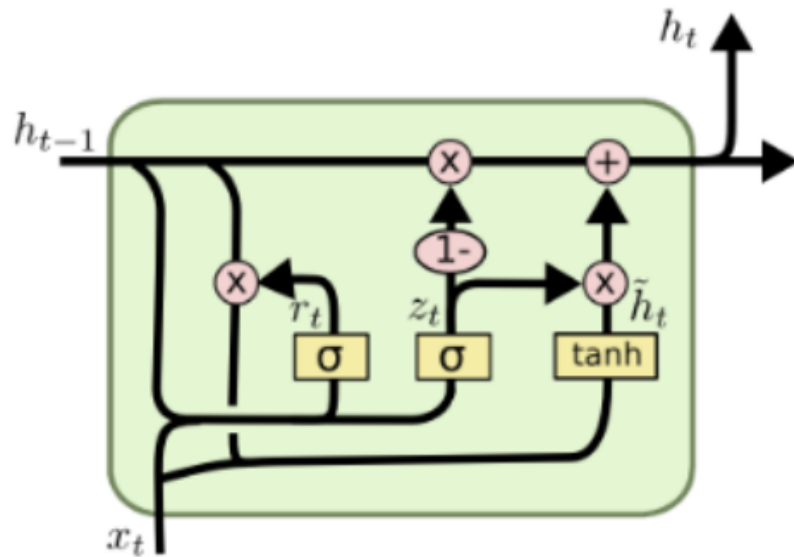


$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$

2. Update gate를 통해 h_{t-1} 과 h_t 간의 비중을 결정한다.

GRU

<https://github.com/heartcored98/Standalone-DeepLearning/blob/master/Lec8/Lec8-A.pdf>

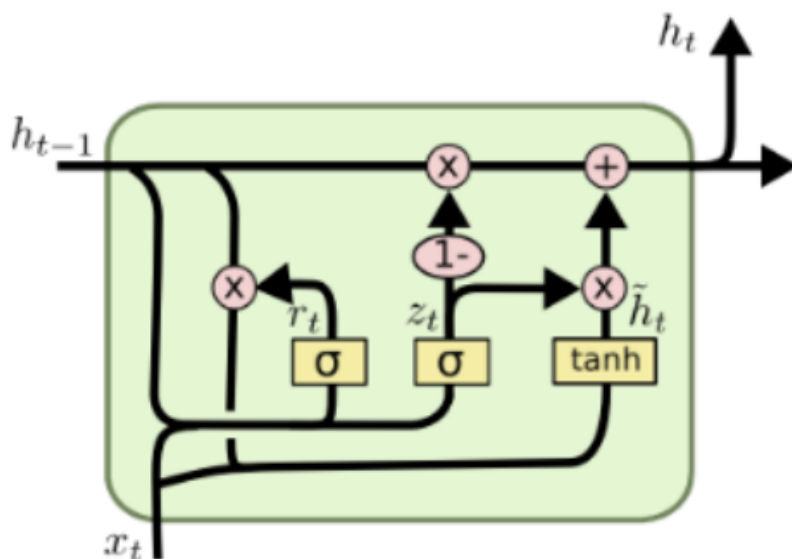


$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$

3. z_t 를 이용해 최종 h_t 를 계산한다.

GRU

<https://github.com/heartcored98/Standalone-DeepLearning/blob/master/Lec8/Lec8-A.pdf>



$$r_t = \sigma(W_r \cdot [h_{t-1}, x_t])$$

$$\tilde{h}_t = \tanh(W \cdot [r_t * h_{t-1}, x_t])$$

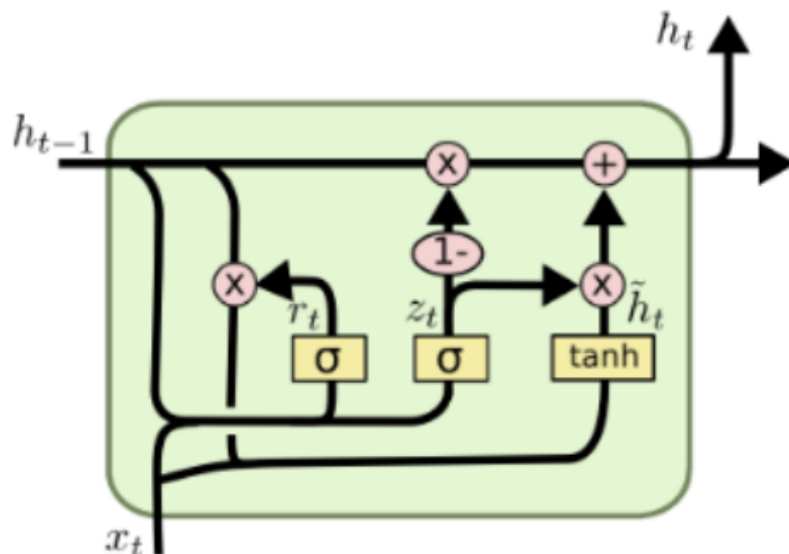
$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$

$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$

1. Reset gate를 계산해서 임시 h_t 를 만든다.
2. Update gate를 통해 h_{t-1} 과 h_t 간의 비중을 결정한다.
3. z_t 를 이용해 최종 h_t 를 계산한다.

GRU

<https://github.com/heartcored98/Standalone-DeepLearning/blob/master/Lec8/Lec8-A.pdf>



$$r_t = \sigma(W_r \cdot [h_{t-1}, x_t])$$

$$\tilde{h}_t = \tanh(W \cdot [r_t * h_{t-1}, x_t])$$

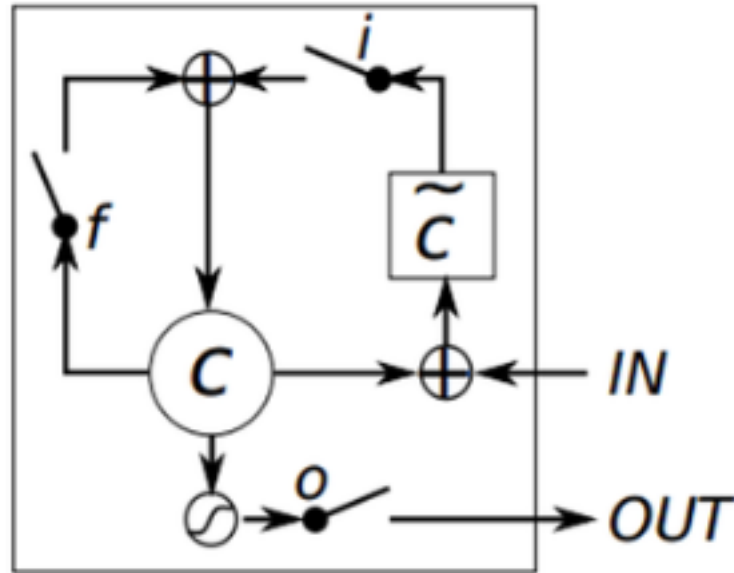
$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$

$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$

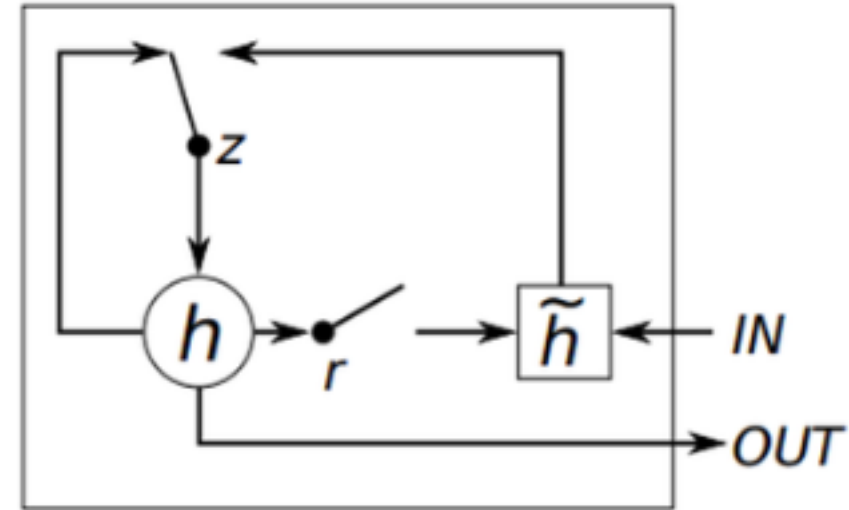
1. Reset gate를 계산해서 임시 h_t 를 만든다.
2. Update gate를 통해 h_{t-1} 과 h_t 간의 비중을 결정한다.
3. z_t 를 이용해 최종 h_t 를 계산한다.

GRU

<https://jay.tech.blog/2016/12/08/lstm-long-short-term-memory-rnn/>



(a) Long Short-Term Memory



(b) Gated Recurrent Unit

$$\begin{aligned}
 z &= \sigma(x_t U^z + s_{t-1} W^z) \\
 r &= \sigma(x_t U^r + s_{t-1} W^r) \\
 h &= \tanh(x_t U^h + (s_{t-1} \circ r) W^h) \\
 s_t &= (1 - z) \circ h + z \circ s_{t-1}
 \end{aligned}$$

$$h_t^j = (1 - z_t^j) h_{t-1}^j + z_t^j \tilde{h}_t^j,$$

Reference

<https://towardsdatascience.com/animated-rnn-lstm-and-gru-ef124d06cf45>
<https://excelsior-cjh.tistory.com/185>

- *Thank you*