

$$x_1 = 0.5 \text{ m}$$

$$f = 40 \text{ Hz}$$

$$A = 0.25 \text{ m}$$

$$\mu = 0.02 \text{ kg/m}$$

$$T = 20.48 \text{ N}$$

Displacement of

piece at  $x_1$  @  $t=0$  if piece @  $x=0$  is moving a

$$\omega = 2\pi f = 2\pi \cdot 40 = 80\pi$$

$$k = \frac{2\pi}{0.8} = \frac{2\pi}{4/5} = \frac{5\pi}{2}$$

$$y(x,t) = 0.25 \cos\left(\frac{5\pi}{2}x - 80\pi t\right)$$

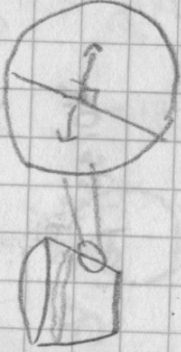
$$y(0.5 \text{ m}, 0) = 0.25 \cos\left(\frac{5\pi}{4}\right) = 0.25 \left(\cos\left(\frac{\sqrt{2}}{2}\right)\right) = -\frac{\sqrt{2}}{8} \approx -0.1767$$

$$k = \frac{2\pi}{\lambda} \quad v = \sqrt{\frac{20.48}{0.02}} = 32 \text{ m/s}$$

$$32 \text{ m/s} = \lambda f \quad \lambda = 0.8 \text{ m}$$

## Lecture 28: Fluid Statics

Pressure due to liquid or gas:



Forces are caused by the movement + collisions of molecules.

Pressure is the Force per unit area due to these collisions.

$$P = \frac{F_{\text{avg}}}{\text{Area}}$$

Think like this: The pressure @ some depth is due to the weight of everything above that depth.



$$P_2 - P_1 = \rho g h$$

$$P_2 = P_1 + \rho g h$$

the pressure at the same depth is the same.

Ex:



Equal height and surface area. What are the comparative magnitudes of the net force due to water?

$$F_A = F_B$$

Atmospheric Pressure: The weight of the atmosphere.

$$P_{\text{atm}} = 1 \times 10^5 \text{ N/m}^2 = 14.7 \text{ lbs/in}^2$$

$$\text{Ex: sphere w/ } r = 0.1 \text{ m}$$

$$A = 4\pi r^2 = 0.125 \text{ m}^2 \rightarrow F = 12,000 \text{ N (over 2500 lbs)}$$

Ex: Can you drink through a straw 40 feet long? No, because  $P = P_{\text{atm}}$  for 10' of water.

$P_1 = P_2 = \rho g h$ , so you would need pressure greater than  $P_{\text{atm}}$ , not possible naturally.

HW 27

2)  $\mu = 2 \times 10^{-4} \text{ kg/m}$   $L = 1.09 \text{ m}$   $T = 103.5 \text{ N}$

a)  $v_{\text{propagation}} = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{103.5}{2 \times 10^{-4}}} \approx 719 \text{ m/s}$

b) Fundamental frequency?

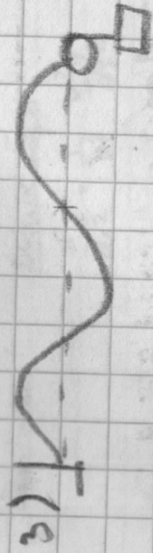
$$v = 2f$$

$$\rightarrow 719 = 2L \cdot f = 2 \cdot 1.8 f \quad f \approx 329.988 \text{ Hz}$$

c) Finger placed 0.172 m from top of guitar. Fundamental f?

$$719 = 2(L - 0.172) f = 2(0.918 \text{ m}) f$$

$$f = 391.6 \text{ Hz}$$



$$\mu = 3 \times 10^{-4} \text{ kg/m}$$

$$f = 66 \text{ Hz}$$

$$L = 0.56 \text{ m}$$

a) Wavelength?

$$L \times \frac{2}{3} = 0.56 \text{ m} \cdot \frac{2}{3} = 0.373 \text{ m}$$

$$b) v = \lambda f$$

$$= 0.373 \cdot 66 = 24.64 \text{ m/s}$$

c)

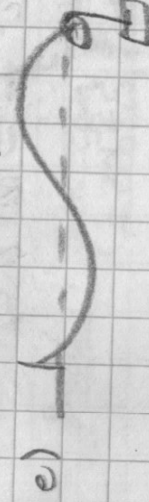
$$24.64^2 = \frac{T}{\mu}$$

$$T = 607.1296 = 3 \times 10^{-4}$$

$$= 0.182 \text{ N}$$

d)  $mg = T$

$$(m = 0.018566544 \text{ kg})$$



f remains 66 Hz, only mass adjusted.

Wavelength?  $L = 0.56 \text{ m}$

f)

$$v = \lambda f = 0.56 \cdot 66 = 36.96 \text{ m/s}$$

g)  $(36.96)^2 = \frac{T}{\mu}$

$$T = 0.4098 \text{ N}$$

h)  $T = mg$

$$m \approx 0.0418 \text{ kg}$$

i) Max  $m$  for coherent standing wave?

$$\lambda = 2L$$

$$v = 0.7392 \text{ m/s} \rightarrow T \approx 1.639 \text{ N}$$

$$m \approx 0.1671 \text{ kg}$$