

Checkpoint:

3 frets

Is it possible to place fingers on the frets to have the lowest string have the same frequency as the highest?
No $v = 2f$

speed of high string is 4x low. Mass unit density $\mu = ?$

$$v^2 = \frac{T}{\mu} \rightarrow \mu = \frac{T}{v^2} \quad \mu_H = \frac{T}{16v^2} \quad \mu_L = \frac{T}{v^2}$$

$$\frac{\mu_H}{\mu_L} = \frac{T/16v^2}{T/v^2} = \frac{1}{16}$$

$$\mu_L = 16\mu_H$$

so $d_{low} = 4 \cdot d_{high}$

$$M = \mu v = \mu L \pi r^2$$

Homework 26

3) $m = 0.86 \text{ kg}$
 $A = 0.2 \text{ m}$

$L_{stretched} = 7.9 \text{ m}$
 $t_{length} = 0.4625$
 $f = 0.45 \text{ Hz}$

a) v wave?

$$7.9 / 0.462 \approx 17 \text{ m/s}$$

b) Tension?
stinky.

$$v = \sqrt{\frac{T}{\mu}}$$

c) Average speed of a piece of stinky:

$$v^2 \mu = T \quad T = 17^2 \cdot 0.86 \text{ kg} / 7.9 \text{ m} \approx 31.8 \text{ N}$$

Distance in period: μ_{IA} $\mu_A = 0.8 \text{ m}$
period $P = \frac{1}{f} \approx 2.2 \text{ s}$

$$\text{speed} = \frac{0.8}{2.2} = 0.36 \text{ m/s}$$

d) wavelength? $v = 2f$

$$17 = \lambda (0.45) \quad \lambda \approx 38 \text{ m}$$

e) stretched to 2L. New tension.

$$F = kx$$

$$\frac{31.8}{7.9} = k$$

$$k = 4.025$$

$$F = 4.025 (7.9 \cdot 2) = 63.6 \text{ N}$$

f) New mass density? $\mu = 0.86 \text{ kg} / 5.8 \text{ m}$

g) new time to travel down stinky? 5.8 m

$$v = \sqrt{\frac{T}{\mu}} = \sqrt{\frac{63.6 \text{ N}}{0.054}} \approx 34.18 \text{ m/s}$$

$$\frac{15.8 \text{ m}}{34.18} \approx 0.46 \text{ s}$$

h) wavelength if f is the same?

$$34.18 = 2 (0.45) \quad \lambda = 75.96$$