LAPORAN TUGAS KECIL II

Penyelesaian Persoalan 15-Puzzle dengan Algoritma Branch and Bound

Laporan dibuat untuk memenuhi salah satu tugas mata kuliah IF2211 Strategi Algoritma



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Algoritma Branch and Bound

Pada kasus ini digunakan algoritma branch and bound yang berbasis BFS dengan struktur data penyimpan berupa priority queue. Priority queue yang dibuat adalah berdasarkan nilai cost function terkecil. Cost function didefinisikan sebagai berikut

$$\hat{c}(i) = \hat{f}(i) + \hat{g}(i)$$

 $\hat{c}(i)$ = ongkos untuk simpul i

 $\hat{f}(i)$ = ongkos mencapai simpul i dari akar

 $\hat{g}(i)$ = ongkos mencapai simpul tujuan dari simpul i.

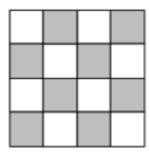
Algoritma ini terdiri dari beberapa bagian

1. Pembuatan Priority Queue

Pada program ini, priority queue diimplementasikan sendiri tanpa menggunakan fitur bawaan python. Implementasi priority queue ini dilakukan dengan memodifikasi struktur data List pada python. Pada program dibuat sebuah class PriorityQueue yang memiliki atribut List queue dan Integer count. Kemudian priority queue diimplementasikan pada member function insert, dimana setelah data dimasukkan ke List queue, List tersebut kemudian di sort sesuai prioritas. Prioritas pada priority queue ini adalah nilai cost terendah diikuti nilai jarak dari akar terendah. Selain itu terdapat pula member function pop, isEmpty, length, dan simpulCount.

2. Menghitung jumlah hasil fungsi Kurang(i) tiap ubin+X

Nilai jumlah Kurang(i) tiap ubin+X ini dapat digunakan untuk mengecek apakah puzzle mungkin untuk diselesaikan atau tidak tanpa mencari kemungkinan yang ada. Kurang(i) didefinisikan sebagai banyaknya ubin bernomor j sedemikian sehingga j < i dan Posisi(j) > Posisi(i), dimana Posisi(i) = posisi ubin bernomor i pada susunan yang diperiksa. Sementara itu X bernilai satu apabila sel kosong terletak pada ubin yang diarsir pada gambar berikut.



Apabila sel kosong tidak pada ubin yang diarsir, maka X bernilai nol.

Setelah didapatkan jumlah Kurang(i)+X, maka dapat diambil kesimpulan puzzle dapat diselesaikan apabila nilai nya genap. Apabila ganjil maka ubin tidak dapat diselesaikan.

3. Pembangkitan simpul

Dari state saat ini, simpul dapat dibangkitkan dengan membuat kemungkinan state apabila puzzle digerakkan ke atas, bawah, kanan, dan kiri ditambah aturan simpul yang baru dibangkitkan ini belum pernah dicek atau dibangkitkan sebelumnya. Dengan tambahan aturan ini dapat dipastikan bahwa puzzle tidak akan kembali ke state yang pernah dialami sebelumnya.

4. Menghitung cost simpul

Tiap simpul yang akan dibangkitkan ini harus dicari nilai cost function nya. Cost function dapat dihitung dengan menjumlahkan jarak simpul dari akar dengan jumlah ubin yang saat ini belum berada pada posisi akhir. Nilai cost function ini dimasukkan pada sebuah tuple yang sama dengan simpul untuk kemudian dimasukkan ke dalam priority queue.

5. Menjalankan algoritma untuk simpul berikutnya

Algoritma ini akan terus berjalan sampai priority kosong atau kondisi akhir telah terpenuhi. Penentuan simpul berikutnya yang akan dicek adalah dengan berdasarkan urutan pada priority queue, dimana simpul yang memiliki cost function terkecil akan diprioritaskan.

Kode Program

```
test.txt
main.py 2
                🕏 prioqueue.py 🗙
                                                  e bnb.py
🜓 prioqueue.py > ધ PriorityQueue > 🗘 insert
       def takeCost(elem):
           return elem[2],elem[1]
       class PriorityQueue(object):
           def init (self):
               self.queue = []
               self.count = 0
  10
           def str (self):
  11
               return ' '.join([str(i) for i in self.queue])
  12
           # for checking if the queue is empty
  13
  14
           def isEmpty(self):
               return len(self.queue) == 0
  15
  17
           def length(self):
               return len(self.queue)
  19
           def simpulCount(self):
  20
  21
               return self.count
  22
           # for inserting an element in the queue
  23
           def insert(self, data):
  24
               self.queue.append(data)
  25
  26
               self.queue.sort(key=takeCost)
               self.count += 1
  28
  29
           # for popping an element based on Priority
           def pop(self):
  32
               item = self.queue[0]
               del self.queue[0]
               return item
```

```
e bnb.py
🥏 main.py 2
               🕏 prioqueue.py
                                 test.txt
<code-block> bnb.py > 🛇 solve</code>
       import prioqueue
       import copy
       import time
       # state adalah tuple dengan urutan (array 15 puzzle, int distFromRoot, int cost, int idx parent di array done)
       def kurang(num, state):
           idx = -1
           for i in range(16):
               if state[0][i] == num:
                   idx = i
           count = 0
           for i in range(idx, 16):
               if state[0][i] != -1 and state[0][i] < num:
                   count += 1
           return count
       def sumKurang(state):
           count = 0
           for i in range(1, 17):
               count += kurang(i, state)
           return count
       def findX(state):
           shadowed = [1, 3, 4, 6, 9, 11, 12, 14]
           for i in range(1, 16):
               if state[0][i] == 16 and i in shadowed:
                   return 1
           return 0
       def kurangPlusX(state):
           return sumKurang(state) + findX(state)
```

```
test.txt
e main.py 2
                🕏 prioqueue.py
                                                   e bnb.py
                                                               ×
e bnb.py > 分 solve
           Tecuri Summurang(Scace) + Timum(Scace)
  38
  40
       def solvable(state):
           return kurangPlusX(state) % 2 == 0
  41
  42
  43
       def costFuncG(matrix):
  44
           count = 0
  45
           for i in range(16):
  46
                if matrix[i] != i + 1 and matrix[i]!=16:
  47
                    count += 1
  49
           return count
  50
  51
  52
       def move(state, direction):
           newMatrix = copy.deepcopy(state[0])
  54
           idx = -1
  55
           for i in range(16):
  56
                if newMatrix[i] == 16:
  57
  58
                    idx = i
  60
           idxTukar = -1
           if direction == "top":
  61
                if idx < 4:
  62
                    return newMatrix
  63
                idxTukar = idx - 4
  64
           elif direction == "bottom":
  65
                if idx > 11:
  66
                    return newMatrix
  67
  68
                idxTukar = idx + 4
           elif direction == "left":
                if idx % 4 == 0:
  70
  71
                    return newMatrix
                idxTukar = idx - 1
  72
  73
           elif direction == "right":
                if (idx + 1) \% 4 == 0:
  74
```

```
test.txt
e main.py 2
               prioqueue.py
                                                 e bnb.py
                                                             X
🥏 bnb.py > 🛇 solve
               if (idx + 1) \% 4 == 0:
                   return newMatrix
  75
  76
               idxTukar = idx + 1
  77
  78
           newMatrix[idx] = newMatrix[idxTukar]
           newMatrix[idxTukar] = 16
  79
           return newMatrix
  82
       def solve(initState, path, simpulTime):
           start = time.perf counter()
  84
           # Nilai fungsi Kurang(i) tiap ubin awal
           for i in range(1, 17):
               print("Kurang",i, kurang(i, initState))
           # Nilai sumKurang(i)+X
           print()
           print("sumKurang(i)+X =",kurangPlusX(initState))
           print()
           prioQueue = prioqueue.PriorityQueue()
           if solvable(initState) == False:
               print("Jumlah simpul dibangkitkan =", prioQueue.simpulCount())
               return False
 100
           prioQueue.insert(initState)
           allPath = []
           done = []
104
           inQueue = []
           while prioQueue.isEmpty()==False:
               currState = prioQueue.pop()
               done.append(currState[0])
               allPath.append(currState)
 110
```

```
e main.py 2
                🗬 prioqueue.py
                                  test.txt
                                                  e bnb.py
🥏 bnb.py > 🛇 solve
                if solvable(currState):
                    if (currState[1]==currState[2]):
                        path.insert(0, currState)
                        while path[0][3]!=-1:
                            path.insert(0, allPath[path[0][3]])
                        print("Here")
                        for i in range(len(path)):
                            print(path[i][0])
121
                        print()
                        print("Jumlah simpul dibangkitkan =", prioQueue.simpulCount())
                        print("Waktu =","{:.5f}".format(time.perf_counter()-start), "detik")
                        simpulTime.append(prioQueue.simpulCount())
                        simpulTime.append(time.perf_counter()-start)
                        return True
                    print(currState)
                    print(prioQueue.length())
                    newTop = move(currState, "top")
newBot = move(currState, "bottom")
                    newLeft = move(currState, "left")
                    newRight = move(currState, "right")
                    f = currState[1] + 1
                    gTop = costFuncG(newTop) if (newTop not in done) and (newTop not in inQueue) else -1
                    gBot = costFuncG(newBot) if (newBot not in done) and (newBot not in inQueue) else -1
                    gLeft = costFuncG(newLeft) if (newLeft not in done) and (newLeft not in inQueue) else -1
                    gRight = costFuncG(newRight) if (newRight not in done) and (newRight not in inQueue) else -1
                    if gTop != -1:
                        stateTop = (newTop, f, f + gTop, len(done)-1)
                        prioQueue.insert(stateTop)
                        inQueue.append(newTop)
                    if gBot != -1:
```

```
e main.py 2
                                  test.txt
                prioqueue.py
                                                  e bnb.py
                                                              ×
🥏 bnb.py > 🛇 solve
                        stateBot = (newBot, f, f + gBot, len(done)-1)
                        prioQueue.insert(stateBot)
                        inQueue.append(newBot)
 149
 150
                    if gLeft -1:
                        stateLeft = (newLeft, f, f + gLeft,len(done)-1)
                        prioQueue.insert(stateLeft)
 152
                        inQueue.append(newLeft)
                    if gRight != -1:
 154
                        stateRight = (newRight, f, f + gRight,len(done)-1)
 156
                        prioQueue.insert(stateRight)
                        inQueue.append(newRight)
           print("Unknown Error")
 158
```

```
🕏 main.py 2 🗙 🥏 prioqueue.py
                                                                 test.txt
                                                                                                  🕏 bnb.py
import sys
              import os
              from PySide6 import (QtCore, QtWidgets, QtGui)
             class MyWidget(QtWidgets.QWidget):
    def __init__(self):
                             super().__init__()
                             self.path = []
self.isSolvable = False
                             self.initState = ()
                             self.button = QtWidgets.QPushButton("Start!")
self.text = QtWidgets.QLabel("Masukkan kondisi awal pada tabel. Cell kosong direpresentasikan dengan angka 16. Asumsi input benar.
Apabila solvable, pencet button start lagi untuk menunjukkan step")
self.table = QtWidgets.QTableWidget()
self.status = QtWidgets.QLabel("Status: Not Started")
self.result = QtWidgets.QTextEdit("")
self.rand = QtWidgets.QPushButton("Randomize!")
self.file = QtWidgets.QFileDialog(filter="Text files (*.txt)")
                              self.table.setRowCount(4)
                              self.table.setColumnCount(4)
                              self.result.setReadOnly(True)
                              layout = QtWidgets.QVBoxLayout(self)
                             layout = Qthidgets.QVBoxLayout
layout.addWidget(self.text)
layout.addWidget(self.texton)
layout.addWidget(self.status)
layout.addWidget(self.result)
layout.addWidget(self.table)
layout.addWidget(self.rand)
layout.addWidget(self.file)
```

```
test.txt
🗬 main.py
               🗬 prioqueue.py
                                                 e bnb.py
🗬 main.py > 😭 MyWidget
               self.button.clicked.connect(self.magic) # type: ignore
               self.rand.clicked.connect(self.randomizer) # type: ignore
  38
           def getTable(self):
               matrix = []
               matrix.append(int(self.table.item(0,0).text()))
               matrix.append(int(self.table.item(0,1).text()))
               matrix.append(int(self.table.item(0,2).text()))
               matrix.append(int(self.table.item(0,3).text()))
               matrix.append(int(self.table.item(1,0).text()))
               matrix.append(int(self.table.item(1,1).text()))
               matrix.append(int(self.table.item(1,2).text()))
               matrix.append(int(self.table.item(1,3).text()))
               matrix.append(int(self.table.item(2,0).text()))
               matrix.append(int(self.table.item(2,1).text()))
               matrix.append(int(self.table.item(2,2).text()))
               matrix.append(int(self.table.item(2,3).text()))
               matrix.append(int(self.table.item(3,0).text()))
               matrix.append(int(self.table.item(3,1).text()))
               matrix.append(int(self.table.item(3,2).text()))
               matrix.append(int(self.table.item(3,3).text()))
               return matrix
           def setTable(self, matrix):
               print(matrix)
               self.table.setItem(0,0,QtWidgets.QTableWidgetItem(str(matrix[0])))
               self.table.setItem(0,1,QtWidgets.QTableWidgetItem(str(matrix[1])))
               self.table.setItem(0,2,QtWidgets.QTableWidgetItem(str(matrix[2])))
 64
               self.table.setItem(0,3,QtWidgets.QTableWidgetItem(str(matrix[3])))
               self.table.setItem(1,0,QtWidgets.QTableWidgetItem(str(matrix[4])))
               self.table.setItem(1,1,QtWidgets.QTableWidgetItem(str(matrix[5])))
               self.table.setItem(1,2,QtWidgets.QTableWidgetItem(str(matrix[6])))
               self.table.setItem(1,3,QtWidgets.QTableWidgetItem(str(matrix[7])))
               self.table.setItem(2,0,QtWidgets.QTableWidgetItem(str(matrix[8])))
               self.table.setItem(2,1,QtWidgets.QTableWidgetItem(str(matrix[9])))
               self.table.setItem(2,2,QtWidgets.QTableWidgetItem(str(matrix[10])))
               self.table.setItem(2.3.OtWidgets.OTableWidgetItem(str(matrix[11])))
  73
```

```
🗙 📗 🥏 prioqueue.py
                                 test.txt
                                                 e bnb.py
🗬 main.py
🥏 main.py > ધ MyWidget
               self.table.setItem(2,3,QtWidgets.QTableWidgetItem(str(matrix[11])))
               self.table.setItem(3,0,QtWidgets.QTableWidgetItem(str(matrix[12])))
               self.table.setItem(3,1,QtWidgets.QTableWidgetItem(str(matrix[13])))
               self.table.setItem(3,2,QtWidgets.QTableWidgetItem(str(matrix[14])))
               self.table.setItem(3,3,QtWidgets.QTableWidgetItem(str(matrix[15])))
           def setTextBox(self):
               for i in range(1,17):
                   self.result.append("Kurang "+str(i)+ " = " +str(kurang(i, self.initState)))
               self.result.append("sumKurang(i)+X = "+ str(kurangPlusX(self.initState)))
           def openFile(self, fileName):
               matrix = []
               f = open(fileName, "r")
               for line in f:
                   matrix.append(int(line.strip('\n').strip()))
               f.close()
               return matrix
           @QtCore.Slot()
           def randomizer(self):
               matrix = random.sample(range(1,17), 16)
               self.setTable(matrix)
               self.initState = (matrix, 0, 0+costFuncG(matrix), -1)
           @QtCore.Slot()
           def magic(self):
               if self.isSolvable==False:
                   if self.initState == ():
                       matrix = []
                       if self.file.selectedFiles()[0]!=os.getcwd().replace('\\', '/'):
                           matrix = self.openFile(self.file.selectedFiles()[0])
105
                           self.setTable(matrix)
                       else:
                           matrix = self.getTable()
                       self.status.setText("Status: Processing")
```

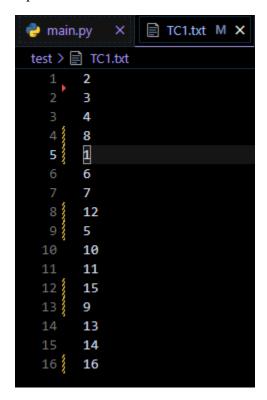
```
🕏 main.py 🗙 🏺 prioqueue.py
                                                             test.txt
                                                                                           e bnb.py
 nain.py > 😝 MyWidget
                                                 matrix = self.getTable()
                                           self.status.setText("Status: Processing")
                                           self.initState = (matrix, 0, 0+costFuncG(matrix), -1)
                                    self.setTextBox()
                                    self.isSolvable = solve(self.initState, self.path, self.arrSimpulTime)
self.status.setText("Status: " + ("Solvable with time "+"{:.5f}".format(self.arrSimpulTime[1]) + " seconds and simpul count " +
str(self.arrSimpulTime[0])) if self.isSolvable==True else "Unsolvable")
                                  str(self.arrSimpulTime[0])) if self.isSolvable==Int
if self.isSolvable==True:
    print("Time =", self.arrSimpulTime[1])
    print("Simpul count =", self.arrSimpulTime[0])
    self.result.append("\n Urutan path")
    for i in range(len(self.path)):
        self.result.append(str(self.path[i][0]))
        amint(self.path[i][0])
                                          print(self.path[i][0])
del self.path[0]
                            elif len(self.path)>0:
    self.setTable(self.path[0][0])
                                    del self.path[0]
             if __name__ == '__main__':
    app = QtWidgets.QApplication([])
                    widget = MyWidget()
widget.resize(800, 600)
                    widget.show()
                     sys.exit(app.exec())
```

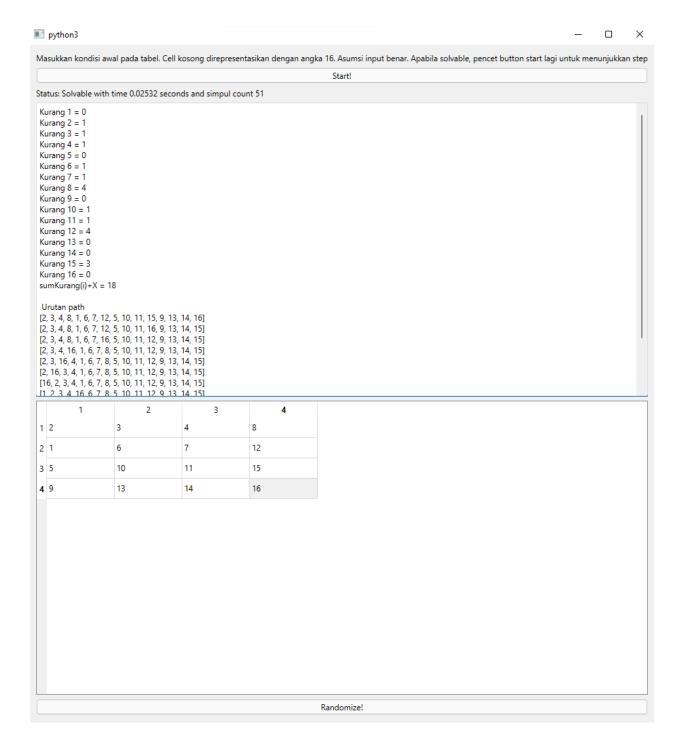
Screenshot Input - Output Program

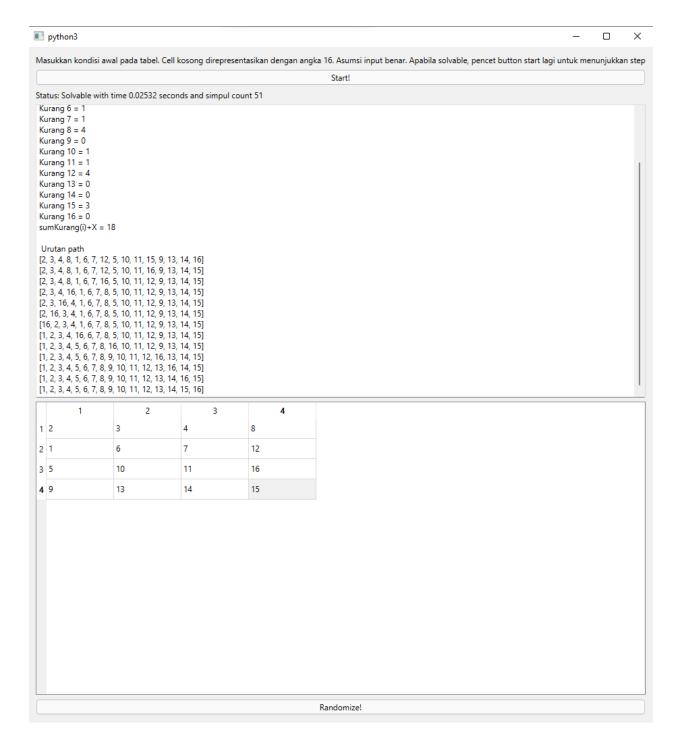
Perhatian: Dalam melakukan input, slot kosong direpresentasikan dengan angka 16

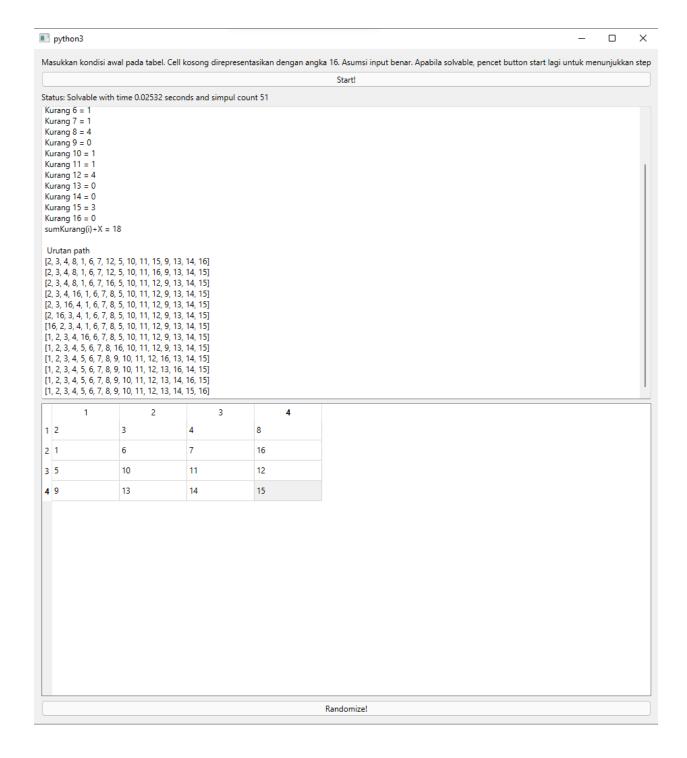
1. TC 1

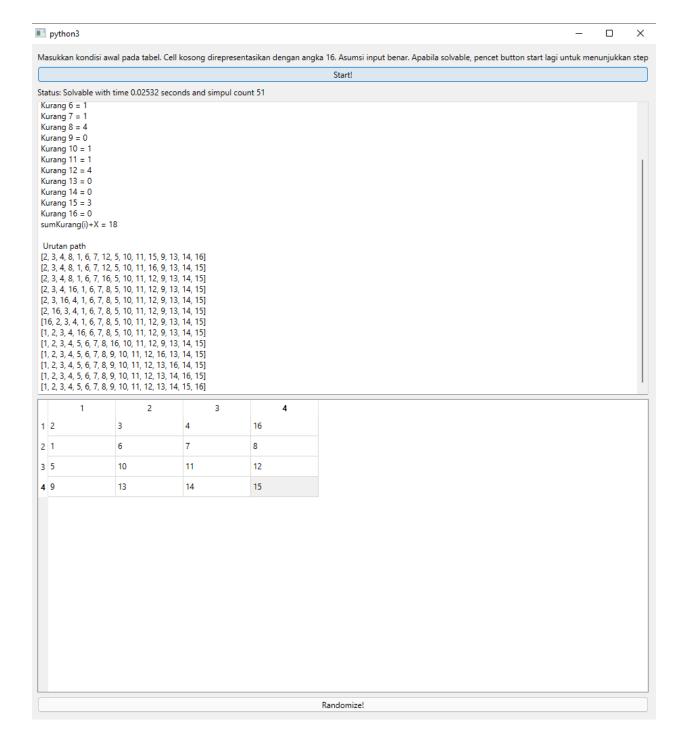
Input

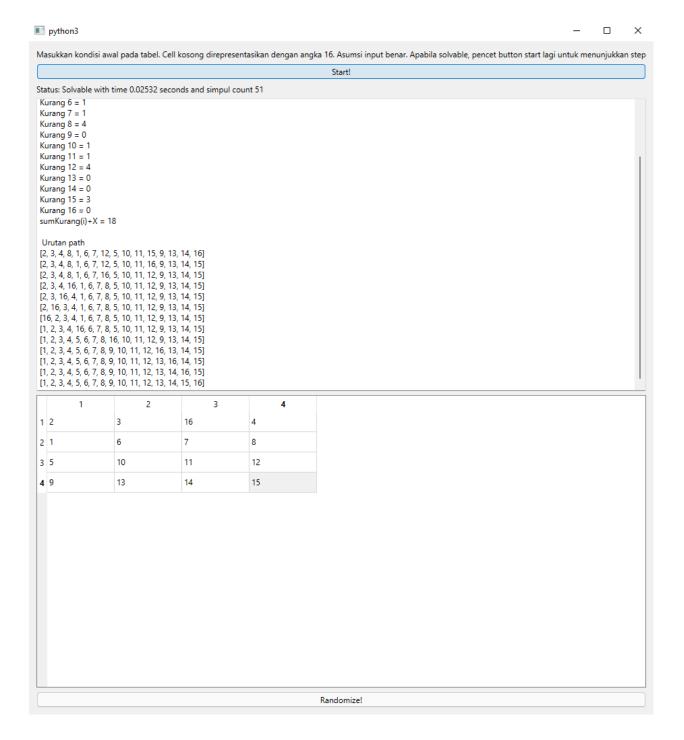


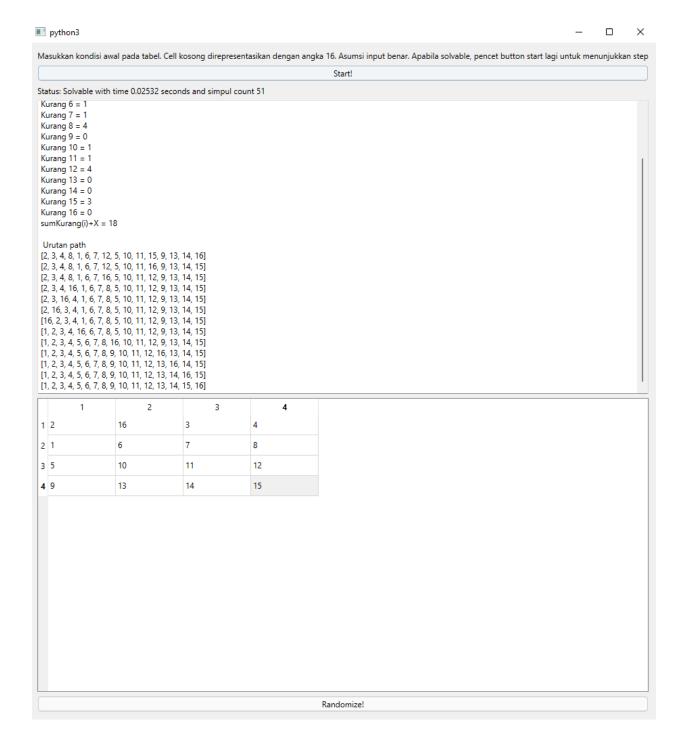


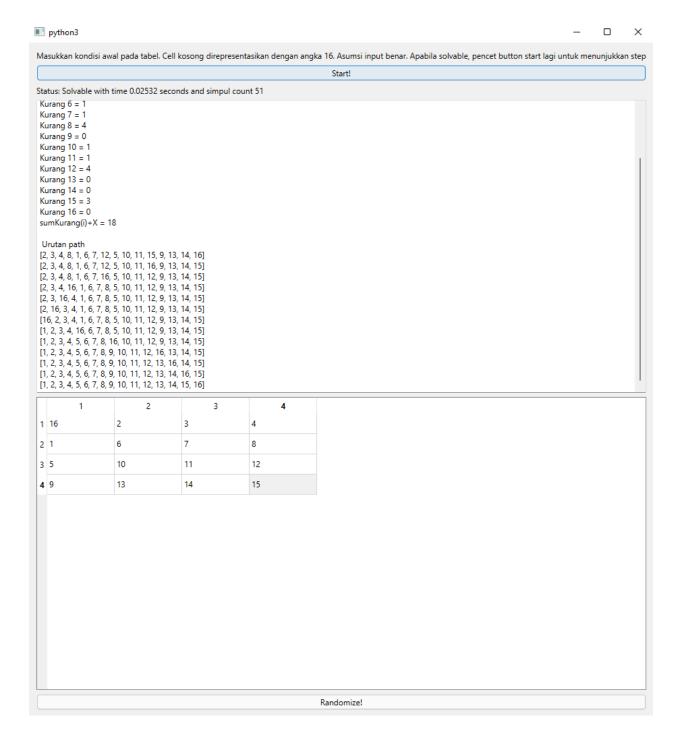


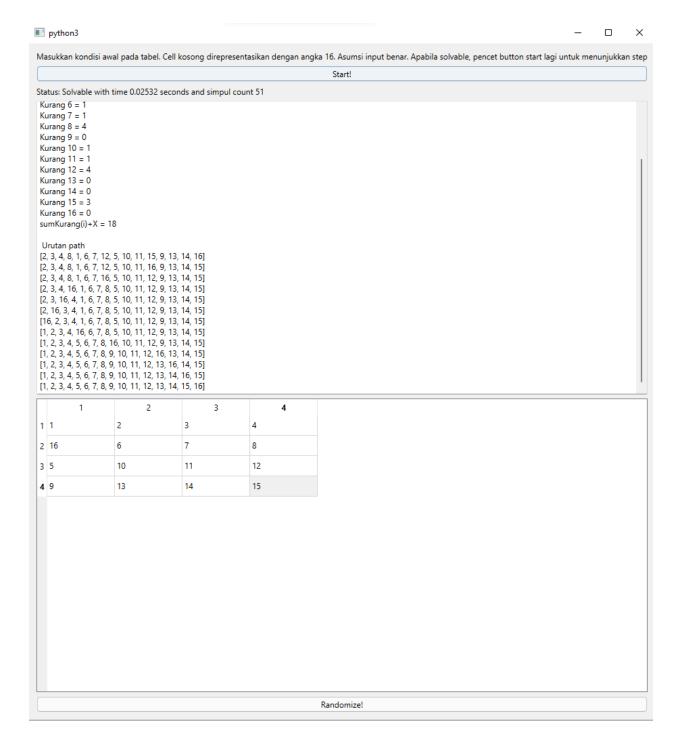


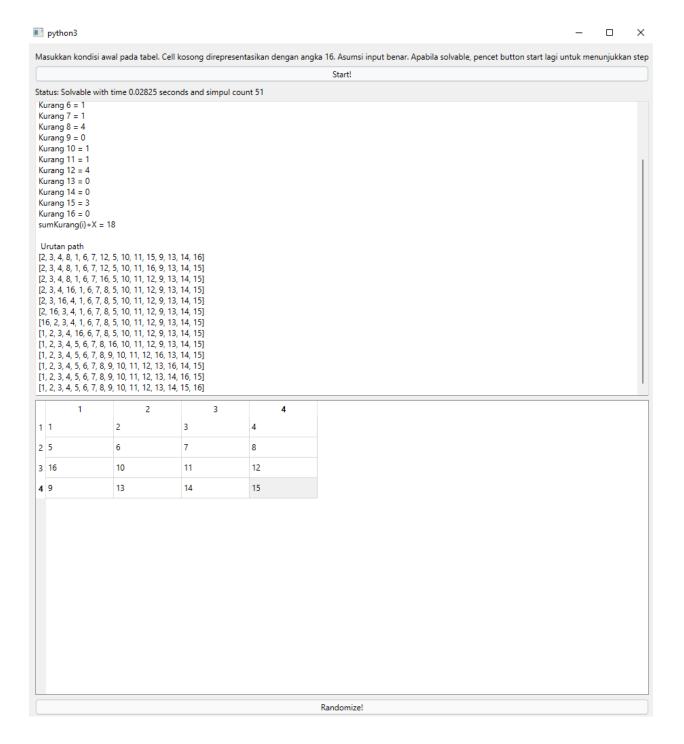


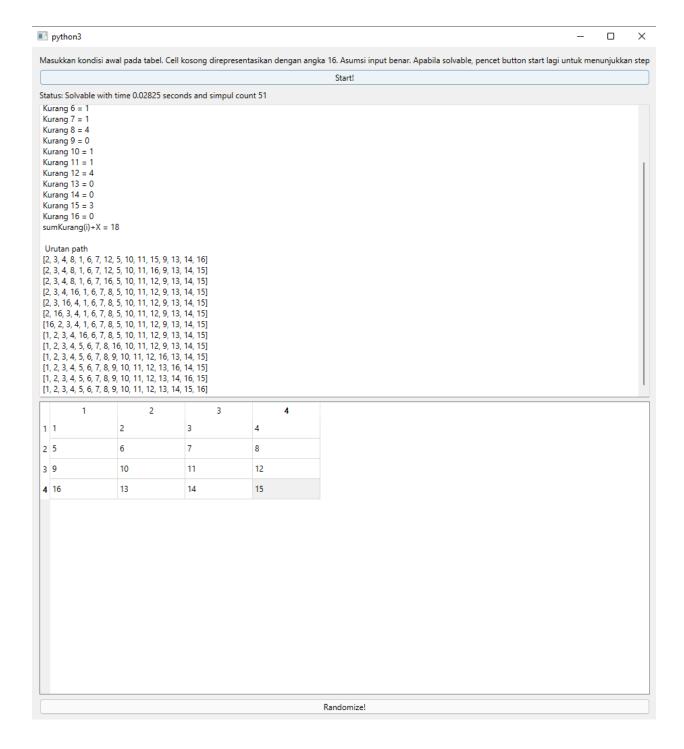


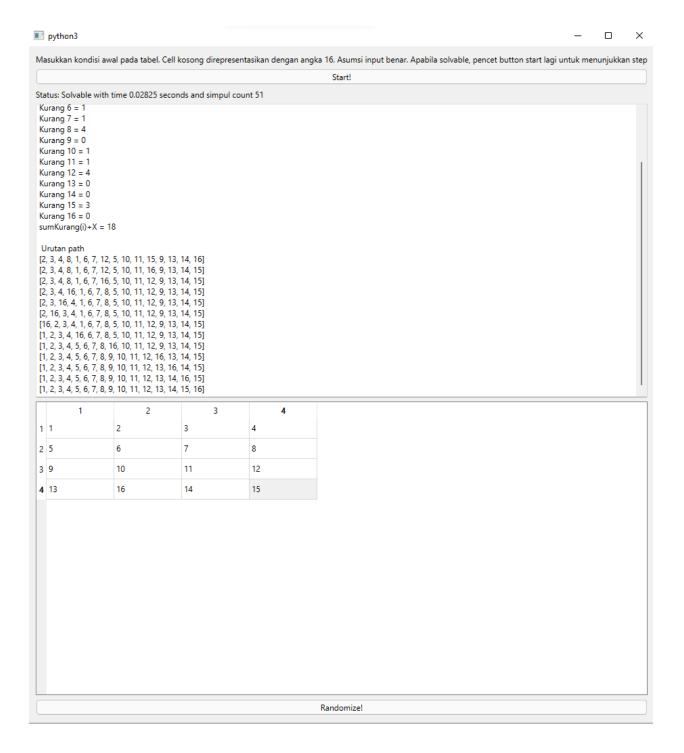


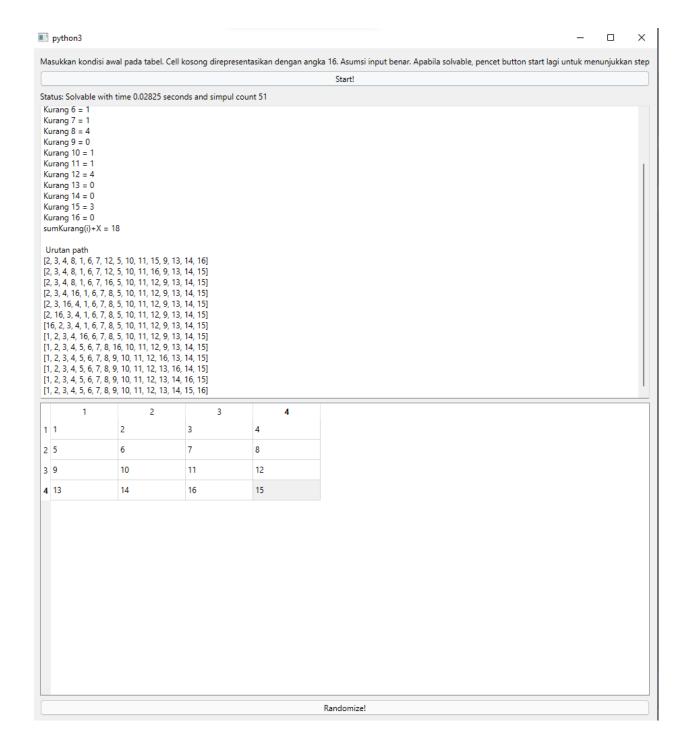


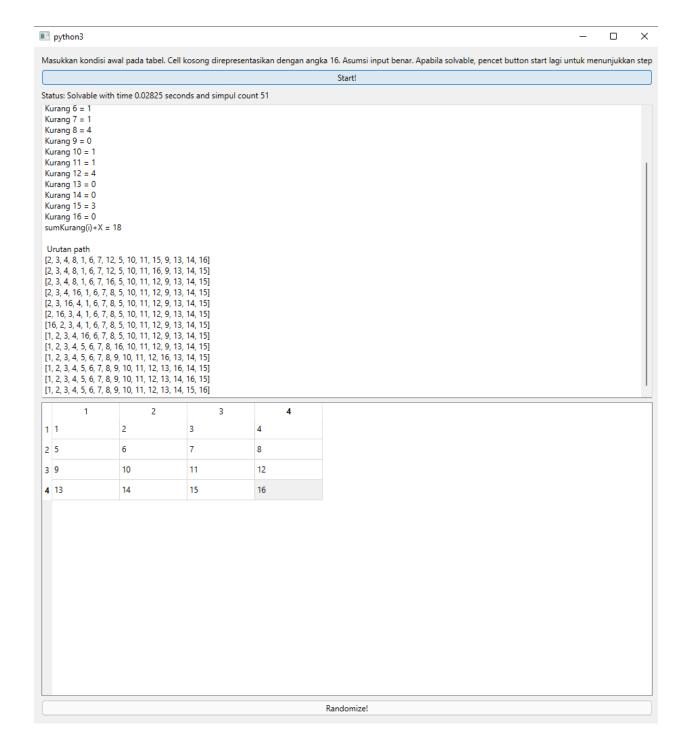






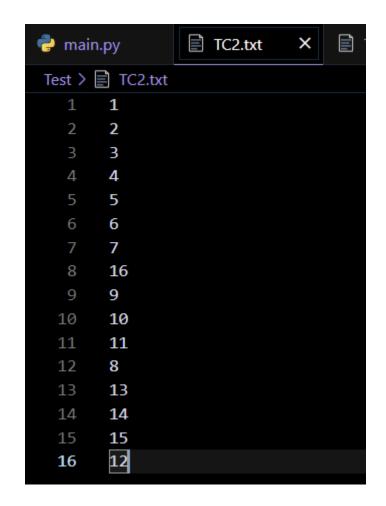


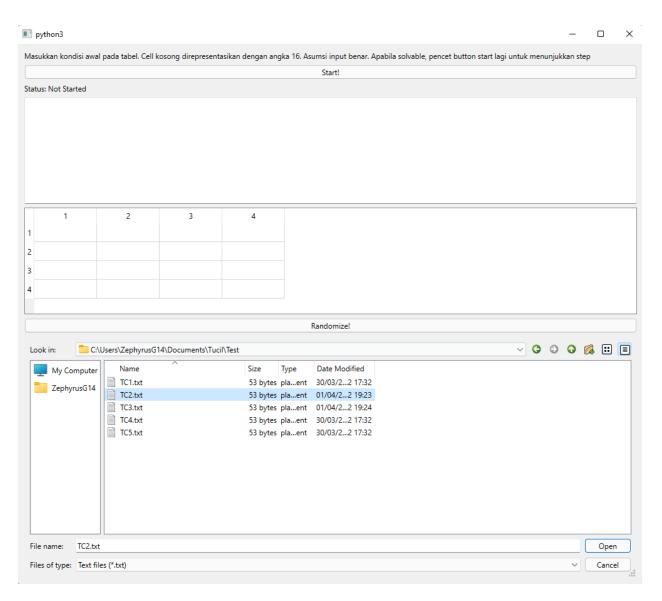


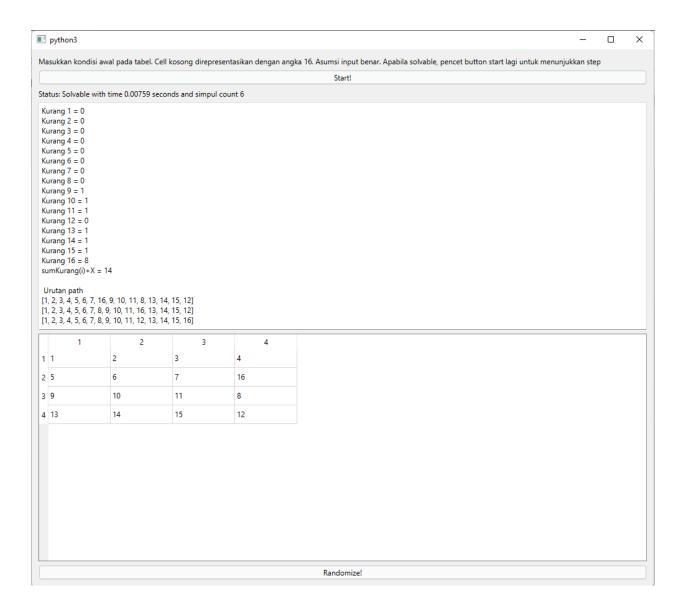


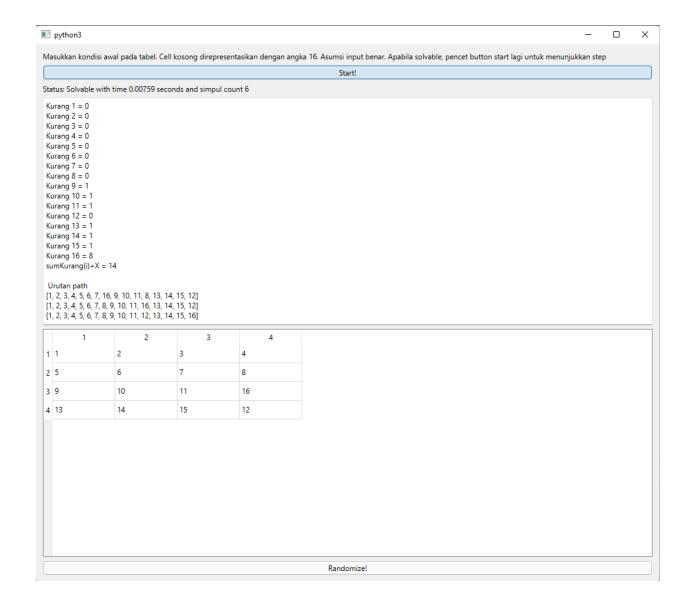
2. TC 2

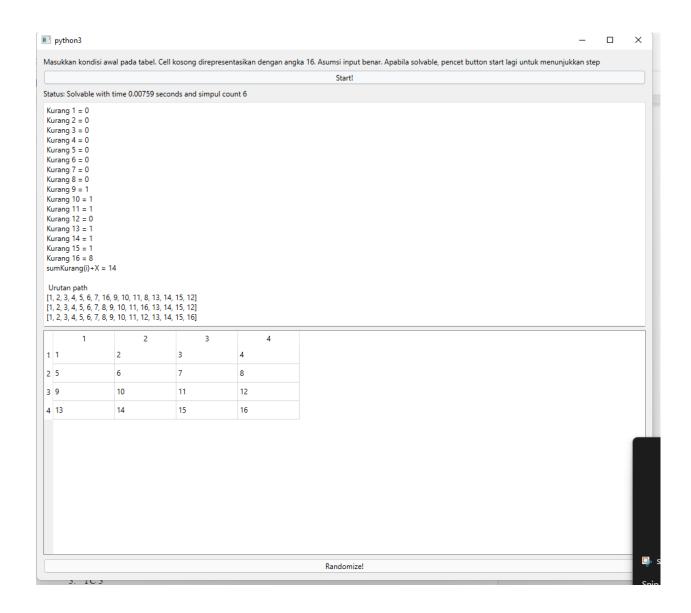
Input



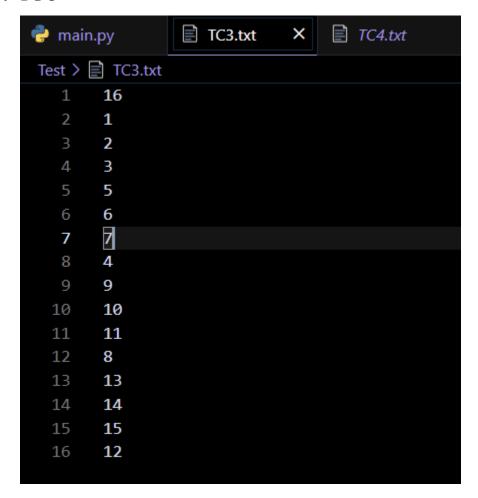






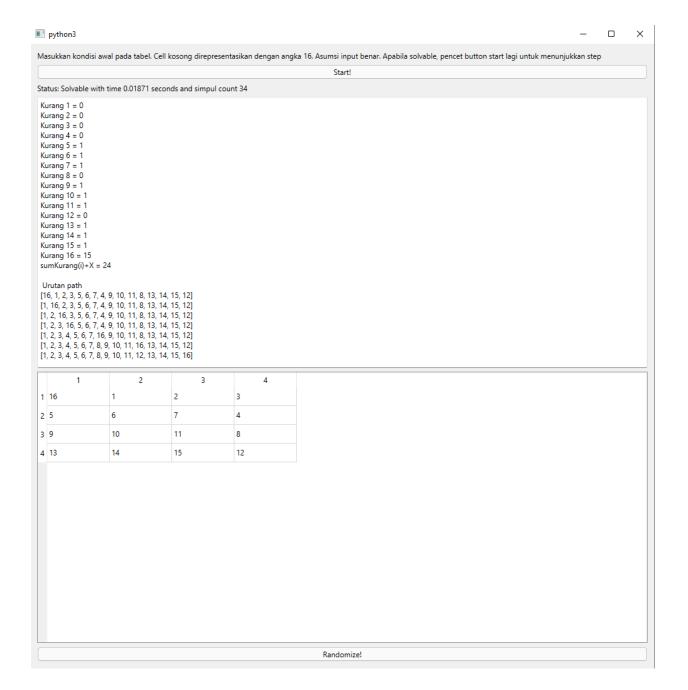


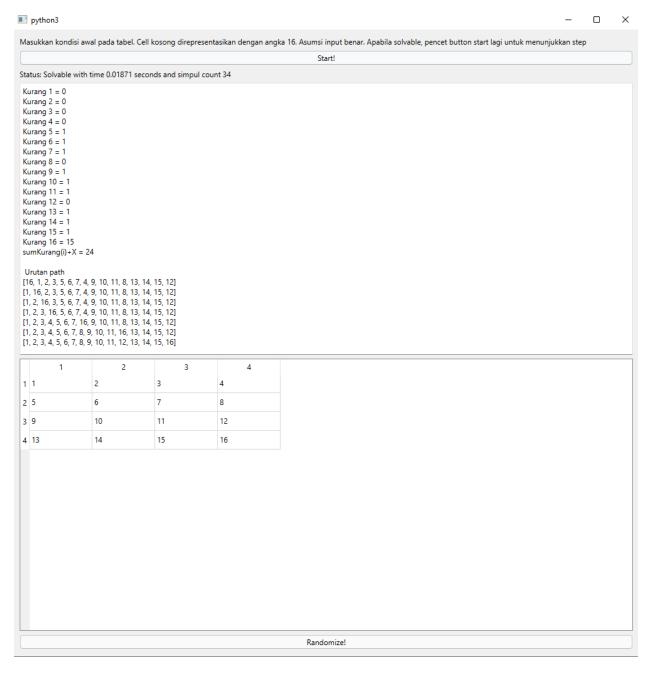
3. TC 3



Output

State awal

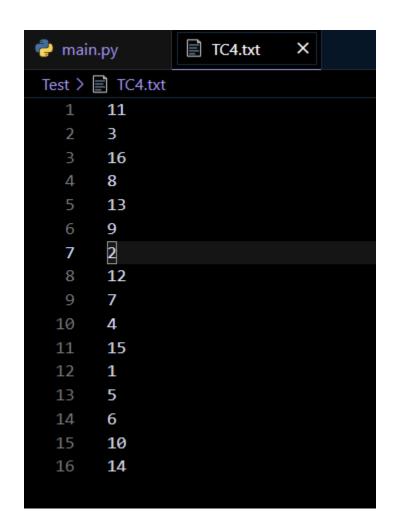


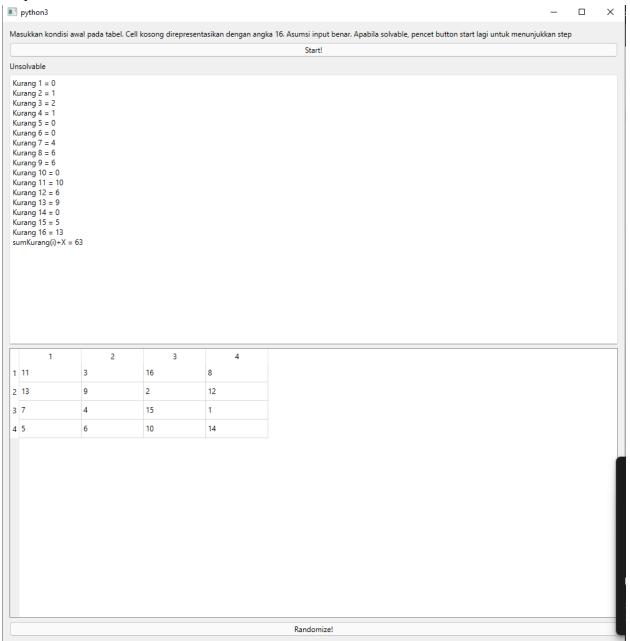


Mohon maaf tidak di screenshot semua karena cukup banyak

4. TC 4

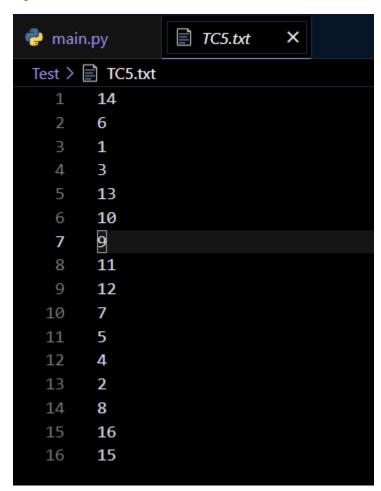
Input

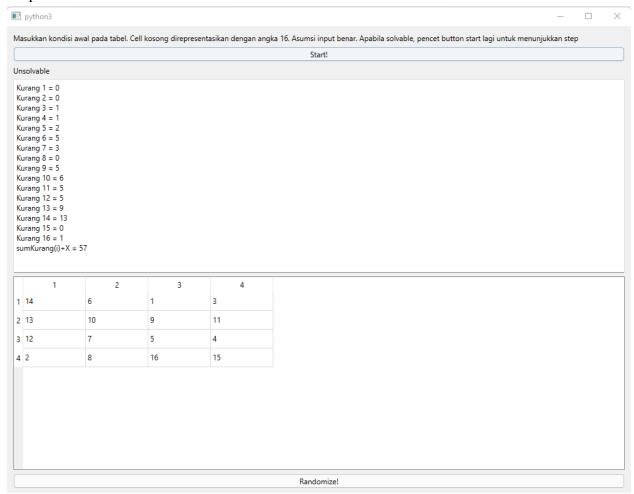




5. TC 5

Input





Link Kode Program

Repository Github: https://github.com/dParikesit/Tucil3 13520087

Checklist

Poin	Ya	Tidak
Program berhasil dikompilasi	~	
2. Program berhasil running	>	
3. Program dapat menerima input dan menuliskan output.	>	
4. Luaran sudah benar untuk semua data uji	~	
5. Bonus dibuat	V	

Daftar Referensi

1. https://informatika.stei.itb.ac.id/~rinaldi.munir/Stmik/2020-2021/Algoritma-Branch-and-Bound-2021-Bagian1.pdf