

prob1

December 16, 2015

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In [40]: import numpy as np
import matplotlib.pyplot as plt
%matplotlib inline

In [41]: # input data
X = np.array([[0,1],[0.5,2]])
y = np.array([2,5])

x_star = np.array([0.5, 1])

# squared exponential kernel function
def se(X):
    D = X[:, :, np.newaxis] - X.T
    return np.exp(-1/2*np.sum(D**2, axis=1))

In [42]: # compute the covariance matrix using the se-kernel function
Ka = se( np.concatenate((X,X_star),0) )

K = Ka[:2,:2]
K_star = Ka[:2,2]
K_starstar = Ka[2,2]

In [43]: print('K:')
print(K)
print()
print('K*:')
print(K_star)
print()
print('K**:')
print(K_starstar)

K:
[[ 1.          0.53526143]
 [ 0.53526143  1.          ]]

K*:
[ 0.8824969  0.60653066]

K**:
1.0

In [44]: # compute the mean expectation and the variance
mu = K_star.dot(np.linalg.inv(K)).dot(y)
var = K_starstar - K_star.dot( np.linalg.inv(K).dot(K_star) )
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In [45]: print('f*|f,X,X* ~ N(%f, %f)' % (mu, var))
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f*|f,X,X* ~ N(2.503884, 0.195971)
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In [ ]:
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