Synthetic Observations: Truth vs. Noisy Measurements