# Learning where to look for a target before seeing it

### \begin{abstract}

A realistic system for object categorization should be able to find the target in possibly large images, independently of its position in visual space. Current solutions leverage this solution by processing the different hypothesis (classes) at all possible spatial configuration. However, this can be costly in terms of computing time especially without dedicated parallel hardware. % We explore here a solution inspired by the anatomy of the human visual system, that is, the combination of a foveated sensor with the capacity of rapidly moving the center of fixation using saccades. Indeed, the position and category of objects in images are a priori independent and we hypothesize that the retinotopic map overlays a central area dedicated to object categorization and a peripheral area dedicated to

Using this hypothesis, we formalize this problem in a probabilistic setting which allows us to build two parallel but interactively connected system: a classical image classification algorithm assuming that gaze is centered on the object on one side and a system learning to infer the position of the target on the other. Until the classification is confident, the system performs a saccade to the most likely position in the image. Overall, the computational cost of this strategy is less than that in holistic methods. %

We tested this framework on a simple task of finding digits in a large, cluttered image. Results demonstrate that it is possible to correctly learn the position of a target from a given class, and this before actually seeing a foveated image of the target. We compare the results of this model with classical psychophysical results in visual search. This provides evidence of the importance of such strategies in computer vision and we highlight some predictions of our model. \end{abstract}

Nites:

Differential processing

periphery: low resolution in space

high in time

tovea: high spatial resolution

low tempor al

caccadic suppression

Ziad Hofeol: elevation of perceptual

Huresholds at the time of succeede

Joequency tuning in SC

Notes existantes 2017-09-28 mann -> papier fronties Coarse paripheny - Hermann grid? - Invariances sujet pienne 2018-03-15 - det niget / protocole des methode avec cante accurage

- onal

2018-12-21 - outline paper - Higures , yaka

# hat of

# 1 Introduction

## 1.1 Issue

### 1.2 State of the art

### 1.3 Outline

### 1.3.1 Notations

• x: visual field (image)

 $\bullet$  y: target category (categorical)

ullet u: target position (real coordinates or categorical, retinocentric referential)

Generative model:

$$\boldsymbol{x} \sim P(X|\boldsymbol{y}, \boldsymbol{u})$$

Full inference (posterior):

$$P(Y, U|\mathbf{x}) \propto P(\mathbf{x}|Y, U)$$

Independence assumptions :

$$P(Y,U) = P(Y)P(U) \text{ (toujours vrai)}$$
(1)

$$P(Y,U|X) = P(Y|X)P(U|X) \text{ (faux s'il y a plusieurs cibles)}$$
 (2)

Partial inference on object category:

$$P(Y|\boldsymbol{x}, \boldsymbol{u}) \propto P(\boldsymbol{x}|Y, \boldsymbol{u})$$

Partial inference on object position:

$$P(U|\boldsymbol{x},\boldsymbol{y}) \propto P(\boldsymbol{x}|U,\boldsymbol{y})$$

Marginals:

- $P(Y|\mathbf{x}) = \int P(Y|\mathbf{x}, \mathbf{u}) d\mathbf{u}$
- $P(U|\mathbf{x}) = \int P(U|\mathbf{x}, \mathbf{y}) d\mathbf{y}$

### 1.3.2 What we did so far...

Consider a view x that contains a single target y at unknown retinocentric position u. The brain needs to guess both y and u with limited computational resources.

We assume here that the brain adopts independence assumption (2), making a separation between the "Where" and the "What" pathways, forming separate (and cheaper) inferences:

- $p(Y|\boldsymbol{x})$
- $p(U|\boldsymbol{x})$

Another assumption is that the category y is translationally invariant: given a transformation  $\mathcal{T}$ ,

$$\mathcal{T}(\boldsymbol{u}, \boldsymbol{y}) = (\mathcal{T}(\boldsymbol{u}), \boldsymbol{y})$$

Now, given x and the separation assumption, it is sensible to change the viewpoint to better estimate y, because y is invariant to the viewpoint transformation.

This is where active inference comes into the play:

a INTRODUCTION

(a) Active Inference in Madrin Learning

Salina

essential comp.

Bethøfe Deep goze - resternal view.

R.botics

- identify gap.

I pagnentation of studies between vennoscience, machine learning and robotics.

Figure 1:

fixation (wait)

display

(tanget)

raccade

rumanse

2

ond

remanse A Problem setting: After a fixation perio

presented with a luminous display which shows a target (here a digit) at a grandom position. The configuration of the display is such that he needs to perform a target to be able to see the digit.

The protocol

(16) Stock-of-the-art

Najemnik

Prietze

Friston.

1c outline of the paper - basaic hypothesis = invariance to position

>			

- ullet Consider that the true target is  $\hat{m{y}}$
- ullet Consider that the target current retinocentric position is  $oldsymbol{u}$
- Then, for any translation  $\delta u$ , the future posterior on the true target is estimated by:  $\mathbb{E}_{x' \sim p(X|\hat{y}, u + \delta u)} p(\hat{y}|x')$
- And the optimal translation is:  $\underset{\delta \boldsymbol{u}}{\operatorname{argmax}} \mathbb{E}_{\boldsymbol{x}' \sim p(X|\hat{\boldsymbol{y}}, \boldsymbol{u} + \delta \boldsymbol{u})} p(\hat{\boldsymbol{y}}|\boldsymbol{x}')$

If now  $\boldsymbol{u}$  is unknown and needs to be guessed from  $\boldsymbol{x}$ , the optimal translation is:

$$\underset{\delta \boldsymbol{u}}{\operatorname{argmax}} \ \mathbb{E}_{\boldsymbol{u} \sim p(\boldsymbol{U}|\boldsymbol{x})} \mathbb{E}_{\boldsymbol{x'} \sim p(\boldsymbol{X}|\hat{\boldsymbol{y}}, \boldsymbol{u} + \delta \boldsymbol{u})} p(\hat{\boldsymbol{y}}|\boldsymbol{x'})$$

with:

- $p(U|\mathbf{x})$  the inferred target position
- and  $\mathbb{E}_{x' \sim p(X|\hat{\boldsymbol{u}}.\boldsymbol{u}+\delta\boldsymbol{u})}p(\hat{\boldsymbol{y}}|x')$  the expected inference on the actual target.

### 1.3.3 Accuracy maps

In practice, it is computationally impossible to make exact guesses about the future observation x'. Our second assumption is that instead of predicting future inferences on true target, the brain trains a parametric accuracy map by experience (trial and error).

In a model-based approach, the  $accuracy\ maps$  can be calculated using a parametric classifier :

- Given a training set  $\{(x_1, u_1, y_1), ..., (x_n, u_n, y_n)\}$ :
  - Train a classifier  $p_{\theta}$  that estimates  $p(Y|\mathbf{x})$ .
- Then, for each class  $\hat{y}$ , taking  $\tilde{y} \sim p_{\theta}(Y|x)$ , the classification rate  $r_{\theta}(u)$  is an estimator of the posterior expectation:

$$r_{\theta}(\boldsymbol{u}) = \mathbb{E}_{\boldsymbol{x} \sim p(X|\hat{\boldsymbol{y}}, \boldsymbol{u})} \mathbb{E}_{\tilde{\boldsymbol{y}} \sim p_{\theta}(Y|\boldsymbol{x})} \delta_{\hat{\boldsymbol{y}} = \tilde{\boldsymbol{y}}}$$

$$= \mathbb{E}_{\boldsymbol{x} \sim p(X|\hat{\boldsymbol{y}}, \boldsymbol{u})} p_{\theta}(\hat{\boldsymbol{y}}|\boldsymbol{x})$$

$$\simeq \mathbb{E}_{\boldsymbol{x} \sim p(X|\hat{\boldsymbol{y}}, \boldsymbol{u})} p(\hat{\boldsymbol{y}}|\boldsymbol{x})$$

that forms an accuracy map for each target position u.

### 1.3.4 Parametric transformation (Colliculus?) map

One can now select  $\delta u$  with the parametric estimator:

$$\widehat{\delta u} \simeq \underset{\delta u}{\operatorname{argmax}} \mathbb{E}_{u \sim p(U|x)} r_{\theta}(u + \delta u)$$

$$= \underset{\delta u}{\operatorname{argmax}} Q(\delta u|x)$$

with  $Q(\delta \boldsymbol{u}|\boldsymbol{x})$  the transformation map, given the view  $\boldsymbol{x}$  and the marginal posterior estimate  $p(U|\boldsymbol{x})$ .

It must be noticed that, given  $\hat{\boldsymbol{u}} = \underset{\boldsymbol{u}}{\operatorname{argmax}} r_{\theta}(\boldsymbol{u})$ , the transformation map is maximal at  $\delta \boldsymbol{u} = \hat{\boldsymbol{u}} - \boldsymbol{u}$ . Each initial  $\boldsymbol{u}$  provides a different transformation map, that is a shift of the original accuracy map (*Ergodic assumption*??).

We assume in the following that a parametric action value map  $Q_{\psi}$  can be trained on top of the parametric classifier  $p_{\theta}$  and its accuracy map  $r_{\theta}$ . The training set is  $\{(\boldsymbol{x}_1, \boldsymbol{u}_1), ..., (\boldsymbol{x}_n, \boldsymbol{u}_n)\}$  and the accuracy map classifier learns to associate each  $\boldsymbol{x}$  with its full transformation map  $Q(.|\boldsymbol{x})$ .

### 1.3.5 Algorithms

Once  $p_\theta$  and  $Q_\psi$  are trained, the recognition algorithm is straightforward:

### Single saccade algorithm:

- 1. Read the view  $\boldsymbol{x}$
- 2. Choose  $\delta \boldsymbol{u}$  according to  $Q_{\psi}(.|\boldsymbol{x})$
- 3. Move the eye
- 4. Update the view x'
- 5. Identify the target with  $\tilde{\boldsymbol{y}} \sim p_{\theta}(Y|\boldsymbol{x}')$

### Multi saccades algorithm:

- 1.  $q(Y) \leftarrow \text{uniform distribution}$
- 2. Read the view  $\boldsymbol{x}$
- 3. Choose  $\delta \boldsymbol{u}$  according to  $Q_{\psi}(.|\boldsymbol{x})$
- 4. Repeat several times up to some posterior confidence threshold:
  - (a) Move the eye
  - (b) Read  $\boldsymbol{x}$
  - (c)  $q(Y) \leftarrow q(Y) \times p_{\theta}(Y|\boldsymbol{x})$
  - (d) normalize q
  - (e) Choose  $\delta \boldsymbol{u}$  according to  $Q_{\psi}(.|\boldsymbol{x})$  (with some inhibition of return mechanism)
- 5. Identify the target with  $\tilde{\boldsymbol{y}} \sim q(Y)$

# 2 Methods

- 2.1 Visual transformation
- 2.1.1 Wavelets
- 2.1.2 Log Gabor
- 2.2 Accuracy map
- 2.3 Network architecture

# 3 Results

 $\verb|https://github.com/laurentperrinet/WhereIsMyMNIST/blob/master/2018-11-13-Where\%20recap\%20 (clutter) | the following state of the property of the property$ 

- 4 Discussion
- 4.1 Summary
- 4.2 Limits
- 4.3 Perspectives

# General case: Visual information gain maximization

Consider a view  $\boldsymbol{x}$  generated from a target  $\boldsymbol{y}$  viewed at retinocentric position  $\boldsymbol{u}$ . Consider first that :

- The generative model  $p(X|\boldsymbol{y},\boldsymbol{u})$  is known
- The retinocentric position u is known.
- The view x is known.
- The target category y is unknown.

The question comes how to choose the new retinocentric position u' in order to maximize the *mutual information* between x|u (current view) and x'|u' (future view).

In general, the visual Information Gain between two visual fields x|u and x'|u' is:

$$IG(\boldsymbol{x}|\boldsymbol{u};\boldsymbol{x}'|\boldsymbol{u}') = -\log p(\boldsymbol{x}|\boldsymbol{u}) + \log p(\boldsymbol{x}|\boldsymbol{u},\boldsymbol{x}',\boldsymbol{u}')$$

**Information Gain Lower Bound** Consider now that given x and u, the target category y can be *inferred* using Bayes rule, i.e.:

$$P(Y|\boldsymbol{x}, \boldsymbol{u}) \propto P(\boldsymbol{x}|Y, \boldsymbol{u})$$

Then, it can be shown (see [?]) that:

$$\operatorname{IG}(\boldsymbol{x}|\boldsymbol{u};\boldsymbol{x}'|\boldsymbol{u}') \geq \mathbb{E}_{\boldsymbol{y} \sim p(Y|\boldsymbol{x},\boldsymbol{u})} \left[ \log p(\boldsymbol{y}|\boldsymbol{x}',\boldsymbol{u}') - \log(\pi(\boldsymbol{y})) \right]$$

with  $\pi(y)$  the prior over the y's. When the prior is uniform, the information gain lower bound (IGLB) simplifies to  $\mathbb{E}_{y \sim p(Y|x,u)} [\log p(y|x',u')] + c$ , with c a constant.

**Predictive approach** One can adopt a *predictive* approach to choose the new eye orientation e':

- First choose a new retinocentric position u' that will maximize the information gain.
- Then choose e' such that

$$z - e' = u'$$

i.e.

$$e' = e + u - u'$$

The predictive approach needs three predictive steps:

- $p(Y|\mathbf{x}, \mathbf{u})$  is the current posterior over the target category inferred from the current observation,
- $x' \sim p(X|y, u')$  is the predicted view generated by the model assuming that the target y is seen from from u',
- and p(y|x', u') is the predicted posterior for assumption y, given x' and u'.

Then the optimal new retinocentric position is:

$$\hat{\boldsymbol{u}}' = \underset{\boldsymbol{u}'}{\operatorname{argmax}} \ \mathbb{E}_{\boldsymbol{y} \sim p(Y|\boldsymbol{x}, \boldsymbol{u})} \left[ \mathbb{E}_{\boldsymbol{x}' \sim p(X|\boldsymbol{y}, \boldsymbol{u}')} \left[ \log p(\boldsymbol{y}|\boldsymbol{x}', \boldsymbol{u}') \right] \right]$$

Taking  $\delta e = u - u'$ , the optimal eye displacement is:

$$\widehat{\delta \boldsymbol{e}} = \underset{\delta \boldsymbol{e}}{\operatorname{argmax}} \; \mathbb{E}_{\boldsymbol{y} \sim p(Y|\boldsymbol{x}, \boldsymbol{u})} \left[ \mathbb{E}_{\boldsymbol{x}' \sim p(X|\boldsymbol{y}, \boldsymbol{u} - \delta \boldsymbol{e})} \left[ \log p(\boldsymbol{y}|\boldsymbol{x}', \boldsymbol{u} - \delta \boldsymbol{e}) \right] \right]$$

(TODO: Attention il faudrait à partir de maintenant une carte qui moyenne les log posteriors car l'espérance du log n'est pas égale au log de l'espérance, i.e.  $r_{\theta}^{log}(\boldsymbol{u}|q) = \mathbb{E}_{\boldsymbol{y} \sim q(Y)} \left[ \mathbb{E}_{\boldsymbol{x} \sim p(X|\boldsymbol{y},\boldsymbol{u})} \log p_{\theta}(\boldsymbol{y}|\boldsymbol{x},\boldsymbol{u}) \right] ).$