

Name:

On homework:

- If you work with anyone else, document what you worked on together.
- Show your work.
- Always clearly label plots (axis labels, a title, and a legend if applicable).
- Homework should be done “by hand” (i.e. not with a numerical program such as MATLAB, Python, or Wolfram Alpha) unless otherwise specified. You may use a numerical program to check your work.
- If you use a numerical program to solve a problem, submit the associated code, input, and output (email submission is fine).

Problem	Points	Score
1	10	
2	10	
3	10	
4	5	
5	5	
6	10	
Total:	50	

Do not write in the table to the right.

1. (10 points) Determine the macroscopic scattering cross section of UO_2 as a function of a generic enrichment factor $\gamma = N_{U-235}/N_{U-238}$ where N is the atom density. Find its value assuming a density of 10 g/cm^3 , $\sigma_s^U \simeq 8.9 \text{ b}$ and $\sigma_s^O \simeq 3.75 \text{ b}$, and 5% weight enrichment.

2. (10 points) Briefly describe what each term in the Transport Equation [Eqn. (2)] physically represents.

$$\underbrace{\hat{\Omega} \cdot \nabla \psi(\vec{r}, \hat{\Omega}, E)}_A + \underbrace{\Sigma(\vec{r}, E) \psi(\vec{r}, \hat{\Omega}, E)}_B = \underbrace{\int_0^\infty dE' \int_{4\pi} d\hat{\Omega}' \Sigma_s(\vec{r}, E' \rightarrow E, \hat{\Omega}' \cdot \hat{\Omega}) \psi(\vec{r}, \hat{\Omega}', E')}_C \\
 + \underbrace{\frac{\chi(E)}{k} \int_0^\infty dE' \nu \Sigma_f(\vec{r}, E') \int_{4\pi} d\hat{\Omega}' \psi(\vec{r}, \hat{\Omega}', E')}_D \quad (2)$$

3. (10 points) List three assumptions *needed* to get from the Transport Equation to the Diffusion Equation.
4. (5 points) List four locations where the Diffusion Equation is not valid because the underlying assumptions do not hold; for each explain why the assumptions do not hold

in that location.

5. (a) (2 points) Write the **steady state**, 2D diffusion equation and explain how we typically characterize it from the viewpoint of labeling second order linear PDEs. Assume D is not a function of x or y for this part.
- (b) (3 points) Can you think of any physical cases in which this characterization would change?
6. (10 points) At what energy is the lowest isolated resonance of ^{235}U , ^{238}U , ^{239}Pu , and ^{240}Pu ? Why do we care about that?