$$\psi_0 = \theta[x + \log(1 - e^{-2x})]$$