$$\langle u_i^2 \rangle_a = \langle u_i \rangle_a^2 + \theta \frac{\delta \langle u_i \rangle_a}{\delta a} + \frac{\theta}{k} (x \coth x - 1)$$