

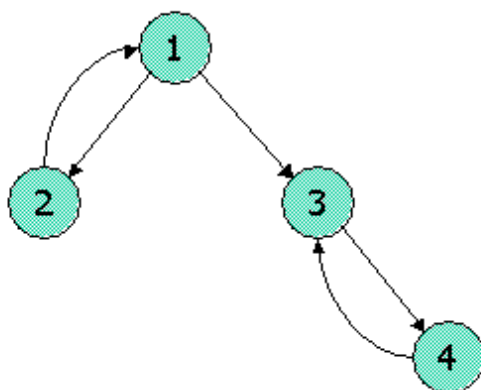
## Feedback — Week7B Basic

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You submitted this quiz on **Fri 20 Mar 2015 7:32 PM PDT**. You got a score of **2.00** out of **2.00**.

### Question 1

Compute the Topic-Specific PageRank for the following link topology. Assume that pages selected for the teleport set are nodes 1 and 2 and that in the teleport set, the weight assigned for node 1 is twice that of node 2. Assume further that the teleport probability,  $(1 - \beta)$ , is 0.3. Which of the following statements is correct?



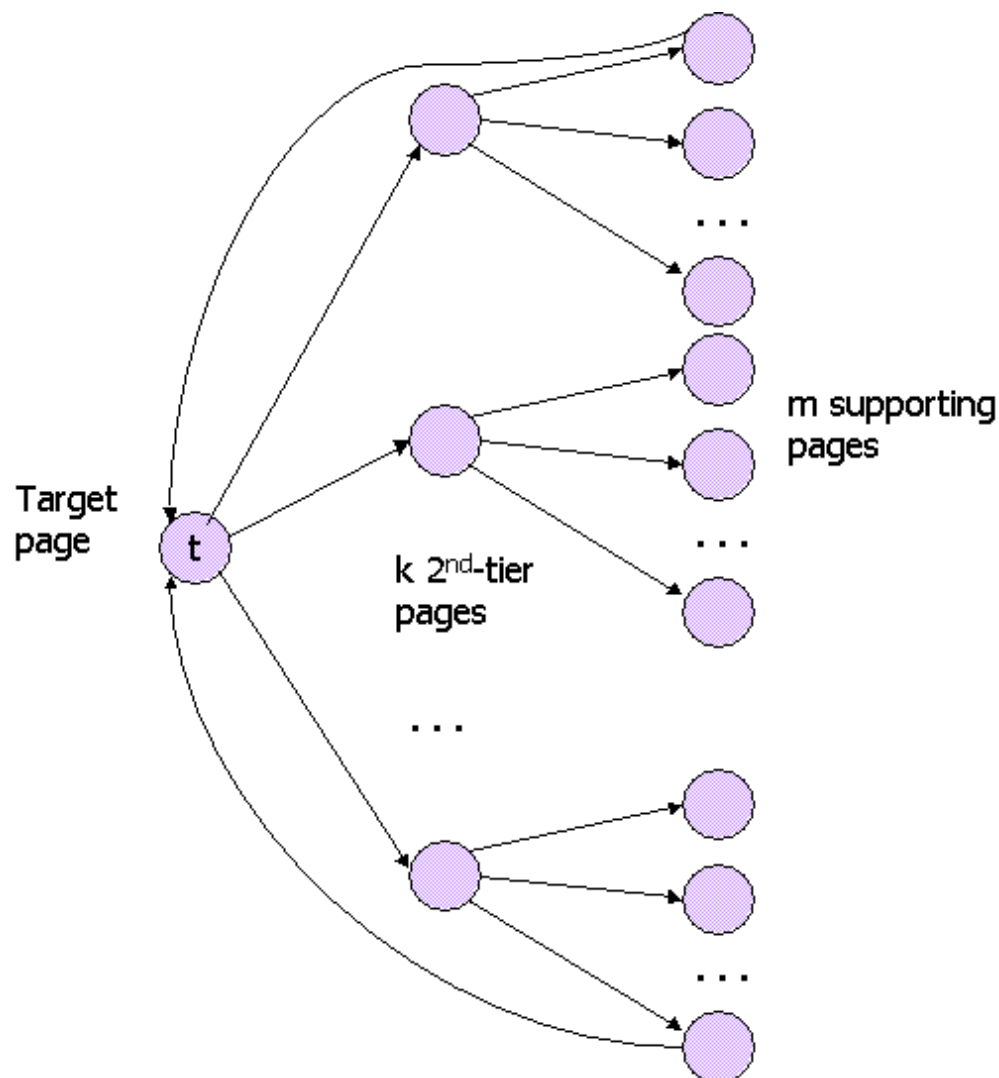
Your Answer	Score	Explanation
<input type="radio"/> TSPR(1) = .4236		
<input type="radio"/> TSPR(2) = .8998		
<input type="radio"/> TSPR(3) = .1092		
<input checked="" type="radio"/> TSPR(4) = .1718	✓ 1.00	
Total	1.00 / 1.00	

#### Question Explanation

"the weight assigned for node 1 is twice that of node 2" means that given a random walker and its current position, its teleport probability to node 1 is twice that to node 2.

## Question 2

The spam-farm architecture described in Section 5.4.1 suffers from the problem that the target page has many links --- one to each supporting page. To avoid that problem, the spammer could use the architecture shown below:



There,  $k$  "second-tier" nodes act as intermediaries. The target page  $t$  has only to link to the  $k$  second-tier pages, and each of those pages links to  $m/k$  of the  $m$  supporting pages. Each of the supporting pages links only to  $t$  (although most of these links are not shown). Suppose the taxation parameter is  $\beta = 0.85$ , and  $x$  is the amount of PageRank supplied from outside to the target page. Let  $n$  be the total number of pages in the Web. Finally, let  $y$  be the PageRank of target page  $t$ . If we compute the formula for  $y$  in terms of  $k$ ,  $m$ , and  $n$ , we get a formula with the form

$$y = ax + bm/n + ck/n$$

Note: To arrive at this form, it is necessary at the last step to drop a low-order term that is a fraction of  $1/n$ . Determine coefficients  $a$ ,  $b$ , and  $c$ , remembering that  $\beta$  is fixed at 0.85. Then, identify the value, correct to two decimal places, for one of these coefficients.

## Your Answer

## Score

## Explanation

☐  $c = 0.46$ 
☐  $b = 0.28$ 
☐  $a = 1.98$ 
☒  $c = 0.28$ 


1.00

Total

1.00 / 1.00

## Question Explanation

Let  $w$  be the PageRank of each of the second-tier pages, and let  $z$  be the PageRank of each of the supporting pages. Then the equations relating  $y$ ,  $w$ , and  $z$  are:

$$y = x + \beta z m + (1-\beta)/n$$

$$w = \beta y/k + (1-\beta)/n$$

$$z = \beta k w/m + (1-\beta)/n$$

The first equation says that the PageRank of  $t$  is the external contribution  $x$ , plus  $\beta z$  (the amount of PageRank not taxed) times the number of supporting pages, plus  $(1-\beta)/n$ , which is the share of "tax" that every page gets. The second equation says that each second-tier page gets  $1/k$ -th of the untaxed PageRank of  $t$ , plus its share of the tax. The third equation says each supporting page gets  $1$  part in  $m/k$  of the untaxed PageRank of the second-tier page that reaches that supporting page, plus its share of the tax.

Begin by substituting for  $z$  in the first equation:

$$y = x + \beta^2 k w + \beta(1-\beta)m/n + (1-\beta)/n$$

Now, substitute for  $w$  in the above:

$$y = x + \beta^3 y + \beta(1-\beta)m/n + \beta^2(1-\beta)k/n + (1-\beta)/n$$

Neglect the last term  $(1-\beta)/n$ , per the directions in the statement of the problem. If we move the term  $\beta^3 y$  to the left, and note that  $\beta^3 = (1-\beta)(1+\beta+\beta^2)$ , we get

$$y = x/(1-\beta^3) + (\beta/(1+\beta+\beta^2))(m/n) + (\beta/(1+\beta+\beta^2))(k/n)$$

For  $\beta = 0.85$ , these coefficients evaluate to:

$$y = 2.59x + 0.33(m/n) + 0.28(k/n)$$