PS6

January 15, 2024

```
[1]: from shap.datasets import adult
     X, y = adult()
     print(X)
     print(y)
                                                                   Occupation
                   Workclass
                                Education-Num
                                                Marital Status
             Age
    0
            39.0
                            7
                                          13.0
                                                                             1
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    1
            50.0
                            6
                                          13.0
    2
            38.0
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                                         Capital Gain
                                                        Capital Loss
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    32560
                 39
    [32561 rows x 12 columns]
    [False False False ... False False True]
[2]: numerical_columns = ['Age', 'Education-Num', 'Capital Gain', 'Capital Loss', 'Hours_
      →per week']
     categorical_columns = ['Workclass', 'Marital__
      ⇒Status','Occupation','Relationship','Race','Sex','Country']
         Conversion of categorical data
[3]: import pandas as pd # for one-hot encoding
     from sklearn.preprocessing import StandardScaler # for normalization
[4]: # Normalization of numerical data
     for column in numerical_columns:
         scaler = StandardScaler()
         X[column] = scaler.fit_transform(X[column].values.reshape(-1,1))
     print(X)
                      Workclass
                                  Education-Num Marital Status
                                                                  Occupation
                 Age
    0
           0.030671
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                                       1.134739
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          -0.042642
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          -0.775768
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    32558 1.423610
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    32560 0.983734
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                          Race
                                Sex
                                     Capital Gain Capital Loss
                                                                   Hours per week
           Relationship
    0
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                                          0.148453
                                                         -0.21666
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                                                                         -2.222153
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                                                                        -0.035429
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                                                           -0.21666
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     [32561 rows x 12 columns]
[5]: # Data type change of categorical data
     for column in categorical_columns:
         X[column] = X[column].astype('category')
     print(X)
                                  Education-Num Marital Status Occupation
                 Age Workclass
    0
            0.030671
                                       1.134739
                                                                           1
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    1
            0.837109
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           -0.042642
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    32560 0.983734
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                                    Capital Gain
           Relationship Race Sex
                                                   Capital Loss
                                                                  Hours per week
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          Country
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    [32561 rows x 12 columns]
[6]: # One-hot encoding of categorical data
     X = pd.get_dummies(X)
     # Conversion of data frame to numpy
     X = X.values
     # Converision: {False, True} --> {0., 1.}
     y = y.astype(float)
[7]: print(X.shape)
     print(y.shape)
     print(y)
    (32561, 91)
    (32561,)
    [0. 0. 0. ... 0. 0. 1.]
    0.2 train-val-test split
[8]: from sklearn.model_selection import train_test_split
     X_,X_test,y_,y_test = train_test_split(X,y,test_size=1/10,stratify=y)
     X_train,X_val,y_train,y_val = train_test_split(X_,y_,test_size=1/9,stratify=y_)
     print(X_train.shape)
     print(X_val.shape)
     print(X_test.shape)
```

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(26048, 91)
(3256, 91)
(3257, 91)
```

0.3 Cross validation

```
[9]: import numpy as np
      from sklearn.model_selection import KFold
      from sklearn.model_selection import train_test_split
      X1 = np.array([10, 20, 30, 40, 50])
      y1 = np.array([60, 70, 80, 90, 100])
     kfold = KFold(n_splits=4,shuffle=True)
      X1_,X1_test,y1_,y1_test = train_test_split(X1,y1,test_size=1/5)
      print(kfold.get_n_splits())
      print(X1_)
      print(y1_)
     [40 50 20 10]
     [ 90 100 70 60]
[10]: for train, val in kfold.split(X1_,y1_):
          print("Train indices: ",train)
          X1_train = X1_[train]
          print("Train datasets: ",X1_train)
     Train indices: [0 1 2]
     Train datasets: [40 50 20]
     Train indices: [1 2 3]
     Train datasets: [50 20 10]
     Train indices: [0 1 3]
     Train datasets: [40 50 10]
     Train indices: [0 2 3]
     Train datasets: [40 20 10]
[11]: from sklearn.model_selection import KFold
      from sklearn.model_selection import train_test_split
      #kfold = KFold(n_splits=4, shuffle=True)
      kfold = KFold(n_splits=4)
      X_,X_test,y_,y_test = train_test_split(X,y,test_size=1/10,stratify=y)
      aaa = kfold.split(X_,y_)
```

```
for train, val in aaa:
     print(train)
     #print(val)
     X_train = X[train]
     print(X_train[0])
    # print(X_train.shape)
[ 7326 7327 7328 ... 29301 29302 29303]
[-0.11595462 0.7460392 -0.14592049 -0.21665953 -0.19740899
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[12]: def scheduler(epoch, lr):
           if epoch in [20,40,60]:
               lr = 0.1*lr
           else:
               lr = lr
          return lr
[13]: from tensorflow.keras.models import Sequential
      from tensorflow.keras.layers import Dense
      from tensorflow.keras.optimizers import Adam
      from tensorflow.keras.regularizers import 12
      from tensorflow.keras.initializers import HeNormal
      from tensorflow.keras.layers import BatchNormalization
      from tensorflow.keras.layers import ReLU
      from tensorflow.keras.layers import Dropout
      from tensorflow.keras.callbacks import EarlyStopping
      from tensorflow.keras.callbacks import LearningRateScheduler
```

```
from sklearn.model_selection import KFold
kfold = KFold(n_splits=4, shuffle=True)
X_,X_test,y_,y_test = train_test_split(X,y,test_size=1/10,stratify=y)
for train, val in kfold.split(X_,y_):
    # Train and val datasets
    X_train, X_val = X[train], X[val]
    y_train, y_val = y[train], y[val]
    #print(X_train.shape)
    #print(X_val.shape)
    # Construct a model
    init = HeNormal()
    model = Sequential()
    model.add(Dense(128,kernel_regularizer=12(0.01),
             bias_regularizer=12(0.01),
             kernel_initializer=init))
    model.add(BatchNormalization())
    model.add(ReLU())
    model.add(Dropout(0.5))
    model.add(Dense(1,activation='sigmoid'))
    # Compile
    opt = Adam(learning_rate=0.01,beta_1 = 0.9,beta_2 = 0.999)
    model.compile(optimizer=opt,
               loss='binary_crossentropy',
               metrics=['acc'])
    # Early stopping & learning rate decaying
    es_callback = EarlyStopping(monitor='val_acc',patience=15)
    ls_callback = LearningRateScheduler(scheduler)
    # Training
    hist = model.fit(X_train, y_train, epochs=100,
                      validation_data=(X_val,y_val),
                      callbacks=[es_callback,ls_callback])
    # Valiation performance
    print(model.evaluate(X_val, y_val))
Epoch 1/100
0.8279 - val_loss: 0.4387 - val_acc: 0.8254 - lr: 0.0100
Epoch 2/100
0.8296 - val_loss: 0.4138 - val_acc: 0.8402 - lr: 0.0100
```

```
Epoch 3/100
0.8299 - val_loss: 0.4219 - val_acc: 0.8194 - lr: 0.0100
Epoch 4/100
0.8304 - val_loss: 0.4034 - val_acc: 0.8395 - lr: 0.0100
Epoch 5/100
0.8300 - val_loss: 0.4015 - val_acc: 0.8369 - lr: 0.0100
Epoch 6/100
0.8276 - val_loss: 0.4371 - val_acc: 0.8351 - lr: 0.0100
Epoch 7/100
0.8283 - val_loss: 0.3949 - val_acc: 0.8421 - lr: 0.0100
Epoch 8/100
0.8311 - val_loss: 0.4040 - val_acc: 0.8296 - lr: 0.0100
Epoch 9/100
0.8285 - val_loss: 0.3962 - val_acc: 0.8441 - lr: 0.0100
Epoch 10/100
0.8310 - val_loss: 0.4159 - val_acc: 0.8318 - lr: 0.0100
Epoch 11/100
0.8255 - val_loss: 0.4062 - val_acc: 0.8415 - lr: 0.0100
Epoch 12/100
0.8287 - val_loss: 0.4081 - val_acc: 0.8235 - lr: 0.0100
Epoch 13/100
0.8297 - val_loss: 0.4230 - val_acc: 0.8223 - lr: 0.0100
Epoch 14/100
0.8299 - val_loss: 0.3989 - val_acc: 0.8339 - lr: 0.0100
Epoch 15/100
0.8300 - val_loss: 0.4086 - val_acc: 0.8354 - lr: 0.0100
Epoch 16/100
0.8270 - val_loss: 0.4172 - val_acc: 0.8234 - lr: 0.0100
Epoch 17/100
0.8289 - val_loss: 0.3941 - val_acc: 0.8361 - lr: 0.0100
Epoch 18/100
0.8297 - val_loss: 0.4111 - val_acc: 0.8411 - lr: 0.0100
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Epoch 19/100
0.8323 - val_loss: 0.3897 - val_acc: 0.8417 - lr: 0.0100
Epoch 20/100
0.8293 - val_loss: 0.3929 - val_acc: 0.8436 - lr: 0.0100
Epoch 21/100
0.8405 - val_loss: 0.3378 - val_acc: 0.8503 - lr: 1.0000e-03
Epoch 22/100
0.8428 - val_loss: 0.3342 - val_acc: 0.8501 - lr: 1.0000e-03
Epoch 23/100
0.8435 - val_loss: 0.3342 - val_acc: 0.8441 - lr: 1.0000e-03
Epoch 24/100
0.8470 - val_loss: 0.3337 - val_acc: 0.8497 - lr: 1.0000e-03
Epoch 25/100
0.8456 - val_loss: 0.3328 - val_acc: 0.8483 - lr: 1.0000e-03
Epoch 26/100
0.8451 - val_loss: 0.3348 - val_acc: 0.8459 - lr: 1.0000e-03
Epoch 27/100
0.8455 - val_loss: 0.3313 - val_acc: 0.8489 - lr: 1.0000e-03
Epoch 28/100
0.8435 - val_loss: 0.3295 - val_acc: 0.8546 - lr: 1.0000e-03
Epoch 29/100
0.8439 - val_loss: 0.3361 - val_acc: 0.8451 - lr: 1.0000e-03
Epoch 30/100
0.8460 - val_loss: 0.3356 - val_acc: 0.8471 - lr: 1.0000e-03
Epoch 31/100
0.8417 - val_loss: 0.3334 - val_acc: 0.8475 - lr: 1.0000e-03
Epoch 32/100
0.8453 - val_loss: 0.3347 - val_acc: 0.8445 - lr: 1.0000e-03
0.8425 - val_loss: 0.3299 - val_acc: 0.8512 - lr: 1.0000e-03
Epoch 34/100
0.8448 - val_loss: 0.3312 - val_acc: 0.8488 - lr: 1.0000e-03
```

```
Epoch 35/100
0.8437 - val_loss: 0.3327 - val_acc: 0.8490 - lr: 1.0000e-03
Epoch 36/100
0.8473 - val_loss: 0.3308 - val_acc: 0.8504 - lr: 1.0000e-03
Epoch 37/100
0.8421 - val_loss: 0.3306 - val_acc: 0.8488 - lr: 1.0000e-03
Epoch 38/100
0.8452 - val_loss: 0.3306 - val_acc: 0.8496 - lr: 1.0000e-03
Epoch 39/100
0.8434 - val_loss: 0.3292 - val_acc: 0.8509 - lr: 1.0000e-03
Epoch 40/100
0.8448 - val_loss: 0.3300 - val_acc: 0.8482 - lr: 1.0000e-03
Epoch 41/100
0.8477 - val_loss: 0.3273 - val_acc: 0.8501 - lr: 1.0000e-04
Epoch 42/100
0.8496 - val_loss: 0.3261 - val_acc: 0.8514 - lr: 1.0000e-04
Epoch 43/100
0.8507 - val_loss: 0.3239 - val_acc: 0.8531 - lr: 1.0000e-04
0.8531
[0.32385891675949097, 0.8531258702278137]
Epoch 1/100
0.8285 - val_loss: 0.4381 - val_acc: 0.8332 - lr: 0.0100
Epoch 2/100
0.8288 - val_loss: 0.4265 - val_acc: 0.8382 - lr: 0.0100
Epoch 3/100
0.8303 - val_loss: 0.4093 - val_acc: 0.8354 - lr: 0.0100
Epoch 4/100
0.8311 - val_loss: 0.4174 - val_acc: 0.8361 - lr: 0.0100
0.8284 - val_loss: 0.4042 - val_acc: 0.8438 - lr: 0.0100
Epoch 6/100
0.8306 - val_loss: 0.4056 - val_acc: 0.8387 - lr: 0.0100
```

```
Epoch 7/100
0.8321 - val_loss: 0.4131 - val_acc: 0.8299 - lr: 0.0100
Epoch 8/100
0.8329 - val_loss: 0.4274 - val_acc: 0.8280 - lr: 0.0100
Epoch 9/100
0.8300 - val_loss: 0.4046 - val_acc: 0.8438 - lr: 0.0100
Epoch 10/100
0.8291 - val_loss: 0.4267 - val_acc: 0.8161 - lr: 0.0100
Epoch 11/100
0.8305 - val_loss: 0.3991 - val_acc: 0.8380 - lr: 0.0100
Epoch 12/100
0.8276 - val_loss: 0.4005 - val_acc: 0.8381 - lr: 0.0100
Epoch 13/100
0.8305 - val_loss: 0.3965 - val_acc: 0.8307 - lr: 0.0100
Epoch 14/100
0.8300 - val_loss: 0.4025 - val_acc: 0.8310 - lr: 0.0100
Epoch 15/100
0.8299 - val_loss: 0.4045 - val_acc: 0.8279 - lr: 0.0100
Epoch 16/100
0.8343 - val_loss: 0.3958 - val_acc: 0.8404 - lr: 0.0100
Epoch 17/100
0.8290 - val_loss: 0.3941 - val_acc: 0.8410 - lr: 0.0100
Epoch 18/100
0.8281 - val_loss: 0.4001 - val_acc: 0.8430 - lr: 0.0100
Epoch 19/100
0.8301 - val_loss: 0.3924 - val_acc: 0.8470 - lr: 0.0100
Epoch 20/100
0.8321 - val_loss: 0.4014 - val_acc: 0.8249 - lr: 0.0100
Epoch 21/100
0.8421 - val_loss: 0.3439 - val_acc: 0.8479 - lr: 1.0000e-03
Epoch 22/100
0.8443 - val_loss: 0.3381 - val_acc: 0.8494 - lr: 1.0000e-03
```

```
Epoch 23/100
0.8468 - val_loss: 0.3365 - val_acc: 0.8508 - lr: 1.0000e-03
Epoch 24/100
0.8437 - val_loss: 0.3377 - val_acc: 0.8488 - lr: 1.0000e-03
Epoch 25/100
0.8455 - val_loss: 0.3338 - val_acc: 0.8504 - lr: 1.0000e-03
Epoch 26/100
0.8419 - val_loss: 0.3395 - val_acc: 0.8479 - lr: 1.0000e-03
Epoch 27/100
0.8443 - val_loss: 0.3383 - val_acc: 0.8459 - lr: 1.0000e-03
Epoch 28/100
0.8452 - val_loss: 0.3385 - val_acc: 0.8505 - lr: 1.0000e-03
Epoch 29/100
0.8475 - val_loss: 0.3362 - val_acc: 0.8493 - lr: 1.0000e-03
Epoch 30/100
0.8462 - val_loss: 0.3336 - val_acc: 0.8509 - lr: 1.0000e-03
Epoch 31/100
0.8436 - val_loss: 0.3371 - val_acc: 0.8467 - lr: 1.0000e-03
Epoch 32/100
0.8452 - val_loss: 0.3344 - val_acc: 0.8496 - lr: 1.0000e-03
Epoch 33/100
0.8483 - val_loss: 0.3351 - val_acc: 0.8511 - lr: 1.0000e-03
Epoch 34/100
0.8433 - val_loss: 0.3373 - val_acc: 0.8507 - lr: 1.0000e-03
Epoch 35/100
0.8435 - val_loss: 0.3350 - val_acc: 0.8489 - lr: 1.0000e-03
Epoch 36/100
0.8457 - val_loss: 0.3379 - val_acc: 0.8500 - lr: 1.0000e-03
0.8448 - val_loss: 0.3391 - val_acc: 0.8492 - lr: 1.0000e-03
Epoch 38/100
0.8451 - val_loss: 0.3352 - val_acc: 0.8478 - lr: 1.0000e-03
```

```
Epoch 39/100
0.8466 - val_loss: 0.3363 - val_acc: 0.8520 - lr: 1.0000e-03
Epoch 40/100
0.8453 - val_loss: 0.3351 - val_acc: 0.8492 - lr: 1.0000e-03
Epoch 41/100
0.8481 - val_loss: 0.3326 - val_acc: 0.8507 - lr: 1.0000e-04
Epoch 42/100
0.8487 - val_loss: 0.3308 - val_acc: 0.8515 - lr: 1.0000e-04
Epoch 43/100
0.8496 - val_loss: 0.3300 - val_acc: 0.8516 - lr: 1.0000e-04
Epoch 44/100
0.8503 - val_loss: 0.3298 - val_acc: 0.8512 - lr: 1.0000e-04
Epoch 45/100
0.8503 - val_loss: 0.3265 - val_acc: 0.8552 - lr: 1.0000e-04
Epoch 46/100
0.8504 - val_loss: 0.3279 - val_acc: 0.8507 - lr: 1.0000e-04
Epoch 47/100
0.8511 - val_loss: 0.3267 - val_acc: 0.8511 - lr: 1.0000e-04
Epoch 48/100
0.8518 - val_loss: 0.3261 - val_acc: 0.8537 - lr: 1.0000e-04
Epoch 49/100
0.8533 - val_loss: 0.3257 - val_acc: 0.8518 - lr: 1.0000e-04
Epoch 50/100
0.8509 - val_loss: 0.3249 - val_acc: 0.8523 - lr: 1.0000e-04
Epoch 51/100
0.8530 - val_loss: 0.3244 - val_acc: 0.8549 - lr: 1.0000e-04
Epoch 52/100
0.8521 - val_loss: 0.3243 - val_acc: 0.8548 - lr: 1.0000e-04
0.8537 - val_loss: 0.3245 - val_acc: 0.8520 - lr: 1.0000e-04
Epoch 54/100
0.8513 - val_loss: 0.3223 - val_acc: 0.8557 - lr: 1.0000e-04
```

```
Epoch 55/100
0.8519 - val_loss: 0.3244 - val_acc: 0.8539 - lr: 1.0000e-04
Epoch 56/100
0.8504 - val_loss: 0.3241 - val_acc: 0.8544 - lr: 1.0000e-04
Epoch 57/100
0.8533 - val_loss: 0.3237 - val_acc: 0.8545 - lr: 1.0000e-04
Epoch 58/100
0.8515 - val_loss: 0.3224 - val_acc: 0.8535 - lr: 1.0000e-04
Epoch 59/100
0.8506 - val_loss: 0.3232 - val_acc: 0.8546 - lr: 1.0000e-04
Epoch 60/100
0.8514 - val_loss: 0.3215 - val_acc: 0.8552 - lr: 1.0000e-04
Epoch 61/100
0.8513 - val_loss: 0.3236 - val_acc: 0.8531 - lr: 1.0000e-05
Epoch 62/100
0.8539 - val_loss: 0.3224 - val_acc: 0.8552 - lr: 1.0000e-05
Epoch 63/100
0.8536 - val_loss: 0.3234 - val_acc: 0.8531 - lr: 1.0000e-05
Epoch 64/100
0.8509 - val_loss: 0.3222 - val_acc: 0.8539 - lr: 1.0000e-05
Epoch 65/100
0.8544 - val_loss: 0.3226 - val_acc: 0.8531 - lr: 1.0000e-05
Epoch 66/100
0.8536 - val_loss: 0.3214 - val_acc: 0.8545 - lr: 1.0000e-05
Epoch 67/100
0.8544 - val_loss: 0.3213 - val_acc: 0.8548 - lr: 1.0000e-05
Epoch 68/100
0.8546 - val_loss: 0.3211 - val_acc: 0.8544 - lr: 1.0000e-05
Epoch 69/100
0.8545 - val_loss: 0.3216 - val_acc: 0.8546 - lr: 1.0000e-05
0.8546
[0.3215961158275604, 0.8546273708343506]
```

```
Epoch 1/100
0.8265 - val_loss: 0.4301 - val_acc: 0.8370 - lr: 0.0100
Epoch 2/100
0.8276 - val_loss: 0.4575 - val_acc: 0.8201 - lr: 0.0100
Epoch 3/100
0.8273 - val_loss: 0.4123 - val_acc: 0.8403 - lr: 0.0100
Epoch 4/100
0.8286 - val_loss: 0.4170 - val_acc: 0.8320 - lr: 0.0100
Epoch 5/100
0.8317 - val_loss: 0.4163 - val_acc: 0.8421 - lr: 0.0100
Epoch 6/100
0.8295 - val_loss: 0.4178 - val_acc: 0.8266 - lr: 0.0100
Epoch 7/100
0.8270 - val_loss: 0.4092 - val_acc: 0.8325 - lr: 0.0100
Epoch 8/100
0.8276 - val_loss: 0.4127 - val_acc: 0.8406 - lr: 0.0100
Epoch 9/100
0.8332 - val_loss: 0.4021 - val_acc: 0.8404 - lr: 0.0100
Epoch 10/100
0.8304 - val_loss: 0.4149 - val_acc: 0.8351 - lr: 0.0100
Epoch 11/100
0.8313 - val_loss: 0.3971 - val_acc: 0.8447 - lr: 0.0100
Epoch 12/100
0.8296 - val_loss: 0.4146 - val_acc: 0.8318 - lr: 0.0100
Epoch 13/100
0.8296 - val_loss: 0.4147 - val_acc: 0.8152 - lr: 0.0100
Epoch 14/100
0.8340 - val_loss: 0.4008 - val_acc: 0.8399 - lr: 0.0100
Epoch 15/100
0.8281 - val_loss: 0.4053 - val_acc: 0.8402 - lr: 0.0100
Epoch 16/100
0.8275 - val_loss: 0.4017 - val_acc: 0.8382 - lr: 0.0100
```

```
Epoch 17/100
0.8317 - val_loss: 0.3938 - val_acc: 0.8378 - lr: 0.0100
Epoch 18/100
0.8303 - val_loss: 0.3941 - val_acc: 0.8458 - lr: 0.0100
Epoch 19/100
0.8327 - val_loss: 0.4013 - val_acc: 0.8382 - lr: 0.0100
Epoch 20/100
0.8313 - val_loss: 0.4098 - val_acc: 0.8332 - lr: 0.0100
Epoch 21/100
0.8412 - val_loss: 0.3523 - val_acc: 0.8411 - lr: 1.0000e-03
Epoch 22/100
0.8458 - val_loss: 0.3407 - val_acc: 0.8474 - lr: 1.0000e-03
Epoch 23/100
0.8471 - val_loss: 0.3379 - val_acc: 0.8488 - lr: 1.0000e-03
Epoch 24/100
0.8433 - val_loss: 0.3416 - val_acc: 0.8494 - lr: 1.0000e-03
Epoch 25/100
0.8444 - val_loss: 0.3364 - val_acc: 0.8497 - lr: 1.0000e-03
Epoch 26/100
0.8463 - val_loss: 0.3376 - val_acc: 0.8468 - lr: 1.0000e-03
Epoch 27/100
0.8448 - val_loss: 0.3409 - val_acc: 0.8432 - lr: 1.0000e-03
Epoch 28/100
0.8473 - val_loss: 0.3394 - val_acc: 0.8478 - lr: 1.0000e-03
Epoch 29/100
0.8450 - val_loss: 0.3397 - val_acc: 0.8481 - lr: 1.0000e-03
Epoch 30/100
0.8469 - val_loss: 0.3401 - val_acc: 0.8455 - lr: 1.0000e-03
0.8436 - val_loss: 0.3376 - val_acc: 0.8468 - lr: 1.0000e-03
Epoch 32/100
0.8451 - val_loss: 0.3400 - val_acc: 0.8447 - lr: 1.0000e-03
```

```
Epoch 33/100
0.8467 - val_loss: 0.3375 - val_acc: 0.8473 - lr: 1.0000e-03
Epoch 34/100
0.8435 - val_loss: 0.3423 - val_acc: 0.8428 - lr: 1.0000e-03
Epoch 35/100
0.8453 - val_loss: 0.3398 - val_acc: 0.8437 - lr: 1.0000e-03
Epoch 36/100
0.8475 - val_loss: 0.3379 - val_acc: 0.8437 - lr: 1.0000e-03
Epoch 37/100
0.8471 - val_loss: 0.3373 - val_acc: 0.8448 - lr: 1.0000e-03
Epoch 38/100
0.8463 - val_loss: 0.3398 - val_acc: 0.8419 - lr: 1.0000e-03
Epoch 39/100
0.8439 - val_loss: 0.3390 - val_acc: 0.8441 - lr: 1.0000e-03
Epoch 40/100
0.8452 - val_loss: 0.3392 - val_acc: 0.8463 - lr: 1.0000e-03
0.8463
[0.3392113745212555, 0.8463008403778076]
Epoch 1/100
0.8263 - val_loss: 0.4201 - val_acc: 0.8479 - lr: 0.0100
Epoch 2/100
0.8303 - val_loss: 0.4263 - val_acc: 0.8428 - lr: 0.0100
Epoch 3/100
0.8291 - val_loss: 0.4092 - val_acc: 0.8429 - lr: 0.0100
Epoch 4/100
0.8278 - val_loss: 0.4082 - val_acc: 0.8471 - lr: 0.0100
Epoch 5/100
0.8270 - val_loss: 0.4072 - val_acc: 0.8501 - lr: 0.0100
0.8295 - val_loss: 0.3946 - val_acc: 0.8451 - lr: 0.0100
Epoch 7/100
0.8271 - val_loss: 0.3984 - val_acc: 0.8380 - lr: 0.0100
```

```
Epoch 8/100
0.8295 - val_loss: 0.4113 - val_acc: 0.8280 - lr: 0.0100
Epoch 9/100
0.8256 - val_loss: 0.4043 - val_acc: 0.8426 - lr: 0.0100
Epoch 10/100
0.8286 - val_loss: 0.4044 - val_acc: 0.8445 - lr: 0.0100
Epoch 11/100
0.8278 - val_loss: 0.3929 - val_acc: 0.8509 - lr: 0.0100
Epoch 12/100
0.8268 - val_loss: 0.3886 - val_acc: 0.8447 - lr: 0.0100
Epoch 13/100
0.8305 - val_loss: 0.3978 - val_acc: 0.8448 - lr: 0.0100
Epoch 14/100
0.8292 - val_loss: 0.3997 - val_acc: 0.8426 - lr: 0.0100
Epoch 15/100
0.8287 - val_loss: 0.3887 - val_acc: 0.8447 - lr: 0.0100
Epoch 16/100
0.8296 - val_loss: 0.3858 - val_acc: 0.8496 - lr: 0.0100
Epoch 17/100
0.8298 - val_loss: 0.3848 - val_acc: 0.8514 - lr: 0.0100
Epoch 18/100
0.8296 - val_loss: 0.3946 - val_acc: 0.8385 - lr: 0.0100
Epoch 19/100
0.8301 - val_loss: 0.3998 - val_acc: 0.8437 - lr: 0.0100
Epoch 20/100
0.8274 - val_loss: 0.3911 - val_acc: 0.8407 - lr: 0.0100
Epoch 21/100
0.8401 - val_loss: 0.3424 - val_acc: 0.8511 - lr: 1.0000e-03
0.8419 - val_loss: 0.3370 - val_acc: 0.8519 - lr: 1.0000e-03
Epoch 23/100
0.8430 - val_loss: 0.3304 - val_acc: 0.8546 - lr: 1.0000e-03
```

```
Epoch 24/100
0.8445 - val_loss: 0.3309 - val_acc: 0.8533 - lr: 1.0000e-03
Epoch 25/100
0.8439 - val_loss: 0.3313 - val_acc: 0.8526 - lr: 1.0000e-03
Epoch 26/100
0.8438 - val_loss: 0.3299 - val_acc: 0.8524 - lr: 1.0000e-03
Epoch 27/100
0.8417 - val_loss: 0.3311 - val_acc: 0.8531 - lr: 1.0000e-03
Epoch 28/100
0.8451 - val_loss: 0.3328 - val_acc: 0.8494 - lr: 1.0000e-03
Epoch 29/100
0.8446 - val_loss: 0.3302 - val_acc: 0.8530 - lr: 1.0000e-03
Epoch 30/100
0.8456 - val_loss: 0.3287 - val_acc: 0.8538 - lr: 1.0000e-03
Epoch 31/100
0.8430 - val_loss: 0.3309 - val_acc: 0.8535 - lr: 1.0000e-03
Epoch 32/100
0.8456 - val_loss: 0.3332 - val_acc: 0.8504 - lr: 1.0000e-03
Epoch 33/100
0.8455 - val_loss: 0.3301 - val_acc: 0.8526 - lr: 1.0000e-03
Epoch 34/100
0.8431 - val_loss: 0.3298 - val_acc: 0.8505 - lr: 1.0000e-03
Epoch 35/100
0.8475 - val_loss: 0.3266 - val_acc: 0.8535 - lr: 1.0000e-03
Epoch 36/100
0.8453 - val_loss: 0.3292 - val_acc: 0.8519 - lr: 1.0000e-03
Epoch 37/100
0.8454 - val_loss: 0.3302 - val_acc: 0.8537 - lr: 1.0000e-03
Epoch 38/100
0.8429 - val_loss: 0.3307 - val_acc: 0.8546 - lr: 1.0000e-03
0.8546
[0.3306540846824646, 0.8546273708343506]
```

```
[15]: model.save("2layerDNN")
    INFO:tensorflow:Assets written to: 2layerDNN\assets
[16]: from tensorflow.keras.models import load_model
     loaded_model = load_model('2layerDNN')
[17]: loaded_model.summary()
    Model: "sequential_3"
     Layer (type)
                            Output Shape
                                                  Param #
    _____
     dense_6 (Dense)
                            (None, 128)
                                                  11776
     batch_normalization_3 (Batc (None, 128)
                                                  512
     hNormalization)
     re_lu_3 (ReLU)
                            (None, 128)
                                                  0
     dropout_3 (Dropout)
                            (None, 128)
     dense_7 (Dense)
                            (None, 1)
                                                  129
    _____
    Total params: 12,417
    Trainable params: 12,161
    Non-trainable params: 256
[]:
```

[]: