Advanced techniques

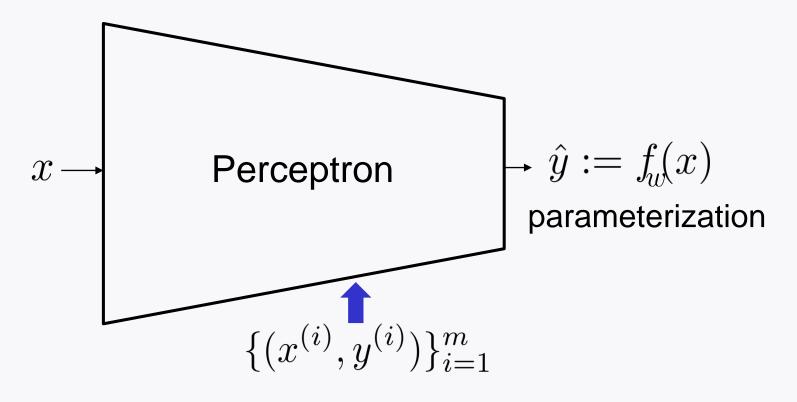
Lecture 4

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January 23, 2024

Data organization & generalization techniques

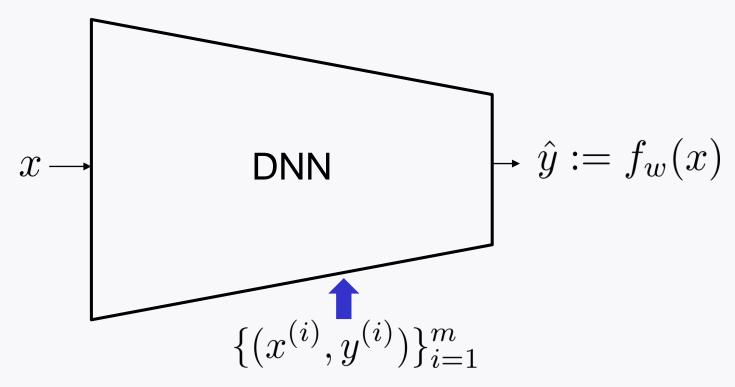
Recap: Machine learning



No activation + squared error loss: Least Squares
Logistic act. + cross entropy loss: Logistic regression

Algorithm: Gradient descent

Recap: Deep neural networks



ReLU (@hidden); Logistic (@output); Cross entropy loss

Algorithm: Gradient descent

Efficient method: backprop

Practical variant: Adam optimizer

Recap: Scikit-learn coding for LS

```
sklearn.datasets
from
                                   import load iris
from
     sklearn.model selection
                                   import train test split
iris=load iris()
X=iris.data
y=iris.target
X train, X test, y train, y test=train test split(X, y, test size=0.2)
from
      sklearn.linear model
                                   import RidgeClassifier
Model LS = RidgeClassifier()
Model LS.fit(X train, y train)
Model LS.predict(X test)
Model LS.score(X test, y test)
```

Recap: Scikit-learn coding for LR

```
from sklearn.datasets
                                  import load iris
from sklearn.model selection
                                  import train test split
iris=load iris()
X=iris.data
y=iris.target
X train, X test, y train, y test=train test split(X, y, test size=0.2)
from
      sklearn.linear model
                                  import LogisticRegression
Model LR = LogisticRegression()
Model LR.fit(X train, y train)
Model LR.predict(X test)
Model LR.score(X test, y test)
```

Recap: TensorFlow coding for DNN

```
from tensorflow.keras.datasets import mnist
from tensorflow.keras.models import Sequential
from tensorflow.keras.layers import Flatten
from tensorflow.keras.layers import Dense
(X train, y train), (X test, y test) = mnist.load data()
X train, X test = X train/255.0, X test/255.0
Model NN = Sequential()
Model NN.add(Flatten(input shape=(28,28)))
Model NN.add (Dense (128, activation='relu'))
Model NN.add (Dense (10, activation='softmax'))
Model NN.compile(optimizer='adam',
loss='sparse categorical crossentropy', metrics=['acc'])
Model NN.fit(X train, y train, epochs=10)
Model NN.predict(X test)
Model NN.evaluate(X test, y test)
```

Question

How to improve model performance?

Outline of today's lectures

Will explore several techniques for improvement.

- 1. Data organization (train/validation/test sets)
- 2. Generalization techniques
- 3. Weight initialization
- 4. Techniques for training stability
- 5. Hyperparameter search
- 6. Cross validation

Focus of Lecture 4

Will explore several techniques for improvement.

- 1. Data organization (train/validation/test sets)
- 2. Generalization techniques
- 3. Weight initialization
- 4. Techniques for training stability
- 5. Hyperparameter search
- 6. Cross validation

Train vs. validation vs. test sets

Data seen during training:

train set validation set

Role: training model **Role:** *Hyperparameter* search

parameters

Data unseen during training: test set

How to split train/val/test sets?

Two important factors to consider:

1. How big "*m*" is

2. Data distribution

How big "m" is

A deciding factor for the **split ratio**.

Small:

$$m \le 1,000$$

train:val:test = 60:20:20

Middle:

$$1,000 \le m \le 10,000$$

80:10:10

Large:

$$10,000 \le m \le 1,000,000$$

98:1:1

Ultra-large:

$$m \ge 1,000,000$$

99.9:0.05:0.05

Set the split ratio such that $m_{\rm test} \approx 100 \sim 1000$

Data distribution

val data dist. ~ test data dist. ~ target dist.

Take the rest as training data.

Coding implementation is easy.

Generalization techniuges

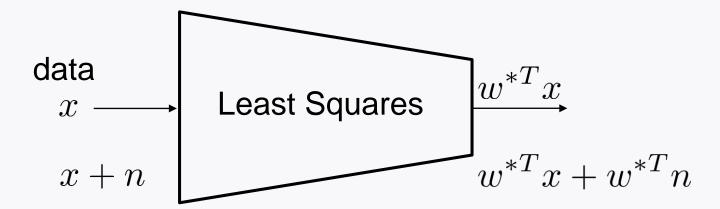
1. Regularization

2. Data augmentation

3. Early stopping

4. Dropout

Regularization: Motivation



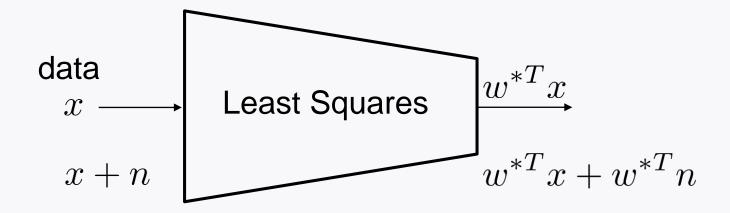
In reality: x contains some noise.

Want: model being robust to such noise.

Challenge:

Large values of $||w^*||$ can boost up such noise.

Regularization: Motivation



For robustness, we want: $||w^*||^2 \downarrow$

Note: At the same time, we also want:

Loss Function ↓

Regularization: Idea

Regulate two objectives at the same time.

$$\min_{w} \text{Loss Function} + \lambda \|w\|^2$$

 λ : regularization factor

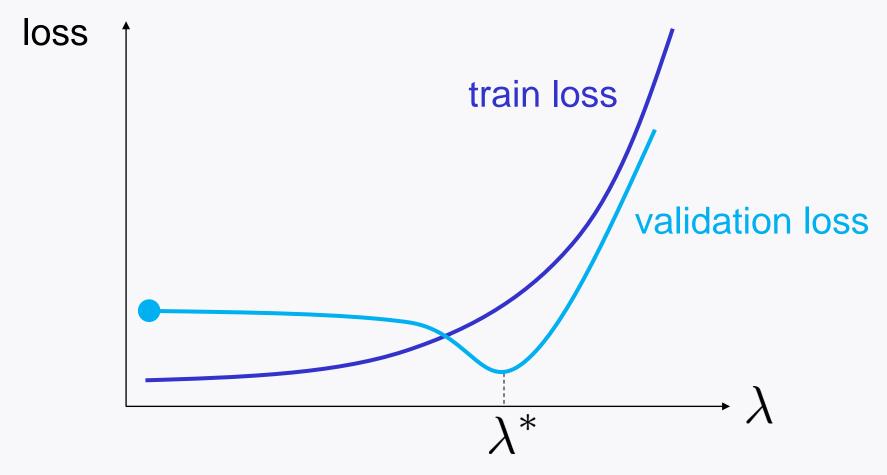
It is a hyperparameter!

How to choose?

Regularization: How λ affects?



Regularization: How to choose λ ?



Find the sweet spot that minimizes validation loss.

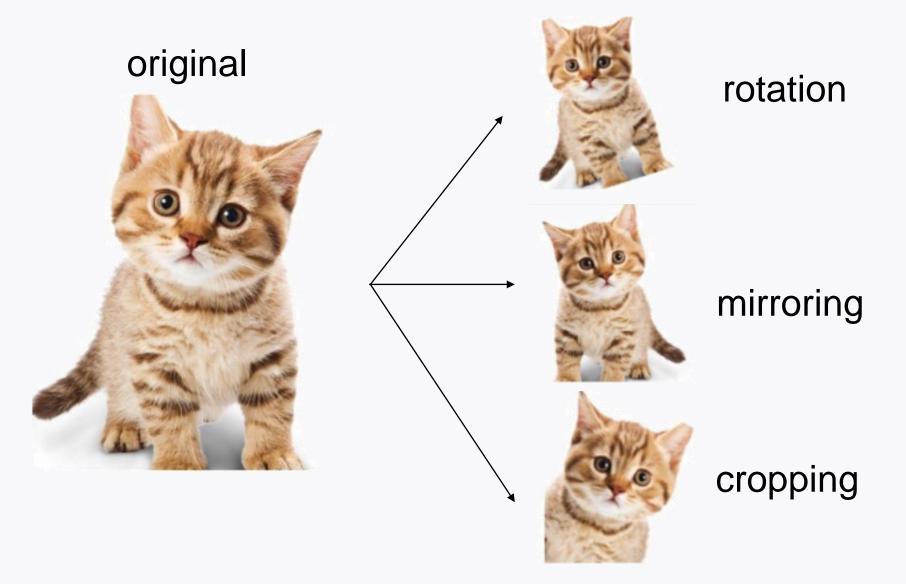
Data augmentation

Idea: Artificially generate diverse data by perturbing original data.

This way: Can make model resilient to unseen data.

Hence: Can improve generalization capability.

Data augmentation for image data



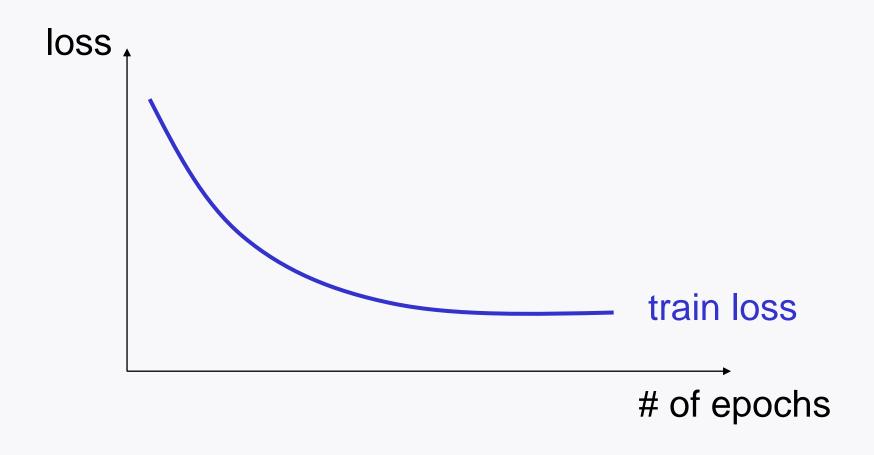
Data augmentation for numerical data

Original data:
$$\{(x^{(i)}, y^{(i)})\}_{i=1}^{m}$$

One prominent way is to add random noise:

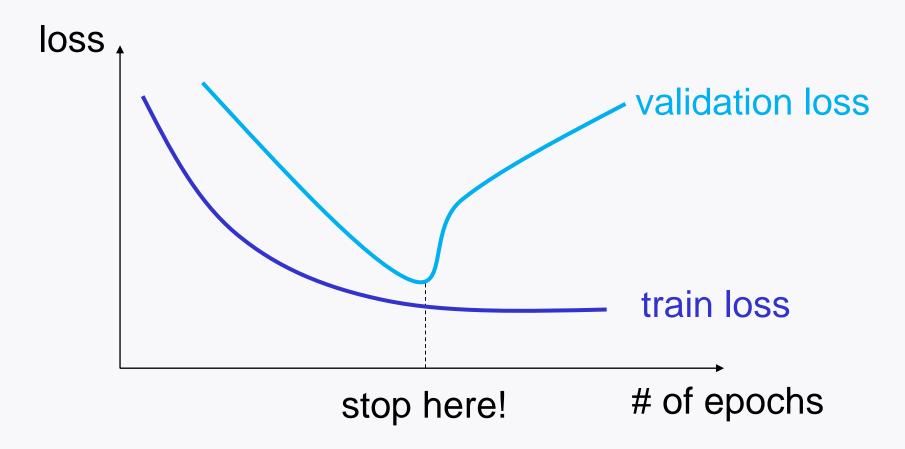
$$x^{(i)} + n$$
 random noise

Early stopping: Motivation



Large # of epochs: Overfitting to train data.

Early stopping: Idea



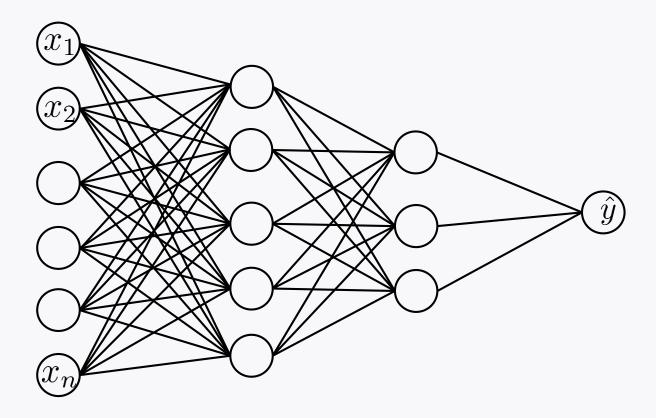
To avoid overfitting: Rely on validation loss.

Dropout

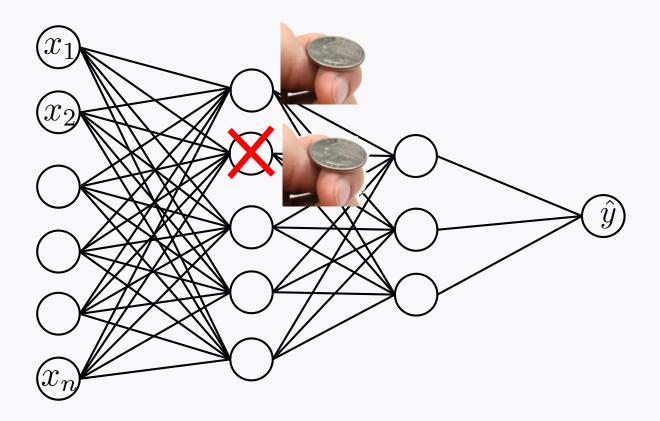
$$J(w) = \frac{1}{m_{\mathcal{B}}} \sum_{i=1}^{m_{\mathcal{B}}} \ell(y^{(i)}, \hat{y}^{(i)})$$

In computing a prediction $\hat{y}^{(i)}$ per example, construct a random neural network.

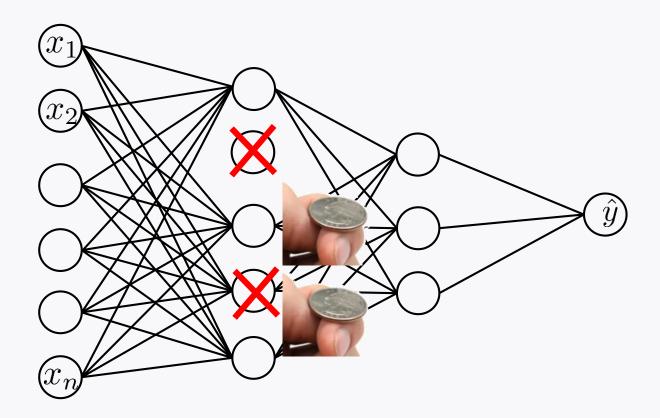
How to construct a random neural network?



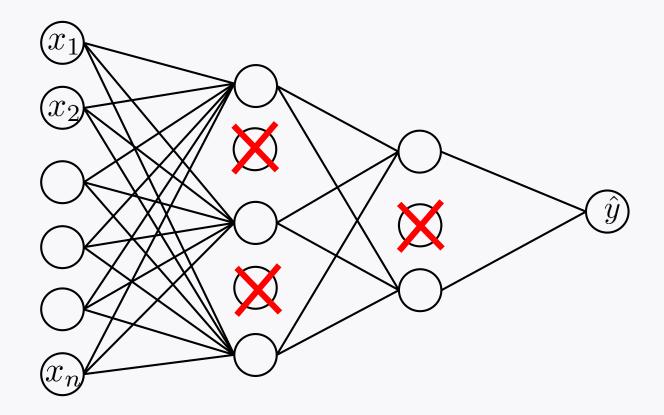
Dropout rate: p (e.g., 0.5)



Dropout rate: p (e.g., 0.5)



Dropout rate: p (e.g., 0.5)



Generate this partial NN per example.

Why dropout works?

Experience many smaller NNs.

Can interpret the resulting NN as an **averaging ensemble** of all these smaller NNs.

Not overfit to a particular NN; hence generalize better.

Look ahead

Will study:

weight initialization

techniques for training stability