

$$S = [1, 1]$$

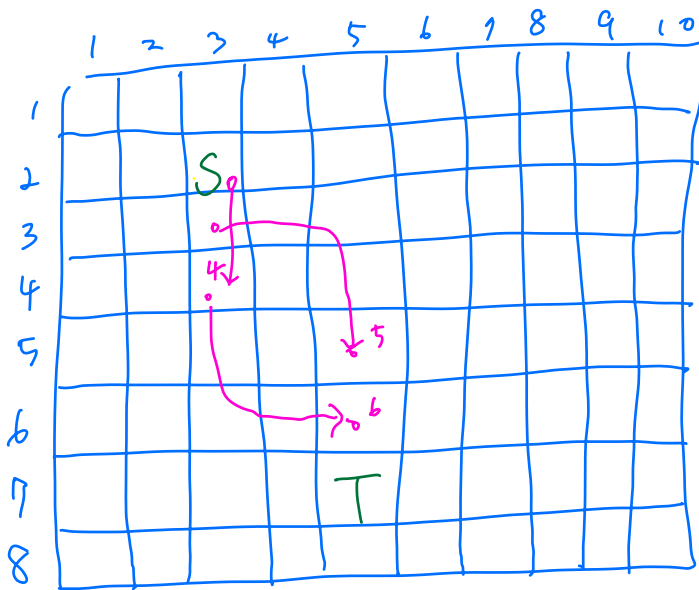
$$T = [4, 5]$$

Special  $[ [1, 2, 3, 3, 2], [3, 4, 4, 5, 1] ]$

Verify min or not.

$$[1, 2, 3, 3, 2] < |1-3| + |2-3| = 3$$

$$[3, 4, 4, 5, 1] < |3-4| + |4-5| = 2$$



$$S = [3, 2]$$

$$T = [5, 7]$$

$X_1$	$Y_1$	$X_2$	$Y_2$	Calculated
3	2	3	4	2
3	3	5	5	4
3	4	5	6	4

$$S-T = |3-5| + |2-7| = 7$$

Start pos =  $[ \text{StartX}, \text{StartY} ]$   
 Target pos =  $[ \text{targetX}, \text{TargetY} ]$  ← Find min cost w/ or w/o  
 Special Roads =  $[ \underbrace{X_1, Y_1}_{\text{Start}}, \underbrace{X_2, Y_2}_{\text{Target}}, \text{cost} ]$  Special Roads  
 Start & Target length == 2

$1 \leq \text{Start } X \leq \text{Target } X < 10^5$   
 $1 \leq \text{Start } Y \leq \text{Target } Y < 10^5$   
 Special Road length = 5  
 $\text{Start } X \in X_i, \text{Start } Y \in Y_i$   
 $1 \leq \text{cost} < 10^5$

1. Special Roads may or may not be minimum  
 2. Minimum cost  $\Rightarrow$  shortest path

Verify special Road = minimum

Relaxation ( if  $d[v] > d[u] + w(u, v)$   
 $d[v] = d[u] + w(u, v)$

$O(V^2)$  w/ Brute Force adjacent matrix

$O(V^2)$  w/ adjacent list

$O(V \lg E + E \lg V)$  w/ minheap

No negative cycle

Weighted Directed Graph

1



Pseudo

# Verify Special Roads

for  $x_1, x_2, y_1, y_2$  in Special Roads

if  $c < (|x_1 - x_2| + |y_1 - y_2|)$ :

$g(x_1, x_2).add(x_2, y_2, c)$

$starts.add(x_1, y_1)$

$ends.add(y_2, y_2)$

# add

Start  $[1, 1]$  Target  $[4, 5]$

SR  $[1, 2, 3, 3, 2]$ ,  $[3, 4, 4, 5, 1]$

$$g(1, 2) = (3, 3, 2) \quad g(3, 4) = (4, 5, 1)$$

starts  $[(1, 2), (3, 4), (4, 5)]$

ends  $[(3, 3), (4, 5), (1, 1)]$

$$g(1, 2) = (3, 3, 2)$$

$$g(3, 4) = (4, 5, 1)$$

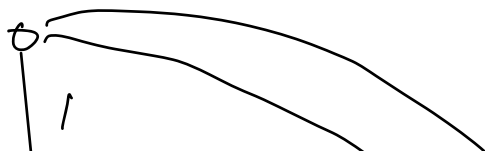
$$g(1, 1) = ((4, 5, 7), (1, 2, 1), (3, 4, 5))$$

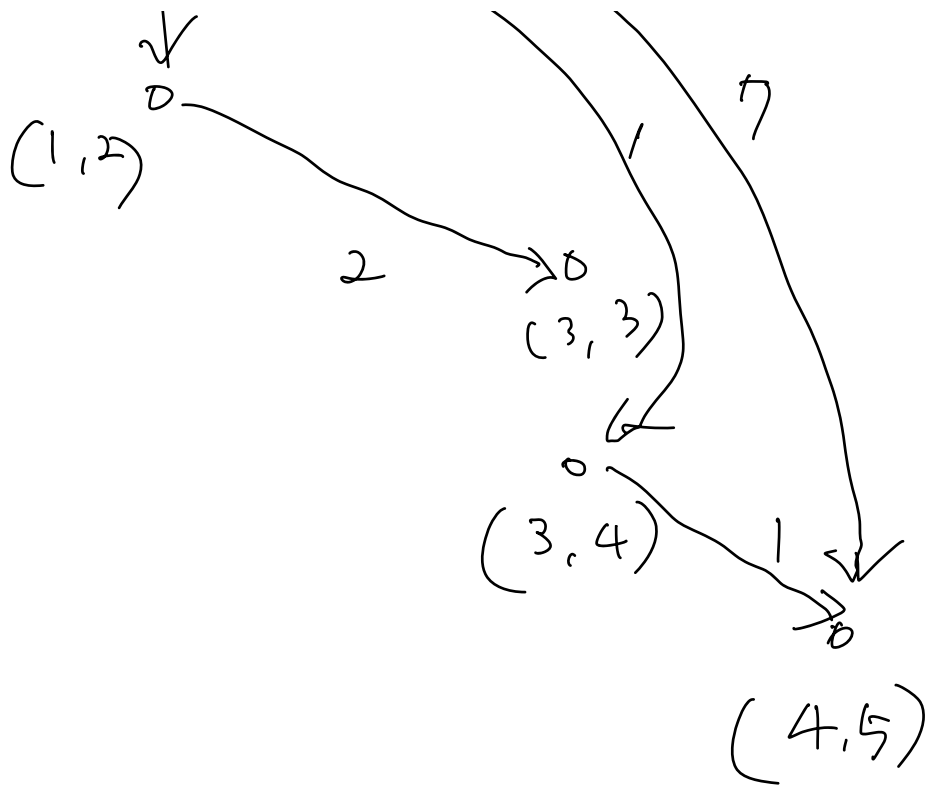
$$g(4, 5) = ((1, 2, 6), (4, 5, 0), (3, 4, 2))$$

$$g(3, 3) = ((4, 5, 3), (1, 2, 3), (3, 4, 1))$$

$$\text{dist}[v] = \inf$$

$(1, 1)$





$$\text{minimal} = |start[0] - target[0]| + |start[1] - target[1]|$$

Start  $[1, 1]$  Target  $[4, 5]$

SR  $[1, 2, 3, 3, 2], [3, 4, 4, 5, 1]$

$$g(1, 2) = (3, 3, 2) \quad g(3, 4) = (4, 5, 1)$$

starts  $[(1, 2), (3, 4), (4, 5)]$

ends  $[(3, 3), (4, 5), (1, 1)]$

$$g(1, 2) = (3, 3, 2)$$

$$g(3, 4) = (4, 5, 1)$$

$$g(3, 3) = (1, 2, 3)$$

$$g(3, 4) = (3, 4, 1)$$

$$g(3, 3) = (4, 5, 3)$$

$$g(4, 5) = (1, 2, 6)$$

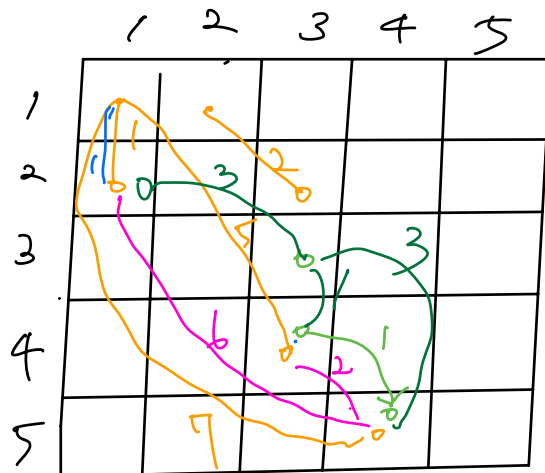
$$g(4, 5) = (3, 4, 2)$$

$$g(4, 5) = (4, 5, 0)$$

$$g(1, 1) = (1, 2, 1)$$

$$g(1, 1) = (3, 4, 7)$$

... ..



$$g(1,1) = (4,5,1)$$