

# Time and Space Complexity

## Assignment Solutions



**Q1. What is the time, and space complexity of the following code snippet?**

```
int a = 0, b = 0;
for (i = 0; i < N; i++) {
    a = a + i;
}
for (j = 0; j < M; j++) {
    b = b + j;
}
```

**Answer:**  $O(N + M)$  time,  $O(1)$  space

**Explanation:** The first loop is  $O(N)$  and the second loop is  $O(M)$ . Since  $N$  and  $M$  are independent variables, so we can't say which one is the leading term. Therefore Time complexity of the given problem will be  $O(N+M)$ . Since variables size does not depend on the size of the input, therefore Space Complexity will be constant or  $O(1)$ .

**Q2. What is the time complexity of the following code snippet?**

```
int a = 0;
for (i = 0; i < N; i++) {
    for (j = N; j > i; j--) {
        a = a + i + j;
    }
}
```

**Answer:**  $O(N*N)$

**Explanation:**

The above code runs total no of times

$$= N + (N - 1) + (N - 2) + \dots 1 + 0$$

$$= N * (N + 1) / 2$$

$$= 1/2 * N^2 + 1/2 * N$$

$O(N^2)$  times.

**Q3. What is the time complexity of the following code snippet?**

```
int i, j, k = 0;
for (i = n / 2; i <= n; i++) {
    for (j = 2; j <= n; j = j * 2) {
        k = k + n / 2;
    }
}
```

**Answer:**  $O(n \log n)$

**Explanation:**  $j$  keeps doubling till it is less than or equal to  $n$ . Thus it is of the form 2,4,8,16,32..... and this makes the complexity as  $O(\log n)$ . Let's take the examples here.

for  $n = 16, j = 2, 4, 8, 16$

for  $n = 32, j = 2, 4, 8, 16, 32$

So,  $j$  would run for  $O(\log n)$  steps.

$i$  runs for  $n/2$  steps.

So, total steps =  $O(n/2 * \log(n)) = O(n * \log n)$

**Q4. What is the time complexity of the following code snippet?**

```
int a = 0, i = N;
while (i > 0) {
    a += i;
    i /= 2;
}
```

**Answer:**  $O(\log N)$

**Explanation:** We have to find the smallest  $x$  such that ' $(N / 2^x) < 1$  OR  $2^x > N$ '  
 $x = \log(N)$

**Q5. What will be the time complexity of the following code snippet?**

```
for(int i=0;i<n;i++){
    i*=k
}
```

**Answer:**  $O(\log kn)$

**Explanation:** Because loops for the  $kn-1$  times, so after taking log, it becomes  $\log kn$ .