

ARIMA

Machine learning

Data → Model

Linear req

log req

Svm

DT

Time Series Data → Model

ARIMN

SARIMN, SARIMAX

DL, RNN, Attention, transformer

AR

(Autoregression)

↓

P

[0, 1, 2, 3, ..., n]

lag value

PACF (Corrlogram)

I

(Integration)

↓

d

- [0, 1, 2, 3, ..., n]

lag value

Differencing

- | Non stationary | Stationary |

MA

(moving average model)

↓

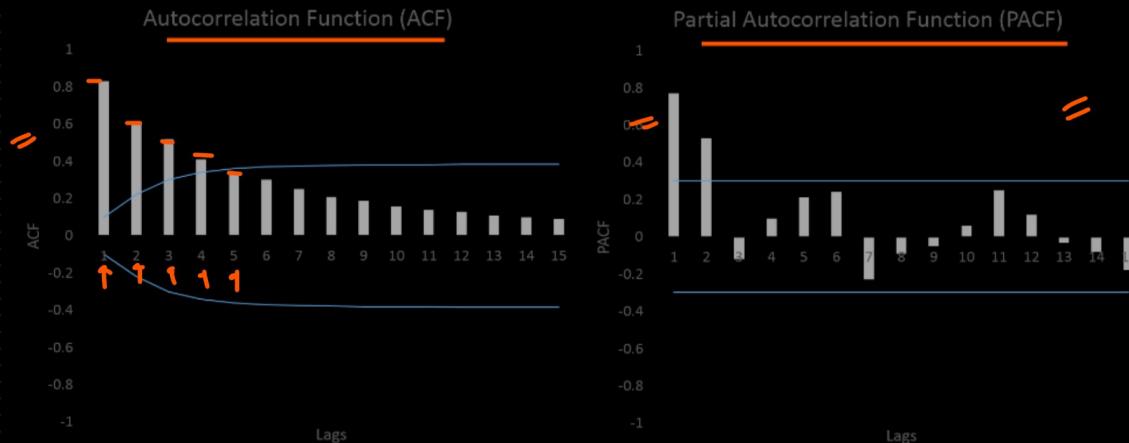
q

[0, 1, 2, 3, ..., n]

lag value

ACF (Corrlogram)

$$\left. \begin{array}{l} -\gamma_t, \gamma_{t-1} \\ -\gamma_t, \gamma_{t-2} \\ -\gamma_t, \gamma_{t-3} \end{array} \right\}$$



$$\hat{\gamma}_t = \frac{\gamma_{t-2} \longleftrightarrow \gamma_t}{\gamma_{t-1}}$$

AR (Autoregression)

$$\boxed{\gamma_t = \psi_1 \gamma_{t-1} + \psi_2 \gamma_{t-2} + \psi_3 \gamma_{t-3} \dots + \psi_n \gamma_{t-n} + c}$$

AR(1) \Rightarrow

$$\boxed{\gamma_t = \psi \gamma_{t-1} + c}$$

lag 1 TS

lag 2

$$\begin{cases} lag = 1 \\ AR = 1 \\ P = 1 \end{cases}$$

| AR(2) or P=2 or lag 2 |

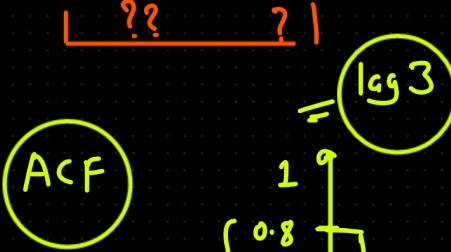
$$\hat{\gamma}_t = \psi_1 \gamma_{t-1} + \psi_2 \gamma_{t-2} + c$$

D_1	10	NA	NA
D_2	20	$D_1 = 10$	NA
D_3	30	$D_2 = 20$	$D_1 = 10 \Rightarrow$
D_4	40	$D_3 = 30$	$D_2 = 20$
D_5	45	$D_4 = 40$	$D_3 = 30$

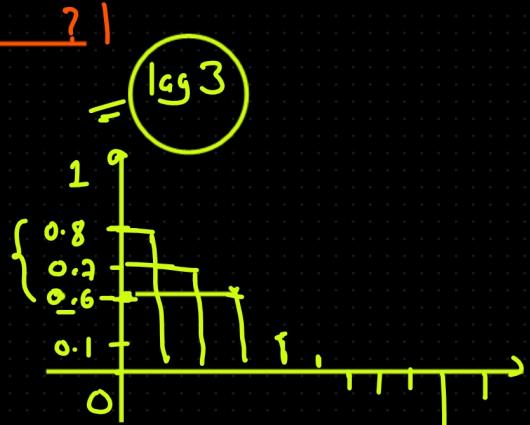
20	10
30	20
40	30
45	40
?	45

$$\Rightarrow \boxed{\gamma_t = \psi \gamma_{t-1} + c}$$

γ_t	γ_{t-1}	γ_{t-2}
30	20	10
40	30	20
45	40	30
?	45	40



AR(3)



D_1	18	lag 2
D_2	20	
D_3	30	
D_4	140	
D_5	10	
D_6	60	20

$$\begin{aligned}
 Y_t &= \gamma_{t-1} \psi_1 + \gamma_{t-2} \psi_2 + \dots + \gamma_{t-h} \psi_n + C \\
 &= Y_t - (\gamma_{t-1} \psi_1 + \gamma_{t-2} \psi_2 + \dots + \gamma_{t-h} \psi_n) + C
 \end{aligned}$$

I \Rightarrow Integration \Rightarrow Difference

$$\begin{array}{c} D=0 \\ \gamma_t - \gamma_1 \quad D_1 \\ \gamma_{t-1} - \gamma_2 \quad D_2 \\ \gamma_{t-2} - \gamma_3 \quad D_3 \\ \vdots \\ \gamma_{t-1} - \gamma_t \quad D_{t-1} \\ \gamma_t - \gamma_t = D_t \end{array}$$
$$\begin{array}{c} (D_2 - D_1) \\ (D_3 - D_2) \\ \vdots \\ (D_t - D_{t-1}) \end{array}$$

$$D_1 = (\gamma_t - \gamma_{t-1})$$

$$D_2 = (\gamma_{t-1} - \gamma_{t-2})$$

$$D_2 = (\gamma_t - \gamma_{t-1} - \gamma_{t-2})$$

Moving average \Rightarrow
(error)

$$Y_t = \varepsilon_{t-1} \psi + C$$

$$Y_t = \varepsilon_{t-1} Y_{t-1} + \varepsilon_{t-2} Y_{t-2} + \overline{\varepsilon_{t-3} Y_{t-3} \dots \varepsilon_{t-n} Y_{t-n}} + C$$

ARIMA \Rightarrow

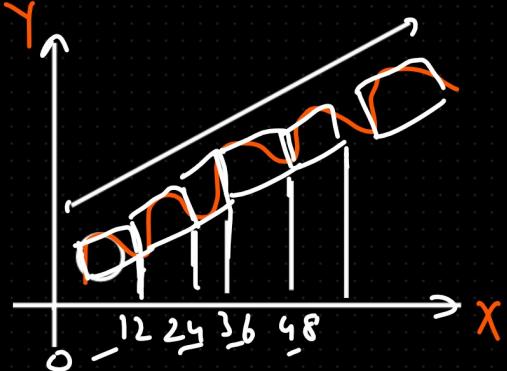
$$\widehat{Y}_t = \frac{(Y_{t-1} Y_{t-1} + Y_{t-2} Y_{t-2} + \dots + Y_{t-n} Y_{t-n} + C) + (Y_{t-1} - Y_t - Y_{t-2} - \dots - Y_{t-n}) +}{(\varepsilon_{t-1} Y_{t-1} + \varepsilon_{t-2} Y_{t-2} + \varepsilon_{t-3} Y_{t-3} - \dots - \varepsilon_{t-n} Y_{t-n} + C)}$$

AR(1), P=1
I(2), d=2 \Rightarrow
MA(1), q=1

$$Y_t = (Y_{t-1} Y_{t-1} + C) + (Y_t - Y_{t-1} - Y_{t-2}) + (\varepsilon_{t-1} Y_{t-1} + C)$$

SARIMA

↳ Seasonal



P,D,Q

(P,D,Q)



$(P,d,q)(P,D,Q)_S$

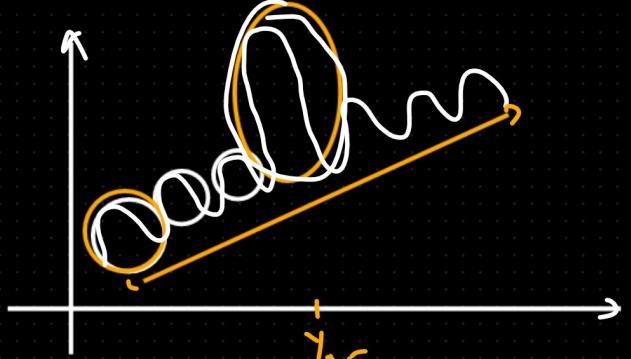
$\Rightarrow (1,1,2)(1,0,2)_{12}$



SARIMX

↳ exogenous

(outlier) (extra effect)



$(P,d,q)(P,D,Q)_S X$

$= \frac{(0,1,2)(1,1,2)_{12} (1,r)}{t \uparrow t \quad t \uparrow t \uparrow t}$